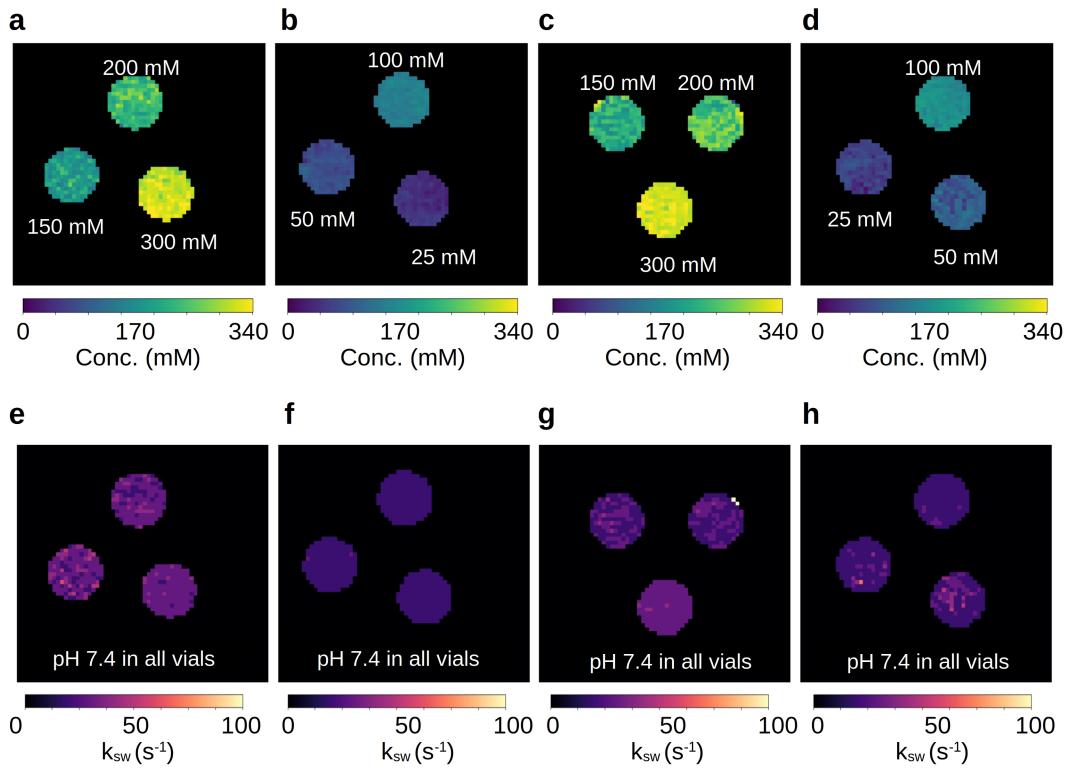


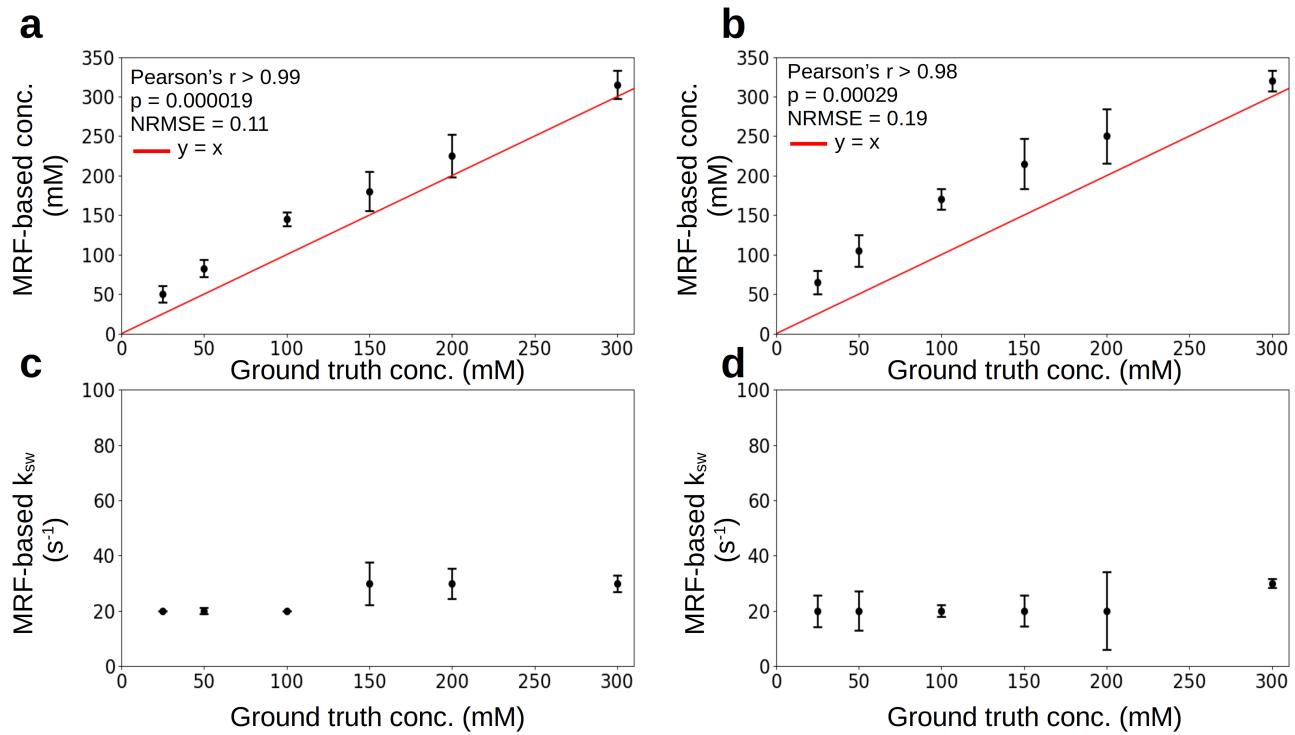
Supplemental information

In vivo mapping of the chemical exchange relayed nuclear Overhauser