Supplementary Materials ¹

1. Supplementary Note ²

1.1. Comparison with other spatial domain identification methods ³ *parameter settings* ⁴

We quantitatively compared STMVGAE with other methods on different $\overline{5}$ datasets, including the non-spatial method SCANPY [[1\]](#page-17-0), and the spatial ϵ methods stLearn [\[2\]](#page-17-1), SEDR [[3\]](#page-17-2), SpaGCN [[4\]](#page-17-3), DeepST [\[5](#page-17-4)], STAGATE [[6\]](#page-17-5) and τ STAMaker[[7\]](#page-17-6). \blacksquare

The selection of these comparison methods was based on the following ⁹ considerations: 10

1.Relevance of methods. The chosen methods are advanced approaches ¹¹ specifically designed for spatial domain identification tasks in spatial tran- ¹² scriptomics. They address key research objectives, including spatial domain 13 recognition, gene expression pattern analysis, and spatial data feature ex- ¹⁴ traction, making them highly relevant to our study.

2. Influence in the Field. These methods have gained widespread recognition $_{16}$ and citations in spatial transcriptomics research and have become benchmark 17 models in the field. 18

3. Method Diversity. The selected methods encompass a variety of technical ¹⁹ paradigms, enabling us to compare the performance of different types of ²⁰ approaches in spatial transcriptomics data analysis. ²¹

The parameter settings of these methods are as follows: 22

- SCANPY: First, we used the same data preprocessing method as STMV- 23 GAE to preprocess gene expression (log-transformed, normalized and selecting the top 3,000 HVGs). PCA dimensionality reduction was then ²⁵ used to reduce the gene expression data to 30 PCs. Finally, we used $_{26}$ the *scanpy.pp.neighbor()* function default parameters provided by the SC- ²⁷ NAPY package [\[1\]](#page-17-0) to calculate neighbors, and the *scanpy.tl.louvain()* func- ²⁸ tion is used to allocate spots. Additionally, the resolution parameter was ²⁹ tuned manually to ensure the number of clustering is equal to the ground $\frac{30}{20}$ $truth.$ 31
- stLearn: We chose default parameters for stLearn on the DLPFC dataset. $\frac{32}{2}$ Specifically, the *stLearn.SME.SME_normalized()* function was performed ³³ on the raw gene expression of all genes with the parameter use_data=*"raw"* ³⁴

1

 and weights=*"physical_distance"*. Then the first 30 PCs of the SME nor- malized matrix were used for clustering. We did not use stLearn for training on the melanoma dataset because it does not support training without histology images.

 • SEDR: SEDR can be trained on all datasets, and we retain all its de- fault parameters except for empirically selecting the number of neigh- bors on different datasets to ensure reasonable results. We perform the same strategy on each dataset, looking for the number of neighbors that gives the best results between 6 and 12 neighbors. We set n in the *SEDR.graph_construction()* function to 10 on the DLPFC dataset and to 12 on all other datasets.

• SpaGCN: We use its recommended parameters for SpaGCN in all datasets.

 • DeepST: We retain all the default parameters of DeepST and set k in the *deepen._get_graph()* function to 12. Additional, We tested the results on the melanoma dataset with DeepST set up without using histological images.

 • STAGATE: STAGATE builds the graph by looking for neighbors within a radius, so the parameter r in the *STAGATE.Cal_Spatial_Net()* function changes in each dataset. We used the same rules as SEDR to select r. In DLPFC, we used the recommended parameter r set to 150, r in the BCDC data set to 350, r in the melanoma data set to 2, and r in the BRCA data set to 300.

 • STAMaker: Recommended parameters are used in STAMaker, and neigh- bor selection is consistent with STAGATE. We set n to randomly initialize the model in STAMaker to 5.

