Kinetics of Na-ATPase Activity by the Na,K Pump

Interactions of the Phosphorylated Intermediates with Na⁺, Tris⁺, and K⁺

JENS G. NØRBY, IRENA KLODOS, and NIELS O. CHRISTIANSEN

From the Institute of Biophysics, University of Aarhus, DK-8000 Aarhus C, Denmark

ABSTRACT To determine the biochemical events of Na⁺ transport, we studied the interactions of Na^+ , Tris⁺, and K^+ with the phosphorylated intermediates of Na,K-ATPase from ox brain. The enzyme was phosphorylated by incubation at 0°C with 1 mM Mg²⁺, 25 µM [³²P]ATP, and 20-600 mM Na⁺ with or without Tris⁺, and the dephosphorylation kinetics of [³²P]EP were studied after addition of (1) 1 mM ATP, (2) 2.5 mM ADP, (3) 1 mM ATP plus 20 mM K⁺, and (4) 2.5 mM ADP plus Na⁺ up to 600 mM. In dephosphorylation types 2-4, the curves were bi- or multiphasic. "ADP-sensitive EP" and "K⁺-sensitive EP" were determined by extrapolation of the slow phase of the curves to the ordinate and their sum was always larger than Ettotal. These results required a minimal model consisting of three consecutive EP pools, A, B, and C, where A was ADP sensitive and both B and C were K⁺ sensitive. At high [Na⁺], B was converted rapidly to A (type 4 experiment). The seven rate coefficients were dependent on [Na⁺], [Tris⁺], and [K⁺], and to explain this we developed a comprehensive model for cation interaction with EP. The model has the following features: A, B, and C are equilibrium mixtures of EP forms; EP in A has two to three Na ions bound at high-affinity (internal) sites, pool B has three, and pool C has two to three low-affinity (external) sites. The putative high-affinity outside Na⁺ site may be on E_2P in pool C. The A \rightarrow B conversion is blocked by K⁺ (and Tris⁺). We conclude that pool A can be an intermediate only in the Na-ATPase reaction and not in the normal operation of the Na,K pump.

INTRODUCTION

In 1957 Skou reported the discovery of Na,K-ATPase and suggested that this enzyme represented the physiological machinery for active transport of Na⁺ and K⁺. Although the identity of the Na,K-ATPase and the active transport system, also called the sodium pump, is considered firmly established, there is still no unambiguous scheme correlating the enzymatic mechanism and the transport kinetics.

J. GEN. PHYSIOL. © The Rockefeller University Press · 0022-1295/83/12/0725/35 \$1.00 Volume 82 December 1983 725-759 The Post-Albers scheme for Na,K-ATPase (e.g., Albers, 1967; Post et al., 1972) is almost universally used as a frame of reference in describing the kinetics of the enzyme. Recently, expanded versions of the original scheme have been proposed with the purpose of defining the biochemical events associated with ion movements during different transport modes of the pump (Karlish et al., 1978; Robinson and Flashner, 1979). In these reaction models the phosphorylated enzyme intermediates, E_1P and E_2P , occupy a central position (for references to earlier work in this field see Klodos et al., 1981). However, it has from time to time been disputed whether the same phosphoenzymes are intermediates in both the Na-ATPase and the Na,K-ATPase activity (Skou, 1965, 1975; Whittam and Chipperfield, 1975; Garrahan and Garay, 1976; Klodos and Nørby, 1979), and several problems regarding the interaction of E_1P and E_2P with the transported cations remain.

In a recent paper from this laboratory (Klodos et al., 1981), we demonstrated that the dephosphorylation kinetics of the acid-stable phosphointermediates of Na,K-ATPase under certain conditions— $[Na^+] = 150 \text{ mM}, [K^+]$ = 0, and various ADP concentrations—could be described by a two-compartment model, scheme S1, involving the consecutive formation of E₁P (ADP-sensitive) and E₂P:

$$\underbrace{ADP}_{E_1P} \stackrel{\longrightarrow}{\rightleftharpoons} E_2P \xrightarrow{\longrightarrow} E_2 + P_i$$
(S1)

