

Supplementary Materials for

**Much more to explore with an oxidation state of nearly four: Pr valence instability in intermetallic  $m$ -Pr<sub>2</sub>C<sub>3</sub>Ge<sub>5</sub>**

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## The Lu<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> and U<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> Structure Types

The Lu<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> (*I2/c*) and U<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> (*Ibam*) (24) structure types are distorted coloring variants of the BaAl<sub>4</sub> structure type (59), representing the compositional and structural intermediate to the BaNiSn<sub>3</sub> (*I4mm*) and CaBe<sub>2</sub>Ge<sub>2</sub> (*P4/nmm*) structure types (60). The slabs are linked via a five-coordinate square pyramidal main-group or transition metal that creates a three-dimensional framework surrounding planar square layers of A atoms. The [Co<sub>3</sub>Ge<sub>5</sub>] tetrahedral slab is distorted from the alternating assignment of M and X such that they are not perfectly aligned and are corrugated (Fig. 1e – 1h). The consequence of the tetrahedral corrugation is that the A layers are not planar or square, and instead form “wavy planes” (61).

The Lu<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> (*I2/c*) structure type is related to the U<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> (*Ibam*) structure type by a monoclinic deformation (25). The Lu<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> structure type is referenced in the pseudo-orthorhombic setting (*I2/c*) related to the standard setting (*C2/c*) by the transformation matrix (101/0 $\bar{1}$ 0/00 $\bar{1}$ ) for this discussion to facilitate comparison with the U<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> type structure. The second coordination sphere of the tetrahedral transition metal environment can be used to understand how the monoclinic deformation takes place. In U<sub>2</sub>Co<sub>3</sub>Si<sub>5</sub> type structures, the tetrahedral transition metal site exists in a “4 + 2” coordination, where the first coordination sphere is a tetrahedral environment of equidistant main group metals, and the second coordination sphere forms a distorted octahedral environment with two additional main group metals spaced further away. When the monoclinic distortion is present (25), the transition metal coordination environment approaches a “5 + 1” geometry through a “push-pull” type distortion dependent upon the degree of distortion, where  $\beta$  has been observed as large as 92.6°. Here, one axial main group metal becomes equidistant to the tetrahedral environment and the other becomes increasingly distant (23). The distortion also corresponds to the dimerization of the five-coordinate transition metal site along the crystallographic *c*-direction. Together, these changes in the 3-dimensional framework result in the reduction in point symmetry of the lanthanide site from *C<sub>s</sub>* to *C<sub>1</sub>*, potentially impactful to the crystal field splitting of 4*f* orbitals. The non-linear behavior coincides with the deformation in the second coordination sphere of the Co1 local environment.

Upon completion of the second order structural phase transformation at  $T = 343$  K in *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>, the tetrahedral Ge<sub>2</sub> and Ge<sub>4</sub> atomic sites that were unique at room temperature become symmetrically equivalent. In the [Co<sub>3</sub>Ge<sub>5</sub>] slab, the intermediate “5 + 1” geometry of the Co1

second coordination sphere increases symmetry to a “4 + 2” geometry with  $d_{\text{Co1-Ge3}} = 2.4395(14)$  Å x2,  $d_{\text{Co1-Ge3}} = 2.4493(12)$  Å x2,  $d_{\text{Co1-Ge4}} = 2.655(2)$  Å, and  $d_{\text{Co1-Ge2}} = 2.764(2)$  Å in room temperature  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  converging to  $d_{\text{Co1-Ge3}} = 2.4419(6)$  Å x4 and  $d_{\text{Co1-Ge2}} = 2.7166(9)$  Å x2 in the high temperature transformed structure. Notably, the five coordinate Co2 atoms that were dimerized along the  $c$ -direction at room temperature undergo the largest change in bond distance within the framework, expanding from  $d_{\text{Co2-Co2}} = 3.464(2)$  Å to  $d_{\text{Co2-Co2}} = 3.5838(7)$  Å at 343 K. While the loss of dimerization of the Co2 sites and convergence of the Co1-Ge distances may seem isolated, they are explicitly linked through a scissor gate folding mechanism: as the Ge atoms converge, the Co2 sites are separated. Such behavior has been seen in other lanthanide intermetallic compounds containing Group 9 transition metals like in the structural phase transformation of CeRhGe (46) and the charge density wave transformation in  $\text{A}_2\text{Ir}_3\text{Si}_5$  (A = Ho, Er, Lu) (33-35).