1.2. Evaluation metrics of clustering

 ARI. The adjusted Rand index (ARI) [[8](#page-17-7)] is a measure of the similarity between two clusterings, and it is an external evaluation index. We introduce ARI to calculate the similarity between the results obtained by STMVGAE spot assignment and manual annotation. The calculation of ARI must first calculate the values of the contingency table. The contingency table contains the following four parts: *T F* is the count of spot pairs classified into the same cluster in both the true and predicted clustering. *T N* is the count of spot pairs classified into different clusters in both the true and predicted clustering. *F N* is the count of spot pairs classified into the same cluster in the true clustering but into different clusters in the predicted clustering. \bar{v} FP is the count of spot pairs classified into different clusters in the true π clustering but into the same cluster in the predicted clustering. The value τ_2 range of ARI is between $[-1,1]$. Generally, the closer the ARI value is to 1, π the better the result. The closer the ARI value is to 0, the clustering result $_{74}$ is the same as the random clustering result. The calculation method of ARI τ is based on paired samples. It considers the combination of samples of the τ_6 same category in different clusters in two clustering results and compares it π with random situations. ARI is computed as: $\frac{78}{78}$

$$
ARI = \frac{TP + TN - E}{TP + TN + FP + FN - E} \tag{1}
$$

The expected value of the index, denoted as *E*, represents the value that ⁷⁹ would be obtained if the clustering were entirely random. It is calculated as $\frac{80}{100}$ follows:

$$
E = \frac{(TP + FP) \times (TP + FN) + (FN + TN) \times (FP + TN)}{TP + TN + FP + FN}
$$
 (2)

NMI. Normalized Mutual Information (NMI) is an indicator used to evaluate $\frac{82}{2}$ the performance of clustering algorithms. It measures the similarity between 83 two clustering results. The NMI value ranges between $[0,1]$. The closer \mathfrak{g}_4 the value is to 1, the more similar the two clustering results are, while the $\frac{1}{100}$ closer the value is to 0, the less similar they are. P represents the spatial $\frac{1}{160}$ domain clustering result and *T* represents the ground truth clustering labels. $\frac{87}{1000}$ Their entropies are denoted as $H(P)$ and $H(T)$ respectively. NMI has been 88 widely used to evaluate the performance of spatial domain identification in \bullet spatial transcriptomic data analysis [\[9](#page-17-8)]. The calculation formula for NMI is \sim as follows: $\frac{91}{2}$

$$
NMI = \frac{MI(P,T)}{\sqrt{H(P)H(T)}}\tag{3}
$$

HS. In unsupervised clustering, Homogeneity Score (HS) is a metric used $\frac{92}{2}$ to evaluate clustering results, which measures whether the samples in each $\frac{93}{2}$ cluster belong to the same category $[6]$. The value of HS ranges from 0 to $\frac{94}{94}$ 1. The closer the value is to 1, the better the clustering result is, that is, ⁹⁵ each cluster contains samples of the same category. $H(C)$ is the entropy of \bullet the true class, which represents the uncertainty of the class distribution of σ

⁹⁸ the samples in the data set; $H(C|K)$ is the conditional category entropy of a given clustering result, which represents the uncertainty of the category dis- tribution of the sample when the clustering result is known. The calculation formula for HS is as follows:

$$
HS = 1 - \frac{H(C|K)}{H(C)}
$$
\n⁽⁴⁾

 Purity. In unsupervised clustering, Purity is a metric used to evaluate clustering results, which measures whether the samples contained in each cluster belong to the same category. The value range of Purity is between 0 and 1. The closer the value is to 1, the better the clustering result is, that is, each cluster contains samples of the same category. *N* is the total number of samples in the dataset, *k* represents the index of the cluster, *j* represents μ ¹⁰⁸ the index of the real category, c_k represents the sample set in cluster k , and *t*^{*j*} represents the sample set in real category *j*. The $|c_k \cap t_j|$ in the formula represents the size of the intersection of samples in cluster *k* and samples in $_{111}$ true category *j*. The calculation formula for Purity is as follows:

$$
Purity = \frac{1}{N} \sum_{k} max_{j} |c_{k} \cap t_{j}|
$$
\n(5)

¹¹² *1.3. Implementation Details*

 Our experiments were performed on a single NVIDIA RTX 4090Ti GPU using PyTorch (version 1.13.1) and Python 3.11. In the "ST data augmenta- tion" section, we selected Resnet50 as the default convolutional neural net-116 work, and then introduced two parameters α_1 and α_2 to balance the image 117 feature matrix and the gene expression matrix. We fixed α_2 to 1.0, and set ¹¹⁸ α_1 to 0.2 through experiments. In the "Spatial graph construction" section, we selected neighbors with a strategy that the number of neighbors will not be zero and will not generate too many neighbors (more than 12), and the best performance is obtained within this range. The baseline method also used the same strategy. On different datasets, the construction parameters of the adjacency matrix are set as follows:

 124 • DLPFC dataset: adjacency matrix parameters based on Radius $r = 250$ ¹²⁵, adjacency matrix parameters based on KNN $k = 12$.

