

26 **Supplementary Discussion 1. Contribution of adsorption and degradation to electrochemical** 27 **removal of estradiol**

- 28 To study the electrochemical removal process as a function of the filtration volume, the mass balance
- 29 analysis was conducted for the experiment at standard conditions within different permeate volume
- 30 range (Supplementary Figure 1).

Supplementary Figure 1. Contribution of electrochemical adsorption and degradation to the mass removal of E2 within the CNT EMR as a function of the permeate volume. $c_{f,E2} = 1 \mu g L$ ¹, $V_{cell} = 1.6 \text{ V}, J_f = 150 \text{ L m}^{-2} \text{ h}^{-1}$ (5 mL min-1), 1 mM NaHCO3, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L -1 MeOH, pH 8.2±0.2, 23 \pm 1 °C. Voltage on at 500 mL. Error bars represent propagated error from operational parameter variations and analytical error.

31 At 500 mL of permeate, the total mass of removed E2 was $63\pm1\%$, solely attributed to adsorption.

32 Upon activating the voltage at 500 mL, total mass removal increased from $63\pm1\%$ to $76\pm10\%$ as the

33 permeate volume increased from 500 to 1000 mL.

34 The contribution from degradation to total mass removal grew from 0 to $61\pm7\%$ over the same volume 35 range.

36 Meanwhile, the contribution from adsorption decreased from $63\pm1\%$ to $19\pm3\%$ as the permeate 37 volume increased from 500 to 800 mL and then stabilized upon further increasing the volume to 1000 38 mL.

39 **Supplementary Discussion 2. Electrochemical degradation of steroid hormone at varying** 40 **parameters**

 The influence of cell voltage, water flux, initial concentration and SH type on the electrochemical degradation was investigated. The profiles of the normalized SHs concentration and the evolution of UHPLC-FSA chromatograms *vs.* cumulative permeate volume for all the electrochemical experiments are shown below. To ascertain the stable conditions during the electrochemical degradation experiments, the variations in the parameters, including pH, transmembrane pressure, conductivity, and temperature were monitored and recorded along with the experiments.

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Data for experiments at varying cell voltage

 Supplementary Figure 2 and Supplementary Figure 3 show the changes of the normalized SHs concentration and the evolution of UHPLC-FSA over 1 L of cumulative permeate volume for experiments at varying cell votage. Supplementary Figure 4 presents the variation of the system conditions during the experiments.

Supplementary Figure 2. Effect of cell voltage on the electrochemical degradation of E2 expressed

55 as normalized (A) E2 concentration in permeate (c_p/c_f) , (B) ³H activity in permeate $(c_{p,3H}/c_{f,3H})$, 56 (C) concentration of byproduct-3m $(c_{p,prod3}/c_{f,prod3})$, and (D) concentration of byproduct-8m

- 57 $(c_{p,prod8}/c_{f,prod8})$ in the permeate *vs.* accumulated permeate. $c_{f,E2} = 1 \mu g L^{-1}$, $J_f = 150$ L m⁻² h⁻¹ (5 58 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2 \pm 0.2,
- 23±1 ℃. Error bars represent propagated error from operational parameter variations and analytical error.
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- The steady-state normalized concentration of E2 in the permeate significantly decreased from
- 0.61 \pm 0.07 to 0.03 \pm 0.01 when the cell voltage was raised from 0.6 to 1.2 V, thereafter stabilizing upon
- further increasing the voltage to 2.5 V.
- 64 Beyond a cell voltage of 1.2 V, the normalized concentration of ${}^{3}H$ surpassed 1 immediately after the voltage was applied and continued to rise steadily with additional voltage increases. Following a
- 66 cumulative permeate volume of 700 mL, the normalized concentration of ${}^{3}H$ leveled off, approaching
- 1. Concurrently, the normalized concentrations of the two byproducts in the permeate exhibited an
- increase in tandem with the cell voltage.

 Supplementary Figure 3. UHPLC-FSA chromatograms of E2 during the electrochemical degradation with increasing accumulated permeate volume at varying cell voltage (A) 0.88, (B)

- 71 1.18, (C) 1.4, (D) 1.66, (E) 1.84, (F) 2.03, and (G) 2.5 V. $c_{f,E2} = 1 \mu g L^{-1}$, $J_f = 150 L m^{-2} h^{-1}$ (5 mL
- 72 min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.

No discernible peaks corresponding to byproducts were detected at 0.6 V, whereas at 0.9 V, three

byproduct peaks appearing at 3, 5, and 8 minutes. With an increase in voltage, the peak associated

with byproduct-5m vanished.

Supplementary Figure 4. Variations of (A) conductivity, (B) pH, (C) temperature conductivity, and

 (D) transmembrane pressure during electrochemical filtration experiments at varying cell voltage. 78 $c_{f,E2} = 1 \mu g L^{-1}$, $J_f = 150$ L m⁻² h⁻¹ (5 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH,

79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.