At room temperature, the shortest Pr-Ge interatomic distance in  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$ ,  $d_{\text{Pr-Ge3}} = 2.9489(11)$  Å, is far shorter than distances observed in similar compounds  $\text{PrCoGe}_3$  ( $d_{\text{Pr-Ge1}} = 3.120(1)$  Å) (62) and  $\text{PrCo}_2\text{Ge}_2$  ( $d_{\text{Pr-Ge}} = 3.153(14)$  Å) (63) and shorter than the sum of the single bond covalent radii of Pr and Ge  $d_{\text{Pr-Ge}}^{\text{calc}} = 2.97$  Å (64). The only other reported Pr-Co-Ge ternary with Pr-Ge bonds shorter than the sum of their covalent radii is  $\text{Pr}_{117}\text{Co}_{56.7}\text{Ge}_{112}$  and no Pr-Ge binaries exhibit such distances, including those synthesized at high-pressure (65-67). Interestingly, the short A-X distance seems to be a feature of the early lanthanide compounds across multiple  $\text{A}_2\text{M}_3\text{X}_5$  structure types (64). The next eight Pr-Ge bond distances are longer,  $d_{\text{Pr-Ge}} = 3.1275(17) - 3.2004(8)$  Å, and correspond more closely with what is observed in  $\text{PrCoGe}_3$  (62) and  $\text{PrCo}_2\text{Ge}_2$  (63), with the remaining Pr-Ge contact having a distance of  $d_{\text{Pr-Ge3}} = 3.2816(11)$  Å. At 343 K, the Pr-Ge3 distances are relatively invariant, with the shortest,  $d_{\text{Pr-Ge3}} = 2.9443(10)$  Å, and longest,  $d_{\text{Pr-Ge3}} = 3.2839(10)$  Å, distances showing little change from the room temperature structure.

While few structures within the  $\text{A}_2\text{M}_3\text{X}_5$  family have been investigated as a function of temperature, structural phase transformation are not common. Neutron diffraction data from compounds isotypic to  $\text{Lu}_2\text{Co}_3\text{Si}_5$  ( $I2/c$ ) either report no temperature dependent anomalies in structure, such as in  $\text{A}_2\text{Co}_3\text{Si}_5$  (A = Tb, Dy), or report minimal changes in the angle  $\beta$ , such as in  $\text{U}_2\text{Rh}_3\text{Si}_5$ . Examples of compounds in the space group  $Ibam$  obtained from powder neutron diffraction, namely  $\text{A}_2\text{Ni}_3\text{Si}_5$  (A = Ce, Pr, Nd, Tb, Dy) (68),  $\text{Tb}_2\text{Ir}_3\text{Si}_5$  (69),  $\text{Ce}_2\text{Ni}_3\text{Ge}_5$  (70), and  $\text{Pr}_2\text{Pd}_3\text{Ge}_5$  (71), indicate that not all compounds of the  $\text{U}_2\text{Co}_3\text{Si}_5$  structure type undergo a low

temperature monoclinic deformation. Additionally, the structural phase transformation of  $m$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$  is reversible (Fig. S2).

### Powder X-ray Diffraction

Table S1. Atomic Positions of Room Temperature  $m$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$  and  $o$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$  obtained from Rietveld Refinement. \*Atomic displacement parameters were obtained from single crystal X-ray diffraction and were not refined.

| Atom  | Wyckoff site | $x$           | $y$          | $z$           | $B_{\text{iso}}(\text{\AA}^2)^*$ |
|---|--------------|---------------|--------------|---------------|----------------------------------|
| RT $m$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$ (Space group: $I2/c$ )       |              |               |              |               |                                  |
| Pr  | $8f$         | 0.26477 (5)   | 0.13473 (5)  | 0.26496 (14)  | 0.536117                         |
| Co1   | $4e$         | 0             | 0.00212 (17) | $\frac{1}{4}$ | 0.634023                         |
| Co2   | $8f$         | 0.10313 (11)  | 0.36109 (10) | 0.1113 (3)    | 0.802201                         |
| Ge1   | $4e$         | 0             | 0.50300 (14) | $\frac{1}{4}$ | 0.626917                         |
| Ge2   | $4e$         | 0             | 0.77049 (13) | $\frac{1}{4}$ | 0.660869                         |
| Ge3   | $8f$         | 0.33909 (10)  | 0.40284 (8)  | 0.3374 (2)    | 0.602441                         |
| Ge4   | $4e$         | 0             | 0.22454 (13) | $\frac{1}{4}$ | 0.650604                         |
| 343 K $m$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$ (Space group: $Ibam$ )    |              |               |              |               |                                  |
| Pr  | $8j$         | 0.26489 (4)   | 0.13432 (4)  | 0             | 0.533748                         |
| Co1   | $4a$         | 0             | 0            | $\frac{1}{4}$ | 0.632444                         |
| Co2   | $8j$         | 0.10475 (10)  | 0.36120 (9)  | 0             | 0.821151                         |
| Ge1   | $4b$         | $\frac{1}{2}$ | 0            | $\frac{1}{4}$ | 0.622180                         |
| Ge2   | $8g$         | 0             | 0.22795 (7)  | $\frac{1}{4}$ | 0.673502                         |
| Ge3   | $8j$         | 0.33878 (9)   | 0.40271 (6)  | 0             | 0.600072                         |
| As-grown $o$ - $\text{Pr}_2\text{Co}_3\text{Ge}_5$ (Space group: $Ibam$ ) |              |               |              |               |                                  |
| Pr  | $8j$         | 0.26453 (4)   | 0.13419 (4)  | 0             | 0.533748                         |
| Co1   | $4a$         | 0             | 0            | $\frac{1}{4}$ | 0.632444                         |
| Co2   | $8j$         | 0.10515 (9)   | 0.36144 (9)  | 0             | 0.821151                         |
| Ge1   | $4b$         | $\frac{1}{2}$ | 0            | $\frac{1}{4}$ | 0.622180                         |
| Ge2   | $8g$         | 0             | 0.22795 (7)  | $\frac{1}{4}$ | 0.673502                         |
| Ge3   | $8j$         | 0.33961 (8)   | 0.40295 (6)  | 0             | 0.600072                         |