effect using deep magnetic resonance fingerprinting

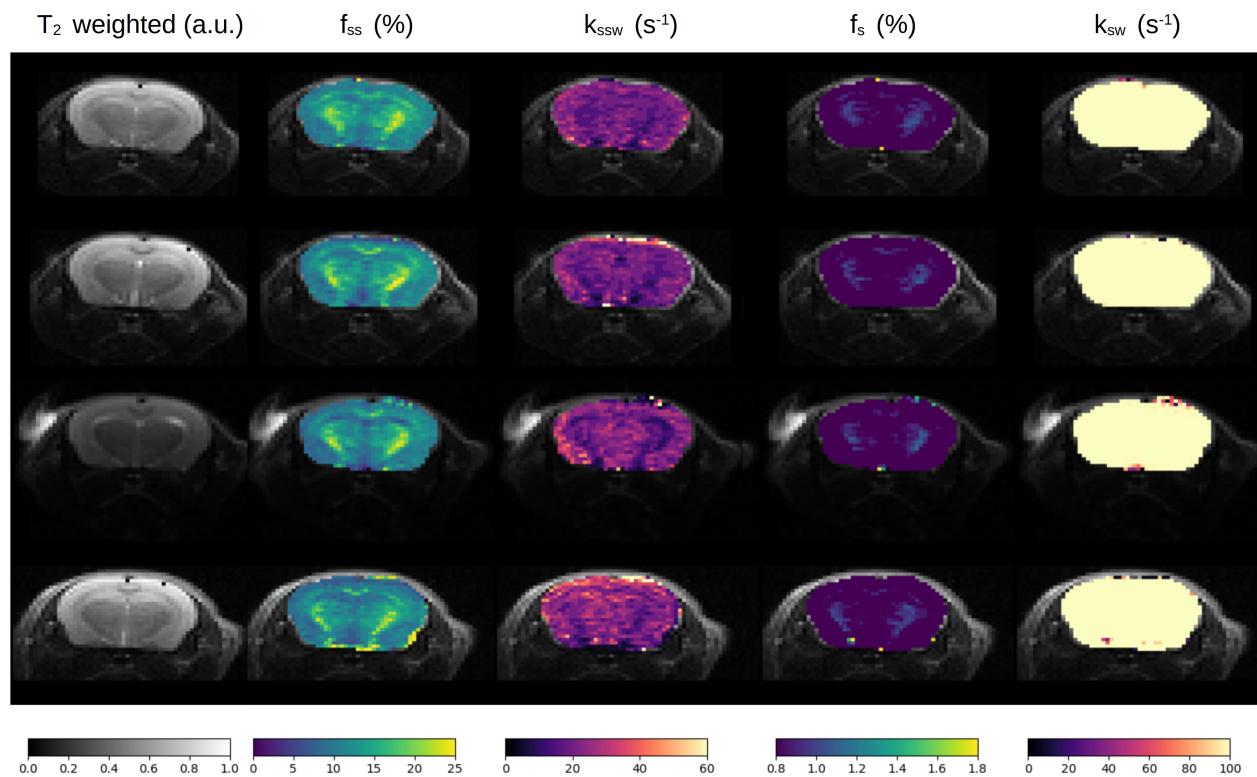
Inbal Power, Michal Rivlin, Hagar Shmuely, Moritz Zaiss, Gil Navon, and Or Perlman



