Enhanced Efficiency of Quantitative Trait Loci Mapping Analysis Based on Multivariate Complexes of Quantitative Traits

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ABSTRACT

An approach to increase the efficiency of mapping quantitative trait loci (QTL) was proposed earlier by the authors on the basis of bivariate analysis of correlated traits. The power of QTL detection using the log-likelihood ratio (LOD scores) grows proportionally to the broad sense heritability. We found that this relationship holds also for correlated traits, so that an increased bivariate heritability implicates a higher LOD score, higher detection power, and better mapping resolution. However, the increased number of parameters to be estimated complicates the application of this approach when a large number of traits are considered simultaneously. Here we present a multivariate generalization of our previous two-trait QTL analysis. The proposed multivariate analogue of QTL contribution to the broad-sense heritability based on interval-specific calculation of eigenvalues and eigenvectors of the residual covariance matrix allows prediction of the expected QTL detection power and mapping resolution for any subset of the initial multivariate trait complex. Permutation technique allows chromosome-wise testing of significance for the whole trait complex and the significance of the contribution of individual traits owing to: (a) their correlation with other traits, (b) dependence on the chromosome in question, and (c) both a and b. An example of application of the proposed method on a real data set of 11 traits from an experiment performed on an F_2/F_3 mapping population of tetraploid wheat (*Triticum durum* \times *T. dicoccoides*) is provided.

THE detection power and mapping resolution of marker analysis of quantitative traits are the major factors affecting practical applications of quantitative trait loci (QTL) mapping. These characteristics strongly depend on the effect of the QTL in question relative to the phenotypic variance of the trait in the mapping population. The higher the discrepancy between QTL groups (or the contribution of the QTL to the trait heritability H^2 , the proportion of genetic variation σ_G^2 in total phenotypic variation σ_{Ph}^2 of the trait) the better the expected QTL detection power and mapping resolution. As shown by LANDER and BOTSTEIN (1989), the expected value of the log-likelihood test statistics increases monotonically with H^2 :

$$ELOD = -\frac{1}{2}N\log(1 - H^2).$$
 (1)

Several strategies have been proposed to improve the precision of QTL mapping. These involve development of (i) new experimental designs to suit specific mapping goals and an organism's breeding system, and (ii) new QTL mapping models and algorithms to extract maximum information about QTL locations and effects. One of the improvements includes multilocus (composite) mapping analysis (JANSEN and STAM 1994; ZENG 1994), selective sampling (LEBOWITZ *et al.* 1987; DARVASI and

SOLLER 1994), replicated progeny testing (SOLLER and BECKMANN 1990), and sequential experimentation (MOTRO and SOLLER 1993). For example, in composite mapping the increase in mapping resolution derives from a reduction of the residual variation by taking into account the effects of cosegregating QTL.

In QTL mapping, the experimental design usually includes simultaneous measurements of many related and unrelated quantitative traits and subsequent treatment of the individual traits. Recently, several groups attempted to improve the efficiency of marker analysis of QTL by taking into account possible effects of the putative QTL on several traits simultaneously (KOROL et al. 1987, 1995, 1998a; Amos et al. 1990; Schork et al. 1994; JIANG and ZENG 1995; RONIN et al. 1995, 1998, 1999; Weller et al. 1996; Almasy et al. 1997; Boomsma and DOLAN 1998; MANGIN et al. 1998; HENSHALL and GODDARD 1999; OLSON et al. 1999; WILLIAMS et al. 1999; ZENG et al. 2000). In the simplest case of two noncorrelated traits, the advantage of joint analysis is in the increase of the *multivariate effect* according to $d^2 = (d_x/dx)^2$ σ_x ² + $(d_y/\sigma_y)^2$ (Figure 1a), where d_x and d_y are the substitution effects of the QTL for traits x and y, and σ_x and σ_y are the corresponding standard deviations within the QTL groups (residual standard deviations). Consequently, for a population with 1:1 ratio of the alternative QTL groups (like backcross, dihaploid, or recombinant inbreds) the bivariate analogue of H^2 could be represented in the form

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$$H_{xy}^2 = \frac{\frac{1}{4}d^2}{1 + \frac{1}{4}d^2}.$$
 (2)

The situation becomes more complicated when correlated traits are involved. It can be shown (KOROL *et al.* 1995) that Equation 1 remains valid in bivariate analysis of correlated traits,

$$\text{ELOD}(x, y) = -\frac{1}{2}N\log(1 - H_{xy}^2)$$
(1')

with

$$H_{xy}^{2} = 1 - \frac{\sigma_{x}^{2}\sigma_{y}^{2} (1 - R_{xy}^{2})}{(\sigma_{x}^{2} + \frac{1}{4}d_{x}^{2})(\sigma_{y}^{2} + \frac{1}{4}d_{y}^{2}) - \sigma_{x}^{2}\sigma_{y}^{2}[R_{xy} + d_{x}d_{y}/(4\sigma_{x}\sigma_{y})]^{2}}.$$
(3)

It was shown earlier that either $ELOD(x, y) \ge ELOD(x)$ and ELOD(x, y) \geq ELOD(y) follow from $H_{xy}^2 \geq H_x^2$ and $H_{xy}^2 \ge H_y^2$, respectively (KOROL *et al.* 1995; RONIN *et al.* 1999). Given fixed d_x/σ_x or $H_x^2 = \frac{1}{4}d_x^2/(\frac{1}{4}d_x^2 + \sigma_x^2)$, how will the resolution be affected by other traits being taken into account? Several situations should be considered to explain the expected gain of joint analysis of multiple traits compared to single-trait analysis. For the sake of simplicity, let us consider two traits. As mentioned above, if $R_{xy} = 0$, the effect of an additional trait is simply due to the increased Euclidean distance between the (two-dimensional) centers of the QTL groups (see Figure 1a). Consider now the situation when the traits are correlated within each of the QTL groups with residual correlation $R_{xy} \neq 0$. It is easy to see from Equation 3 that if $d_{y} \neq 0$ and $R_{xy} \neq 0$ and $\operatorname{sign}(R_{xy}d_{x}d_{y}) < 0$, then $H_{xy}^2 \ge H_x^2$ and one could expect a respective increase in ELOD. Moreover, the inequality $H_{xy}^2 > H_x^2$ holds even if $d_y = 0$ but $R_{xy} \neq 0$, independent of the sign of correlation (Figure 1b). Therefore, we can further assume that the increment in H_{xy}^2 , compared with H_x^2 , will result in an increased resolution of the mapping analysis (in spite of complications due to certain statistical nonequivalence), no matter how this increment in H_{xy}^2 was produced, due to (i) the pleiotropic effect of the QTL on x and y, (ii) residual correlation between x and y (within the QTL groups) caused by nongenetic effects or segregation of unlinked QTL, or (iii) the combined effect of both factors (i) and (ii) (Figure 1c). In other words, instead of separate analyses of traits x and y, one can conduct joint analysis of these traits that is formally equivalent to transformation of a two-dimensional phe-



FIGURE 1.—The main sources for improvement of QTL mapping efficiency in multiple-trait analysis: (a) due to the pleiotropic effects; (b) due to correlation between the traits (within the QTL groups) caused by nongenetic effects and segregation of unlinked QTL; or (c) due to *combined effect* of both foregoing factors.

notype into a one-dimensional phenotype. For the new phenotype, a higher ratio of the between-OTL group difference to the residual variation can be achieved owing to the pleiotropic effect of the QTL on both traits, and residual correlation between the traits caused by nongenetic factors and segregation at other QTL. These expectations, illustrated geometrically in Figure 1, are confirmed by both Monte Carlo simulations and analytical approximations, for marker and interval analysis (KOROL et al. 1995, 1998a; RONIN et al. 1995, 1999). Although the described approach resembles the principal component analysis (PCA), it differs from PCA significantly. Besides technical differences, the main dissimilarity is that our trait transformations are interval dependent (KOROL et al. 1995), whereas in PCA the transformation is applied to the initial trait complex (WELLER et al. 1996). This difference may be important if the mapping population segregates for more than one QTL (see below).