Table S2. Bond Distances of the Pr Local Environment (Å) in Room Temperature *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>, 343 K *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>, and, for Comparison, As-grown *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>.

|      |             | RT <i>m</i> -Pr <sub>2</sub> Co <sub>3</sub> Ge <sub>5</sub> ( <i>I2/c</i> ) | 343 K <i>m</i> -Pr <sub>2</sub> Co <sub>3</sub> Ge <sub>5</sub> ( <i>Ibam</i> ) | As-grown <i>o</i> -Pr <sub>2</sub> Co <sub>3</sub> Ge <sub>5</sub> ( <i>Ibam</i> ) |
|------|-------------|--|---|--|
| Pr:  | Pr          | 4.0216 (11)  | 4.0346 (6)  | 4.0349 (5)   |
|      | Pr          | 4.0290 (11)  | -   | -  |
|      | Pr          | 4.3464 (11)  | 4.3414 (6)  | 4.3370 (5)   |
|      | Ge1         | 3.1417 (11)  | 3.1684 (5)  | 3.1699 (4)   |
|      | Ge1         | 3.1981 (10)  | -   | -  |
|      | Ge2         | 3.1661 (11)  | 3.1907 (7)  | 3.1922 (6)   |
|      | Ge2/4       | 3.2167 (10)  | -   | -  |
|      | Ge2         | 3.2004 (8)   | 3.1853 (6)  | 3.1843 (5)   |
|      | Ge2/4       | 3.1551 (9)   | -   | -  |
|      | Ge3         | 2.9489 (11)  | 2.9443 (10)   | 2.9394 (9)   |
|      | Ge3         | 3.1275 (17)  | 3.1305 (4)  | 3.1338 (3)   |
|      | Ge3         | 3.1300 (14)  | -   | -  |
|      | Ge3         | 3.2816 (11)  | 3.2851 (10)   | 3.2867 (9)   |
|      | Co2         | 3.1330 (13)  | 3.1301 (13)   | 3.1279 (11)  |
|      | Co2         | 3.1657 (18)  | 3.1952 (4)  | 3.1969 (4)   |
| Co2  | 3.2326 (21) | -  | -   |  |
| Co1: | Ge2         | 2.764 (3)  | 2.7174 (10)   | 2.7166 (8)   |
|      | Ge3         | 2.4411 (16)  | 2.4483 (8)  | 2.4419 (6)   |
|      | Ge3         | 2.4476 (13)  | -   | -  |
|      | Ge4         | 2.654 (3)  | -   | -  |
|      | Co1         | 2.92449 (5)  | 2.92731 (1)   | 2.92904 (1)  |
| Co2: | Ge1         | 2.4207 (19)  | 2.4386 (9)  | 2.4367 (8)   |
|      | Ge1         | 2.4421 (18)  | -   | -  |
|      | Ge2         | 2.4081 (17)  | 2.3949 (11)   | 2.3962 (10)  |
|      | Ge2/4       | 2.3764 (19)  | -   | -  |
|      | Ge3         | 2.3690 (15)  | 2.3500 (14)   | 2.3547 (12)  |