Together with the conclusions from a parallel study on the interaction of Na,K-ATPase with Mg, ATP, and K⁺ (Plesner and Plesner, 1981*a*, *b*; Plesner et al., 1981), the kinetic characterization of the phosphoenzymes led us to propose a new, minimal model for the activities of Na,K-ATPase (Plesner et al., 1981). This model is different from the Post-Albers scheme in that E_1P is an intermediate in ATP hydrolysis in the absence of K⁺ but not in its presence. However, it was clear that the two-component phosphoenzyme description (S1) was inadequate to explain the known effects of variation in [Na⁺] on, for instance, the E_1P/E_2P ratio, ATP:ADP exchange, Na-ATPase activity, and Na:Na exchange.

With the aim of characterizing these interactions of the cations with the phosphoenzymes of Na,K-ATPase, we have investigated the effect of Na⁺ (from 20 to 600 mM), K⁺ (20 mM), and ADP (2.5 mM) on the dephosphorylation time course of preformed, radioactive phosphointermediates, $[^{32}P]EP$. In one series of experiments, Tris (tris-[hydroxymethyl]-aminomethane) was added to keep the ionic strength constant.

The study somewhat surprisingly disclosed that the sum of ADP-sensitive and K-sensitive EP was >100%, which clearly indicates the insufficiency of the two-pool model in S1. The results could, however, be accurately fitted to a three-pool model:

726

where A is ADP-sensitive EP, B is Na-sensitive in the sense that it is converted to A by Na⁺ acting at low-affinity sites, and C, as well as B, is dephosphorylated rapidly by K⁺. Computer simulation allowed estimation of each of the rate coefficients involved.

To explain the dependence of the rate coefficients on Na⁺, Tris⁺, and K⁺, we propose that this three-pool model is a condensation of the detailed reaction scheme shown in Fig. 8. Besides being able to provide a quantitative analysis of the data, this scheme assigns component unitary processes (Hearon et al., 1959) to the composite three-pool model (allowing only one event to take place at each reaction step) and furthermore encompasses the sidedness of the transport system. Our analysis calls for a loosening of the strict classic concepts of ADP-sensitive and K-sensitive phosphoenzymes and it gives further support to the proposal that ATP hydrolysis in the presence of Na⁺ alone (Na-ATPase) proceeds via intermediates, some (if not all) of which are different from those of the Na,K-ATPase cycle.

A preliminary account of some of the experiments and of the comprehensive model has been given by Klodos et al. (1983).

MATERIALS AND METHODS

Enzyme Preparation

The Na,K-ATPase preparations were from ox brain (Klodos et al., 1975) and had the same properties as described earlier (Klodos et al., 1981; Plesner et al., 1981): specific activity, $\sim 3 \text{ U} \cdot (\text{mg protein})^{-1}$, maximum phosphorylation sites, $\sim 300-360 \text{ pmol} \cdot (\text{mg protein})^{-1}$.

Phosphorylation and Dephosphorylation Experiments

The experimental conditions (see also *Experimental Plan* and Fig. 1), including the determination of acid-stable [³²P]EP specific for Na,K-ATPase, were as described in detail by Klodos et al. (1981) unless otherwise indicated. It should be emphasized that the phosphorylation was always performed without added K⁺ and with [Na⁺] \geq 20 mM, and that under these conditions, almost 100% of the enzyme was phosphorylated in steady state. In one series of experiments, Tris buffer (pH 7.4 at 0°C) was added to the medium so that [Na⁺] + [Tris⁺] was constantly 300 mM. The anion was always chloride.

Na-ATPase activity was measured at $0.5-1^{\circ}$ C either under the conditions of the phosphorylation experiment with $25 \,\mu$ M [³²P]ATP (Fig. 1) or with 1 mM ATP (which contributes ~7 mM Tris⁺ to the assay; see below) as the substrate. The enzyme concentration was ~50 nM. The ³²P released was determined by the method of Lindberg and Ernster (1956) with the modification that the organic phase, which was isobutanol, and the water phase were pre-equilibrated with each other before use. Inorganic phosphate, when 1 mM ATP was the substrate, was determined as described by Ottolenghi (1975) with the modification (suggested by P. Ottolenghi) that 5% sodium dodecyl sulfate be added to the ascorbic acid/ammonium heptamolybdate reagent to abolish an opacity caused by the high protein concentration. The ouabain-independent activity was measured at 0°C after preincubation of the enzyme at 37°C for 30 min with 10⁻⁴ M ouabain (without ATP).