The system parameters remained stable during the filtration exeperiments.

Data for experiments at varying flux

 Supplementary Figure 5 and Supplementary Figure 6 show the changes of the normalized SHs concentration and the evolution of UHPLC-FSA over 1 L of cumulative permeate volume for experiments at varying flux. Supplementary Figure 7. presents the variation of the system conditions during the experiments.

Supplementary Figure 5. Effect of water flux on the electrochemical degradation of E2 expressed as

- 88 normalized (A) E2 concentration in permeate $(c_{p,E2}/c_{f,E2})$, (B) ³H activity in permeate
- 89 ($c_{p,3H}/c_{f,3H}$), (C) concentration of byproduct-3m ($c_{p,\text{met3}}/c_{f,\text{met3}}$), and (D) concentration of
- 90 byproduct-8m $(c_{p,mets}/c_{f,mets})$ in the permeate *vs.* accumulated permeate. $c_{f,E2} = 1 \mu g L^{-1}$, $V_{cell} =$
- 91 1.66 V, 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2 \pm 0.2,
- 23±1 ℃. Error bars represent propagated error from operational parameter variations and analytical error.
- 94 Elevating the flux from 30 to $1500 \text{ L m}^{-2} \text{h}^{-1}$ had a negligible impact on the steady-state concentration
- 95 of E2, which observed a slight increase from 0.02 ± 0.01 to 0.14 ± 0.05 .
- 96 After activating the voltage, the normalized concentration of ${}^{3}H$ in the permeate rose as the flux
- decreased. Similarly, the normalized concentration of byproducts in the permeate also augmented
- with the reduction in flux.
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100 Supplementary Figure 6. UHPLC-FSA chromatograms of E2 during the electrochemical

- 101 degradation with increasing accumulated permeate volume at varying flux (A) 30, (B) 150, (C) 600,
- 102 (D) 900, (E) 1200 and (F) 1500 L m⁻² h⁻¹. $c_{f, E2} = 1 \mu g L^{-1}$, $V_{cell} = 1.6 \text{ V}$, 1 mM NaHCO₃, 10 mM
- 103 NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.

104 In the UHPLC chromatograms, two byproducts appearing at approximately 3 and 8 minutes were

105 detected at flux of 30 and 150 L $m^{-2}h^{-1}$.

106 A byproduct emerging at 5 minutes became evident when the flux was increased to 300 L m⁻² h⁻¹. The

107 peak area of byproduct-5m initially rose with an increase in flux to 600 L $m^{-2} h^{-1}$ and then declined 108 upon further increasing the flux to $1500 \text{ L m}^{-2} \text{h}^{-1}$.

110 Supplementary Figure 7. Variations of (A) conductivity, (B) pH, (C) temperature conductivity, and 111 (D) transmembrane pressure during electrochemical filtration experiments at varying flux. $c_{f, E2} = 1$ 112 μ g L⁻¹, $V_{cell} = 1.6 \text{ V}$, 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 113 8.2 ± 0.2 , 23 ± 1 °C.

114 The temperature at 30 L m⁻² h⁻¹ exhibited large variation, which was likely due to the sensors being

115 accidentally touched by the operator.

116 The large variation in pressure at high flux may be attributed to the pulsating nature of the peristaltic 117 pump. Peristaltic pumps operate by compressing and releasing a length of tubing, inherently

118 producing a pulsating flow. This effect tends to be more significant at higher fluxes, where the

119 pulsations can greatly influence pressure stability.

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Data for experiments at varying steroid hormone concentration

 Supplementary Figure 8. and Supplementary Figure 9. show the changes of the normalized SHs concentration and the evolution of UHPLC-FSA over 1 L of cumulative permeate volume for experiments at varying E2 concentration. Supplementary Figure 10. presents the variation of the system conditions during the experiments.

Supplementary Figure 8. Effect of SH concentration on the electrochemical degradation of E2

- 128 expressed as normalized (A) E2 concentration in permeate $(c_{p,E2}/c_{f,E2})$, (B) ³H activity in permeate
- 129 $(c_{p,3H}/c_{f,3H})$, (C) concentration of byproduct-3m $(c_{p,met3}/c_{f,met3})$, and (D) concentration of
- 130 byproduct-8m $(c_{p,mets}/c_{f,mets})$ in the permeate *vs.* accumulated permeate. $V_{cell} = 1.6 \text{ V}, J_f = 150 \text{ L}$
- 131 m⁻² h⁻¹ (5 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH
- 8.2±0.2, 23±1 ℃. Error bars represent propagated error from operational parameter variations and analytical error.
- At elevated concentrations of E2, the membrane becomes saturated with E2 more quickly.
- The steady-state normalized concentration of E2 remained relatively constant across the
- 136 concentration range of 50 to 500,000 ng L^{-1} , but sharply increased to 0.66 \pm 0.07 at an E2 concentration
- 137 of 10^6 ng L⁻¹.
- 138 After activating the voltage, the normalized concentration of ${}^{3}H$ in the permeate decreased with an
- 139 increase in E2 concentration from 10^2 to 10^6 ng L⁻¹, a trend that was similarly observed for the
- 140 normalized concentration of byproducts in the permeate.