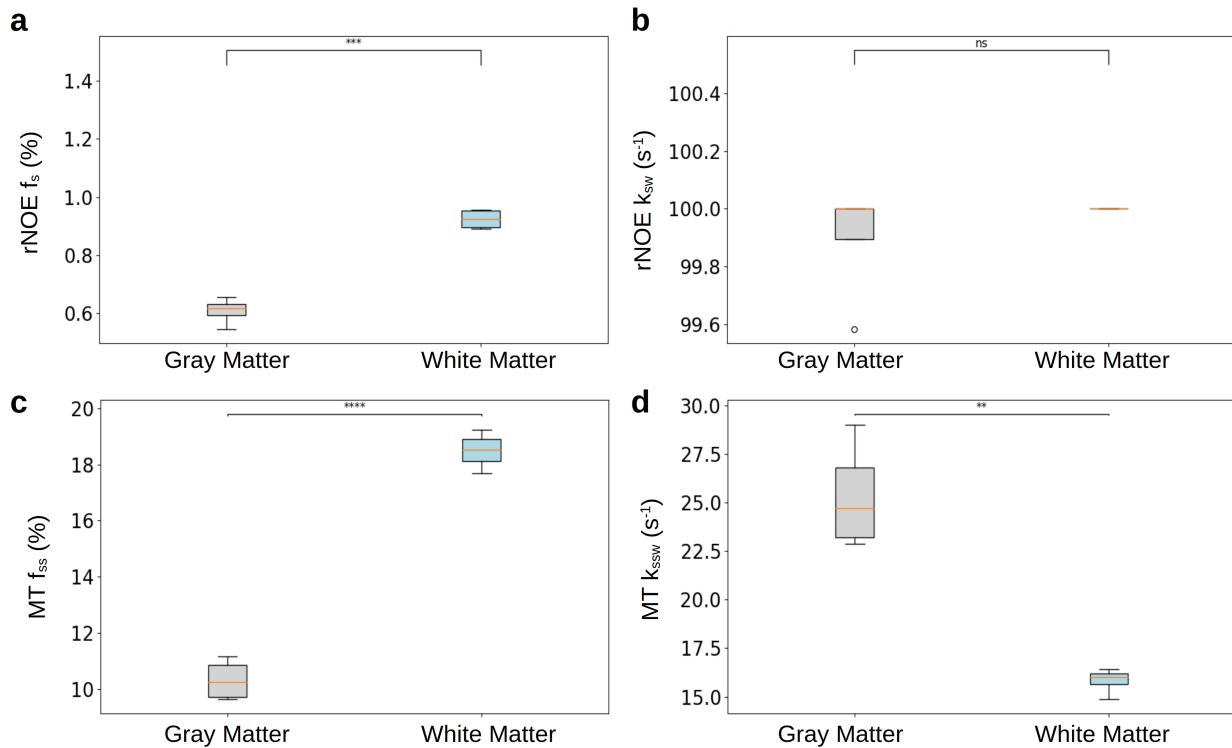
Supporting Information Fig. S1. In vitro quantification of NOE proton exchange parameters using dot-product MRF. (a-d) Glucose-unit concentration and (e-h) NOE proton exchange rate maps of bovine (a,b,e,f) and rabbit (c,d,g,h) liver phantoms. The white text next to each vial represents the ground truth.