Reagents

ATP and ADP were obtained as sodium salts from Boehringer Mannheim Biochem-

icals, Federal Republic of Germany, and $[\gamma^{32}P]ATP$ was obtained from New England Nuclear, Boston, MA. ATP was converted to its Tris⁺ salt by chromatography on a Dowex I column (Sigma Chemical Co., St. Louis, MO), and $[\gamma^{32}P]ATP$ was purified on DEAE-Sephadex G-25 (Nørby and Jensen, 1971). Purified ATP contained <0.5 mol% ADP. Since the K⁺ contamination in commercial ADP batches can be rather high (corresponding to ~100 μ M K⁺ in a 2.5-mM ADP solution), ADP was purified by chromatography on a Dowex 50 WH⁺ column. The acid eluate was neutralized immediately by propanediol. All other reagents were reagent grade.

Experimental Plan

The underlying hypothesis of the experiments to be described is that the reaction sequence of Na-ATPase leading from the ADP-sensitive EP form to the unphosphorylated form(s) (presumably, but not exclusively, via the K⁺-sensitive form[s]) consists of several steps and therefore several different EP intermediates. One or more of these steps must involve a reaction with Na⁺ and/or K⁺.

The experiments were therefore designed with the purpose of (a) localizing the reactions involving Na⁺ and K⁺ and (b) achieving a qualitative and quantitative description of the reaction sequence involving the acid-stable phosphorylated intermediates of Na-ATPase.

The experiments can be divided into two series. In the first, the enzyme was phosphorylated (see also Klodos et al., 1981) with 25 μ M [γ^{32} P]ATP, 1 mM Mg²⁺, and [Na⁺] = 20-600 mM. In the second series, Tris buffer (pH 7.4 at 0 °C) was added so that during phosphorylation and dephosphorylation [Na⁺] + [Tris⁺] was 300 mM.

In each of these series the dephosphorylation of the preformed radioactive $[^{32}P]$ -EP intermediates (in their steady state proportions) was followed for up to 10 s under four different conditions. Under all conditions, further phosphorylation by radioactive ATP was immediately reduced to a very low rate (Klodos et al., 1981), either by the addition of unlabeled ATP to reduce the specific activity, or by the addition of ADP, which reduces the concentration of E by forming EADP. To illustrate the general experimental layout, examples of experiment types 1, 2, and 3 (below) are given in Fig. 1.

(1) AFTER THE ADDITION OF 1 MM ATP This experiment measures the sum of the rates of dephosphorylation of all $[^{32}P]EP$ species involved. Note that the addition of ATP contributes ~ 7 mM Tris⁺ to the reaction mixture.

(2) AFTER THE ADDITION OF 2.5 MM ADP The dephosphorylation curves are biphasic (Klodos et al., 1981). The ADP-sensitive [³²P]EP and species converted rapidly to this intermediate are removed at a high rate. The slow phase may therefore serve to characterize the dephosphorylation, as well as the conversion to ADP-sensitive intermediates, of all the other [³²P]EP species.

(s) AFTER THE ADDITION OF 1 MM ATP AND 20 MM K^+ In analogy to experiment type 2, this experiment allows the determination of the proportion of K-sensitive EP's and species rapidly converted thereto. Similarly, the slow phase [and the curves are indeed biphasic with a substantial proportion ([Na⁺]-dependent) of EP turning over slowly] serves to characterize the turnover of a K⁺-insensitive EP pool.

(4) AFTER THE ADDITION OF 2.5 MM ADP AND NA⁺ UP TO 600 MM This illustrates the importance of Na⁺ in the conversion of ADP-insensitive to ADP-sensitive EP and is vital for our attempts to localize the decisive step(s).

