

APPENDIX

Sets of rate equations and kinetic parameters used for mathematical modelling.

V_{\max} values of the glycolytic enzymes and all kinetic parameters for the TPI reaction were determined experimentally. The rate equations and additional kinetic parameters used for computation of the whole glycolytic pathway were taken from the model of Mulquiney and Kuchel [10] for the glycolytic enzymes. Expressions for bisphosphoglycerate mutase (BPGM), bisphosphoglycerate phosphatase (BPGP) and their parameters were based on the results described in reference [9].

v^{HK}	Glucose + ATP = G6P + ADP
v^{GPI}	G6P = F6P
v^{PFK}	F6P + ATP = FBP + ADP
$v^{Aldolase}$	FBP = DHAP + GAP
v^{TPI}	GAP = DHAP
v^{GAPDH}	GAP + NAD + Pi = G1,3DP + NADH + H ⁺
v^{PGK}	G1,3DP + ADP = 3-PG + ATP
v^{PGM}	3-PG = 2-PG
$v^{Enolase}$	2-PG = PEP
v^{PK}	PEP + ADP = Pyruvate + ATP + Pi
v^{LDH}	Pyruvate + NADH = Lactate + NAD
v^{BPGM}	G1,3DP = G2,3DP
v^{BPGM}	G2,3DP = 3-PG + Pi

HK EC 2.7.1.1

$$v^{HK} = \frac{V_{\max}^{HK} * \left(\frac{[Glucose] * [ATP]}{K_M^{HK} * K_{M1}^{HK}} - \frac{[G6P] * [ADP]}{K_e^{HK}} \right)}{1 + \frac{[Glucose]}{K_M^{HK}} + \frac{[ATP]}{K_{M1}^{HK}} + \frac{[G6P]}{K_{M2}^{HK}} + \frac{[ADP]}{K_{M3}^{HK}} + \frac{[Glucose] * [ATP]}{K_M^{HK} * K_{M1}^{HK}} + \frac{[G6P] * [ADP]}{K_{M2}^{HK} * K_{M3}^{HK}}}$$

$$K_M^{HK} = 50 \mu\text{M}, K_{M1}^{HK} = 1000 \mu\text{M}, K_{M2}^{HK} = 50 \mu\text{M}, K_{M3}^{HK} = 1000 \mu\text{M}, K_e^{HK} = 7.75 * 10^6 \mu\text{M}^2$$

$$V_{\max}^{HK} = 0.62 \text{ U/g Hb for control}, V_{\max}^{HK} = 1.47 \text{ U/g Hb for patient}$$

GPI**EC 5.3.1.9**

$$v^{GPI} = \frac{V_{\max}^{GPI}}{K_M^{GPI}} * \frac{[G6P] - \frac{[F6P]}{Ke^{GPI}}}{1 + \frac{[G6P]}{K_M^{GPI}} + \frac{[F6P]}{K_{M1}^{GPI}}}$$

$$K_M^{GPI} = 200 \mu\text{M}, K_{M1}^{GPI} = 80 \mu\text{M}, Ke^{GPI} = 0.329$$

$$V_{\max}^{GPI} = 30 \text{ U/g Hb for control}, V_{\max}^{GPI} = 30 \text{ U/g Hb for patient}$$

PFK**EC 2.7.1.11**

$$v^{PFK} = \frac{V_{\max}^{PFK} * \left(\frac{[F6P] * [ATP]}{K_M^{PFK} * K_{M1}^{PFK}} - \frac{[FBP] * [ADP]}{Ke^{PFK}} \right)}{1 + \frac{[F6P]}{K_M^{PFK}} + \frac{[ATP]}{K_{M1}^{PFK}} + \frac{[FBP]}{K_{M2}^{PFK}} + \frac{[ADP]}{K_{M3}^{PFK}} + \frac{[F6P] * [ATP]}{K_M^{PFK} * K_{M1}^{PFK}} + \frac{[FBP] * [ADP]}{K_{M2}^{PFK} * K_{M3}^{PFK}}} * \frac{1}{1 + f}$$

$$f = \frac{\left(\frac{h}{Ka} \right)^n * \left(1 + \frac{[ATP]}{K_{M1}^{PFK}} \right)^4 * \left(1 + \frac{[Mg^{2+}]}{K_{M4}^{PFK}} \right)^4}{\left(1 + \frac{[F6P]}{K_M^{PFK}} + \frac{[FBP]}{K_{M2}^{PFK}} \right)^4 * \left(1 + \frac{[P_i]}{K_{M5}^{PFK}} \right)^4}$$