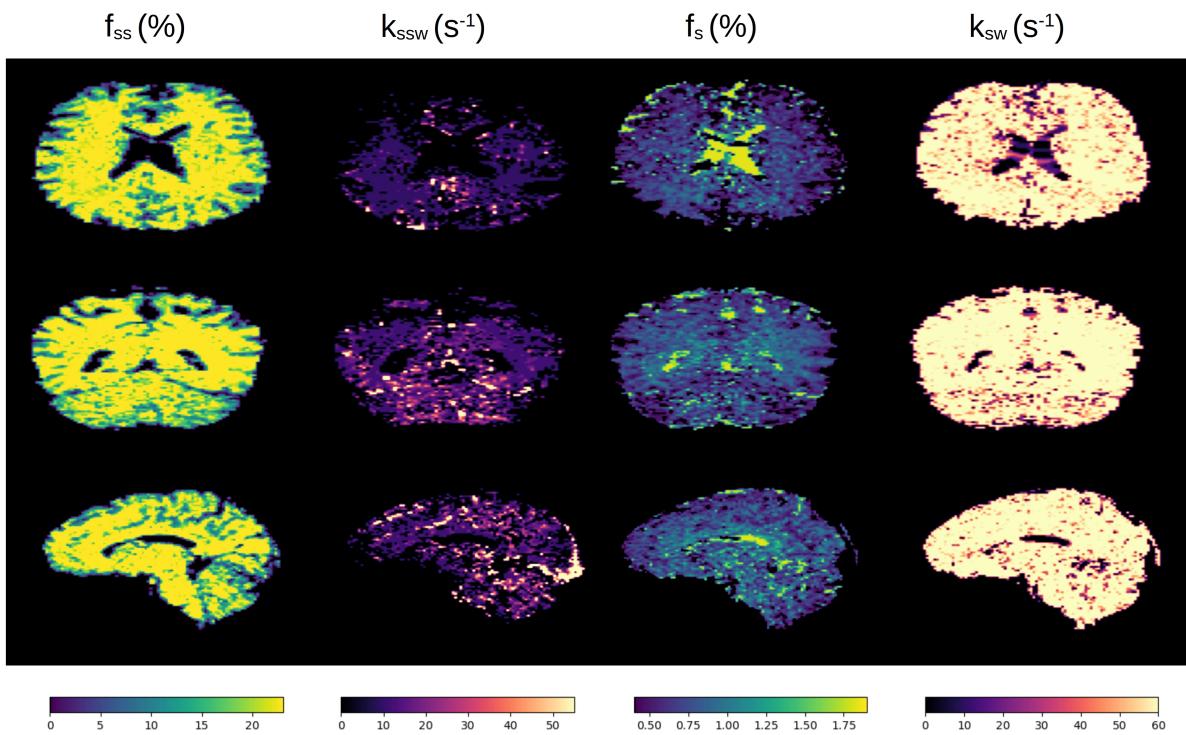
Supporting Information Fig. S2. Statistical analysis of the quantitative proton exchange parameters obtained in-vitro using dot-product matching. MRF determined glucose-unit concentrations in bovine (a) and rabbit (b) liver phantoms were significantly correlated (Pearson's $r > 0.98$, $p < 0.001$) with known concentrations. (c-d) The NOE MRF determined proton exchange rates for the same phantoms. The black circles represent the mean and the bars represent the standard deviation.