EXPERIMENTAL RESULTS

In the following section we first report the results of the different types of experiment. We then outline the strategy for computer simulation of the data according to the three-pool model (scheme S2) and give the results of this simulation in terms of steady state values for the pool sizes and values for the rate coefficients. Finally, we present an evaluation of the dependence of these apparent rate constants on $[Na^+]$, $[K^+]$, and $[Tris^+]$ in the light of the detailed reaction scheme (Fig. 8).

The points in the figures concerning the dephosphorylation experiments are data points and the curves are those obtained with the rate coefficients determined by simulation of the three-pool model. The headings of the sections below refer to the type of experiment described in the preceding section.



FIGURE 1. A typical experiment, here with $[Na^+] = 150$ mM, illustrating the conditions for phosphorylation and three (types 1, 2, and 3; see text) of the four types of dephosphorylation experiments performed in the present paper. The curves are computer simulations of the three-pool model in scheme S2 and the intercepts iADP and iK are obtained by linear extrapolation (by eye) using the data points. These intercepts are used in the computer simulation as described in the text. Note that 100% - iADP + 100% - iK = 45% + 81% = 126% is >100% (see Table I).

(1) Dephosphorylation with 1 mM ATP

The ATP curves of Figs. 2 and 3 clearly illustrate that the rate of dephosphorylation of the EP pools as a whole increases with $[Na^+]$. The effect levels off at 300 mM, and at 600 mM the rate is again lower. Comparison of Figs. 2 and 3 reveals that Tris⁺, at any given Na⁺ concentration, inhibited dephosphorylation.

Although the curves appear monoexponential and have often been assumed to be so, close inspection of these and previously published curves reveals that this is not necessarily so. The curves through the points of the type 1 experiments in Figs. 2 and 3 are actually calculated from the sum of three exponentials related to the three-pool model (see below).

(2) Dephosphorylation with 2.5 mM ADP

Two principal features of these experiments are apparent from Figs. 2 and 3. First, Na⁺ increases the proportion of EP that is rapidly dephosphorylated



FIGURE 2. Dephosphorylation curves at $[Na^+] = 20, 150, 300, and 600 \text{ mM}$ after addition of 1 mM ATP, 2.5 mM ADP, or 1 mM ATP + 20 mM K⁺. $[Na^+]$ was the same during phosphorylation and dephosphorylation. A similar experiment with 50 mM Na⁺ is not shown. The experiments were performed at 0°C as described in Materials and Methods; see also Fig. 1. The points are data points expressed as $100\% \cdot [EP]/[EP]_{\circ}$, which is calculated as $(EP'_t - EP'_{\infty})/(EP'_{\circ} - EP'_{\infty})$ (see Klodos et al., 1981), where EP'_{\circ} was 300-360 and EP'_{∞} (EP dephosphorylated for 5 min) was ~10 pmol P · mg protein⁻¹. Every point is the mean value of at least three experiments. The SEM was on the average ± 3 pmol P · mg protein, which corresponds to $\pm 1\%$. The curves are computer simulations of the three-pool model (S2) as described in the text.

by ADP, called the ADP-sensitive EP, here estimated (see Fig. 1) as 100% – iADP (Table I). Second, the rate of dephosphorylation of the remaining EP, ADP-insensitive EP, is higher with a higher Na⁺ concentration. This part

of the dephosphorylation seems to follow a monoexponential course at least at high [Na⁺] (see also Figs. 1 and 4 in Klodos et al. [1981]).

Again, the results with added Tris⁺ are somewhat different. Tris⁺, at a given [Na⁺] up to 150 mM, increased the proportion of ADP-sensitive EP and slowed the decay of the remaining EP species.



FIGURE 3. Dephosphorylation curves (as in Fig. 2) at $[Na^+] = 20, 150, 225$, or 300 mM in Tris buffer. The experimental conditions were such that $[Na^+] + [Tris^+]$ was held constant at 300 mM both during phosphorylation and dephosphorylation. The $[Na^+] = 300$ mM experiment is from Fig. 2 for comparison. An experiment with 50 mM Na⁺ + 250 mM Tris⁺ was also performed (not shown). See Figs. 1 and 2 for further details.