$$K_M^{PFK} = 100 \mu\text{M}, K_{M1}^{PFK} = 100 \mu\text{M}, K_{M2}^{PFK} = 600 \mu\text{M}, K_{M3}^{PFK} = 600 \mu\text{M},$$

$$K_{M4}^{PFK} = 4 \text{ mM},$$

$$K_{M5}^{PFK} = 30 \text{ mM}, Ke^{PFK} = 1.44 * 10^7 \mu\text{M}^2, h = [H^+], pKa = 7.05, n = 5$$

$$V_{\max}^{PFK} = 17.3 \text{ U/g Hb for control}, V_{\max}^{PFK} = 34.3 \text{ U/g Hb for patient}$$

Aldolase**EC 4.1.2.13**

$$v^{ALD} = \frac{V_{\max}^{ALD} * \left(\frac{[FBP]}{K_M^{ALD}} - \frac{[DHAP] * [GAP]}{Ke^{ALD}} \right)}{1 + \frac{[FBP]}{K_M^{ALD}} + \frac{[DHAP]}{K_{M1}^{ALD}} + \frac{(K_{M3}^{ALD} * [GAP]) + ([DHAP] * [GAP])}{K_{M1}^{ALD} * K_{M2}^{ALD}} + \frac{K_{M3}^{ALD} * [FBP] * [GAP]}{K_{M1}^{ALD} * K_{M2}^{ALD} * K_{M4}^{ALD}}}$$

$$K_M^{ALD} = 8 \mu\text{M}, K_{M1}^{ALD} = 10 \mu\text{M}, K_{M2}^{ALD} = 40 \mu\text{M}, K_{M3}^{ALD} = 40 \mu\text{M},$$

$$K_{M4}^{ALD} = 15 \mu\text{M}, Ke^{ALD} = 140 \mu\text{M}^2,$$

$$V_{\max}^{ALD} = 4.6 \text{ U/g Hb for control}, V_{\max}^{ALD} = 6.7 \text{ U/g Hb for patient}$$

TPI EC 5.3.1.1

$$v^{TPI} = \frac{V_{\max}^{TPI}}{K_M^{TPI}} * \frac{[GAP] - \frac{[DHAP]}{K_e^{TPI}}}{1 + \frac{[GAP]}{K_M^{TPI}} + \frac{[DHAP]}{K_{M1}^{TPI}}}$$

$K_M^{TPI} = 650 \mu\text{M}$, $K_{M1}^{TPI} = 1300 \mu\text{M}$, $K_e^{TPI} = 9$, $V_{\max}^{TPI} = 1750 \text{ U/g Hb}$ for control,
 $V_{\max}^{TPI} = 36.5 \text{ U/g Hb}$ for patient

GAPDH EC 1.2.1.12

$$v^{GAPDH} = \frac{V_{\max}^{GAPDH} * \left(\frac{[GAP] * [NAD] * [P_i]}{K_M^{GAPDH} * K_{M1}^{GAPDH} * K_{M2}^{GAPDH}} - \frac{[G1,3DP] * [NADH] * [H^+]}{K_e^{GAPDH} * K_{M3}^{GAPDH} * K_{M4}^{GAPDH}} \right)}{\left(\frac{[GAP]}{K_{M2}^{GAPDH}} + \frac{[G1,3DP]}{K_{M3}^{GAPDH}} + \frac{[GAP] * [P_i]}{K_{M1}^{GAPDH} * K_{M2}^{GAPDH}} \right) \left(1 + \frac{[GAP]}{K_{M5}^{GAPDH}} \right) + w1 + w2 + w3 + w4}$$

$$w1 = \frac{K_{M6}^{GAPDH} * [NADH] * [H^+]}{K_{M3}^{GAPDH} * K_{M4}^{GAPDH}} + \frac{K_{M7}^{GAPDH} * [NAD] * [P_i]}{K_M^{GAPDH} * K_{M1}^{GAPDH} * K_{M2}^{GAPDH}} + \frac{[NAD] * [GAP]}{K_{M8}^{GAPDH} * K_{M2}^{GAPDH}}$$