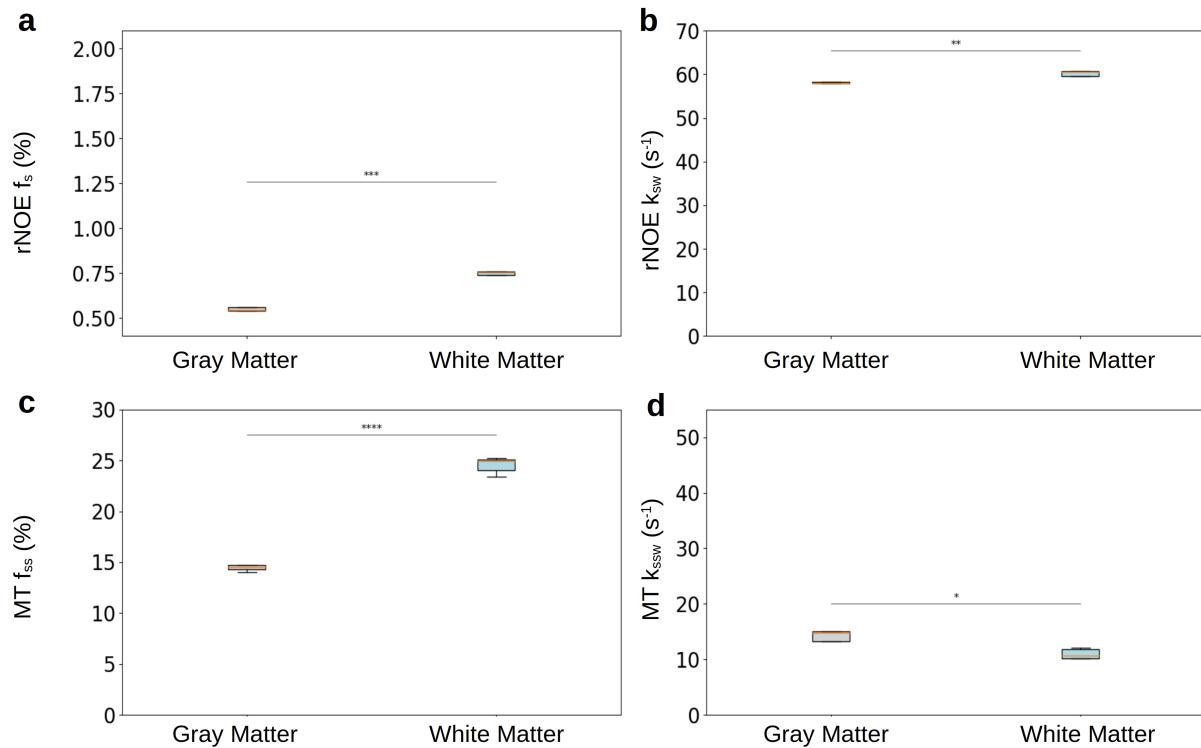
Supporting Information Fig. S3. Quantitative semisolid MT (f_{ss} , k_{ssw}) and rNOE (f_s , k_{sw}) parameter maps obtained using dot-product matching in four representative mice, alongside an anatomical T_2 -weighted image.



Supporting Information Fig. S4. Statistical analysis of the semisolid MT and rNOE proton volume fraction (f_{ss} , f_s) and exchange rate (k_{ssw} , k_{sw}) parameters extracted from *in vivo* mice brains (n=7) using dot-product matching. Note the false classification of the rNOE k_{sw} (fixed at the maximum value available in the dictionary). **p<0.01, ***p<0.001, ****p<0.0001, ns = not significant.



Supporting Information Fig. S5. Quantitative semisolid MT and rNOE proton volume fraction (f_{ss} and f_s , respectively) and exchange rate (k_{ssw} and k_{sw} , respectively) parameter maps obtained from a representative human volunteer using dot-product matching. **(Top)** Representative axial slice. **(Center)** Representative coronal slice. **(Bottom)** Representative sagittal slice.