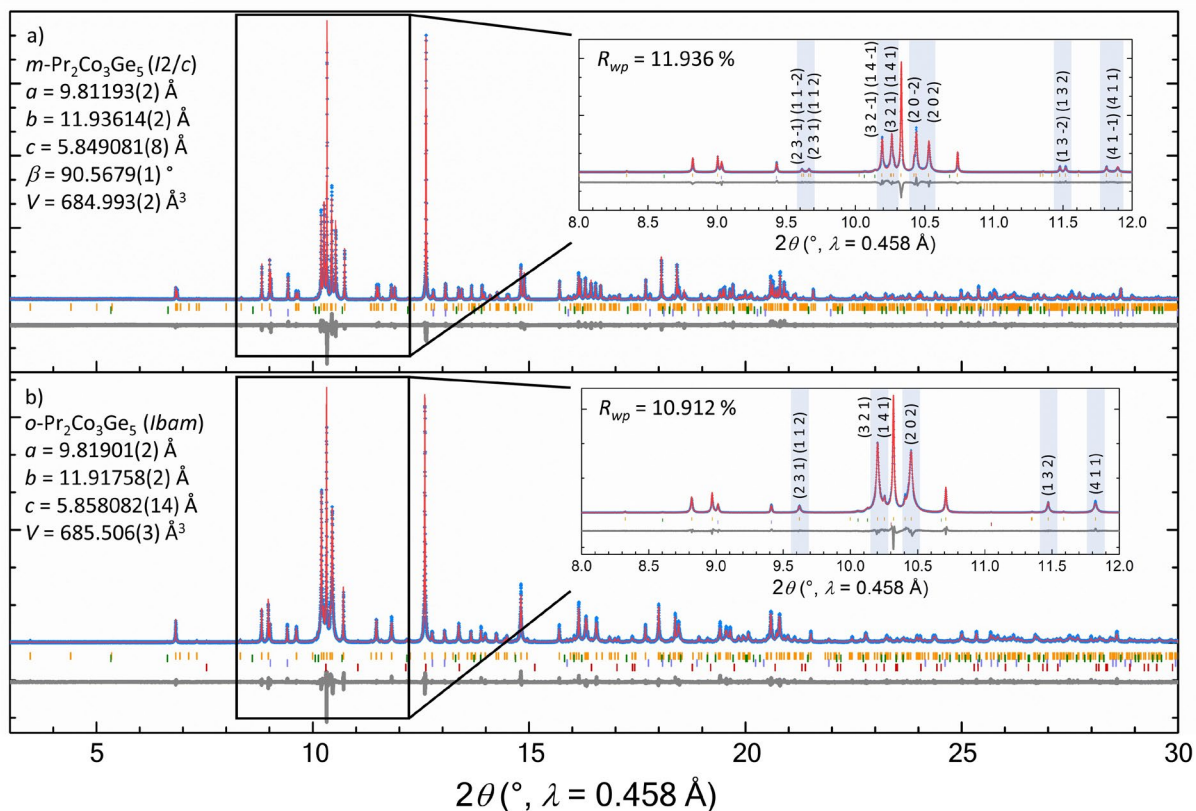


Figure S1. High resolution powder X-ray diffraction of (a)  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  and (b)  $o\text{-Pr}_2\text{Co}_3\text{Ge}_5$ . Observed data, Rietveld refinement, and difference curves are shown in blue, red, and grey, respectively. Tick marks of  $\text{Pr}_2\text{Co}_3\text{Ge}_5$ ,  $\text{PrCoGe}_3$ ,  $\text{Sn}$ , and  $\text{Al}_2\text{O}_3$  are shown in orange, green, purple, and red, respectively. The insets highlight splitting of select reflections corresponding to a loss in symmetry with  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  indexed in the unconventional space group setting  $I2/c$ . The lattice parameters of  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  in the standard setting  $C2/c$  are  $a = 11.37315(2) \text{ \AA}$ ,  $b = 11.93614(2) \text{ \AA}$ ,  $c = 5.849081(8) \text{ \AA}$ ,  $\beta = 120.3803(1)^\circ$ ,  $V = 684.993(2) \text{ \AA}^3$ .

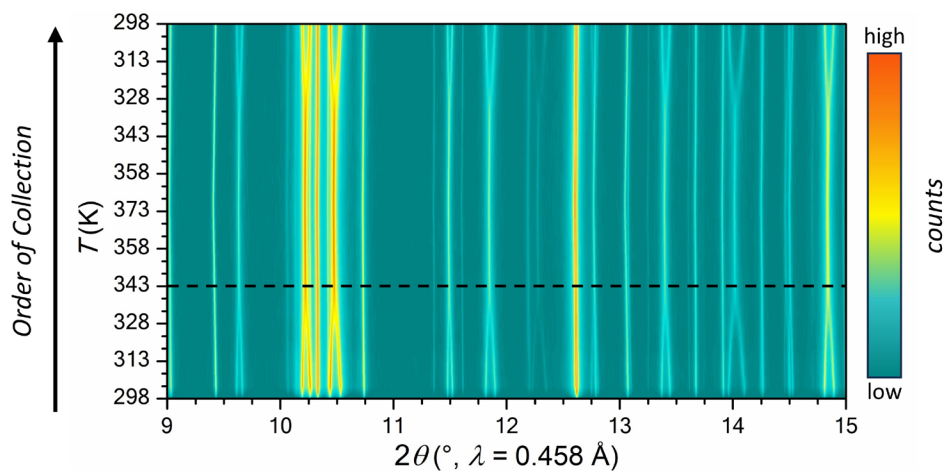


Figure S2. Contour plot of temperature dependent X-ray diffraction data of  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  as obtained from high resolution powder X-ray diffraction. The temperature of phase transformation is given with the dashed black line.