- 141 Supplementary Figure 9. UHPLC-FSA chromatograms of E2 during the electrochemical
- 142 degradation with increasing accumulated permeate volume at varying flux (A) 50, (B) 10^2 , (C) 10^3 ,
- 143 (D) 10^4 , (E) 10^5 , (F) $5 \cdot 10^5$, and (G) 10^6 ng L⁻¹. $c_{f,E2} = 1$ µg L⁻¹, $V_{cell} = 1.6$ V, $J_f = 150$ L m⁻² h⁻¹ (5
- 144 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 ℃.
- The peak area of the byproducts showed a consistent decrease as the E2 concentration increased from
- $10²$ to $10⁶$ ng L⁻¹. However, this decrease should not be interpreted as fewer byproducts being
- generated at higher concentrations.
- 149 The reason is that feed solutions with E2 concentrations above 100 ng L^{-1} were composed of a mixture
- of radiolabeled and non-labeled E2, and the non-labeled E2 was not detectable using the UHPLC-
- FSA method.

 Supplementary Figure 10. Variations of (A) conductivity, (B) pH, (C) temperature conductivity, and (D) transmembrane pressure during electrochemical filtration experiments at varying concentration. 155 $c_{f,E2} = 1 \text{ µg } L^{-1}$, $V_{cell} = 1.6 \text{ V}$, $J_f = 150 \text{ L m}^{-2} \text{ h}^{-1}$ (5 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2

156 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.

The system parameters remained stable during the filtration exeperiments.

Data for experiments at varying steroid hormone types

- Supplementary Figure 11. shows the changes of the normalized SHs concentration and the evolution
- of UHPLC-FSA over 1 L of cumulative permeate volume for experiments at varying SH types.
- Supplementary Figure 12. presents the variation of the system conditions during the experiments.

- Supplementary Figure 11. UHPLC-FSA chromatograms of E2 during the electrochemical
- degradation with increasing accumulated permeate volume at varying flux (A) testosterone, (B) 164 progesterone, (C) estradiol and (D) estrone. $c_{f,SH} = 1 \mu g L^{-1}$, $V_{cell} = 1.6 \text{ V}$, $J_f = 150 \text{ L m}^{-2} \text{ h}^{-1}$ (5 mL
- 165 min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.
- No significant byproducts were detected in the UHPLC chromatograms for for T and P.

 Supplementary Figure 12. Variations of (A) conductivity, (B) pH, (C) temperature conductivity, and (D) transmembrane pressure during electrochemical filtration experiments at varying SH types. 170 $c_{f,SH} = 1 \mu g L^{-1}$, $V_{cell} = 1.6 \text{ V}$, $J_f = 150 \text{ L m}$ m (5 mL min⁻¹), 1 mM NaHCO₃, 10 mM NaCl, 27.2 mg

171 L⁻¹ EtOH, 79.2 mg L⁻¹ MeOH, pH 8.2±0.2, 23±1 °C.

The change in the pattern of pressure fluctuations before and after 300 mL permeate volume for P

and T was likely due to a decrease in the intervals of data sampling, resulting in a more continuous

- line before 300 mL.
- **Supplementary Methods**

Supplementary Discussion 3. Experimental system and protocol

Electrochemical filtration system

 A custom-built flow-through electrochemical filtration set-up (Figure 1) was used in this work for investigation of SH removal with the CNT electrochemical membrane. The experimental setup is comprehensively equipped with various key components: A thermostatic circulator (Pilot One CC- K6s, Huber, Germany) is connected to a 1-L jacketed glass container to maintain the temperature of 182 the feed solution at 23 ± 1 °C, a peristaltic pump (07528-30, MasterFlex, USA) is utilized to drive the

- influent solution, a commercial electrochemical filtration cell (CF016A, SterliTech, USA), with its
- voltage regulated by a direct current power supply (DPPS 60-15, VoltCraft, Germany). The
- transmembrane pressure is monitored by in-line pressure sensors (0-25 bar, WIKA A-10, Alexander
- Wiegand SE & Co. KG, Germany) on both sides of the cell. A pH meter (pH/cond 3320, WTW,
- Germany) equipped with an electrode (SenTix81, WTW, Germany) and a conductivity sensor (CR-

EC, JUMO, Germany) are employed for the measurement of pH and conductivity of the feed solution.

Further, the temperature and conductivity of the permeate are assessed using an in-line thermocouple

(NI USB-TC01, NI, USA) and another conductivity sensor (CR-EC, JUMO, Germany). Finally, a

- data acquisition card (DAQ, USB-6000, NI, USA) is integrated into the system for the acquisition
- and management of data from these various components.