Clearly, not only statistical reasons are of interest when discussing the advantages of the joint analysis of correlated trait complexes. The multitrait approach allows for an integral evaluation of the effects of genomic segments on a defined group of traits. Because of the internal balance of the organism's systems (SCHMAL-HAUSEN 1942), such an approach for QTL mapping seems to be much more justified biologically than the usual "trait-by-trait" analysis. It may assist in testing numerous biologically important hypotheses concerning manifold effects of genomic segments on quantitative variation, to distinguish between linkage and pleiotropy as mechanisms of genetic correlation, to address the problem of QTL-by-environment interaction, etc. (KOROL et al. 1994, 1998b; JIANG and ZENG 1995; LEBRETON et al. 1998; RONIN et al. 1999). Such analysis may be of major importance in formulating marker-assisted breeding strategies, dissecting heterosis as a multilocus multitrait phenomenon, developing optimized programs for evaluation and bioconservation of genetic resources, and revealing the genetic architecture of fitness systems in natural populations and of multifactorial diseases in humans.

The increased number of parameters to be estimated complicates the application of this approach when a large number of traits are considered. With n traits to be analyzed simultaneously in the simplest case of a

backcross (as well as a dihaploid or recombinant inbred lines) mapping population using single-interval mapping, the model should include $(n^2 + 5n + 2)/2$ parameters [QTL position, *n* mean values, *n* effects, *n* residual variances, and n(n-1)/2 covariances]. At n = 10, this amounts to 76 parameters.

One possible *ad hoc* simplification of the estimation aspects is based on a reduction to two-trait analysis (KOROL et al. 1995, 1998a; RONIN et al. 1995, 1999; JIANG and ZENG 1995) that appeared to be very efficient in allowing for an increase in QTL detection power and mapping resolution. In specific situations, such a reduction to a two-trait analysis may also be justified by the biological nature of the involved traits. However, in real multitrait situations this approach may result in statistical difficulties caused by the large number of trait pairs. Corresponding multiple tests may be interdependent, causing a further complication in defining the critical values of the test statistics. Another possibility is related to the attempt at space transformation, e.g., using the PCA (WELLER et al. 1996; MANGIN et al. 1998) applied to the multivariate trait distribution across the entire data set. Although this approach seems to be very attractive, it cannot directly solve the problem when the mapping population segregates for more than one QTL, especially if some of the effects are relatively strong. Indeed, assume that in such a case the PCA transformation was applied to the initial trait complex (without taking out the effects of the target QTL), i.e., for all individuals independent of their genotypes. Then, the independence of the resulting derivative traits over the entire mapping population cannot guarantee their independence within the alternative QTL groups. Moreover, this problem may exist even in the case of one QTL segregating in the mapping population, because the total (across all individuals) variance-covariance matrix of the initial trait complex may differ from the residual one (i.e., for the matrix characterizing the within-QTL group variation). It is noteworthy that the largest principal components may be irrelevant in such an analysis, as can be seen from Figure 1c (see also OLSON et al. 1999). Nevertheless, in some cases this approach may work (in situations represented by Figure 1a).

Here we present a generalization of our previous twoand three-trait QTL mapping algorithm (KOROL *et al.* 1995; RONIN *et al.* 1995), which is free of the mentioned difficulties, to multivariate trait complexes that allow analysis of a large number of traits. It is based on transformation of the initial trait space into a space of a lower dimension. In the simplest case of a single-QTL analysis of a backcross (dihaploid) mapping population, the resulting space is one-dimensional independent of the number of traits, whereas two-QTL analysis for such a population will employ a two-dimensional model (for F_2 these will be three- and eight-dimensional models, correspondingly). The main difference between our previous two-trait models (KOROL *et al.* 1995, 1998a; RONIN *et al.* 1995, 1998, 1999; see also JIANG and ZENG 1995) and the foregoing PCA-based models lies in the fact that the residual variance-covariance matrix was considered interval dependent, in the following sense. Its elements are a subset of the vector of unknown parameters to be estimated by the employed procedure *for each interval*, so that for QTL residing in different genomic segments the resulting (transformed) traits could be very different. This interval dependence remains a notable characteristic of our new multivariate algorithm.

THE PROPOSED METHOD

The model: Assume first that only one QTL segregates in the mapping population. Consider the genomic segment carrying this QTL (with alleles Q and q) flanked by markers M_1/m_1 and M_2/m_2 , with recombination rates r_1 and r_2 in intervals $M_1/m_1-Q/q$ and $Q/q-M_2/m_2$. On the basis of the marker scores and the measurements of the trait complex $\mathbf{x} = (x_1, x_2, \ldots, x_n)$, we should test whether or not variation of any trait of \mathbf{x} indeed depends on the interval $M_1/m_1-M_2/m_2$ and identify the corresponding locus Q/q. The expected joint distributions of the traits \mathbf{x} in each of the marker groups, $U_{m_1m_2} =$ $U_1(\mathbf{x})$, $U_{M_1m_2}(\mathbf{x}) = U_2(\mathbf{x})$, $U_{m_1M_2}(\mathbf{x}) = U_3(\mathbf{x})$, and $U_{M_1M_2}(\mathbf{x}) = U_4(\mathbf{x})$, can be written as

$$U_i(\mathbf{x}) = \pi_i fqq(\mathbf{x}) + (1 - \pi_i) fQq(\mathbf{x}), \quad i = 1, \ldots, 4,$$

where the proportions $\pi_i = \pi_i(r_1, r_2)$ depend on unknown recombination rates r_1 and r_2 and mode of interference. The specification of the *n*-dimensional densities $fqq(\mathbf{x})$ and $fQq(\mathbf{x})$ depends on the assumptions made about the genetic control of the traits. The simplest case of additive control can be represented by the model

$$\mathbf{x} = \mathbf{m} + \mathbf{0.5d}g_q + \mathbf{e},$$

where $\mathbf{x} = (x_1, \ldots, x_n)$ is the vector of phenotype scores for an arbitrary individual, $\mathbf{e} = (e_2, \ldots, e_n)$ is a vector of random variables that obey multivariate normal distribution with zero expectations for all coordinates and (residual) variance-covariance matrix $\Sigma_{\mathbf{R}} = \{s_{ij}\}$, **m** is the vector of trait means, **d** is the vector of the effects of substitution at the Q/q locus with respect to mean values of **x**, *i.e.*, $dx_i = \mu_{x_i}(Qq) - \mu_{x_i}(qq)$, and g_q denotes the genotype at locus $Q/q(g_q = -1$ for qq and 1 for Qq).

Expected improvement owing to multiple-trait analysis: As in the bivariate case, the QTL detection power should depend on the total contribution of the QTL to multivariate phenotypic variation (V_{Ph}) of the correlated trait complex. If V_R is the multivariate residual variation (within the QTL groups) and V_G is the combined between-QTL-group discrepancy, then

$$H_{\rm T}^2 = V_{\rm G}/V_{\rm Ph} = V_{\rm G}/(V_{\rm G} + V_{\rm R}).$$
 (4)

In the case of noncorrelated traits, the improvement is

due to the "Euclidean effect," which grows with the number of traits:

$$H_{\rm Eu}^2 = \frac{\frac{1}{4}\sum (d_i/\sigma_i)^2}{1 + \frac{1}{4}\sum (d_i/\sigma_i)^2}.$$
 (5)

Clearly, in the general case of correlated traits, the pure Euclidean contribution is only a part of the total effect, so that $H_{Eu}^2 < H_T^2$. Note that an analogue of Equation 5 can be obtained by canonical transformation of the initial trait space (with the within-group covariance matrix associated with the QTL under consideration), allowing the evaluation of the total effect as defined by Equation 4. Then, the multivariate effect of the QTL will be manifested as in Equation 5, but with relative effects (d_i/σ_i) in the new coordinate system. Moreover, using scale transformations $x'_i = x_i / \sigma_i$ and corresponding angular transformations, one can map the multivariate space into another multivariate space where the QTL affects only one trait, with $H_D^2 = \frac{1}{4}D^2/(1 + \frac{1}{4}D^2)$ being equal to the total contribution of the QTL, as in Equation 4 (where D is the total multivariate effect of the QTL).