¹²⁶ • BCDC dataset: adjacency matrix parameters based on Radius $r = 300$, $_{127}$ adjacency matrix parameters based on KNN $k = 5$.

- Melanoma dataset: adjacency matrix parameters based on Radius $r = 3$ 128 $,$ adjacency matrix parameters based on KNN $k = 7$.
- BRCA dataset: adjacency matrix parameters based on Radius $r = 500$, 130 adjacency matrix parameters based on KNN $k = 11$.

The linear encoder was set to $[1000, 400, 30]$. Then, the hidden representation $_{132}$ is learned through a two-layer GCN encoder. The GCN waw set to $[64, 8]$ and 133 the linear decoder is set to $[400, 1000]$. The training strategy was established 134 for 1000 epochs, the learning rate set at 0.001 and the weight decay set at 135 0.0001. For the loss function, we chose the hyperparameters empirically, we ¹³⁶ set λ_1 and λ_4 to 0.1, λ_2 and λ_3 to 1.0.

2. Supplementary Figure

See next page

Figure S1. Comparison of spatial domains identification by clustering assignments via STMVGAE, STAGATE, SEDR, DeepST, stLearn, and manual annotation in all 12 slices of the DLPFC dataset.

See next page

See next page

Figure S2. UMAP visualization and PAGA trajectory inference by STMVGAE, SEDR, STAGATE, DeepST, SpaGCN, and stLearn embeddings respectively.

Figure S3. (**A**) UMAP visiulization of multi-slice joint analysis on 151507-151510 slices in DLPFC datasets. Each row represents the use of STMVGAE, SCANPY, and SEDR methods with Harmony for batch integration, and each column represents batches, identification spatial domains, and ground truth labels, respectively. (**B**) STMVGAE performs multi-slice joint analysis on 151669-151672 slices in the DLPFC dataset. (**C**) STMVGAE performs multi-slice joint analysis on 151673-151676 slices in the DLPFC dataset.

Figure S4. Box plot and significance markers of the NMI values of the STMVGAE method under multiple view combinations. The significance markers are calculated by the Wilcoxon rank sum test.

Figure S5. Box plot and significance markers of the HS values of the STMVGAE method under multiple view combinations. The significance markers are calculated by the Wilcoxon rank sum test.

Figure S6. Box plot and significance markers of the Purity values of the STMVGAE method under multiple view combinations. The significance markers are calculated by the Wilcoxon rank sum test.

¹³⁹ **3. Supplementary Table**

Table S1: Overview of comparative spatial domain identification methods.

Table S2: Summary of the datasets in this study.

Table S3: Experiments on selection of hyperparameters α_1 and α_2 . Because gene expression is important for spatial transcriptomics analysis, we want to preserve its raw gene expression matrix, so we fixed α_2 to 1.0. We explored the impact of the "ST data augmentation" module on performance by changing *α*1.

α_1		DLPFC.			BCDC.	BRCA						
	ARI		NMI HS Purity ARI NMI HS Purity ARI NMI HS Purity									
			1.0 0.261 0.384 0.377 0.540 0.523 0.415 0.393 0.865 0.535 0.635 0.626 0.583									
			0.5 0.437 0.592 0.614 0.752 0.677 0.572 0.547 0.914 0.569 0.682 0.671 0.634									
			0.2 0.562 0.638 0.648 0.789 0.730 0.584 0.583 0.931 0.660 0.699 0.689 0.678									

Table S4: STMVGAE performs graph combination test results on 12 slices of the DLPFC dataset. STMVGAE integrates the results of four different graphs in a free combination manner to calculate ARI, NMI, HS, and Pur (Purity) respectively. $A^{(1)}$, *A*(2) , *A*(3), and *A*(4) represent Radius_balltree, Radius_kdtree, KNN_balltree, and KNN_kdtree respectively. The best result is underlined.