Electrochemical filtration cell

- The EMR (Supplementary Figure 13.) used in this work, constructed from durable acrylic, is designed
- for the study of electrochemical strategies within an electrochemical membrane in a flow-through
- configuration.

Supplementary Figure 13. Schematic diagram of the electrochemical membrane reactor.

- Its central feature is an electrochemical membrane with a working area of 20 cm² (4.5 cm x 4.5 cm),
- serving as the flow-through anode. Opposite to this, a stainless steel plate positioned 2.3 mm apart

from the membrane functions as the cathode, with good conductivity and strength. Other design of

- the cell includes a titanium rod connected to the cathode and a platinum (Pt) wire atop the membrane,
-
- facilitating electrical connections to an external power supply.

Electrochemical filtration protocol

- 203 All electrochemical filtration experiments were conducted in dead-end mode, following a protocol
- 204 outlined in Supplementary Table 1.

No.	Step	Conditions	Justification	
$\mathbf{1}$	Purging of the pump with MilliQ	90 mL min ⁻¹ for 30 s of MilliQ with valve \odot & valve \odot open, and with valve \odot closed	-Remove the air bubbles in the pump head	
$\overline{2}$	Flushing the system with MilliQ	40 mL min ⁻¹ for 2 min of MilliQ with valve \odot closed, and valve \odot & \odot open (cross-flow)	Remove the bubbles in the system	
3	Permeability	- Close valve $\textcircled{1} \& \textcircled{3}$ closed, and open valve $\circled{2}$ (dead-end)	Evaluate the membrane permeability before the	
		- Run different flow rates $(10, 7.5, 5, 2,$ and 1 mL min^{-1} for 5 min and collect the pressure data	experiments	
$\overline{4}$	Pure water flux	Run 10 mL min ⁻¹ (300 L m ⁻² h ⁻¹) of MilliQ for 40 min and collect the pressure data	- Achieve stable flux prior to the experiment	
\mathfrak{S}	Preparation of conductivity and pH meters	Put the conductivity and pH in the feed tank and turn them on	Monitor the conductivity and pH in the feed solution	
6	Power supply connection and setting	- Connect the anode and cathode to the power supply	Apply electric potential on the membrane	
		- Set the required applied voltage		
τ	Setting pump flowrate	Set the required pump flowrate	Drive the influent at a constant flow rate	
8	Preparation of vials for permeate sample	Label the sample vials and put under the switching valve for taking samples during the filtration		
9	Adsorption	- Switch the inlet tube to $1 \mu g L^{-1}$ SH feed solution	Determine the adsorption of SHs on the EM	
		- Run with power supply off for 500 mL		
		- Take a sample of the feed solution before starting adsorption phase		
10	Electrochemical degradation	-Power supply is switched on while the working flowrate is still kept	Determine the degradation efficiency of SHs on the EM	
		-The volume of filtered SHs is 500 mL		
11	Flushing the system with MilliQ	Repeat step 1 and 2 with MilliQ	Remove the residual SH from the system	
12	Permeability	Repeat step 3 with MilliQ	Evaluate the membrane permeability after the experiments	
13	Lines cleaning	Clean each line of the switching valve using MilliQ at 10 mL min ⁻¹ for 5 min	Clean the lines for sample collections	

205 Supplementary Table 1. Experiment protocol for electrochemical filtration experiments.

Supplementary Discussion 4. Membrane characterization

Pure water flux

 Pure water flux of the electrochemical CNT membrane was measured over the transmembrane pressure, as shown in Supplementary Figure 14..

Supplementary Figure 14. Pure water flux for the fresh electrochemical CNT membrane.

- The pure water flux of the CNT membrane across the transmembrane pressure ranging from 1 to 20
- 212 bar demonstrated a perfect linear relationship $(R^2=1)$. Error bars represent propagated error from
- operational parameter variations and analytical error.
- 214 Permeability of the membrane was determined to be $218 \pm 1 \text{ L m}^{-2} \text{ h}^{-1}$ bar as the slope of the linear fit
- of water flux vs. transmembrane pressure.

Measurement of membrane surface resistivity

- The intrinsic resistivity of the CNT membrane was measured using a four-point probe (4PP,
- 218 Supplementary Figure 15)¹ with specifics provided in
- Supplementary Table 2.

Supplementary Figure 15. Schematic diagram of a collinear four-point probe measurement.

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221 Supplementary Table 2. Specifications of the four-point probe source meter and probe head.