The short review in the Introduction indicates that correlation between traits may be no less (if not more) an important factor affecting the detection power of multitrait QTL analysis. Therefore, it is of great interest to evaluate the contribution of correlations between the traits to H_T^2 in Equation 4. Consequently, in the following illustrations, we present the expected improvement due to the Euclidean effect and the additional contribution due to correlations. Moreover, although no effect is expected from correlations if all effects d_i are 0, situations are possible where for only a small subset of traits $d_i \neq 0$, the remaining traits are still very informative because of their correlations to the foregoing traits (the simplest such example is provided in Figure 1b).

The numerical procedures of interval analysis: The distinctive feature of our analysis is that all the multivariate transformations are *interval-specific* (as can be seen from procedures 1 and 2 described below; see also KOROL et al. 1987, 1995, 1998a; JIANG and ZENG 1995; RONIN et al. 1998), in contrast to the aforementioned attempts based on canonical transformation applied to the entire mixed distribution (WELLER et al. 1996; MAN-GIN et al. 1998). To explain why this is important, let us consider the simplest situation with a mapping population polymorphic for two unlinked QTL, say Q_1/q_1 and Q_2/q_2 . A double haploid (or recombinant inbred, backcross, etc.) population will consist of four groups, such as $Q_1Q_1Q_2Q_2$, $Q_1Q_1q_2q_2$, $q_1q_1Q_2Q_2$, and $q_1q_1q_2q_2$. Assume that the residual (nongenetic) multitrait variation is the same in all four groups and can be described by a variance-covariance matrix $\Sigma_{\mathbf{R}}$.

Two possibilities for incorporating the joint variation of the traits exist when single-QTL mapping analysis is conducted on the basis of markers of one chromosome. These are (a) to consider the general variance-covariance matrix of the traits, which differs from $\Sigma_{\mathbf{R}}$ due to the contribution of both QTL (the higher the individual effects of Q_1/q_1 and Q_2/q_2 , the higher the difference); and (b) to consider the residual variation for each QTL as a combined result of nongenetic variation and the contribution of all other QTL excluding the one under consideration. The second possibility provides a relevant description of the residual variation for each QTL.

Two different approximated procedures, giving very similar results, were employed to implement this approach. In both, the LOD score serves as the major criterion in interval mapping; the steps of evaluating the QTL effects and QTL position are separated. Both are based on our earlier maximum-likelihood approach (KOROL *et al.* 1995). Although the proposed procedures are only approximations of the full procedure, their major advantage is that they allow treatment of a large number of traits simultaneously.

Procedure 1: For each interval, a five-step procedure is conducted.

- 1. The vector of mean trait values in alternative QTL groups defined by flanking markers M_1M_2 and m_1m_2 is evaluated.
- 2. The same groups are used to define the elements of the residual (for the current *i*th interval) covariance matrix, Σ_{R_i} . Throughout this article, we assume no variance-covariance effect (but see KOROL *et al.* 1995, 1996a), so that $\Sigma_{R}(QQ) = \Sigma_{R}(qq)$ and $\Sigma_{R_i}(QQ) = \Sigma_{R_i}(qq)$.
- 3. Transformation of the trait space, as described earlier, reduces the problem to a single-trait analysis. This step includes solving the problem of eigenvalues and eigenvectors of matrix Σ_{R} followed by scale and angular transformations, resulting in a new space with all effects being absorbed by only one variable ("integral" trait; see also ALLISON *et al.* 1998).
- 4. For the resulting variable, a single-trait analysis is conducted, with the likelihood function being dependent on four parameters, $\theta = (\mu, D, \sigma, r)$, where μ , D, σ , and r stand for the mean value of the new trait, total substitution effect, residual standard variation, and recombination rate from the left marker, respectively.
- 5. After getting the estimates, back transformations can be conducted, making it possible to get more precise estimates of mean values of the QTL groups. Consequently, the analysis could be repeated from step (2) until a convergent result is obtained.

Procedure 2: This is a simplified version of procedure one. It includes three steps and gives approximated results compared with those of procedure 1. However, the differences appear to be very small. For each interval, the three-step analysis is conducted.

1. The vector of mean trait values in alternative QTL

groups defined by flanking markers M_1M_2 and m_1m_2 is evaluated.

- 2. The same groups are used to define the elements of the residual (for the current *i*th interval) covariance matrix, Σ_{R_i} .
- 3. The entire sample is used to calculate the conditional maximum-likelihood estimate of the QTL position within the interval with all other parameters being fixed at the estimates obtained at steps (1) and (2).

Clearly, two factors influence the results obtained by this procedure. First, the estimates of the QTL effects will be biased downward owing to undetectable double recombinants among the parental (for the flanking markers) haplotypes. With interval size of $\sim 10-15$ cM this danger is negligible unless high negative interference is characteristic of multiple exchanges in the considered region of the genome. The second factor results in a slight reduction of the sample size: when the QTL effects and the residual covariance matrix are determined according to the foregoing steps (1) and (2), the recombinants for the flanking markers are ignored. Consequently, the sampling error of the estimates is increased by a factor $1/\sqrt{(1-r)}$, where r is the rate of recombination between the flanking markers; for an interval of 10–15 cM the loss of precision is \sim 5.4–8.5%.

Monte Carlo simulations: For mapping a population of the dihaploid (or recombinant inbred, backcross, etc.) type, 200 individuals were simulated with one, two, and three unlinked QTL and a trait complex including up to 10 traits. For each chromosome six equidistant markers were simulated, with recombination rate r =0.1 between the neighbors and no interference and QTL residing in the middle of the third interval. To get the critical level of the test statistics two approaches were employed: Monte Carlo simulations with parameters corresponding to H₀ (no QTL in the simulated chromosome) and permutation of the data set corresponding to H_1 . In both cases, 5000 runs were assayed for each situation. To evaluate the detection power and the precision of the estimated QTL effects and chromosomal position, 500 runs were assayed for each situation. In some isolated examples the numbers of permutation and bootstrap runs were increased to 10,000 and 1000, respectively. The majority of calculations were conducted using the multiple-trait algorithms implemented in the MultiQTL package (http://www.MultiQTL.com). With this program, 1000 permutation runs or 1000 bootstrap runs using a single-QTL model to analyze a 10variate trait complex for a chromosome with 20 markers and population size 150 genotypes takes a Pentium III 600 MHz \sim 3.5 min or 2 min, respectively.

RESULTS

QTL detection power and mapping resolution: Example 1: Improved quality of QTL analysis: To demonstrate the contribution of different factors to the detection power and mapping resolution of multivariate QTL mapping, a series of variants were simulated that differ with respect to the number of traits (from 1 to 10), the type of the covariance matrix, the number of QTL, the effects of the target QTL(s) on the traits, etc. These were based on four 10 × 10 covariance matrices $\Sigma_{\mathbf{R}}$ (Table 1), with a common vector of alternating effects $\mathbf{d} = (0.25, -0.25, 0.25, -0.25, ...)$ and the same residual standard variation $s_i = 1.0$ for all traits. Table 2 represents a diversity of examples with a single QTL: covariance matrices of the majority of variants were derived as major minors of corresponding dimension of the matrix for the 10-trait problem.