w2=

$$\frac{[NAD] * [G1,3DP]}{K_{M3}^{GAPDH} * K_{M8}^{GAPDH}} + \frac{[GAP] * [NAD] * [P_i]}{K_M^{GAPDH} * K_{M1}^{GAPDH} * K_{M2}^{GAPDH}} + \frac{K_{M7}^{GAPDH} * [NAD] * [P_i] * [G1,3DP]}{K_M^{GAPDH} * K_{M2}^{GAPDH} * K_{M1}^{GAPDH} * K_{M9}^{GAPDH}}$$

$$w3 = \frac{[G1,3DP] * [NADH] * [H^+]}{K_{M3}^{GAPDH} * K_{M4}^{GAPDH}} + \frac{[GAP] * [NADH] * [H^+]}{K_{M10}^{GAPDH} * K_{M2}^{GAPDH}} + \frac{K_{M6}^{GAPDH} * [P_i] * [NADH] * [H^+]}{K_{M1}^{GAPDH} * K_{M3}^{GAPDH} * K_{M4}^{GAPDH}}$$

$$w4 = \frac{[GAP] * [P_i] * [NADH] * [H^+]}{K_{M1}^{GAPDH} * K_{M2}^{GAPDH} * K_{M10}^{GAPDH}} + \frac{K_{M6}^{GAPDH} * [G1,3DP] * [P_i] * [NADH] * [H^+]}{K_{M3}^{GAPDH} * K_{M9}^{GAPDH} * K_{M1}^{GAPDH} * K_{M4}^{GAPDH}}$$

$K_M^{GAPDH} = 45 \mu\text{M}$, $K_{M1}^{GAPDH} = 3200 \mu\text{M}$, $K_{M2}^{GAPDH} = 1.6 * 10^{-14} \mu\text{M}$, $K_{M3}^{GAPDH} = 1.6 * 10^{-15} \mu\text{M}$,

$K_{M4}^{GAPDH} = 21 \mu\text{M}$, $K_{M5}^{GAPDH} = 31 \mu\text{M}$, $K_{M6}^{GAPDH} = 0.67 \mu\text{M}$, $K_{M7}^{GAPDH} = 100 \mu\text{M}$, $K_{M8}^{GAPDH} = 45 \mu\text{M}$,

$K_{M9}^{GAPDH} = 1 \mu\text{M}$, $K_{M10}^{GAPDH} = 64 \mu\text{M}$, $K_e^{GAPDH} = 1.34$,

$V_{\max}^{GAPDH} = 130 \text{ U/g Hb}$ for control, $V_{\max}^{GAPDH} = 210 \text{ U/g Hb}$ for patient

PGK**EC 2.7.2.3**

$$v^{PGK} = \frac{V_{\max}^{PGK} * \left(\frac{[G1,3DP] * [ADP]}{K_M^{PGK} * K_{M1}^{PGK}} - \frac{[3-PG] * [ATP]}{K_e^{PGK} * K_{M2}^{PGK} * K_{M3}^{PGK}} \right)}{1 + \frac{[G1,3DP]}{K_{M4}^{PGK}} + \frac{[ADP]}{K_M^{PGK}} + \frac{[3-PG]}{K_{M5}^{PGK}} + \frac{[ATP]}{K_{M2}^{PGK}} + \frac{[G1,3DP] * [ADP]}{K_M^{PGK} * K_{M1}^{PGK}} + \frac{[3-PG] * [ADP]}{K_{M2}^{PGK} * K_{M3}^{PGK}}}$$

$$K_M^{PGK} = 80 \mu\text{M}, K_{M1}^{PGK} = 2 \mu\text{M}, K_{M2}^{PGK} = 200 \mu\text{M}, K_{M3}^{PGK} = 1100 \mu\text{M}, K_{M4}^{PGK} = 1600 \mu\text{M},$$

$$K_{M5}^{PGK} = 205 \mu\text{M}, K_e^{PGK} = 2.5,$$

$$V_{\max}^{PGK} = 290 \text{ U/g Hb for control}, V_{\max}^{PGK} = 290 \text{ U/g Hb for patient}$$