(3) Dephosphorylation with 1 mM ATP and 20 mM K^+

The proportion of $[{}^{32}P]EP$ dephosphorylated rapidly by addition of ATP + K⁺ is estimated as 100% - iK (see Figs. 1-3 and Table I). This fraction, which can be called K⁺-sensitive EP, decreases with a rise in [Na⁺], and at a given [Na⁺], Tris⁺ decreases the proportion of this EP form. There is an

indication that the slope of the initial fast decay (ATP + K curves in Figs. 2 and 3) is Na⁺ dependent. The slope of slow phase of these curves, however, is affected by neither [Na⁺] nor [Tris⁺]. The corresponding rate coefficient is approximately equal to 0.1 s^{-1} . The EP component represented by this slow phase is ADP-sensitive EP because it disappears very rapidly if ADP is added together with ATP and K⁺ (not shown).

(4) Dephosphorylation with 2.5 mM ADP + $Na^+ Up$ to 600 mM

As shown in the foregoing experiments of types 2 and 3, the steady state composition of the EP pool with respect to ADP-sensitive and K-sensitive EP is determined by the composition of the phosphorylation medium, notably the Na⁺ and the Tris⁺ concentrations. In Fig. 4 we demonstrate that for a given steady state situation, addition of Na⁺ together with ADP at the start of the dephosphorylation experiment changes the course of [³²P]EP decay.

TABLE I
Proportion (%) of ADP-sensitive E1P and K ⁺ -sensitive E2P as a Function of /Na ⁺
and [Tris ⁺]

[Na ⁺]	[Tris ⁺]	E ₁ P (100% - iADP)	E ₂ P (100% - iK)	$E_1P + E_2P$
mM	mM			
20	0	15	88	103
50	0	27	87	114
150	0	45	81	126
300	0	67	68	135
600	0	83	38	121
20	280	35	68	103
50	250	38	66	104
150	150	48	65	113
225	75	57	70	127

The ordinate intercepts iADP and iK were determined as described in Fig. 1 and the text.

It is obvious that the slope of the slow phase is increased by Na⁺, as is expected from the results of the type 2 experiments. More interesting is the fact that the proportion of ADP-sensitive EP, measured as 100% - iADP, is increased by the addition of Na⁺ to the dephosphorylation medium (see Fig. 4; e.g., enzyme phosphorylated with 20 mM Na⁺: with 20 mM Na⁺ in the dephosphorylation medium, 100% - iADP is ~20%; with 600 mM it is ~60%). This apparently indicates that Na⁺, in a concentration-dependent way, can convert an ADP-insensitive [³²P]EP pool (or part of it) during the dephosphorylation period to ADP-sensitive EP. We have previously (Klodos et al., 1983) called this pool Na⁺-sensitive EP.

Before we describe the curve-fitting method by which the experiments are evaluated, we want to single out two features of the results obtained.

(a) Traditionally, EP in steady state is considered to consist of ADP-sensitive EP and K⁺-sensitive EP, sometimes called E_1P and E_2P , respectively, so that

 $EP = E_1P + E_2P$. It is customary (e.g., Kuriki and Racker, 1976; Hara and Nakao, 1981) to determine E_1P as 100% – iADP and E_2P as 100% – iK (see Fig. 1). Using this procedure, we find that when $[Na^+] = 20$ mM during



FIGURE 4. Dephosphorylation curves with ADP + Na⁺ corresponding to experiment type 4 (see text). The enzyme was phosphorylated as described in the presence of 20, 50 (not shown), 150, 300, or 600 mM Na⁺, as indicated at the top of each panel. Dephosphorylation was accomplished by addition of 2.5 mM ADP and Na⁺ to give the final Na⁺ concentration shown for each curve. The 600-mM experiment in the lower right panel is the same as that shown in Fig. 2. See Figs. 1 and 2 for further experimental details. The curves are calculated using the values for A_o, B_o, and C_o characteristic for [Na⁺] during phosphorylation as initial values at t = 0 and the rate coefficients of the threepool model (S2) corresponding to [Na⁺] during dephosphorylation.

phosphorylation, $E_1P + E_2P$ is close to the expected 100%, but with $[Na^+] > 50 \text{ mM}$, $E_1P + E_2P$ becomes >100% (Table I).