As expected, the increase in H_T^2 (see Equation 4) owing to higher information content of multivariate complexes of greater dimension than those of lower dimension brought about an appreciable improvement in the quality of the QTL mapping analysis. This is manifested in higher LOD values and, correspondingly, a better detection power and higher precision of QTL mapping (Table 2). As expected, the improvement strongly depends on correspondence between the QTL effects and the signs of correlation coefficients (e.g., compare cases 2 and 6). The same mechanism appeared to work already in the two-trait analysis, as manifested by the inequality $d_x d_y R_{xy} < 0$ being the necessary condition for ELOD(x, y) > ELOD(x) and/or ELOD(x, y) > ELOD(y) to hold (KOROL *et al.* 1995). The remarkable fact is that it makes no difference whether the increase in $H_{\rm T}^2$ is caused by correlation between the traits or by the Euclidean contribution H_{Eu}^2 (Figure 2). Indeed, the variants represented in Figure 2 differ qualitatively. These include the number of traits taken from the entire 10-dimensional complex, the values and signs of the effects of the QTL on the selected traits, the values of correlations, and even the covariance matrices in general (e.g., numbers 3, 4, 6, 10, 11, 13–15, 17, and 18). In spite of this diversity, the detection power (P) and mapping precision (σ_L) display a unified pattern across variants reflected in the curves $P(H^2)$ and $\sigma_L(H^2)$ in Figure 2.

The results presented in Table 2 and Figure 2 indicate the high potential for improving the QTL detection power and mapping resolution by employing the information contained in the multivariate trait complex without increasing the sample size. Thus, for the same data set corresponding to the first matrix (case 10) with no d_i/σ_i exceeding 0.25, the detection power grows from 13 to 100% (at significance level 0.01) for single- and 10-trait analyses, respectively. Especially pronounced is the improvement of mapping precision: standard deviation of the estimated QTL position, σ_L , decreases from 14.8 cM in single-trait, to 9.3 cM in 2-trait, to 4.0 cM for the matrix A defined in Table 1 (compare cases 1, 2, and 10), or correspondingly, 14.8, 9.4, and 1.4 cM for the matrix C (compare cases 1, 16, and 18). Clearly,

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TABLE 1

Residual covariance matrices and QTL effects used in the simulations

	1	2	3	4	5	6	7	8	9	10	Effect
						А					
1	1.00	0.60	0.50	0.40	0.30	0.20	0.10		0	00	0.25
2	0.60	1.00	0.60	0.50	0.40	0.30	0.20	0.10	0.	00	-0.25
3	0.50	0.60	1.00	0.60	0.50	0.40	0.30	0.20	0.10		0.25
4	0.40	0.50	0.60	1.00	0.60	0.50	0.40	0.30	0.20	0.10	-0.25
5	0.30	0.40	0.50	0.60	1.00	0.60	0.50	0.40	0.30	0.20	0.25
6	0.20	0.30	0.40	0.50	0.60	1.00	0.60	0.50	0.40	0.30	-0.25
7	0.10	0.20	0.30	0.40	0.50	0.60	1.00	0.60	0.50	0.40	0.25
8		0.10	0.20	0.30	0.40	0.50	0.60	1.00	0.60	0.50	-0.25
9	0	00	0.10	0.20	0.30	0.40	0.50	0.60	1.00	0.60	0.25
10	0.	00		0.10	0.20	0.30	0.40	0.50	0.60	1.00	-0.25
					B_1 (bl	ocks 2×2))				
1	1.00	0.70									0.25
2	0.70	1.00									-0.25
3			1.00	0.70				0.	00		0.25
4			0.70	1.00							-0.25
5					1.00	0.70					0.25
6					0.70	1.00					-0.25
7		0.	00				1.00	0.70			0.25
8							0.70	1.00	1.00		-0.25
9									1.00	0.70	0.25
10									0.70	1.00	-0.25
_					B_2 (bl	ocks 5×5)				
1	1.00	0.60	0.50	0.40	0.30						0.25
2	0.60	1.00	0.60	0.50	0.40			0.00			-0.25
3	0.50	0.60	1.00	0.60	0.50			0.00			0.25
4	0.40	0.50	0.60	1.00	0.60						-0.25
Э С	0.30	0.40	0.50	0.60	1.00	1.00	0.00	050	0.40	0.90	0.25
0 7						1.00	0.00	0.50	0.40	0.30	-0.25
0			0.00			0.00	1.00	1.00	0.50	0.40	-0.25
0						0.30	0.00	0.60	1.00	0.50	0.25
10						0.40	0.30	0.00	0.60	1.00	-0.25
10						0.50	0.10	0.50	0.00	1.00	0.45
1	1.00	0.70	0.50	0.39		C					0.95
9	0.70	1.00	0.50	0.52	0.89						-0.25
4	0.70	0.70	1.00	0.30	0.52	0.39			0.00		0.25
4	0.30	0.70	1.00 0.70	1.00	0.30	0.52	0.39				-0.25
5	0.34	0.30	0.70	0.70	1.00	0.50	0.52	0.39			0.25
6		0.34	0.30	0.70	0.70	1.00	0.50	0.52	0.39		-0.25
7			0.34	0.30	0.70	0.70	1.00	0.50	0.52	0 39	0.25
8				0.34	0.30	0.70	0.70	1.00	0.50 0.70	0.52	-0.25
9		0.00			0.34	0.39	0.50	0.70	1.00	0.70	0.25
10						0.04	0.32	0.50	0.70	1.00	-0.25
10							0.32	0.50	0.70	1.00	-0.2

The four multitrait sets (A, B_1 , B_2 , and C) were used in Monte Carlo experiments presented in Table 2 and Figures 2 and 3. The trait complex B_1 includes five pairs of traits with nonzero correlation (0.7) only within pairs; likewise, trait complex B_2 includes two five-trait blocks with nonzero correlations only within the blocks. Empty cells in the covariance matrices correspond to zero correlation coefficients.

this trend reflects the fact that the increasing H^2 caused by joint multiple-trait analysis results not only in higher LOD values and detection power, but also in increased probability to find the QTL in the true interval (interval 3; see footnote *a* in the right column of Table 2). At the level of an individual experiment, the increased resolution derives from the effect of H^2 on the form of the LOD as a function of chromosomal position (l): at high H^2 values the function LOD(l) is more steep than at small H^2 (Figure 3). Clearly, increased precision of the estimated QTL position should also allow a more accurate estimation of the QTL effect. This is indeed the case, as illustrated by Figure 4. The increase in H^2 accompanied by a more strict slope of the LOD function