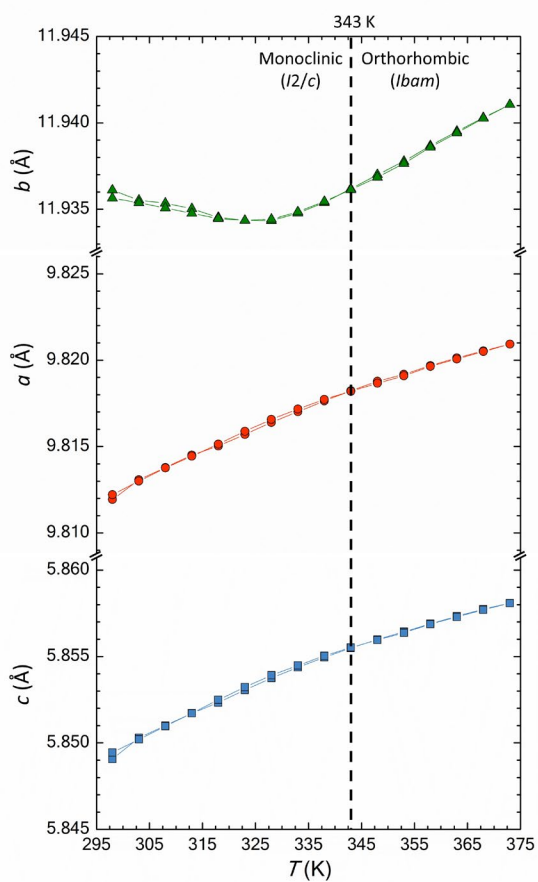


Figure S3. The temperature dependent lattice parameters of  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  as obtained from high resolution powder X-ray diffraction. Lattice parameters  $a$ ,  $b$ , and  $c$  are given as red, green, and blue, respectively.

## Room Temperature Electron-Energy Loss Spectroscopy

Monochromated EEL spectra were collected for both polymorphs from the Pr  $M_{4,5}$  and the Co  $L_{2,3}$  energy ranges (Figs. 2a and 2b, respectively). For Pr, there are two dominant edges with peaks at 928.1 and 947.9 eV, corresponding to the dipole-allowed transitions from  $3d^{5/2}$  to  $4f^{7/2}$  and  $3d^{3/2}$  to  $4f^{5/2}$ , respectively. The  $M_5:M_4$  edge height ratio increases from 1.6:1 to 1.72:1 and the total integrated area, which serves as a measure of unoccupied density of states (shaded area in Fig. 2c), decreases from 8.24 to 6.81 eV\*counts when comparing the room temperature and high temperature structures. A chemical shift is not observed in Pr as the edge onset is similar between the monoclinic and orthorhombic polymorphs; however, there is a dramatic difference in valency, with *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> predominantly Pr<sup>4+</sup> (Pr<sup>*n+*</sup>, *n* = 3.80(5)) and *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> predominantly Pr<sup>3+</sup> (Pr<sup>*n+*</sup>, *n* = 3.00(5)) based on MLLS fits and reference spectra (see Methods). Since only one crystallographically unique Pr atomic site exists in both polymorphs of Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>, the oxidation state of Pr must be in an intermediate valence state in *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>. Pr was observed to be weakly tetravalent in PrFe<sub>10</sub>Mo<sub>2</sub> and PrNi<sub>5</sub> based on X-ray absorption spectroscopy, with valences of 3.08(3) and 3.10(3) respectively (72), but this is far less than what is observed in *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>.

Like Pr, the Co  $L_{2,3}$  edges result from dipole allowed electron transitions; however, for cobalt, these transitions are from the  $2p^{3/2}$  to  $3d^{5/2}$  states and the  $2p^{1/2}$  to  $3d^{3/2}$  states. The edge onset for both polymorphs is similar with the onset slightly lower in *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> (775.06 eV) compared to *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> (775.10 eV). The Co  $L_{2,3}$  edge onset is lower for the orthorhombic structure when compared to the monoclinic structure, implying that the orthorhombic  $3d$  Co electrons possess a lower ionization energy threshold compared to their monoclinic counterparts. In other words, the orthorhombic crystal structure facilitates removal of electrons from the  $3d$  orbitals of Co atoms, resulting in a lower energy requirement for ionization compared to the monoclinic crystal structure. Additionally, the small high energy shift of the Co  $L_{2,3}$  edge onsets in *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> compared to *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> suggest a slightly higher oxidation state of the monoclinic Co. However, the Co  $L_{2,3}$  edge maxima in *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> are at higher energies compared to the monoclinic structure. The intensity of the peaks reflects the occupancy of the relevant orbitals, while the shape informs on hybridization and interactions between the electronic orbitals involved in the orbital transitions. Broader edges are indicative of more rapid decay processes, suggesting that *m*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> contains more unoccupied  $3d$  states compared to *o*-Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>.