222 In the 4PP measurement, current *I* passes between the two outer probes while the resultant voltage 223 drop V is measured across the two inner probes. Separating current injection and voltage 224 measurement eliminates the contact resistance because the two probes that detect voltage, draw little 225 current 2 . To avoid the edge effects, which refered to disturbances in the electrical field near the edges 226 of the material, it was ensured that the distance from any probe to the nearest boundary (a) was at 227 least five times greater than the probe spacing $(1.016 \text{ mm})^3$. The resistivity measured by 4PP is 228 determined to be $7.2 \cdot 10^{-4} \Omega \cdot m$ using Eq. (S1):

$$
\rho = \frac{V_c}{I} h_m f \tag{S1}
$$

229 where $I(A)$ is the applied current, $V_c(V)$ is the detected voltage, h_m is the thickness of the sample 230 (2·10⁻⁶ m⁴), and f is a geometric factor. Since $h_m \le 5$ s, f is determined as π/ln2³.

231 **Zeta-potential**

232 To characterize the surface charge of the CNT membrane as a function of pH, the zeta-potential were 233 measured at pH ranging from 2 to 10 in 10 mM NaCl electrolyte solution (Supplementary Figure 16).

Supplementary Figure 16. Zeta-potential of CNT membranes as a function of pH. 10 mM NaCl electrolyte solution, pH adjustment using 0.05 M HCl and 0.05 M NaOH.

 The CNT membrane exhibited a negative surface charge from pH 2 to 10, likely attributable to the – COOH groups on the surface of the CNTs.

Three electrode set-up

The electrochemical surface potential of the CNT membrane were assessed through an open circuit

potential measurement in a three-electrode configuration. Supplementary Figure 17 illustrates this

setup, comprising a CNT membrane as the working electrode, a platinum (Pt) wire as the counter

electrode, and a Ag/AgCl electrode acting as the reference electrode.

Membrane surface potential at varying cell voltage

Supplementary Figure 18. shows the electrochemical surface potential of the CNT membrane

measured at varying applied cell voltage from 0.6 to 2.5 V.

Supplementary Figure 18. Membrane surface potentials *vs*. Ag/AgCl at varying cell voltage in 10 mM NaCl and 1 mM NaHCO₃.

 The surface potentials of the CNT membrane remain stable over time across all cell voltages. The surface potential without application of a voltage was determined to be 0.19 V in the electrolyte 247 containing 10 mM NaCl and 1 mM NaHCO₃. In 10 mM NaCl and 1 mM NaHCO₃ electrolyte, the CNT membrane exhited lower surface potentials than the apllied cell voltage (ranged from 0.6 to 2.5

249 V), primarily due to the Ohmic drop across the electrolyte, electrode materials, and interfaces.

250 **Supplementary Discussion 5. Characterics and analytical methods for radiolabeled steroid** 251 **hormone**

252 **Characteristics of steroid hormone**

253 Four SH types, estrone (E1), β-estradiol (E2), progesterone (P), and testosterone (T), were used as 254 surrogates micropollutants in aquatic environment in this study, of which the structure and properties 255 are summarized in Supplementary Table 3. $6-16$.

	Estrone (E1)	Estradiol (E2)	Progesterone (P)	Testosterone (T)
Chemical structure	н 3 _H Ĥ H _O 3 _H 3 _H	OH н 3 _H Ā. HO [*] 3 _H 3н	OH зH $\rm{^3H}$ 3 _H 3 _H	3H 3 _H
Formula	$C_{18}H_{22}O_2$	$C_{18}H_{24}O_2$	$C_{19}H_{28}O_2$	3 _H $C_{21}H_{30}O_2$
Molecular weight $(g \text{ mol}^{-1})$	270.4	272.4	314.5	288.4
pKa ¹	$10.3 - 10.8$	10.2-10.7		
Stokes diameter $(nm)^2$	$0.79 - 0.82$	0.80	0.86	0.82
Solubility in H_2O $(g L^{-1})^3$	$0.80 - 1.30(25\degree C)$	$0.16 - 5.00(25\degree C)$	7.9-16.8 $(25^{\circ}C)$	20.0-48.0 $(25^{\circ}C)$
Electron-affinity ⁴	-0.42	-0.50	0.05	0.12

256 Supplementary Table 3. Chemical structures and selected properties of E1, E2, P, and T^{6-16} .

¹Data are adapted from literatures ⁶⁻⁸. ²Data are adapted from literatures ⁹. ³Data are adapted from literatures ¹⁰⁻¹⁵. ⁴Electron-affinity is a measure of the tendency of a molecule to attract electrons. a compound with high electron affinity is more likely to attract electrons, whereas a compound with low electron affinity would be less likely to attract electrons and thus could be more susceptible to reactions with nucleophiles rather than electrophiles $17-19$. The data are adapted from previous work 16 .

257 **Elution parameters for UHPLC**

258 The UHPLC-FSA analytical method utilized in this study for analyzing SH concentrations was

259 adapted from Lyubimenko *et al.* ²⁰, with a modification in the elution flow rate from 0.25 to 0.2 mL

- 260 min⁻¹, and injection volume from 100 to 200 mL to reduce the operating pressure using the same
- 261 instrument. The detailed elution parameters are presented in Supplementary Table 4.