$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
13 16 71 5	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	13 16 71 55 84 22 94 22 12 23 83 34 98 33 98 1	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{c} 13\\ 13\\ 71\\ 71\\ 84\\ 84\\ 94\\ 83\\ 83\\ 83\\ 83\\ 83\\ 83\\ 83\\ 83\\ 83\\ 83$
0.072	$\begin{array}{c} 0.015\\ 0.072\\ 0.106\\ 0.140\\ 0.025\\ 0.074\end{array}$	0.015 0.072 0.106 0.140 0.025 0.074 0.108 0.173	$\begin{array}{c} 0.015\\ 0.1072\\ 0.106\\ 0.140\\ 0.074\\ 0.074\\ 0.108\\ 0.173\\ 0.254 \end{array}$	$\begin{array}{c} 0.015\\ 0.072\\ 0.106\\ 0.140\\ 0.074\\ 0.074\\ 0.173\\ 0.173\\ 0.173\\ 0.294 \end{array}$	$\begin{array}{c} 0.012\\ 0.105\\ 0.106\\ 0.140\\ 0.074\\ 0.074\\ 0.173\\ 0.173\\ 0.173\\ 0.175\\ 0.175\\ 0.175\\ 0.175\end{array}$	$\begin{array}{c} 0.0.12\\ 0.106\\ 0.106\\ 0.140\\ 0.025\\ 0.074\\ 0.173\\ 0.173\\ 0.173\\ 0.173\\ 0.173\\ 0.249\\ 1\\ 0.249\\ 1\\ 0.301\\ 1\end{array}$
0.67 3.27	0.67 3.27 4.85 6.56 1.10 3.35	0.67 3.27 4.85 6.56 1.10 3.35 4.95 8.27	0.67 3.27 4.85 6.56 1.10 3.35 3.35 4.95 8.27 12.72 15.13	0.67 3.27 4.85 6.56 1.10 1.10 3.35 8.27 15.13 15.13 15.13 8.35 8.35	0.67 3.27 4.85 6.56 1.10 1.10 1.272 12.72 12.72 13.13 12.72 13.62 8.35 8.35 8.35 8.27 8.27	0.67 3.27 4.85 6.56 6.56 1.10 1.10 3.35 4.95 1.2.72 1.5.13 4.95 4.95 1.5.13 1.5.5 1.
0.94 3.60	$\begin{array}{c} 0.94 \\ 3.60 \\ 5.09 \\ 6.91 \\ 2.13 \\ 4.08 \end{array}$	$\begin{array}{c} 0.94 \\ 3.60 \\ 5.09 \\ 6.91 \\ 2.13 \\ 5.40 \\ 5.40 \\ 8.64 \end{array}$	$\begin{array}{c} 0.94 \\ 3.60 \\ 5.09 \\ 6.91 \\ 6.91 \\ 2.13 \\ 5.40 \\ 5.40 \\ 8.64 \\ 13.14 \\ 16.41 \\ 16.41 \end{array}$	$\begin{array}{c} 0.94\\ 3.60\\ 5.09\\ 6.91\\ 2.13\\ 2.13\\ 4.08\\ 5.40\\ 8.64\\ 13.14\\ 13.14\\ 16.41\\ 16.41\\ 16.41\\ 8.39\end{array}$	0.94 3.60 5.09 6.91 5.09 6.91 2.13 8.64 8.64 13.14 13.14 13.14 16.41 13.14 16.41 13.14 8.69 8.39 8.39 8.66	$\begin{array}{c} 0.94\\ 3.60\\ 5.09\\ 6.91\\ 2.13\\ 2.13\\ 5.40\\ 8.64\\ 1.3.14\\ 4.47\\ 1.3.14\\ 4.47\\ 1.3.16\\ 1.3$
2.59 4.27	2.59 4.27 5.64 7.03 4.33 5.10	2.59 5.64 7.03 7.03 5.10 5.10 5.10 5.10 5.10	2.59 4.27 5.64 7.03 4.33 5.10 5.10 5.10 5.10 5.10 5.10 5.10 13.14 16.41	$\begin{array}{c} 2.59\\ 2.59\\ 5.64\\ 7.03\\ 7.03\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 1.3.14\\ 1.8.14\\ 16.41\\ 16.41\\ 8.42\\ 8.42\\ 8.42\\ \end{array}$	$\begin{array}{c} 2.59\\ 2.596\\ 5.64\\ 7.03\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 5.10\\ 5.41\\ 16.41\\ 16.41\\ 16.41\\ 16.42\\ 18.71\\ 8.73\\ 8.73\end{array}$	2.59 5.64 7.03 5.64 7.03 5.10 5.10 8.51 16.41 16.41 16.41 16.42 18.73 8.73 18.71 8.73 15.96 8.73 18.71 8.73 15.96
1.97 2.62	$\begin{array}{c} 1.97\\ 2.62\\ 3.07\\ 3.59\\ 3.59\\ 3.59\\ 3.59\end{array}$	$\begin{array}{c} 1.97\\ 2.62\\ 3.07\\ 3.59\\ 3.59\\ 3.59\\ 3.59\\ 3.59\\ 3.59\\ 3.94\end{array}$	1.97 2.062 3.59 3.59 3.59 3.59 5.23 5.23	1.97 2.62 3.59 3.59 3.59 3.59 3.59 5.23 3.51 3.61	1.97 2.62 3.59 3.59 3.59 3.59 5.23 3.51 2.55 3.61 3.61	$\begin{array}{c} 1.97\\ 2.07\\ 2.07\\ 2.07\\ 2.07\\ 2.07\\ 2.07\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\ 2.03\\ 2.05\\$
$\begin{array}{c} 14.8\\ 9.3\end{array}$	14.8 9.3 7.9 11.5 8.9	14.8 9.3 7.9 7.2 8.9 8.9 8.2 6.4	$\begin{array}{c} 14.8\\ 9.3\\ 7.9\\ 7.2\\ 8.9\\ 8.9\\ 8.2\\ 8.4\\ 4.8\\ 4.0\end{array}$	$\begin{array}{c} 14.8\\ 9.3\\ 7.9\\ 7.2\\ 8.9\\ 8.9\\ 8.2\\ 8.2\\ 8.4\\ 8.0\\ 8.0\\ 8.0\\ 6.0\end{array}$	$\begin{array}{c} 14.8\\ 9.3\\ 7.9\\ 7.2\\ 8.9\\ 8.2\\ 8.2\\ 8.2\\ 8.0\\ 8.0\\ 8.0\\ 8.0\\ 8.0\\ 8.0\\ 8.0\\ 8.0$	14. 17. 17. 17. 17. 17. 17. 17. 17
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	<i>v</i> 4 <i>v</i> 0	x 4 v 0 r x	x 4 7 0 L 8 C O	10 0 8 4 0 0 1 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0	4 2 2 1 0 0 8 4 0 2 7 4 <i>3</i>	x 4 v 0 7 x 0 0 1 0 x 4 v 0

Improvement of the efficiency of QTL mapping owing to joint analysis of multiple-trait complexes **TABLE 2**

LUDf IS URE AVELAGE cnromosome does not affect the trait complex); LOD_m is the mean value of the test statistics averaged over the runs with $LOD > LOD_{0,01}$ whereas all runs; LOD_t is the theoretical value of LOD calculated based on multivariate generalization of the connection between LOD and H^2 . ^{*a*} The simulated QTL position was the middle of the third interval.

Multitrait QTL Mapping



FIGURE 2.—Multivariate heritability as a predictor of the LOD value (affecting QTL detection power) and mapping resolution. Right-hand scale, ELOD (\bigcirc), left-hand scale, SL (standard deviation of the estimated QTL position; \bullet). The graphs are based on Monte Carlo simulations described in Table 1 and partially represented in Table 2.

may justify a saturation of the chromosomal region in the detected QTL by additional markers. This may allow a reduction of the chances of incorrect QTL location and finer QTL mapping, as well as an attempt at resolving the pleiotropy-linkage alternative (JIANG and ZENG 1995; ALMASY *et al.* 1997; LEBRETON *et al.* 1998; KOROL *et al.* 1998a; RONIN *et al.* 1999).

It is noteworthy that ELOD calculated on the basis of H_T^2 appeared to be a very good predictor of the averaged LOD obtained from Monte Carlo simulations (see the column LOD_m in Table 2). This indicates that Equa-



FIGURE 3.—The dependence of the LOD function on the number of traits. The numbers in the solid circles indicate the number of traits; the simulated position of the QTL is marked by an arrowhead (based on the last example of Table 1).

tion 1 obtained by LANDER and BOTSTEIN (1989) for a single trait, and generalized by KOROL *et al.* (1995) for two-trait analysis, also holds in a general multivariate case. The last statement follows from the fact that heritability of a complex of *noncorrelated* traits with a single QTL affecting only one trait can be represented as $H_D^2 = \frac{1}{4}D^2/(1 + \frac{1}{4}D^2)$, where *D* is the multivariate effect and σ^2 the residual variance for the "integral" trait described in *The numerical procedures of interval analysis*.