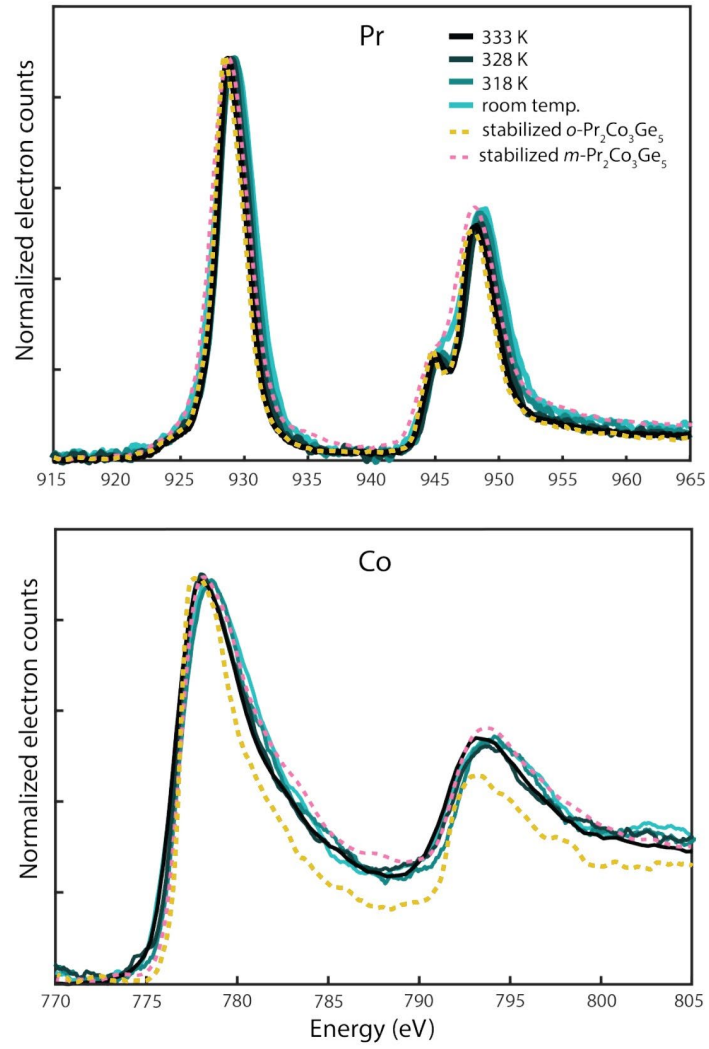


Figure S4. Temperature dependent EEL spectra across the structural phase transformation of  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  overlaid for feature comparison. Data were normalized based on the  $M_5$  or  $L_3$  edge maxima.

## Field Dependent and Temperature Dependent Magnetic Measurements

For the orthorhombic polymorph, temperature dependent magnetic susceptibility measurements along the  $a$ -,  $b$ -, and  $c$ -crystallographic directions result in one magnetic transition above  $H = 0.2$  T. With an applied field of  $H \geq 0.2$  T parallel to the  $a$ -direction, a single broad magnetic transition is visible at  $T_{\text{sp}} = 32.5$  K (Fig. S5a); however, at reduced fields of  $H = 0.05$  T, this magnetic transition shifts to  $T_{\text{sp}} = 30.8$  K and a second feature emerges at  $T_{\text{M}} = 3.4$  K (Fig. S5). With field applied parallel to either the  $b$ - or  $c$ -directions, two magnetic transitions are present for all fields at  $T_{\text{sp}} \sim 32$  K and  $T_{\text{M}} = 3.2$  K or  $T_{\text{M}} = 10$  K, respectively. Unlike the transitions observed along the  $a$ -direction, the magnitude of magnetic ordering along the  $b$ - and  $c$ -directions are strongest at  $T_{\text{M}}$ , with ordering along the  $c$ -direction being significantly more pronounced than the other directions. Additionally, with magnetic fields applied parallel to the  $a$ -direction, there is a slight bifurcation of the zero field-cooled and field-cooled magnetization below  $T = 4$  K for  $H = 0.05$  and  $0.5$ , but no difference is observed for fields applied along the  $b$ - and  $c$ -directions. Compared to the magnetic susceptibility of  $o$ -Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> with a magnetic field of  $H = 0.2$  T applied along the  $a$ -direction, the first transition in  $m$ -Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> occurs at a higher temperature of  $T_{\text{sp}} = 35.3$  K and an additional magnetic transition is observed at  $T_{\text{M}} = 10$  K. The magnetic ordering event with field applied along the  $c$ -direction also shows a shift towards higher temperature ( $T_{\text{sp}} = 34.8$  K).