262 Supplementary Table 4. Elution parameters for the UHPLC-FSA analytic procedure.

263 **Calibration curves for UHPLC and LSC**

264 Supplementary Figure 19. presents the calibration curve for E2, performed using a range of E2 265 concentrations $(0.1 - 100 \text{ ng } L^{-1})$ for UHPLC and LSC analyses.

266 Supplementary Figure 19. E2 calibration curve for (A) UHPLC-FSA and (B) LSC in log-scale. The 267 data for calibration before method modification was adapted from 2^1 . Error bars represent 268 propagated error from operational parameter variations and analytical error.

269 The UHPLC-FSA demonstrated good linear relationships across the E2 concentration ranging from 270 2.5 to 100 ng L^{-1} . The UHPLC-FSA achieved a LOD at 2.5 ng L^{-1} , maintaining comparability with

- 271 results prior to the modification of operational parameters. The LSC demonstrated strong linear
- 272 correlations for E2 concentrations spanning from 0.1 to 100 ng L^{-1} and a LOD of 0.1 ng L^{-1} .

273 **Supplementary Discussion 6. Data processing**

274 **Membrane performance**

- 275 Table S5 shows the calculation of electric conductivity (σ , S m⁻¹), permeate flow rate (Q_p , L h⁻¹),
- 276 water flux $(J_w, L \text{ m}^{-2} \text{h}^{-1})$, permeability $(L, L \text{ m}^{-2} \text{h}^{-1} \text{ bar})$, and mean hydraulic residence time (t_r, h) of
- 277 the CNT layer on the electrochemical membrane.

278 Supplementary Table 5. Calculation parameter and equations.

279 where $I(A)$ is the applied current, $V_c(V)$ is the detected cell voltage, h_m is the thickness of the CNTs 280 layer (2·10⁻⁶ m^{4, 22}). Measurement of a standard indium tin oxide (ITO) film with known sheet 281 resistance of 15 Ω square⁻¹ showed the error of electric conductivity was within \pm 10%.

- 282 V_{t2} and V_{t1} (L) were the accumulated volume of the permeate concerted from the permeate mass at time t2 and t1 (h). The density of pure water (ρ) at the operating temperature of 23 °C (997.3 kg m⁻ 283 284 ^{3 23}), was utilized to convert the mass of the permeate (m_{t2} and m_{t1} , kg) at t2 and t1 into its 285 corresponding volume for all experiments.
- 286 A is the effective membrane surface area (2·10⁻² m²), ΔP is the transmembrane pressure (bar), Q_f is 287 the feed flow rate $(L h^{-1})$.
- 288 ε is the porosity of the CNT layer on the membrane support, which is estimated to be 66% from the 289 porosity of a similar CNTs membrane 24 .

290 **Determination of SHs removal**

291 To reduce potential errors in calculating *, arising from variations in data points, the experimental* 292 data of the normalized SH concentration in permeate $(c_{p,SH}/c_{f,SH})$ *vs*. the accumulated permeate

293 volume (V_n) were analysed through a fitting procedure ²⁵. This process utilized a power model ($y =$ 294 $a \cdot x^b$) within the V_p range between 520 and 1000 mL. Subsequently, the $c_{p,eq}/c_f$ was obtained from 295 the curve fitted to the data at $V_p = 1000$ mL, as depicted in Supplementary Figure 20..

Supplementary Figure 20. Example of determination of SH removal (R) by fitting the $c_{p,SH}/c_f$ data in the range of $550 - 1000$ mL of permeate volume. Error bars represent propagated error from operational parameter variations and analytical error.

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298 **Determination of the total mass of removed SH with the membrane**

299 To calculate the total mass of SH removed with the EMR over the entire experiment including 300 adsorption and degradation phase, the dataset of c_p against V_p was analyzed using a polynomial 301 fitting model $(y = A + B \cdot x + C \cdot x^2 + D \cdot x^3)$ for the adsorption phase and a power model $(y = a \cdot x^2 + D \cdot x^3)$ $302 \times$ x^b) for the degradation phase. The integration of the fitting curve with permeate volume as the 303 independent variable, provided the cumulative mass of SH in permeate and the total removal mass of 304 SH can be subsequently quantified. An illustrative example of this quantification process for the 305 overall mass of removed E2 in the EMR is presented in Supplementary Figure 21..

Supplementary Figure 21. Example of determination of total mass of E2 removed within the EMR. Error bars represent propagated error from operational parameter variations and analytical error.

306 In Supplementary Figure 21., the purple-shaded area indicates the accumulative mass of E2 in the 307 permeate, while the total mass of E2 removed within the EMR during the 1 L filtration experiment is 308 represented by the areas shaded in grey.

309 **Determination of the total mass of byproducts**

310 Figure S7 illustrates the quantification of the total mass of byproducts in the permeate. This was

311 achieved by fitting the experimental data obtained from UHPLC-FSA and LSC and then integrating

312 the resulting curve.