Example 2: Interval-specific estimation of the covariance matrix: Another comment concerns the interval specificity that is a characteristic of our approach to defining the elements of the residual covariance matrix, $\Sigma_{\mathbf{R}}$. If, instead of that, one uses the total (interval-independent) covariance matrix defined on the entire sample, the efficiency of mapping may be lowered. The numerical example with a three-trait complex shown in Table 3 illustrates the difference between the two approaches. One can easily see that if the approach based on total covariance matrix is employed, instead of our intervalspecific procedure, a reduction in the LOD value (hence lower detection power) and increase in the bias (δ) and standard variation (σ) of the estimated QTL effects (d_i) and, especially, chromosomal position (L), may be obtained. Note that in the foregoing example only a single QTL was simulated in the mapping population. The difference between the methods derives from the noncorrespondence between the residual correlation matrix and the directions of the pleitropic effects. Nevertheless, in some cases, where the total covariance matrix does not differ strongly from $\Sigma_{\mathbf{R}}$, the loss will be less pronounced (see MANGIN et al. 1998).

Example 3: Multiple QTL: We now illustrate the efficiency of the proposed algorithm in situations with more than one QTL segregating in the mapping population. We simulated two and three identical unlinked QTL with the residual 10×10 covariance matrix equal to that of example 10 and the same pleiotropic effects (see Tables 1 and 2). As before, 500 Monte Carlo runs were made. The results (Table 4) confirm the previous conclusion: a dramatic improvement can be achieved by use of joint analysis of the correlated traits. Note that segregation for one or two additional QTL resulted in an increase in the residual variances (as compared with Example 1). Consequently, we obtained a slightly lower detection power and a lower mapping precision. For the 10-trait analysis, the standard deviation of the estimated QTL position (SL) increased from 4.0 to 5.0-5.6 cM in case of two QTL and to 5.8-6.7 cM in the case of three QTL. Clearly, this reduction in mapping precision can be recovered by a composite interval mapping approach (ZENG 1994; JANSEN and STAM 1994) but within the framework of multiple-trait analysis.

Significance of the detected effects: Testing for significance is a difficult problem in QTL mapping analysis, especially when multiple intervals and/or multiple traits are involved (LANDER and BOTSTEIN 1989; LANDER and



FIGURE 4.—Improved correspondence between the simulated and estimated QTL effects in multiple-trait analysis as compared to singletrait analysis. (a) Single-trait analysis; (b) 10-trait analysis (based on the first example of Table 1).

KRUGLYAK 1995; WELLER et al. 1998). To get the critical level of the test statistics in the foregoing analysis we employed Monte Carlo simulations with parameters corresponding to H_0 (no QTL in the chromosome, with 5000 runs per each variant). Clearly, this technique can also be used for real data analysis, but it would be much more preferable to take into account the distribution properties of the real data set. The best way to do this in testing significance is the permutation test (DOERGE and CHURCHILL 1996). A few different, although related, questions about the significance of the results can be recognized in the multiple-trait procedure: (i) What is the significance level of the detected QTL?, (ii) which traits significantly contributed to the criterion (multivariate LOD score)?, and (iii) which traits depend significantly on the detected QTL? The difference between the second question and the third is caused by the fact that the information value of a trait may derive from its correlation to other traits of the complex, from the pleiotropic effect of the QTL on this trait, or from both these factors (see Figure 1).

Example 4: Selecting significant traits and effects: The fore-

going aspects are illustrated in a simulated example with seven quantitative traits and a chromosome with five intervals (10 cM each) with a QTL residing in the middle of the third interval. The pleiotropic effects of the simulated QTL, the residual correlation matrix, and residual variances were as shown in Table 5. The results can be outlined as follows:

i. To evaluate the significance of the QTL detected by using seven-dimensional mapping analysis, the entire vector of trait values was reshuffled relative to the marker scores (while retaining the structure within the trait complex). For each such permutated data set, the mapping procedure was applied, resulting in a corresponding value of the test statistics LOD score. This process was repeated many times (10,000 in our experiment). The significance of the H_0 hypothesis (no effect of the considered chromosome on the multivariate trait complex) is calculated as the proportion of permutation runs that resulted in LOD values equal to or exceeding LOD* obtained on the nonpermutated data.

TABLE	3
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Effect Matrix LOD Parameter L (cM) d_1 d_2 d_3 0.02 0.010 0.007 $\Sigma_{\rm R}$ 48.10 δ -0.0031.44 0.048 0.050 0.050 σ Σ_{total} 27.58 δ 0.04 0.027 -0.0230.018 σ 3.60 0.069 0.068 0.064 2 1 3 Trait Effect 1 1.000.010.70+0.752 1.000.70-0.750.013 0.700.701.00 +0.50

Comparison of the QTL mapping results obtained by the proposed method (based on interval-specific determination of the residual covariance matrix Σ_R) and by using the total covariance matrix (Σ_{total})

Three-trait complex was analyzed, with QTL effects and the residual covariance matrix as presented above. The parameters δ and σ denote the bias and standard deviation of the estimated QTL position (*L*) and QTL effects (d_1 , d_2 , and d_3).

TABLE 4

The effect of the number of traits on efficiency of QTL mapping analysis with multiple QTL segregating in the mapping population

			Precision of estimation		Test st	Interval distribution of the detected QTL (%)				D		
No.		δ_L	σ_L	$LOD_{0.01}$	LOD _m	1	2	3^a	4	5	rower (%)	
					Two QT	L						
QTL1	19	1×1	1.14	12.72	9.19	12.45	9	29	31	18	13	14
	20	2×2	-0.02	9.58	11.74	19.21	5	21	50	20	4	61
	22	10×10	-0.01	5.63	28.04	57.16	2	9	79	9	1	100
QTL2	23	1×1	-0.82	11.82	9.19	12.46	9	30	34	19	8	13
	24	2×2	0.12	9.03	11.74	19.66	3	24	50	18	5	68
	30	10×10	0.28	4.98	28.04	56.51	1	6	82	10	1	99
					Three Q1	TL						
QTL1	31	1×1	1.09	12.56	9.29	13.51	6	31	35	16	12	13
•	32	2×2	-0.77	10.09	11.66	19.22	7	19	49	20	5	57
	34	10×10	0.09	6.67	27.05	46.52	1	13	71	13	2	97
QTL2	31	1×1	1.12	14.09	9.29	12.55	10	18	39	15	18	12
•	32	2×2	0.15	10.24	11.66	18.44	7	20	50	18	5	60
	34	10×10	0.31	5.83	27.04	47.60	1	11	71	16	1	97
QTL3	31	1×1	-2.92	12.72	9.29	12.15	16	21	39	19	5	12
•	32	2×2	0.03	9.94	11.66	18.49	5	19	52	18	6	62
	34	10×10	0.29	6.38	27.04	47.67	1	11	72	14	2	95

The parameters δ_L and σ_L denote the bias and standard deviation of the estimated QTL position; LOD_{0.01} is the threshold value of the test statistics (obtained by 5000 simulations under the assumption H₀ that the analyzed chromosome does not affect the trait complex); LOD_m is the mean value of the test statistics averaged over the runs with LOD > LOD_{0.01}.

^{*a*} The simulated position of each of the two or three QTL on the corresponding chromosomes was the middle of the third interval.