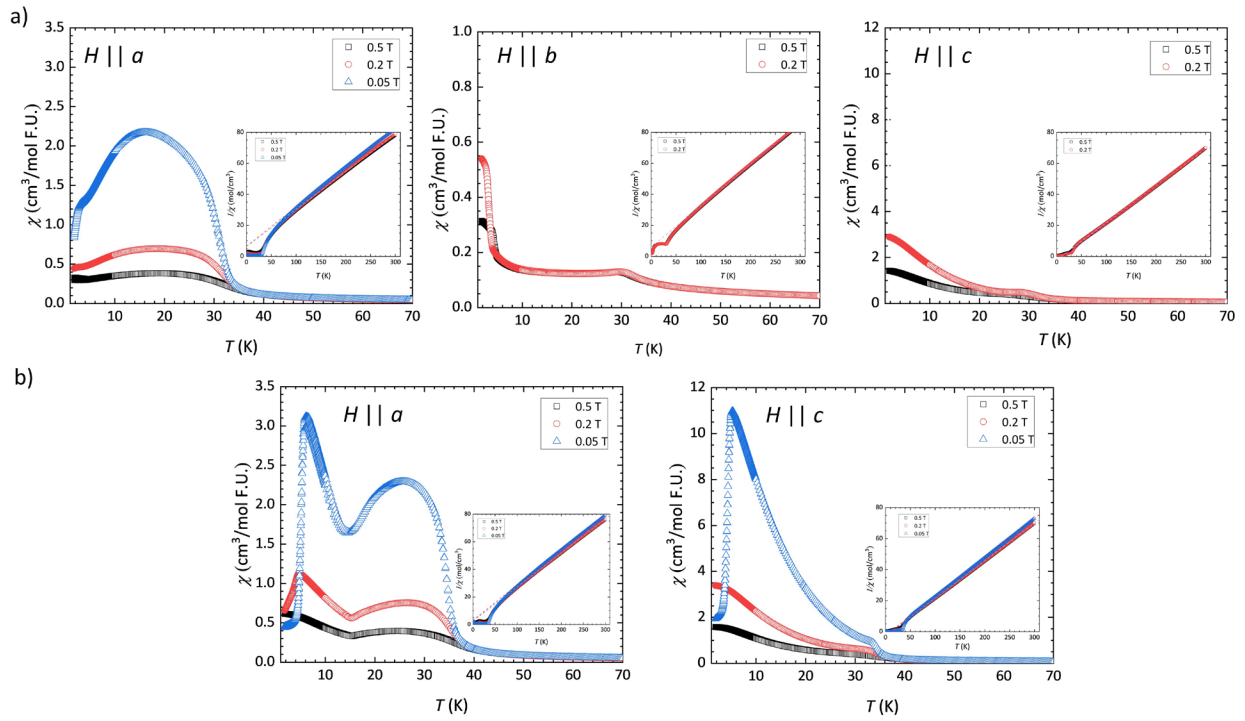


Figure S5. Temperature dependent magnetization of (a)  $o\text{-Pr}_2\text{Co}_3\text{Ge}_5$  and (b)  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  at applied fields of 0.05 T (blue), 0.2 T (red), and 0.5 T (black).

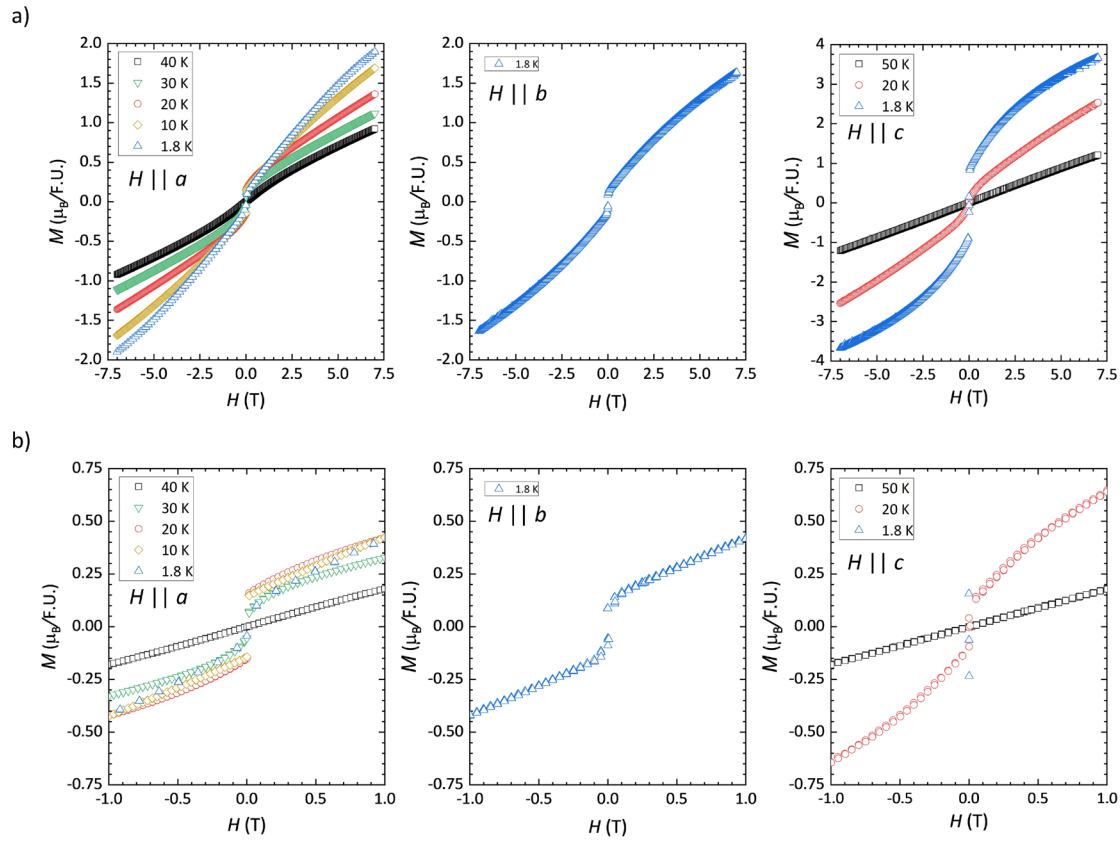


Figure S6. Field dependent magnetization of  $o\text{-Pr}_2\text{Co}_3\text{Ge}_5$  with (a) the applied fields from -7.5 to 7.5 T and (b) -1 T to 1 T.