(b) With a given steady state composition of EP, the value for 100% –

iADP = ADP-sensitive EP can clearly be increased by increasing [Na⁺] during dephosphorylation. Thus, Na⁺ increased both the rate of dephosphorylation and the apparent proportion of ADP-sensitive EP.¹

Both these features are unexplainable by a traditional two-pool model and we were forced to try the three-pool model shown in scheme S2 as the minimum requirement for a successful curve fitting.

$$\frac{k \cdot ADP}{A} \qquad A \qquad A \qquad B \qquad A \qquad B \qquad C \\
\frac{k_{A}}{k_{-B}} \qquad B \qquad k_{b} \qquad C \\
\frac{k_{a}}{k_{a}} \qquad k_{b} \qquad k_{c} \qquad P_{i} \qquad P_{i}$$

SCHEME S2. Three-pool model for the interconversion and hydrolysis of the phosphoenzymes of Na-ATPase. A, B, and C are different phosphoenzyme pools. For the experiments in which $[Tris^+] + [Na^+]$ was 300 mM, the coefficients have a subscript T, e.g., k_{AT} , k_{-BT} , etc.

This scheme implies that A is ADP sensitive and $E_{ADP}^{\sim P}$ (which of course cannot react with ADP) is thus not included among the acid-stable EP forms in this scheme. This seems justified for the following reasons. Let us assume that $E_{ADP}^{\sim P}$ was acid stable and constituted a significant (measurable) proportion of the EP forms at steady state (a hypothetical pool X, not shown in S2, but placed to the left of A in scheme S2: $\xleftarrow{k_X} x \xleftarrow{k \cdot ADP} A$). Since the addition of ADP, which stops phosphorylation and converts A to X, leads to a rapid disappearance of a portion of the acid-stable EP, k_X must be large. But if $E_{ADP}^{\sim P}$ is acid stable and k_X is large, the addition of unlabeled ATP (see experiment type 1; $k \cdot ADP \cong 0$) would also lead to a significant drop in the [³²P]EP concentration, a drop corresponding to [X], and this is not observed (Figs. 1–3). We therefore conclude that if $E_{ADP}^{\sim P}$ is acid stable, it is present in insignificant amounts.

KINETIC ANALYSIS OF DATA

As mentioned in the Introduction, all results under different conditions could be accurately fitted to the three-pool model shown in scheme S2. The mathematical formulation of that model is shown in Fig. 5. The three-pool model does not permit an analytical solution as regards the dephosphorylation equations, and the curves (which are a sum of three exponentials) must therefore be generated by numerical methods. This necessitates a primary estimation (see below) of reasonable starting values for the parameters in these equations. The strategy used in and the logic behind the estimation of the necessary starting values for the curve fitting were as follows.

Assumptions and Preliminary Estimates of $[A]_o$, $[B]_o$, and $[C]_o$

(i) Dephosphorylation of pool C (and perhaps B), but not A, is fast in the presence of K^+ (the ATP + K^+ curves). Therefore, the ordinate intercept of

¹ If this effect of Na⁺ were due to an increased rate of conversion of E_2P to E_1P in a two-pool system, Na⁺ would not change the intercept but only the slope of the ADP-insensitive decay (see Klodos et al., 1981, for an analysis of the two-pool model).

the slow phase, iK (see Figs. 1-3), is equal to $[A]_o + a[B]_o$, where $0 \le a < 1$. As a first approximation, we assume that the monoexponential behavior of the slow phase reflects that both C and B are dephosphorylated rapidly so that $a \cong 0$, which makes iK a reliable starting value for $[A]_o$.

