Supplementary Information for

Convection-Enhanced Delivery of Solutes to the Brain Using Electrokinetic Transport

Amir H. Faraji, Andrea S. Jaquins-Gerstl, Alec C. Valenta, Yanguang Ou, and Stephen G. Weber

Corresponding Author: Stephen G. Weber Email: sweber@pitt.edu

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Fig. S1. A collection of fluorescent *in vivo* images demonstrating electrokinetic transport may be directed along anatomical structures within the tissue. Once the infusate reached the corpus callosum, flow occurs along the horizontal track of the axons in this region. Numbers correspond to bregma (anterior to bregma). Slices were 300 µm in thickness.



Fig. S2. An example of directionality *in vivo* of $Ru(bpy)_{3}^{2+}$, from the prefrontal cortex to the striatum with 75 µA applied for 5 hours. Fluorescent images are superimposed onto bright field images. Row C, second column (C2) represents the plane of the infusion cannula and B5 represents the plane of the counter cannula. Slices were cut to 300 µm and sequentially imaged; starting with row A to E. Scale bar is 1,000 µm.



Fig. S3. ECED of $\text{Ru}(\text{bpy})_3^{2+}$ *in vivo* into the prefrontal cortex (top of panel L) to the striatum (panel K) with 75 µA applied for 5 hours from a 100 µm inner diameter fused silica infusion cannula. Fluorescent microscopy images are in panels to the left and their corresponding surface intensity plots are to the right. Although, the $\text{Ru}(\text{bpy})_3^{2+}$ molecules tend to move along the corpus callosum (images H-J), they also move into the striatum as well (images K-R). L represents the plane of the infusion cannula and K represents the plane of the counter cannula. Slices were cut to 300 µm and sequentially imaged. Scale bar is 1,000 µm.



Fig. S4. An example of the thresholding process using NIS Element Advanced Research software for *in vivo* analysis. (A) Black and white 300 µm section of brain tissue with $\text{Ru}(\text{bpy})_3^{2^+}$. (B) Original image using an appropriate fluorescence laser line of $\text{Ru}(\text{bpy})_3^{2^+}$. (C) Post-thresholding image with the ROI coded in blue. Only the threshold area (blue) was used to calculate the V_d . This analysis was performed on all slices containing $\text{Ru}(\text{bpy})_3^{2^+}$, and pixels outside this region were not considered in the calculation of V_d with this methodology.



Fig. S5. Electroosmotic infusion of Bodipy-labeled dextran (10 kDa) and Texas Red-labeled dextran (70 kDa) for 45 min at 25 μ A from a 100 μ m inside diameter fused silica cannula into the thalamus of an adult male rat. Row 1. Brightfield and fluorescence images from controls (current = 0). Blue arrowhead points at cannula tracks. Rows 2a-c: From anterior to posterior, coronal slices were 300



Fig. S6. Reproduction of Fig. 5 in the text without enhanced contrast in the experimental images.



Fig. S7. Solution to the curvilinear coordinate systems module, in which the vector field v was determined. The vector field v follows the curvature of the corpus callosum.



Fig. S8. Mesh elements for the anistropic electrokinetic convention-enhanced delivery (ECED) model. The geometry is finely meshed in the capillaries, at the site of infusion, and in the corpus collosum.



Fig. S9. 3D geometry for ECED model. A- non-corpus callosum brain tissue, B - corpus callosum, C - ventricles, D - counter capillary, E - infusion capillary. All of the boundaries are labeled as numbers and the domains are labeled as letters. Boundaries 2 & 9 indicate boundaries at either end of the corpus callosum. These are important for generating a curvilinear coordinate system for anistropic studies. Boundaries 4 & 10 have equivalent boundaries on the other side of the geometry and are used to generally denote boundaries on both sides. Boundary 11 indicates the walls of the corpus callosum domain. Boundaries 12 and 13 indicate the outer walls of the capillaries that are in contact with the tissue.

Table S1. Boundary conditions for Electric Currents module in COMSOL Multiphysics v5.3 for ECED model. J is the current density, σ is the conductivity, V is the voltage drop, J_e is the external current density source, n is the normal vector, and I₀ is the applied current.

Boundary/Domain	Boundary condition	Equation, if applicable
A, D-F	Current conservation using global coordinate system	$\nabla \cdot \overset{u}{J} = -\nabla \cdot (\sigma \nabla V - \overset{u}{J}_e) = 0$
В	Current conservation using curvilinear coordinate system	$\nabla \cdot \overset{u}{J} = -\nabla \cdot (\sigma \nabla V - \overset{u}{J}_e) = 0$
1, 3-6, 10	Electric insulation	$\overset{\parallel}{n}\cdot\overset{\scriptstyle \perp}{J}=0$
7	Terminal, current	$i = i_0$, where
		$i_0 = -75 \ \mu A$
8	Ground	<i>V</i> = 0

Table S2. Boundary conditions for curvilinear coordinate system. The coordinate system settings are set with respect to the y-axis. This coordinate system is setup so that the normal Cartesian coordinate system orients with respect to the curvature of the corpus callosum. This module computes the vector field v.

Boundary/Domain	Boundary condition	Equation, if applicable
В	Diffusion method	$\nabla \cdot (\nabla U) = 0$
		$\mathbf{v} = \frac{-\nabla U}{ -\nabla U }$
11	Wall	$-\boldsymbol{n}\cdot\nabla\boldsymbol{U}=\boldsymbol{0}$
2	Inlet	Condition on: value
		$U_0 = 1 m$ (default)
9	Outlet	U = 0

Table S3. Boundary conditions for Free and Porous Media Flow for EOPPP model. *u* is the superficial velocity, μ_{eo} is the electroosmotic mobility, *E* is the electric field, *P* is the pressure, L_m is the length of the capillary unaccounted for in the model geometry (the capillaries were truncated to save on computation time), η is the dynamic viscosity, Δu is the difference between the wall velocity and average velocity, *a* is the radius of the capillary, and f_0 is the normal stress.

