nature portfolio

Corresponding author(s):	Steven Lee
Last updated by author(s):	May 27, 2024

Reporting Summary

Nature Portfolio wishes to improve the reproducibility of the work that we publish. This form provides structure for consistency and transparency in reporting. For further information on Nature Portfolio policies, see our <u>Editorial Policies</u> and the <u>Editorial Policy Checklist</u>.

_				
· ·	+~	+ 1	st	100
`	_		\sim 1	11 \

For	all st	atistical analyses, confirm that the following items are present in the figure legend, table legend, main text, or Methods section.
n/a	Cor	nfirmed
		The exact sample size (n) for each experimental group/condition, given as a discrete number and unit of measurement
	\boxtimes	A statement on whether measurements were taken from distinct samples or whether the same sample was measured repeatedly
\boxtimes		The statistical test(s) used AND whether they are one- or two-sided Only common tests should be described solely by name; describe more complex techniques in the Methods section.
\boxtimes		A description of all covariates tested
\boxtimes		A description of any assumptions or corrections, such as tests of normality and adjustment for multiple comparisons
		A full description of the statistical parameters including central tendency (e.g. means) or other basic estimates (e.g. regression coefficient) AND variation (e.g. standard deviation) or associated estimates of uncertainty (e.g. confidence intervals)
\boxtimes		For null hypothesis testing, the test statistic (e.g. <i>F</i> , <i>t</i> , <i>r</i>) with confidence intervals, effect sizes, degrees of freedom and <i>P</i> value noted <i>Give P values as exact values whenever suitable.</i>
\boxtimes		For Bayesian analysis, information on the choice of priors and Markov chain Monte Carlo settings
\boxtimes		For hierarchical and complex designs, identification of the appropriate level for tests and full reporting of outcomes
\boxtimes		Estimates of effect sizes (e.g. Cohen's d, Pearson's r), indicating how they were calculated
		Our web collection on statistics for biologists contains articles on many of the points above

Software and code

Policy information about <u>availability of computer code</u>

Data collection

The open-source software Micro-Manager (version 2.0.0) was used for microscope control and data acquisition, and downloaded from https://micro-manager.org/Download_Micro-Manager_Latest_Release. A Micro-Manager device adapter for the polarization camera used in this work was included as part of the free image acquisition software ThorCam (v3.6.0, Thorlabs), which was downloaded from https://www.thorlabs.com/software_pages/ViewSoftwarePage.cfm?Code=ThorCam.

Data analysis

Basic image inspection and image cropping was performed in ImageJ (v1.53t). Single-molecule data was analyzed using custom MATLAB (version R2022a, Mathworks) application POLCAM-SR for which the source code and installer are available on GitHub at https://github.com/ezrabru/POLCAM-SR. Diffraction-limited, high-dimensional polarisation camera image processing and visualization was performed using a custom plugin napari-polcam for the open source software napari (v0.4.17), installed using the instructions at https://napari.org/stable/. The source code for the plugin is available at https://github.com/ezrabru/napari-polcam.

For manuscripts utilizing custom algorithms or software that are central to the research but not yet described in published literature, software must be made available to editors and reviewers. We strongly encourage code deposition in a community repository (e.g. GitHub). See the Nature Portfolio guidelines for submitting code & software for further information.

Data

Policy information about availability of data

All manuscripts must include a data availability statement. This statement should provide the following information, where applicable:

- Accession codes, unique identifiers, or web links for publicly available datasets
- A description of any restrictions on data availability
- For clinical datasets or third party data, please ensure that the statement adheres to our policy

The datasets generated as part of this study were uploaded to Zenodo: pixel-dependent camera calibration results (\url{https://doi.org/10.5281/zenodo.10578307}), single SYTOX Orange on a cover glass (\url{https://doi.org/10.5281/zenodo.10469322}), PAINT data of single Nile red dyes binding to lipid bilayer-coated silica microspheres (\url{https://doi.org/10.5281/zenodo.10469444}), TAB-PAINT data (\url{https://doi.org/10.5281/zenodo.10470795}), dSTORM phalloidin-AF488 (\url{https://doi.org/10.5281/zenodo.10470982}), dSTORM phalloidin-AF647 (\url{https://doi.org/10.5281/zenodo.10732697}) and T cells (\url{https://doi.org/10.5281/zenodo.10471496}).

Human research participa	pants
--------------------------	-------

Policy information at	out studies involving human research participants and Sex and Gender in Research.					
Reporting on sex a	nder n.a.					
Population charact	opulation characteristics n.a.					
Recruitment	n.a.					
Ethics oversight	n.a.					
Note that full informati	on on the approval of the study protocol must also be provided in the manuscript.					
Field-spec	cific reporting					
Please select the one	below that is the best fit for your research. If you are not sure, read the appropriate sections before making your selection.					
Life sciences	Behavioural & social sciences Ecological, evolutionary & environmental sciences					
For a reference copy of the	document with all sections, see nature.com/documents/nr-reporting-summary-flat.pdf					
Life scien	ces study design					
All studies must discl	ose on these points even when the disclosure is negative.					
Sample size	All experiments used in this study have been performed at least 3 times, to assure results generated by the presented method are repeatable.					
	ocalisations with less than 500 detected photons were excluded from all single-molecule datasets in this study, to avoid biased orientation estimates (as explained in the manuscript).					
' 1	ment presented in this work was replicated successfully at least 3 times to assure repeatability of the results. Single dye on glass or was replicated successfully >10 times on different optical setups, days, sample regions and different dyes. PAINT imaging of lipids microspheres was successfully repeated >3 times on separate days and sample regions. TAB-PAINT imaging of alpha-synuclein uccessfully repeated >3 times on different optical setups, days and sample regions. dSTORM imaging of the actin network of HeLa ccessfully repeated 3 times (3 cells per labelling method). Live T cell imaging was successfully repeated 3 times on separate days at sample regions.					
Randomization (Randomization is not relevant to this study.					
Blinding	linding is not relevant to this study					

Reporting for specific materials, systems and methods

We require information from authors about some types of materials, experimental systems and methods used in many studies. Here, indicate whether each material, system or method listed is relevant to your study. If you are not sure if a list item applies to your research, read the appropriate section before selecting a response.

Materials & experime	ntal systems	Methods
n/a Involved in the study		n/a Involved in the study
Antibodies		ChIP-seq
☐ ☐ Eukaryotic cell lines		Flow cytometry
Palaeontology and a	rchaeology	MRI-based neuroimaging
Animals and other o	rganisms	
Clinical data		
Dual use research of	concern	
1		
Antibodies		
Antibodies used OKT3 antibody (provided by		the Human Immunology Unit, WIMM, Oxford, UK)
Validation Unknown		
Eukaryotic cell line	es	
Policy information about <u>ce</u>	II lines and Sex and Gende	<u>r in Research</u>
COS7 cells: derived codes for wild type		rom cells isolated from the cervix of a 31-year-old female with adenocarcinoma. rom the CV-1 cell line (ATCC CCL-70) by transformation with an origin defective mutant of SV40 which antigen. This is an African green monkey kidney fibroblast-like cell line. of the Jurkat-FHCRC cell line (ATCC TIB-152), established from the peripheral blood of a 14-year-old, Jkemia patient.
Authentication The cell lines used v		ere not authenticated.
/ 1		T cells are periodically tested for mycoplasma contamination and tested negative. It is unknown were tested for mycoplasma contamination.
Commonly misidentified lines (See ICLAC register)		