Slice	$A^{(1)} + A^{(2)}$			$A^{(1)} + A^{(3)}$			$A^{(1)} + A^{(4)}$				$A^{(2)} + A^{(3)}$				$A^{(2)} + A^{(4)}$				$A^{(3)} + A^{(4)}$					
	ARI	NMI	HS	Pur	ARI	NMI	HS	Pur	ARI	NMI	HS	Pur	AR1	NMI	HS	Pur	AR1	NМ	HS	$P_{\rm HF}$	ARI	NМ	НS	Pur
151507	0.549	0.662	0.664	0.685	0.692	0.712	0.763	0.860	0.548	0.644	0.658	0.737	0.561	0.677	0.675	0.698	0.501	0.648	0.673	0.754	0.567	0.698	0.710	0.750
151508	0.594	0.657	0.681	0.813	0.696	0.703	0.724	0.821	0.666	0.689	0.739	0.841	0.582	0.620	0.640	0.801	0.503	0.604	0.606	0.691	0.573	0.664	0.654	0.686
151509	0.421	0.585	0.573	0.672	0.567	0.644	0.636	0.783	0.421	0.588	0.581	0.704	0.504	0.637	0.609	0.699	0.411	0.567	0.560	0.673	0.604	0.653	0.643	0.773
151510	0.557	0.651	0.610	0.737	0.444	0.562	0.532	0.660	0.403	0.559	0.530	0.653	0.548	0.651	0.607	0.719	0.496	0.648	0.613	0.734	0.410	0.560	0.544	0.648
151669	0.400	0.523	0.513	0.775	0.422	0.570	0.530	0.739	0.415	0.562	0.527	0.776	0.201	0.405	0.386	0.670	0.375	0.492	0.499	0.769	0.342	0.512	0.467	0.701
151670	0.386	0.509	0.468	0.722	0.455	0.559	0.527	0.758	0.337	0.475	0.433	0.693	0.324	0.486	0.433	0.650	0.314	0.455	0.412	0.688	0.246	0.414	0.376	0.601
151671	0.770	0.724	0.711	0.866	0.744	0.707	0.720	0.895	0.784	0.751	0.741	0.894	0.706	0.688	0.665	0.833	0.746	0.703	0.773	0.921	0.698	0.708	0.688	0.833
151672	0.670	0.697	0.814	0.925	0.722	0.724	0.740	0.851	0.640	0.658	0.690	0.811	0.700	0.713	0.762	0.902	0.686	0.701	0.710	0.805	0.617	0.654	0.692 0.831	
151673	0.446	0.624	0.670	0.731	0.440	0.618	0.639	0.708	0.464	0.638	0.659	0.739	0.430	0.618	0.647	0.744	0.496	0.645	0.699	0.804	0.499	0.647	0.656	0.749
151674	0.454	0.584	0.591	0.689	0.483	0.608	0.655	0.801	0.427	0.607	0.610	0.667	0.458	0.544	0.552	0.725	0.420	0.554	0.584	0.743	0.466	0.588	0.599	0.711
151675	0.504	0.628	0.656	0.764	0.530	0.601	0.641	0.817	0.538	0.621	0.674	0.839	0.479	0.629	0.697	0.815	0.486	0.601	0.641	0.764	0.528	0.652	0.665	0.767
151676	0.444	0.601	0.641	0.750	0.548	0.643	0.667	0.773	0.513	0.602	0.632	0.758	0.469	0.634	0.664	0.762	0.488	0.611	0.652	0.780	0.477	0.632	0.642	0.715
Average	0.516	0.620	0.633	0.761	0.562	0.638	0.648	0.789	0.513	0.616	0.623	0.759	0.497	0.608	0.611	0.751	0.494	0.602	0.618	0.761	0.502	0.615	0.611	0.730

Table S5: STMVGAE performs graph combination test results on 12 slices of the DLPFC dataset. STMVGAE integrates the results of four different graphs in a free combination manner to calculate ARI, NMI, HS, and Pur (Purity) respectively. $A^{(1)}$, $A^{(2)}$, $A^{(3)}$, and $A^{(4)}$ represent Radius_balltree, Radius_kdtree, KNN_balltree, and KNN_kdtree respectively. The best result is underlined.

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