## **Supplementary Information**

## 1. Support vector machine

The support vector machines are supervised learning models to classify data represented by vectors in multi-dimensional spaces with boundaries defined by associated algorithms. In detail, the training set of the classification problem is in the form:  $\{x_i, y_i\}$ ,  $i = 1, 2, ..., n$ , where  $x_i \in \Re^d$ are vectors representing the data, and  $y_i \in \{+1,-1\}$  are class labels for two classes.

In this study, we used support vector machines with linear kernel, with which the classifier boundaries are hyperplanes in the form  $w \cdot x + b = 0$  where w is the normal vector of the hyperplane and  $b$  is the term determining offset. For separable cases the decision function for classification is then defined as  $f(x) = w \cdot x + b$  so that  $f(x_i) \ge 1$  if  $y_i = 1$  or  $f(x_i) \le -1$  if

 $y_i = -1$ . Thus the margin between two classes is  $\frac{1}{\|u_i\|}$ . SVMs optimize the classification by *w* 2

maximizing the margin and the problem can be formulated as:

$$
\underset{(\mathbf{w},b)}{\arg\min} \left(\frac{1}{2} \|\mathbf{w}\|^2\right) \tag{S1}
$$

subject to  $y_i(\mathbf{w} \cdot \mathbf{x} + b) \ge 1$ , (for any  $i = 1,2,...,n$ )

For non-separable cases, compromise of the decision functions and mislabeling are allowed, which are described by the "slack variables":  $\zeta_i \geq 0, i = 1,2,...,n$ . Thus SVMs optimize the classification by both maximization of the margin and minimization of the penalty caused by the slack variables. The problem is formulated as:

$$
\underset{(\mathbf{w},b,\xi)}{\arg\min} \left( \frac{1}{2} \left\| \mathbf{w} \right\|^2 + C \sum_{i=1}^n \xi_i \right) \tag{S2}
$$

subject to  $y_i(w \cdot x + b) \ge 1 - \xi_i, \xi_i \ge 0$ 

Introducing Lagrange multipliers, we can solve the problem by optimizing the Lagrangian:

$$
\arg\min_{(\mathbf{w},b,\xi)} \max_{(\mathbf{a},\mathbf{\beta})} \frac{1}{2} ||\mathbf{w}||^2 + C \sum_{i=1}^n \xi_i - \sum_{i=1}^n \alpha_i \big[ y_i (\mathbf{w} \cdot \mathbf{x} + b) - 1 + \xi_i \big] - \sum_{i=1}^n \beta_i \xi_i
$$
 (S3)

Therefore the normal vector of the hyperplane is  $w = \sum_{i=1}^{\infty} \alpha_i y_i x_i$ . For data points correctly classified and out of the margin,  $\alpha_i = 0, \xi_i = 0$ . For data points on the margin boundary,  $0 < \alpha_i < C, \xi_i = 0$  and  $f(x_i) = \pm 1$ . For data points within the margin or misclassified,  $\alpha_i = C, \xi_i > 0$ . Any  $x_i$  with  $\alpha_i > 0$  are named support vectors which contribute to define the normal vector of the classifier hyperplane. Therefore, support vectors are those data points on the margin boundary or with compromised decision function, suggesting they are not well classified by the trained classifier. *n i*  $i y_i x_i$ 1  $w = \sum \alpha_i y_i x_i$ 

2. Selection of "median cells"

The "median cells" are single cells that we selected to represent the population morphological difference of two classes in each pairwise SVM comparison. Subsequent to each loop of the SVM training on supercells at supercell size of 5 with the selected features, the trained classifier was employed to classify the original single cells. Single cells with decision functions higher than 1 or lower than -1 were recorded as well classified single cells respectively for two classes. We then selected those single cells which are always well classified by the classifier of each training loop.

In the next step, for each class we calculated the total Euclidean distance from each selected single cell to all the other selected single cells in metric space established with only the selected features. The list of the selected single cells of each class was then sorted according to the total Euclidean distances. We then extracted the binary segmentations of those single cells with the lowest total Euclidean distances to represent the morphology of each class in Fig. 5.

## **Supplementary Table 1**



Explanations of some shape metrics of the total 22 shape metrics









Maximum intensity projections of 3-D z-stack images in xy plane of hBMSCs of FS







Maximum intensity projections of 3-D z-stack images in xy plane of hBMSCs of SC







Maximum intensity projections of 3-D z-stack images in xy plane of hBMSCs of FS+OS







Maximum intensity projections of 3-D z-stack images in xy plane of hBMSCs of SC+OS

**Supplementary Fig 1.** Maximum intensity projections of 3-D z-stack images of actin (red) and nucleus (blue).









Supplementary Fig 2. (a) Shape metrics quantifying cell shapes of hBMSCs in FS, SC, FS +OS and SC+OS. All error bars represent standard error of the mean. (b) Summary of the statistical analysis of each cell shape metrics with 1-way ANOVA and Tukey Multicomparison test (ns: p  $> 0.05$ , \*: p < 0.05, \*\*: p < 0.01, \*\*\*: p < 0.001).



**Supplementary Fig 3.** Flow chart of the training and feature selection procedure followed by the flow chart of subsampling validation for the selected metrics.