Boundary	Boundary condition	Equation, if applicable
2, 9, 12-13	No slip walls	$\vec{u} = 0$
5-6	Moving walls	$ \begin{array}{c} \begin{bmatrix} 1 \\ u \\ $
8	"Hagen-Poiseuille inlet"	$\Delta \boldsymbol{P} = \frac{8L_m \eta \Delta \boldsymbol{u}}{\boldsymbol{a}^2}$
7	"Hagen-Poiseuille outlet"	$\Delta \boldsymbol{P} = \frac{8L_m \eta \Delta \boldsymbol{u}}{\boldsymbol{a}^2}$
1, 3, 4, 10	Open boundary	$f_0 = 0$

Table S4. Boundary conditions for Transport of Diluted Species module for EOPPP model. N is the flux, c is the concentration at any time t, c_0 is the initial concentration, and D is the diffusion coefficient.

Boundary/Domain	Boundary condition	Equation, if applicable
2, 5, 6, 9, 12, 13	No flux	$-\overset{\parallel}{n}\cdot\overset{\scriptstyle\scriptstyle}{N}=0$
7	Flux 1	$\overset{\mathbf{u}}{N} = \overset{\mathbf{u}}{n} \cdot (c\overset{\mathbf{u}}{u} - D\nabla c)$
8	Flux 2	$\overset{\mathbf{u}}{N} = \overset{\mathbf{u}}{n} \cdot (c\overset{\mathbf{u}}{u} - D\nabla c)$
8	Concentration	$c = c_{0;} c_0 = 45 \text{ mM}$
1, 3, 4, 10	Open boundary	$\begin{cases} -\stackrel{u}{n} \cdot D\nabla c = 0 & \text{if } \stackrel{u}{n} \cdot \stackrel{u}{u} \ge 0\\ c = 0 & \text{if } \stackrel{u}{n} \cdot u < 0 \end{cases}$
A, B, D	Initial values	$c_0 = 0$
Е	Initial values	$c_0 = 45 \text{ mM}$

Domain(s)	Property	Value
A, B, D, E	Density (p)	1 x 10 ³ kg/m ³
	Permittivity of water (ε_w)	7.1 x 10 ⁻¹⁰ F/m
	Permittivity of vacuum (ε_0)	8.85 x 10 ⁻¹² F/m
	Dynamic viscosity (η)	6.9 x 10 ⁻⁴ Pa s
D, E	Conductivity (σ) of buffer	1.79 S/m
	Capillary ζ-potential	-46.5 mV
А	Tissue ζ-potential	-22.8 mV
	Electroosmotic mobility* (μ_{eo})	5.14 x 10 ⁻⁸ m ² /(V s)
	Electrophoretic mobility* (μ_{ep})	3.34 x 10 ⁻⁸ m ² /(V s)
	Effective charge density* (ρ_{eff})	1166.9 C/m ³
	Permeability (κ)	10 ⁻¹⁵ m ²
	Porosity (ε)	0.2
	Tortuosity (λ)	1.61
	Conductivity of tissue*	0.14 S/m
	$\sigma^* = \sigma(\epsilon/\lambda^2)$	
В	Tissue ζ-potential	-22.8 mV
	Electroosmotic mobility* (μ_{eo})	5.14 x 10 ⁻⁸ m ² /(V s)
	Permeability (κ)	$\kappa_x, \kappa_y, \kappa_z = [1.19, 1.02, 1.00](31)$
	(curvilinear coordinate)	x 10 ⁻¹⁴ m ²
	Porosity (ε)	0.2
	Tortuosity (λ)	$\lambda_x, \lambda_y, \lambda_z = [1.46, 1.70, 1.72]$
	(curvilinear coordinate)	
	Conductivity of tissue*	$\sigma_x, \sigma_y, \sigma_z = [0.16, 0.12, 0.12]$
	$\sigma^* = \sigma(\varepsilon/\lambda^2)$	S/m
	(curvilinear coordinate)	
	Effective charge density*	$\rho_{\text{eff,x}}, \rho_{\text{eff,y}}, \rho_{\text{eff,z}} = [119, 102, 101] C/m^3$
	(ρ_{eff})	

Property	Values
Diffusion coefficient of Ru(bpy) ₃ ²⁺ in	2.7 x 10 ⁻¹⁰ m ² /s
free solution	
Diffusion coefficient of Ru(bpy) ₃ ²⁺ in	2.0 x 10 ⁻¹¹ m ² /s
non-corpus callosum tissue	
Diffusion coefficient of Ru(bpy) ₃ ²⁺ in	$D_x, D_y, D_z = [2.5, 1.8, 1.8]$
corpus callosum (curvilinear coordinate)	x 10 ⁻¹¹ m ² /s
Electrophoretic mobility of Ru(bpy) ₃ ²⁺	3.24 x 10 ⁻⁸ m ² /(V s)
<i>C</i> ₀	45 mM

Table S7. Boundary conditions for Darcy's law module, used to calculate flow rate using pressure driven CED. 3000 Pa was chosen for the pressure boundaries because it induced a comparable flow rate in the infusion capillary as that in ECED model for 75 µA current.

Boundary/Domain	Boundary condition	Equation, if applicable
8	Pressure 1	P = 3000 Pa
7	Pressure 2	P = -3000 Pa
1-6,9-13	No flow	$-\vec{n}\cdot\vec{\rho u}=0$