- ii. The second test aimed to evaluate the significance of contributions of each of the traits for the QTL detection power. This test is conducted separately for each trait. For this, the individual values of the trait under consideration are reshuffled relative to the remaining data (the other trait values and marker scores). The resulting data set is treated as before and the proportion of runs with LOD \geq LOD* is used as the measure of significance of the trait contribution. The permutations are always performed regarding all the traits included in the model independently of the contribution value of the remaining traits. Clearly, some traits may prove to be insignificant because they contribute the same information as one (or a few) of the remaining traits. Thus, one can exclude insignificant traits from consideration by creating a new trait set that does not include the insignificant traits(s). This procedure should be applied by simple steps, excluding only one trait per step and repeating the permutation test for the remainder. The last warning is important because after excluding one of the traits at some step, the significance of contributions of the remaining traits may change.
- iii. The same procedure as in (ii) can be used to test the significance of the QTL effect for each of the

traits. Namely, we calculate the proportion of permutated cases where the estimated QTL effect for the considered trait x_i fits the condition $abs(d_i) \ge$ $abs(d_i^*)$, where d_i^* is the estimated effect on trait x_i obtained on initial (not reshuffled) data.

In the example of Table 5, trait 7 displayed the lowest contribution and hence was removed after the first step. Reevaluation of the remaining complex revealed the next candidate to remove, trait 3, and then, similarly, trait 4. All the remaining traits (1, 2, 5, and 6) showed significant contribution. This trait complex provides also the narrowest confidence interval for the estimated QTL position (σ_L), as shown by the results of bootstrap analysis. The last result means that maintenance of excessive (noninformative) traits is not neutral, a reduced precision of the estimated QTL position being the penalty. Filtering out of the nonsignificant traits should affect the QTL detection power, but further reduction of the trait complex by removing the significant traits may result in a reduced power and lowered mapping precision (see the characteristics obtained for the last two trait combinations, 1, 2, 5, and, especially, 2, 5, 6).

An example of application to real data: We illustrate the efficiency of the proposed approach using real data on a wheat mapping population characterized for 11

TABLE 5

	1	_7	1	-6	1, 2	, 4–6	1, 2	, 5, 6	1, 2, 5		2, 5, 6	
Traits	Trait	Effect	Trait	Effect	Trait	Effect	Trait	Effect	Trait	Effect	Trait	Effect
		Sig	gnificance	e (%) base	ed on 10,0	00 permuta	ations fo	or each tes	sted trait	combinat	ion	
1	0.00	0.07	0.00	0.07	0.00	0.08	0.00	0.07	0.00	0.08		_
2	0.03	84.16	0.02	84.23	0.02	83.87	0.02	83.01	1.18	85.10	71.99	83.14
3	21.76	5.10	21.85	5.08		_		_				_
4	18.46	1.56	19.28	1.56	11.94	1.59		_				_
5	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.01	0.00	0.01	0.00
6	0.20	63.17	0.19	63.15	0.16	62.56	0.15	61.52	_	_	73.06	62.62
7	58.40	41.10	—	—	_	—	—	—	_	—	—	—
				Estimate	es resulting	g from boo	tstrap ai	nalysis (10	00 runs)			
LOD _m	12.72		12.43		11.90		11.16		8.83		4.88	
σLOD_m	2.86		2.87		2.	71	2.71		2.48		1.86	
Power (%)	99.5		99.6		99.	7	<i>99</i> .7		95.9		47	.4
H^2	0.346		0.324		0.	304	0	.290	0.	.204	0	.172
σ_{H^2}	0.	.086	0.079		0.	078	0	.070	0.	.062	0	.083
<i>L</i> (cM)	24.	12	24.17		24.	53	23	.81	23.	.58	21	.03
σ_L	5.	.26	5.09		5.00		3	.88	5.	.22	7.04	
Traits	1	2		3	4	5		6	7	E	ffect	σ
		Occur	red corre	lation ma	trix, OTL	effects, and	l residua	al standaro	d deviatio	ns		
1	1.0	0.618	3 (0.062	0.165	0.05	4	0.155	0.15	6 (0.504	0.955
2		1.0	(0.126	0.020	0.11	2	0.723	0.15	6 (0.037	1.013
3				1.0	0.236	0.07	2	0.092	0.00	7 (0.281	1.002
4					1.0	-0.06	9.	-0.112	0.03	2 ().283	1.088
5						1.0		0.034	-0.05	0 (0.674	0.982
6								1.0	0.10	5 (0.044	0.968
7									1.0	-().149	0.960

Permutation test of significance for the contribution of the traits: the multitrait LOD and the pleiotropic effects of the QTL

The simulated effects, residual correlation matrix, and standard deviations are as shown in the bottom; note that one out of seven traits, no. 7, was simulated as "noise", trait 2 was independent on the QTL but correlated with traits 1 and 6.

On the basis of the permutation test, the significance of contribution to the LOD score as well as the QTL effect was evaluated for each trait. After the first step, trait 7 that appeared to have the lowest contribution was removed. Reevaluation of the remainder complex revealed the next candidate to remove, trait 3, and then, similarly, trait 4. All the remainder traits, 1, 2, 5, and 6, show significant contribution. This complex (italic) also provides the narrowest confidence interval for the estimated QTL position (σ_L), as shown by the results of bootstrap analysis. This filtering out of the nonsignificant traits did not affect the QTL detection power, whereas further reduction of the trait complex by removing the significant traits may result in a reduced power and lowered mapping precision (see the characteristics obtained for the last two trait combinations).

morphological quantitative traits. The experiment was performed on an F2/F3 mapping population derived from a cross between a highly stripe-rust-resistant wild emmer wheat Triticum dicoccoides (accession no. H52, from Mt. Hermon, Israel) and a T. durum cultivar, Langdon, released in North Dakota. The tetraploid wild emmer, T. dicoccoides, is the progenitor of cultivated wheat; hence, the genetic dissection of quantitative trait differences between the wild species and the cultivated crop is of great interest from the viewpoint of domestication evolution. It is also important for the ever-increasing utilization of T. dicoccoides as a rich genetic resource for wheat improvement. The molecular markers [microsatellites and amplified fragment length polymorphisms (AFLP)] were scored on 150 F₂ individuals resulting in a rather dense genetic map (PENG et al. 2000). The quantitative traits were scored on the selfed progeny in

field trials conducted in Neve Yaar Agricultural Experimental Station, Israel, during the 1997–1998 cropping season. Eleven quantitative traits were scored on F_3 progeny (for ~10 individual plants from each family): plant height (HT), plant heading date—the days from sowing to heading (HD); spike number/plant (SNP); spike weight/plant (SWP) including the grains, hulls, and rachis; single spike weight (SSW); kernel number/plant (KNP); kernel number/spike (KNS); kernel number/ spikelet (KNL); 100-grain weight (GWH); grain yield/ plant (YLD); and spikelet number/spike (SLS).

A detailed QTL description of the obtained QTL mapping results on these traits will be presented elsewhere (J. H. PENG, A. B. KOROL, T. FAHIMA, Y. I. RONIN and E. NEVO, unpublished results). Here we employ the obtained data only to illustrate the efficiency of the multitrait analysis, using as an example markers of chro-

TABLE 6

No. of	LOD		QTL thr	Circuit Corrections have		
traits	$\sigma_{ m LOD_f}$	$L\sigma_L$ (cM)	$\alpha = 0.05$	$\alpha = 0.01$	$\alpha = 0.001$	permutation test
1	$4.38 \\ 1.63$	271 74	91	71	42	0.011
11	$19.71 \\ 3.43$	265 36	100	100	100	< 0.0001
5	$\begin{array}{c} 13.82\\ 2.91 \end{array}$	262 30	100	100	99	< 0.0001

Interval analysis of a multitrait complex that includes 11 morphological traits scored in F_2/F_3 mapping population of wheat *Triticum durum* \times *T. dicoccoides* (PENG *et al.* 2000)

The example is based on markers of chromosome 7A.