PGM**EC 5.4.2.1**

$$v^{PGM} = \frac{V_{\max}^{PGM} * \left(\frac{[3-PG] - \frac{[2-PG]}{K_e^{PGM}}}{1 + \frac{[3-PG]}{K_M^{PGM}} + \frac{[2-PG]}{K_{M1}^{PGM}}} \right)}{1 + \frac{[3-PG]}{K_M^{PGM}} + \frac{[2-PG]}{K_{M1}^{PGM}}}$$

$$K_M^{PGM} = 168 \mu\text{M}, K_{M1}^{PGM} = 26 \mu\text{M}, K_e^{PGM} = 0.17,$$

$$V_{\max}^{PGM} = 22 \text{ U/g Hb for control}, V_{\max}^{PGM} = 22 \text{ U/g Hb for patient}$$

Enolase**EC 4.2.1.11**

$$v^{enolase} = \frac{V_{\max}^{enolase} * \left(\frac{[2-PG] * [Mg^{2+}]}{K_M^{enolase} * K_{M1}^{enolase}} - \frac{[PEP] * [Mg^{2+}]}{K_e^{enolase} * K_{M2}^{enolase} * K_{M3}^{enolase}} \right)}{1 + \frac{[2-PG]}{K_{M4}^{enolase}} + \frac{[Mg^{2+}]}{K_M^{enolase}} + \frac{[PEP]}{K_{M2}^{enolase}} + \frac{[2-PG] * [Mg^{2+}]}{K_M^{enolase} * K_{M1}^{enolase}} + \frac{[PEP] * [Mg^{2+}]}{K_{M2}^{enolase} * K_{M3}^{enolase}}}$$

$$K_M^{enolase} = 46 \mu\text{M}, K_{M1}^{enolase} = 140 \mu\text{M}, K_{M2}^{enolase} = 111 \mu\text{M}, K_{M3}^{enolase} = 111 \mu\text{M},$$

$$K_{M4}^{enolase} = 140 \mu\text{M}, K_e^{enolase} = 4,$$

$$V_{\max}^{enolase} = 10 \text{ U/g Hb for control}, V_{\max}^{enolase} = 10 \text{ U/g Hb for patient}$$

PK**EC 2.7.1.40**

$$v^{PK} = \frac{V_{\max}^{PK} * \left(\frac{[PEP]*[ADP]}{K_M^{PK} * K_{M1}^{PK}} - \frac{[Pyr]*[ATP]}{K_e^{PK} * K_{M2}^{PK} * K_{M3}^{PK}} \right)}{1 + \frac{[PEP]}{K_M^{PK}} + \frac{[ADP]}{K_{M1}^{PK}} + \frac{[Pyr]}{K_{M2}^{PK}} + \frac{[ATP]}{K_{M3}^{PK}} + \frac{[PEP]*[ADP]}{K_M^{PK} * K_{M1}^{PK}} + \frac{[Pyr]*[ATP]}{K_{M2}^{PK} * K_{M3}^{PK}}} * \frac{1}{1 + f^{PK}}$$

$$f^{PK} = \frac{\left(\frac{h}{K_a} \right)^n * \left(1 + \frac{[ATP]}{K_{M4}^{PK}} \right)^4}{\left(1 + \frac{[PEP]}{K_{M5}^{PK}} + \frac{[Pyr]}{K_{M2}^{PK}} \right)^4 * \left(1 + \frac{[FBP]}{K_{M6}^{PK}} \right)^4}$$

$$K_M^{PK} = 225 \mu\text{M}, K_{M1}^{PK} = 474 \mu\text{M}, K_{M2}^{PK} = 2000 \mu\text{M},$$

$$K_{M3}^{PK} = 3000 \mu\text{M}, K_{M4}^{PK} = 3.4 \text{ mM},$$

$$K_{M5}^{PK} = 255 \mu\text{M}, K_{M6}^{PK} = 5 \mu\text{M}, K_e^{PK} = 425, h = [\text{H}^+], \text{pKa} = 6.8, n = 1,$$

$$V_{\max}^{PK} = 14 \text{ U/g Hb for control}, V_{\max}^{PK} = 26 \text{ U/g Hb for patient}$$