Supporting Information Fig. S6. Statistical analysis of the semisolid MT and rNOE proton volume fraction (f_{ss} , f_s) and exchange rate (k_{ssw} , k_{sw}) parameters extracted from *in vivo* human volunteer brains ($n=5$) using dot-product matching. * $p<0.05$, ** $p<0.01$, * $p<0.001$, **** $p<0.0001$.**

Supporting Information Table S1. Acquisition parameters used.

BSA / In Vivo Mice rNOE																															
B ₁ (μ T)	2	2	1.7	1.5	1.2	1.2	3	0.5	3	1	2.2	3.2	1.5	0.7	1.5	2.2	2.5	1.2	3	0.2	1.5	2.5	0.7	4	3.2	3.5	1.5	2.7	0.7	0.5	
ω_{rf} (ppm)	-3.5																														
T _{sat} (s)	2.5																														
T _{rec} (s)	1																														
FA ($^{\circ}$)	90																														
Glycogen Phantoms rNOE																															
B ₁ (μ T)	.2	.08	.46	.01	.0	.02	.09	.4	.09	.0	.02	.03	.42	.2	.11	.1	.6	0	.38	.02	.0	.18	.31	.33	.38	.1	.03	.2	.0	.27	.42
ω_{rf} (ppm)	-1																														
T _{sat} (s)	1																														
T _{rec} (s)	3																														
FA ($^{\circ}$)	90																														
In Vivo Mice MT																															
B ₁ (μ T)	2	2	1.7	1.5	1.	1.	3	0.	3	1	2.2	3.	1.	0.	1.	2.	2.	1.	3	0.	1.5	2.5	0.7	4	3.2	3.5	1.5	2.7	0.7	0.5	
ω_{rf} (ppm)	8	6	6	10	10	10	8	6	8	14	14	10	6	10	8	6	8	10	14	14	6	8	14	6	14	14	14	8	10	8	
T _{sat} (s)	2.5																														
T _{rec} (s)	1																														
FA ($^{\circ}$)	90																														
Human Subjects Semisolid MT																															
B ₁ (μ T)	2	2	1.7	1.5	1.2	1.2	3	0.5	3	1	1	2.2	3.	1.	0.7	0.7	2.2	2.5	1.2	3	0.2	1.	2.5	0.7	4	3.	3.5	1.5	2.	0.7	0.5
ω_{rf} (ppm)	8	6	6	10	10	10	8	6	8	1	14	10	6	10	8	6	8	10	14	14	6	8	14	6	1	14	8	10	8		
T _{sat} (s)	A saturation pulse train of 13 rectangular pulses, 100 ms "on", 50% duty cycle.																														
T _{rec} (s)	1																														
FA ($^{\circ}$)	15																														
Human Subjects rNOE																															
B ₁ (μ T)	2	2	1.7	1.	1.	1.	3	0.	3	1	2.2	3.	1.	0.7	1.5	2.	2.5	1.	3	0.2	1.	2.5	0.7	4	3.2	3.5	1.5	2.7	0.7	0.5	
ω_{rf} (ppm)	-3.5																														
T _{sat} (s)	A saturation pulse train of 13 rectangular pulses, 100 ms "on", 50% duty cycle.																														
T _{rec} (s)	1																														
FA ($^{\circ}$)	15																														

B₁ = Saturation pulse power (average amplitude); ω_{rf} = sauration pulse frequency offset; T_{sat} = saturaion pulse duration; T_{rec} = recovery time; FA = flip angle.

Supporting Information Table S2. Quantitative *in vivo* exchange parameters obtained in this study and previous literature.