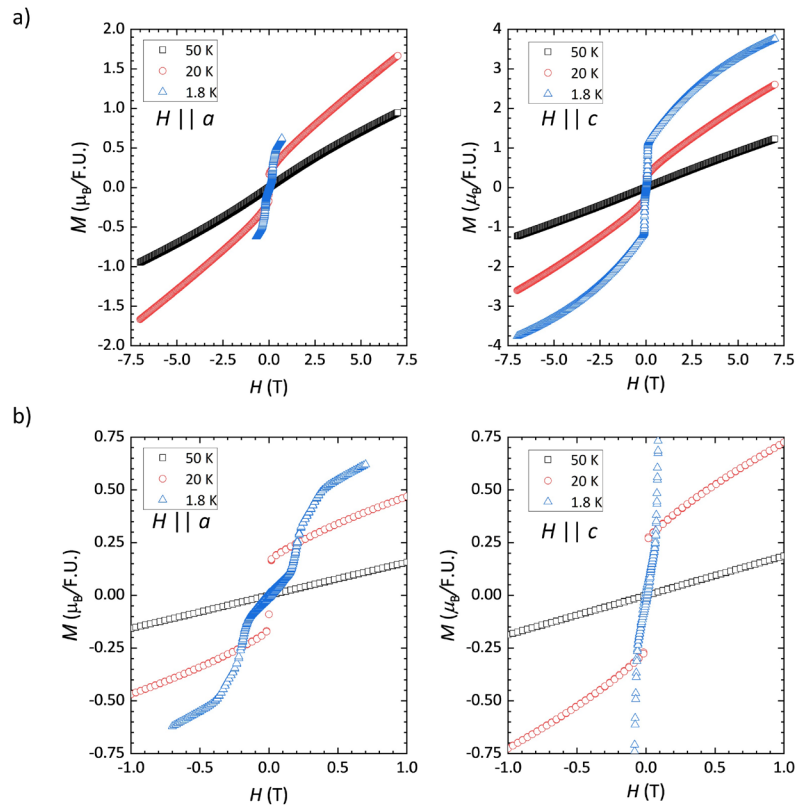


Figure S7. Field dependent magnetization of  $m\text{-Pr}_2\text{Co}_3\text{Ge}_5$  with (a) the applied fields from -7.5 to 7.5 T and (b) - 1 T to 1 T.

Table S3. Summarized Magnetic Susceptibility for  $o$ -Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub> and  $m$ -Pr<sub>2</sub>Co<sub>3</sub>Ge<sub>5</sub>

|  | Applied Field (T)                                    | $\mu_{\text{eff}} (\mu_{\text{B}} \text{Pr}^{-1})$ | $\mu_{\text{eff}} (\mu_{\text{B}} \text{F.U.}^{-1})$ | $\theta_{\text{CW}} (\text{K})$ | $T_{\text{sp}} (\text{K})$ | $T_{\text{M}} (\text{K})$ |    |
|--|--|--|--|---------------------------------|----------------------------|---------------------------|----|
| $o$ -Pr <sub>2</sub> Co <sub>3</sub> Ge <sub>5</sub> | $H // a$ ; 0.5                                       | 4.05 (1)   | 5.72 (2)   | -25.5 (2)                       | 32.5                       | -                         |    |
|  | 0.2  | 4.03 (1)   | 5.70 (2)   | -25.7 (1)                       | 31.9                       | -                         |    |
|  | 0.05   | 3.95 (1)   | 5.58 (1)   | -25.4 (1)                       | 30.8                       | 3.4                       |    |
|  | $H // b$ ; 0.5                                       | 3.87 (1)   | 5.47 (1)   | -22.6 (1)                       | 31.9                       | 4.3                       |    |
|  | 0.2  | 3.86 (1)   | 5.46 (1)   | -22.6 (1)                       | 32.3                       | 3.2                       |    |
|  | $H // c$ ; 0.5                                       | 4.04 (1)   | 5.72 (1)   | 13.4 (1)                        | 31.9                       | 10                        |    |
|  | 0.2  | 4.04 (1)   | 5.71 (1)   | 13.5 (1)                        | 31.3                       | 10                        |    |
|  | $m$ -Pr <sub>2</sub> Co <sub>3</sub> Ge <sub>5</sub> | $H // a$ ; 0.5                                     | 4.02 (1)   | 5.68 (1)                        | -10.4 (1)                  | 36.4                      | 10 |
|  |  | 0.2  | 4.02 (1)   | 5.68 (1)                        | -11.0 (1)                  | 35.3                      | 10 |
| 0.05   |  | 3.95 (1)   | 5.58 (1)   | -12.3 (1)                       | 34.5                       | 10                        |    |
| $H // c$ ; 0.5                                       |  | 4.05 (1)   | 5.72 (1)   | 12.2 (1)                        | 35.7                       | 10                        |    |
| 0.2  |  | 4.05 (1)   | 5.73 (1)   | 11.3 (1)                        | 34.8                       | 10                        |    |
| 0.05   |  | 3.97 (1)   | 5.62 (1)   | 10.2 (1)                        | 34.4                       | 10                        |    |

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