LDH**EC 1.1.1.27**

$$v^{LDH} = \frac{V_{\max}^{LDH} * \left(\frac{[NADH]*[Pyr]}{K_M^{LDH} * K_{M1}^{LDH}} - \frac{[Lac]*[NAD]}{K_e^{LDH} * K_{M2}^{LDH} * K_{M3}^{LDH}} \right)}{q1 + \frac{[NADH]}{K_M^{LDH}} + \frac{[NAD]}{K_{M3}^{LDH}} + \frac{[NADH]*[Pyr]}{K_M^{LDH} * K_{M1}^{LDH}} + q2 + \frac{[Lac]*[NAD]}{K_{M2}^{LDH} * K_{M3}^{LDH}} +}$$

$$q1 = \left(1 + \frac{K_{M4}^{LDH} * [Pyr]}{K_M^{LDH} * K_{M1}^{LDH}} + \frac{K_{M5}^{LDH} * [Lac]}{K_{M2}^{LDH} * K_{M3}^{LDH}} \right) * \left(1 + \frac{[Pyr]}{K_{M6}^{LDH}} \right)$$

$$q2 = \frac{[NADH]*[Lac]*K_{M5}^{LDH}}{K_M^{LDH} * K_{M2}^{LDH} * K_{M3}^{LDH}} + \frac{[NAD]*[Pyr]*K_{M4}^{LDH}}{K_M^{LDH} * K_{M1}^{LDH} * K_{M3}^{LDH}}$$

$$q3 = \frac{[NADH]*[Pyr]*[Lac]}{K_M^{LDH} * K_{M1}^{LDH} * K_{M7}^{LDH}} + \frac{[NAD]*[Pyr]*[Lac]}{K_{M8}^{LDH} * K_{M2}^{LDH} * K_{M3}^{LDH}}$$

$$K_M^{LDH} = 2.45 \mu\text{M}, K_{M1}^{LDH} = 137 \mu\text{M}, K_{M2}^{LDH} = 503 \mu\text{M}, K_{M3}^{LDH} = 1070 \mu\text{M},$$

$$K_{M4}^{LDH} = 8.44 \mu\text{M},$$

$$K_{M5}^{LDH} = 107 \mu\text{M}, K_{M6}^{LDH} = 101 \mu\text{M}, K_{M7}^{LDH} = 7330 \mu\text{M}, K_{M8}^{LDH} = 228 \mu\text{M}, K_e^{LDH} = 4,$$

$$V_{\max}^{LDH} = 185 \text{ U/g Hb for control}, V_{\max}^{LDH} = 185 \text{ U/g Hb for patient}$$

BPGM EC 5.4.2.4

$$v^{BPGM} = \frac{V_{\max}^{BPGM} * [G1,3DP]}{K_M^{BPGM} + K_{M1}^{BPGM} * [G1,3DP] + [G2,3DP]}$$

$$K_M^{BPGM} = 40 \mu\text{M}, K_{M1}^{BPGM} = 0.013,$$

$$V_{\max}^{BPGM} = 170 \text{ U/g Hb for control}, V_{\max}^{BPGM} = 170 \text{ U/g Hb for patient}$$

BPGP EC 3.1.3.13

$$v^{BPGP} = \frac{V_{\max}^{BPGP} * [G2,3DP]}{K_M^{BPGP} * (1 + ([2 - PG] + [3 - PG]) / K_{M1}^{BPGP}) + [G2,3DP]}$$

$$K_M^{BPGP} = 20 \mu\text{M}, K_{M1}^{BPGP} = 0.006,$$

$$V_{\max}^{BPGP} = 0.027 \text{ U/g Hb for control}, V_{\max}^{BPGP} = 0.027 \text{ U/g Hb for patient}$$

$$\frac{d[\text{Glu cos e}]}{dt} = -v^{HK}, \frac{d[G6P]}{dt} = -v^{GPI} + v^{HK}, \frac{d[F6P]}{dt} = v^{GPI} - v^{PFK},$$

$$\frac{d[FBP]}{dt} = v^{PFK} - v^{ALD}, \frac{d[DHAP]}{dt} = v^{ALD} + v^{TPI},$$

$$\frac{d[GAP]}{dt} = v^{ALD} - v^{TPI} - v^{GAPDH}, \frac{d[G1,3DP]}{dt} = v^{GAPDH} - v^{PGK} - v^{BPGM},$$

$$\frac{d[3 - PG]}{dt} = v^{PGK} + v^{BPGP} - v^{PGM}, \frac{d[2 - PG]}{dt} = v^{PGM} - v^{enolase},$$

$$\frac{d[PEP]}{dt} = v^{enolase} - v^{PK}, \frac{d[NAD]}{dt} = v^{LDH} - v^{GAPDH}, \frac{d[NADH]}{dt} = v^{GAPDH} - v^{LDH}$$