Supplementary Figure 22. Example of determination of total byproducts formed and desorbed from the membrane within the EMR. Error bars represent propagated error from operational parameter variations and analytical error.

313 The area shaded in green represents the cumulative mass of byproducts that formed and were 314 desorbed from the membrane throughout the electrochemical degradation process.

315 **Determination of the mass of electrochemical adsorbed and degraded SH**

 To determine the total mass of SH adsorbed on the membrane (under the assumption that all 317 byproducts are fully desorbed), the experimental data of the total ${}^{3}H$ activity, as measured by LSC, are integrated over the range of permeate volumes (Supplementary Figure 23). The total mass of degraded SH is then calculated by subtracting the adsorbed SH from the removed SH.

Supplementary Figure 23. Example of determination of the contribution of electrochemical adsorption and degradation. Error bars represent propagated error from operational parameter variations and analytical error.

320 Supplementary Figure 23 illustrates the calculation of the total mass of adsorbed SH, determined as 321 the difference between areas (1) and (2) . Consequently, the mass of degraded SH is quantified by 322 subtracting the adsorbed SH (1) - 2) from the total removed SH (1) + 3). It was observed that the 323 total mass of degraded SH is equivalent to the mass of the formed byproducts ($(2 + 3)$), which arises 324 from the assumption that all degradation byproducts are completely desorbed from the membrane.

325

326 **Mass balance analysis for the pre-adsorption experiments**

327 As an illustration of the mass balance analysis conducted using the integrated UHPLC-FSA and LSC 328 method, the contribution of degraded, adsorbed, and unremoved E2 in the experiments with and 329 without pre-adsorption, is shown in Supplementary Figure 24.

330 Supplementary Figure 24. Illustration of the mass balance analysis of the degraded, adsorbed, and 331 unremoved E2 in the experiments with and without pre-adsorption. Error bars represent propagated 332 error from operational parameter variations and analytical error.

- 333 In the pre-adsorption experiment (Supplementary Figure 24A), prior to activating the voltage, $19\pm4\%$ 334 of the initial E2 mass was released into the permeate (unremoved), corresponding to the integrated 335 area Ω over the volume range of 0-500 mL. Additionally, $31\pm4\%$ was adsorbed onto the membrane 336 (area (2)). After activating the voltage, 5 \pm 2% of the E2 passed through the system unremoved, as 337 determined by the integrated area $\circled{5}$ for the 500-1000 mL permeate volume. In total, 61 \pm 7% of E2 338 was degraded (area $(3)+(4)$) during the degradation phase (500-1000 mL), while 15 \pm 3% remained 339 adsorbed on the membrane (area $(2)-(4)$).
- 340 In the experiment without pre-adsorption (Supplementary Figure 24B), $77\pm3\%$ of E2 was degraded
- 341 (area $\overline{1}$) and 22 \pm 4% (area $\overline{2}$) was adsorbed onto the membrane, while the remaining 2 \pm 2% was
- 342 released into the permeate.

343 **Supplementary Discussion 7. Error estimation**

 In this study, an error propagation method was employed to estimate experimental error, as described 345 previously 26 . The following sections provide the detailed method of the error determination considering different variabilities, including: i) preparation of feed solutions (∆prep) due to the uncertainties of pipetting and volumetric variations; ii) EMR system caused by the uncertainties of 348 its components (ΔS); and the quantification of SH concentration and ³H activity using the analytical tools (∆anal) - UHPLC-FSA (∆UHPLC) and LSC (∆LSC). Supplementary Table 6. summarized the sources and their estimated relative errors that contribute to the total the error in research data.

351 Supplementary Table 6. Error sources and their estimated relative errors in the SH concentration 352 anaylysis.

Parameter	Error source	Justification	Calculation	Relative error $(\%)$
Sample preparation $(\Delta$ prep)	Pipettes $(\Delta pip);$ Volumetric flasks $(\Delta vol. \,flasks)$	The feed concentration (c_p) is variable with the volume of SH stock and MilliQ measured by pipettes and flasks	Δ Prep $=\sqrt{\Delta p i p^2 + \Delta vol. f lasks^2}$	$\overline{4}$
Experimental system (ΔS)	Flow rate (ΔQ) ; Electrolyte conductivity $(\Delta \sigma)$ Cell voltage $(\Delta voltage)$	Flow rate, electrolyte conductivity, and cell voltage affects the SH removal by varying the number of SH molecule to be treated per unit of time, electrolyte resistance, and anodic potential	ΔS $=\sqrt{\Delta Q^2+\Delta \sigma^2+\Delta voltag{2}}$	6

where: σ_{NC} - standard deviation of net counts, N_{NC} - net number of counts, σ_{TC} - standard deviation of number of total counts, σ_{BG} - standard deviation of background counts, c_{cLSC} measured is the permeate concentration measured by LSC

353 The relative error for each system parameter was determined with the data acquired by different 354 sensors using the following equations:

$$
\Delta y_{abs} = \frac{y_{max} - y_{min}}{2}
$$
 (S7)

$$
\Delta y_{rel} = \frac{\Delta y_{abs}}{\bar{y}}\tag{S8}
$$

355 where Δy_{abs} is the absolute error of the system parameter y, y_{max} and y_{min} are the maximum and 356 minimum values of y, respectively for sufficient repeats, Δy_{rel} is the relative error, and \bar{y} is the mean 357 value. The approaches described in previous work were employed for the error propagation of 358 analytic tools, UHPLC-FSA 20 and LSC 27 .

