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 Supplementary Table 1. Details of the nine dynamical models in the period of 1993–2016 used in this study. These nine dynamical models are provided by the China Meteorological Administration (CMA) and the Copernicus Climate Change Service (C3S).

 Supplementary Table 2. The information of six climate indices and corresponding correlations with six precursors. Column 1 lists the six climate indices denoting climate variability modes 47 influencing East Asia rainfall variability, and columns 3–8 represent the correlation coefficients between climate indices and precursors in this study. Endings with two (one) asterisks indicate the values exceeding the 99% (90%) confidence level.

51 **Supplementary Table 3.** Details of three satellite-gauge-based precipitation datasets for the

52 period of 1980–2022.

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55 Supplementary Table 4. A list of data sources for the climate indices listed in Supplementary

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59 **of East-Asian rainfall anomalies in boreal summer**. The three rows from top to bottom represent the monthly spatial patterns of the three distinct spatiotemporal patterns identified in the training 62 period of 1980–2009. Unit of the color bar is mm d^{-1} . The five columns from left to right are spatial rainfall patterns for May, June, July, August, and September, respectively.

 Supplementary Figure 2. Spatiotemporal patterns of continental East-Asian summer rainfall anomalies derived from GPCP observation. The left panels (a, c, e) display the spatiotemporal evolution patterns corresponding to the leading three modes of empirical orthogonal functions (EOFs) derived from monthly precipitation anomalies zonally averaged over East Asia during training period of boreal 1980–2009 summers. The unit of the color bar for the spatiotemporal 72 patterns is mm d^{-1} . The bars in the right panels (b, d, f) are the year-to-year variability of normalized principal components (PCs) of the three spatiotemporal patterns.

Supplementary Figure 3. Same as Supplementary Fig. 2, but for the GPCC.

Supplementary Figure 4. Same as Supplementary Fig. 2, but for the CMAP.

Supplementary Figure 5. Same as Supplementary Fig. 2, but for the monthly station-based

precipitation.

 Supplementary Figure 6. Prediction skills of spatiotemporal evolution based on the three spatiotemporal patterns of East-Asian rainfall anomalies in the physical-statistical prediction model. (a) The observed spatiotemporal evolution using the three spatiotemporal patterns in the independent prediction period. (b) The predicted spatiotemporal evolution reconstructed from the three spatiotemporal patterns and their predicted principal components (PCs) in the independent prediction period. The ordinate is latitude and the abscissa is day of boreal summer in each year. (c) The prediction skills are assessed by the spatiotemporal pattern correlation between the predicted and observed spatiotemporal evolution only based on the three patterns in each boreal summer. The black vertical line separates the retrospective prediction skills in the training period of 1980–2009 from the independent prediction skills in the period of 2010– 2022.

 Supplementary Figure 7. Prediction skills for individual dynamical models. Multi-year mean forecast skills of the spatial pattern correlation against the total rainfall anomalies in individual months for each dynamical model and the physical-statistical prediction model (PSM). Grey dots indicate the multi-model ensemble (MME) mean forecast skill during 1993–2016 derived from nine dynamical models. The blue, red, and pink bars represent the prediction skills of the individual dynamical model (1993–2016), PSM (1993–2016), and PSM (1980–2022), respectively.

 Supplementary Figure 8. Seasonal prediction skills for the spatiotemporal evolution of rainfall anomalies over East Asia. The forecast skills of temporal correlation against total observed anomalies of monthly and spatial rainfall anomalies in boreal summer using the physical- statistical prediction model (PSM) during (a)1993–2016 and (b) 1980–2022.

 East Asia. The prediction skills of spatial pattern correlation against the observed summer rainfall anomalies predicted by the multi-model ensemble (MME) mean of the dynamical models and the physical-statistical prediction model (PSM). The multi-year mean prediction skills during 1993– 2016 for the MME and PSM are 0.07 and 0.43, respectively. The blue line segments represent the ranges of prediction skills derived from individual dynamical models.

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 Supplementary Figure 10. Prediction skills against the observed spatiotemporal evolution of East-Asian rainfall anomalies in individual months. The multi-year mean forecast skills of the spatial pattern correlation against the total rainfall anomalies in each month during 1993–2016 in the multi-model ensemble (MME) mean of the dynamical models and the physical-statistical prediction model (PSM), based on different observation datasets. The abscissa represents the months of May through September.

 Supplementary Figure 11. Seasonal predictions against the observed spatiotemporal evolution of rainfall anomalies as function of latitude and month over East Asia. The spatiotemporal evolution is denoted by (a) the total rainfall anomalies derived from GPCP observation, (b) the predicted field from the physical-statistical prediction model (PSM), and (c) forecasted field from the multi-model ensemble (MME) mean of the dynamical models. The ordinate is latitude and the abscissa is month of boreal summer in each year. The overall forecast skills shown in the top right corner in (b) and (c) are assessed by the spatiotemporal correlation coefficient between forecasted and observed evolution of East-Asian rainfall anomalies for the period of 1993–2016.

- **Supplementary Figure 12.** Same as Supplementary Fig. 11, but for the GPCC.
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- **Supplementary Figure 13.** Same as Supplementary Fig. 11, but for the CMAP.
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150 Supplementary Fig. 14. Schematic diagram of the independent retrospective prediction in a

152 **forward rolling manner**. The independent prediction is based on the three multi-regression

153 models derived from each PC_j ($j = 1, 2, 3$) and their two precursors (X^i_j , $i = 1, 2$).

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