Proton pool	Semisolid MT				rNOE			
	WM f _{ss} (%)	GM f _{ss} (%)	WM k _{ssw} (s ⁻¹)	GM k _{ssw} (s ⁻¹)	WM f _s (%)	GM f _s (%)	WM k _{sw} (s ⁻¹)	GM k _{sw} (s ⁻¹)
This study (mice)	15.00±0.34	9.20±0.75	36.06±1.64	43.55±2.00	1.49±0.06	0.99±0.2	67.51±0.41	53.50±4.21
This study (humans)	11.28±1.50	5.44±0.54	22.20±1.57	29.19±0.93	1.43±0.07	1.15±0.08	41.46±1.15	37.46±1.79
Samsanov et al., 2012 ³⁴ (dogs)	12.1±0.4	5.4±0.2	21.05±0.5	30.09±1.1				
Stanisz et al., 2005 ³¹ (bovine)	13.9 ±2.8	5.0 ±0.5	23±4	40±1				
Liu et al., 2013 ³² (humans)	6.18±0.43	3.43±0.42	67.5±6.98	63.48±4.5	2.39±0.22	1.18±0.16	27.45±2.18	24.50±1.65
Gadeas et al., 2017 ³⁶ (humans)	8.9 ± 0.3*	4.4 ± 0.4*			5 ± 0.1*	3 ± 0.1*		
Xu et al., 2014 ⁴¹ (rats)								17
Jones et al., 2013 ⁴² (humans)							11	
Yarnykh et al., 2015 ³³ (humans)	13.48±0.37	5.77±0.34						
Perlman et al., 2022 ²⁹ (mice)	19.8±0.5	12.8 ± 0.8	43.87±2.36	56.54±3.1				

WM = white matter. GM = gray matter. f = proton volume fraction. k = proton exchange rate.

*In the study by Gadeas et al the K_{ssw} was restricted to 50 s⁻¹ and the K_{sw} restricted to 10 s⁻¹.

Supporting Information Table S3. Properties of the MR-fingerprinting dictionaries used for training the deep reconstruction networks.

Imaging target	Glycogen rNOE (7T)	BSA rNOE (7T)	Mouse Brain semisolid MT (7T)	Mouse Brain rNOE (7T)	Human Brain semisolid MT (3T)	Human Brain rNOE (3T)
Water T ₁ (ms)	[2200, 3205]	[2600, 4000]	[1300, 1900]	[1425, 1925]	[800, 3000]	[1084, 1820]
Water T ₂ (ms)	[50, 1205]	[90, 500]	[40, 90]	[45, 95]	[50, 150]	[50, 150]
Semi-solid T ₁ (ms)	---	---	1000	1000	Equal to water T ₁	1000
Semi-solid T ₂ (μs)	---	---	10**	10**	10**	10**
k _{ssw} (s ⁻¹)	---	---	[5, 100]	[7, 102]	[5, 100]	[5, 100]
f _{ss} (%)	---	---	[1.82, 27.27]	[3.18, 28.64]	[1.82, 27.27]	[1.82, 27.27]
Semi-solid offset frequency (ppm)	---	---	-2.5	-2.5	-2.5	-2.5
Solute T ₁ (ms)	2600	3000	---	1300	---	1000
Solute T ₂ (ms)	10	0.5	---	5	---	5
k _{sw} (s ⁻¹)	[20, 140]	[10, 50]	---	[7, 102]	---	[5, 60]
f _s (%)	[0, 0.309]	[0.045, 2.273]	---	[0.114, 1.84]	---	[0.114, 1.84]
Solute offset frequency (ppm)	-1	-3.5	---	-3.5	---	-3.5
Number of dictionary entries	4,757,688	1,394,820	12,600	9,828,000	531,300	2,574,000
Dictionary generation time***	1.5 min	20 s	1 s	10.77 min	5.64 min	119.9 min

*The notation [x, z] represents the [minimum, maximum] parameter values. Various uniformly sampled values were taken within each parameter range to ultimately yield the total number of dictionary entries specified in the second row from the bottom.

**The Bloch-McConnell equations based dictionary generator used a Lorentzian line-shape for the semi-solid pool. To generate a linewidth equivalent to the commonly reported super-Lorentzian of 10 μs, a four times higher value (40 μs) was input to the dictionary generator²⁵.

***A desktop computer with an Intel I9-12900F processor and 32 GB RAM was used for dictionary generation.