Supporting Information

Theoretical Insights into High-*T*_c Superconductivity of Structurally Ordered YThH₁₈: A First-Principles Study

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Table S1: Crystal structures of Y-Th-H predicted at each pressure (*P*). Lattice parameters (*a*, *b* and *c*) are given in unit of Å.

Compound	Space group	P (GPa)	Lattice parameters	Atomic coordinates (fractional)
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Compound	Space group	P (GPa)	Lattice parameters	Atomic coordinates (fractional)			
				Atoms	x	у	Z.
				Atoms	x	У	Z.
YThH ₈	P4/mmm	200	<i>a</i> = 2.71221	Y(1b)	-0.00000	0.00000	0.50000
			b = 2.71221	Th(1c)	0.50000	0.50000	-0.00000
			c = 5.52173	H(4i)	-0.00000	0.50000	0.26329
			$\alpha = 90.0^{\circ}$	H(2g)	0.00000	0.00000	0.14890
			$\beta = 90.0^{\circ}$	H(2h)	0.50000	0.50000	0.37151
			$\gamma = 90.0^{\circ}$				
Y ₂ ThH ₁₂	I4/mmm	200	<i>a</i> = 2.69993	Y(2e)	0.829360	0.829360	0.341270
			<i>b</i> = 2.69993	Th(1b)	0.500000	0.500000	0.000000
			<i>c</i> = 8.35315	H(4g)	0.910710	0.410710	0.178580
			$\alpha = 80.7^{\circ}$	H(2e)	0.948380	0.948380	0.103240
			$\beta = 80.7^{\circ}$	H(2e)	0.713000	0.713000	0.574010
			$\gamma = 90.0^{\circ}$	H(2e)	0.625680	0.625680	0.748630
				H(2d)	0.750000	0.250000	0.500000
YThH ₁₈	P6m2	200	<i>a</i> = 3.52410	Y(1e)	1.000000	0.000000	0.000000
			b = 3.52410	Th(1d)	0.666670	0.333330	0.500000
			c = 5.20468	H(6n)	0.022580	0.511290	0.172700
			$\alpha = 90.0^{\circ}$	H(6n)	0.181690	0.363370	0.305830
			$\beta = 90.0^{\circ}$	H(2i)	0.000000	1.000000	0.397400
			$\gamma = 120.0^{\circ}$	H(2h)	0.666670	0.333330	0.110920
				H(1a)	0.333330	0.666670	0.000000
				H(1b)	0.333330	0.666670	0.500000
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Compound	Space group	P (GPa)	Lattice parameters	Atomic coordinates (fractional)			
				Atoms	x	У	Z
YThH ₈	P4/mmm	300	<i>a</i> = 2.57068	Y(1b)	0.00000	0.00000	0.50000
			b = 2.57068	Th(1c)	0.50000	0.50000	0.00000
			c = 5.40869	H(4i)	0.00000	0.50000	0.26272
			$\alpha = 90.0^{\circ}$	H(2g)	-0.00000	0.00000	0.15549
			$\beta = 90.0^{\circ}$	H(2h)	0.50000	0.50000	0.36811
			$\gamma = 90.0^{\circ}$				
Y ₂ ThH ₁₂	I4/mmm	300	<i>a</i> = 2.56013	Y(2e)	0.829050	0.829050	0.341700
			b = 2.56013	Th(1b)	0.500000	0.500000	1.000000
			c = 8.17191	H(4g)	0.911260	0.410080	0.178960
			$\alpha = 81.0^{\circ}$	H(2e)	0.946170	0.946170	0.107740
			$\beta = 81.0^{\circ}$	H(2e)	0.713880	0.713880	0.572580
			$\gamma = 89.7^{\circ}$	H(2e)	0.624740	0.624740	0.750800
				H(2d)	0.749790	0.250210	0.500000

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(a) P4/mmm-YThH₈ at 200GPa

(b) I4/mmm-Y₂ThH₁₂ at 200GPa





(e) I4/mmm-Y2ThH12 at 300GPa



Figure S1: Electronic band structure together with projected density of states (PDOS) for all the stable structures.



Figure S2: Phonon dispersion, projected phonon density of states (PHDOS), and Eliashberg spectral function $\alpha^2 F(\omega)$ associated with electron-phonon integral ($\lambda(\omega)$) for all the stable compounds. No imaginary modes suggest that all the structure in addition to their thermodynamic stability are dynamically stable.

Workflow for Novel Pressurized Superconducting Ternary Hydride Discovery and T_c Calculation

1. Set Up Problem Definition

- Select Elements (Y-Th-H): Choose the ternary hydride system (Y-Th-H) based on literature, known properties, and/or chemical intuition.
- **Define Pressure Conditions:** Specify the pressure range under which the hydride is expected to form, as high pressures often stabilize hydrogen-rich phases based on earlier work.

2. Evolutionary Algorithm (EA) Search for Stable Structures

- Use of Evolutionary Algorithm (e.g., USPEX, CALYPSO):
 - Step 1: Generate Initial Population: Start with random crystal structures in the desired composition system under the target pressure.
 - Step 2: Energy and Structural Relaxation: For each generated structure, perform initial energy minimization and structural relaxation using density functional theory (DFT) (e.g., with VASP or Quantum ESPRESSO).
 - Step 3: Fitness Evaluation: Rank structures by their formation energy (from DFT) and select the lowest energy structures for reproduction (crossover and mutation).
 - Step 4: Iterative Evolution: Continue the evolutionary search over several generations, with DFT energy and force evaluations guiding the algorithm to find the most stable structures.

3. Structure Optimization and Stability Check

• Phonon Calculations (e.g., Using DFT or DFPT):

 Perform phonon dispersion calculations to check the dynamical stability of the discovered hydrides. Dynamical stability is confirmed if there are no imaginary phonon frequencies across the Brillouin zone.

• Convex Hull Analysis:

 Calculate the formation enthalpy of the ternary hydride relative to binary phases and elemental components. Check if the structure lies on the convex hull to confirm its thermodynamic stability.

4. Electron-Phonon Coupling (EPC) and Eliashberg Function

- Electron-Phonon Coupling Calculation (e.g., Quantum ESPRESSO with EPW):
 - Step 1: DFT Ground State: Calculate the electronic ground state using DFT with a high k-point mesh.
 - Step 2: Phonon Dispersion: Perform detailed phonon calculations using density functional perturbation theory (DFPT).
 - Step 3: EPC Matrix Elements: Calculate the electron-phonon coupling matrix elements for the system.
 - Step 4: Eliashberg Function $\alpha^2 F(\omega)$: Use the EPC data to compute the Eliashberg spectral function $\alpha^2 F(\omega)$, which provides insights into the strength of the electron-phonon interaction.

5. Superconducting Transition Temperature (T_c) Calculation

- McMillan-Allen-Dynes Formula:
 - Estimate the superconducting transition temperature T_c using the McMillan-Allen-Dynes formula:

$$T_c = \frac{\omega_{\log}}{1.2} \exp\left(\frac{-1.04(1+\lambda)}{\lambda - \mu^*(1+0.62\lambda)}\right)$$

where:

- * ω_{log} : Logarithmic average phonon frequency
- * λ : EPC constant
- * μ^* : Coulomb pseudopotential (typically 0.1-0.13 for hydrides)