Error analysis of SH concentration, 359 **³H activity, normalized concentration and removal**

360 The total relative error of the SH concentration and ³H activity (ΔE) quantified through HPLC-FSA 361 and LSC was estimated using Eq. (S9).

$$
\Delta E = \sqrt{\Delta \text{Prep}^2 + \Delta S^2 + \Delta \text{anal}^2}
$$
 (S9)

 To make this calculation clear, as an example, the errors for feed concentrations measured using UHPLC-FSA and LSC in variation of sample preparation (4%) and analytical method (1.1% for UHPLC, 10-16% for FSA, and 2-6% for LSC) are reported (Supplementary Figure 25.). The errors of feed concentrations analyzed with UHPLC-FSA were determined to be ±11-17%, and those 366 measured through LSC were estimated to be \pm 4-7% using Eq (S9).

367 Supplementary Figure 25. Feed concentrations measured using UHPLC-FSA and LSC for the 368 electrochemical filtration experiments.

369 Supplementary Figure 25. showed that the feed concentrations measured by UHPLC-FSA ranged 370 from 940 to 1149 μ g L⁻¹, while those measured by LSC varied between 947 and 1073 μ g L⁻¹. The 371 errors associated with these measurements fall within the range calculated using the error propagation 372 method.

373 The relative error of normalized SH concentration and ³H activity in the permeate ($\Delta c_p/c_f$) is directly 374 related to the error of c_p and c_f , which is determined using the equation:

$$
\Delta(c_p/c_f) = \frac{c_p}{c_f} \cdot \sqrt{\Delta c_f^2 + \Delta c_p^2} = \frac{c_p}{c_f} \cdot \sqrt{(\Delta \text{Prep}^2 + \Delta \text{anal}^2) + \Delta E^2}
$$
(S10)

375 Correspondingly, the relative error of removal ($R = 100 \cdot (1 - c_p/c_f)$) is calculated *via* the equation:

$$
\Delta R = \frac{c_p}{c_f} \cdot \Delta (c_p / c_f) \tag{S11}
$$

376 **Error analysis of total mass of removed SH and rate of SH removal**

377 According to the calculation of total mass removal either by adsorption or degradation (Eq. (S12)), 378 error of the total mass removal (Δm_{rem}) is determined by the error of c_f and the accumulative SH 379 mass in the permeate (m_p) . The absolute error of m_p ($\Delta m_{n,abs}$) was calculated by fitting the data of -380 $c_p + \Delta c_{p,abs}$ and $c_p - \Delta c_{p,abs}$, and then the $\Delta m_{p,abs}$ can be determined by integrating the fitting 381 curves (Supplementary Figure 26.).

$$
m_{rem} = m_f - \sum_{i=1}^{n} m_{p,i}
$$
 (S12)

382 where $V_{p,i}$ and $c_{p,i}$ are the volume and concentration of the permeate sample *i*, *n* is the total number 383 of the permeate samples.

Supplementary Figure 26. Example of determination of the absolute error of total SH mass in the permeate. Error bars represent propagated error from operational parameter variations and analytical error.

384 The $\Delta m_{p,abs}$ was determined by half the difference in the integrated area under the fitting curve for $t_p + \Delta c_{p,abs}$ and $c_p - \Delta c_{p,abs}$, presented by half the green area in Supplementary Figure 26.. Thus,

386 the absolute error for the removed SH ($\Delta m_{rem, abs}$) can be calculated using the equation below.

$$
\Delta m_{rem,abs} = \frac{m_{rem,max} - m_{rem,min}}{2}
$$

=
$$
\frac{\{(c_f + \Delta c_{f,abs}) - (c_p - \Delta c_{p,abs})\} - \{(c_f - \Delta c_{f,abs}) - (c_p + \Delta c_{p,abs})\}}{2}
$$
 (S13)

According to the definition of the apparent rate of SH removal ($r'_{rem} = \frac{m_{rem}}{r M A}$ 387 •• According to the definition of the apparent rate of SH removal $(r'_{rem} = \frac{m_{rem}}{t \cdot M \cdot A})$, the relative error of

388 r'_{rem} ($\Delta r'_{rem}$) was directly determined by the Δm_{rem} , which can be calculated using:

$$
\Delta r'_{rem} = \Delta m_{rem} = \frac{\Delta m_{rem,abs}}{m_{rem}}\tag{S14}
$$

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