The results of single-trait interval analysis (for trait GWH) are compared with those of the entire 11-trait complex and the "filtered" five-trait complex obtained by excluding nonsignificant traits (as in the example shown in Table 5). The traits remaining in the five-trait complex are: GWH, YLD, HD, HT, and SWP. The significance level for each trait and trait complex was calculated using a permutation test (10,000 runs). In addition to the analysis of the initial data set, 1000 bootstrap runs were conducted, enabling us to evaluate the QTL detection power and precision of the parameter estimates. LOD_f and σ_{LOD_f} are the mean value and standard deviation of the test statistics estimated on the basis of 1000 bootstrap runs; correspondingly, *L* and σ_L are the QTL map position and its standard deviation.

mosome 7A. With single-trait analysis applied separately to each of the traits, only one significant QTL was found on 7A, for trait GWH, with significance level ~ 0.01 (Table 6). This level should be corrected for multiple comparisons, taking into account the fact that the analyzed traits are correlated (e.g., by using the method based on factor analysis, as suggested by SPELMAN et al. 1996). Therefore, the corrected significance will be even worse. The mapping precision evaluated by bootstrap analysis is not high ($\sigma_L = 74$ cM), as one would expect for the modest population size employed (n = 150). Therefore, it makes sense to attempt improvement of the mapping by utilizing the information contained in the entire trait complex, owing to possible pleiotropic effects of the putative QTL and/or correlations between GWH and the remaining traits. This was done exactly in the same way as described in the foregoing simulated example presented in Table 5. First, the entire complex of 11 traits was analyzed and then the traits that did not contribute significantly to the test statistics were removed. The results presented in Table 6 and Figure 5 show a more than twofold increase in the mapping precision (σ_L decreased from 74 to 30 cM) and an increase in detection power that is especially clear at higher significance level (98.9% vs. 42.9%).

DISCUSSION

A multivariate generalization of our previous two-trait QTL mapping analysis (KOROL *et al.* 1987, 1995, 1998a; RONIN *et al.* 1995, 1999; see also JIANG and ZENG 1995) is proposed here. It is not difficult to extend this method



FIGURE 5.—Joint analysis of 11 traits scored in F_2/F_3 mapping population of wheat *Triticum durum* × *T. dicoccoides* using markers of chromosome 7A. The results of removing nonsignificant traits are presented. (a) LOD score distribution along chromosome 7A for the 5-trait complex (GWH, YLD, HD, HT, and SWP). (b) Interval distribution of the maximum LOD values along chromosome 7A based on 1000 bootstrap runs. Both graphs are outputs of the MultiQTL package (http://www.MultiQTL.com).

to other situations (e.g., analyzing F₃ populations), to deal with linked QTL (similar to the analysis of KOROL et al. 1998a; RONIN et al. 1999), to combine it with selective genotyping design (RONIN et al. 1998; HENSHALL and GODDARD 1999), or to adopt composite interval mapping (JANSEN and STAM 1994; ZENG 1994). Especially promising may be its application to fine mapping (Y. I. RONIN, E. BRITVIN, E. NEVO and A. B. KOROL, unpublished results). Indeed, the dramatic increase in mapping resolution derived from using the entire multivariate complex, as compared with univariate or even bivariate analysis, effectively increases the score D_n^2 that was found to affect the mapping resolution (DARVASI and SOLLER 1997). Consequently, it becomes reasonable to saturate the revealed intervals by additional markers even at modest population sizes like 200-500 individuals; usually this is pointless because with small effects no increase in precision is expected by addition of new markers to the map (DARVASI et al. 1993). Therefore, the transition from a single- or even two-trait analysis to treatment of genuine multiple-trait complexes significantly improves all aspects of utilizing the mapping information contained in the data.

However, the application of multivariate complexes not only increases the QTL detection power, mapping resolution, and estimation accuracy but it may also increase the power of discriminating various important hypotheses that concern the genetic architecture of complex traits, such as linkage vs. pleiotropy (SCHORK et al. 1994; JIANG and ZENG 1995; ALMASY et al. 1997; LEBRETON et al. 1998; RONIN et al. 1999), genetic interaction within and across QTL (additive vs. dominant or overdominant effects, and additive vs. epistatic effects or canalization; RONIN et al. 1999; SHOOK and JOHNSON 1999), and QTL-environment interaction (FRY et al. 1998; KOROL et al. 1998b). Multivariate QTL analysis may be helpful in genetic dissection of such types of complex traits as multifactorial diseases (MANSFIELD et al. 1997), development (Wu et al. 1999), longevity and aging (NUZHDIN et al. 1997), behavior (PLOMIN and CRAIG 1997; WEHNER et al. 1997), fitness-related trait complexes and species differentiation (ZENG et al. 2000), heterosis (XIAO et al. 1995), marker-assisted breeding (LANDE and THOMPSON 1990; VISSCHER et al. 1996), characterizing the regulatory networks of structural genes (DAMERVAL et al. 1994), bridging between gene-structure-and-function studies (*e.g.*, when looking for functions of massively expressed sequence tags; LAH-BIB-MANSAIS et al. 1999), analyzing the genetic transmission system (breeding system, recombination, and mutation control; KOROL et al. 1994; BERNACCHI and TANKSLEY 1997), and so on.

As a not-so-remote analogy, one could compare the situation of multivariate QTL analysis with that characteristic of medical diagnoses: excluding simple situations, a good physician will never rely on one trait (symptom or analysis, etc.) Instead, he/she will try to take into account all available information concerning the patient. However, this does not mean that increasing the number of traits to be analyzed simultaneously will necessarily improve the quality of the QTL mapping results. A technical obstacle with high dimensionality is an increasing probability that many loci may affect the analysis along the chromosome, whereas a small-to-moderate population size could hardly justify fitting more than two or three linked QTL simultaneously. Another problem is the interpretation of the results. Therefore, in choosing the initial set of traits for joint QTL analysis, one may find it reasonable to restrict such sets by functionally related traits. The examples presented in this article, on both simulated and real data, show that maintenance of excessive traits in the model may be penalized. These concerns indicate that in spite of high potential and biological "compatibility" of the multiple-trait analysis to the main targets of QTL analysis, a lot of work remains to be done to fully extract the mapping information hidden in the collected data.

An additional complication that is worth mentioning is the possible effect of the model assumption on the obtained results. It was shown earlier that for testing for linkage, erroneous models may lead to valid tests for linkage (WRIGHT and KONG 1997). For example, QTL mapping analysis may be quite robust to violations of the assumption of normality in single-trait situations (KOROL et al. 1996b) and more sensitive in multivariate ones. Likewise, the assumption of homoscedastic distributions (*i.e.*, equal residual variances in QTL groups) that is usually applied automatically may be wrong, leading to reduced QTL detection power and biased estimates of parameters. On the contrary, if a correct model is fitted, this may increase the detection power and mapping accuracy compared to situations when no such disturbances exist. We demonstrated these effects earlier for single- and two-trait analysis (KOROL et al. 1995, 1996a). Especially important is the assumption of a single QTL per chromosome, which being violated may lead to the LOD score peaking in the wrong place (see KNOTT and HALEY 1992; WRIGHT and KONG 1997). For the two-trait case we found that joint analysis of correlated traits increases the power of the test aimed to discriminate between the single QTL and two-linked QTL situations (RONIN et al. 1999). All these aspects should be taken into account in multivariate QTL analysis.

The described approach is implemented in the MultiQTL package (http://www.MultiQTL.com) for both single- and two-linked QTL models.

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