(ii) Pool A is assumed to disappear very rapidly after addition of 2.5 mM ADP (the ADP curves, Figs. 1-4). Thereafter, the curve follows the curve corresponding to a two-pool model described by Klodos et al. (1981) and the extrapolated ordinate intercept of the "final" monoexponential phase, iADP, is thus equal to $[C]_o + b[B]_o$, where $0 \le b < 1$. Note that iK + iADP = $[A]_o + [C]_o + (a + b)[B]_o$ is always <100%. This means that (a + b) < 1 and thus b < 1.

$$\frac{[A]_{\circ}}{[B]_{\circ}} = \frac{1}{k_{A}}(k_{-B} + k_{b} + k_{c} \cdot \frac{k_{B}}{k_{-C} + k_{c}}) \qquad \frac{[C]_{\circ}}{[B]_{\circ}} = \frac{k_{B}}{k_{-C} + k_{c}}$$
$$[A]_{\circ} + [B]_{\circ} + [C]_{\circ} = 100$$

$$\boxed{\text{DEPHOSPHORYLATION}}$$

$$[A]_{t+dt} = [A]_{t} - ([A]_{t} \cdot (k_{A} + k_{a}) - [B]_{t} \cdot k_{-B}) \cdot dt$$

$$[B]_{t+dt} = [B]_{t} - ([B]_{t} \cdot (k_{B} + k_{b} + k_{-B}) - [A]_{t} \cdot k_{A} - [C]_{t} \cdot k_{-C}) \cdot dt$$

$$[C]_{t+dt} = [C]_{t} - ([C]_{t} \cdot (k_{c} + k_{-C}) - [B]_{t} \cdot k_{B}) \cdot dt$$

FIGURE 5. Mathematical model for the three-pool model shown in scheme S2. It should be noted that in the computer simulation, as described in the text, the rate constants are only allowed to vary with the concentration of Na⁺, Tris⁺, and K⁺. In experiments of types 3 (where K⁺ is added) and 4 (where Na⁺ is added to the dephosphorylation medium), one can thus have one set of rate constants during steady state and another set during dephosphorylation. Dephosphorylation with 2.5 mM ADP is assumed to result in $[A]_t = 0$ just after the addition of ADP (see Klodos et al., 1981). $[A]_o$, of course, is not zero. See text for further details.

(*iii*) With a constant steady state composition, determined by $[Na^+]$ during phosphorylation, the addition of Na⁺ to ADP decreases iADP, as shown in Fig. 4. This is taken as evidence for an increased rate of conversion of B to A, and therefore iADP will approach $[C]_o$ with increasing $[Na^+]$.

In summary, an estimate of $[A]_o$ and $[C]_o$ is obtained from points *i* and *iii*, respectively, and the estimate of $[B]_o$ is then calculated as $100\% - [A]_o - [C]_o$.

Preliminary Estimates of Rate Coefficients

The general assumption is that the rate coefficients are dependent upon $[Na^+]$, $[K^+]$, and $[Tris^+]$ only, as noted also in the legend to Fig. 5.

(*iv*) The slope of the dephosphorylation curves after the addition of cold ATP (the ATP curves, Figs. 1–3) is a weighted (with respect to [A], [B], and [C]) average of k_a , k_b , and k_c .

(v) As described under point *ii*, the ADP curves follow a two-pool model after ~ 1 s and $[A]_t$ is accordingly set to 0. The early curvature (Figs. 1-4) is primarily dependent on $(k_{-B} + k_b)$, whereas the slope of the monoexponential phase is determined mostly by k_c (and k_{-C}) (cf. Klodos et al., 1981). The slope and the extrapolated ordinate intercepts of the curve will depend on $[A]_o$, $[B]_o$, and $[C]_o$, and on $k_{-B} + k_b$.

(vi) Estimates of k_A and k_B can now be obtained from the steady state equations. Note that $k_B/(k_{-C} + k_c)$ appears in both steady state expressions.

Curve Fitting Using the Three-Pool Model

The starting values obtained were then fed into an HP 85 desk computer (Hewlett-Packard Co., Palo Alto, CA), which was programmed with the equations in Fig. 5. The time step, dt, could be varied between 1 and 50 ms without any consequence for the shape and position of the simulated curves, and a step of 10 ms was finally chosen. The rate coefficients and [A]_o, [B]_o, and [C]_o were then varied by trial and error until a satisfactory fit to the data points was obtained. The fact that there are, for each steady state condition, no less than four different dephosphorylation experiments places considerable constraints on the variability of the results of this curve fitting (see Fig. 6). The restrictions imposed by the steady state expressions were of course obeyed and so were the conditions described in the legend to Fig. 5. One further note regarding the simulation of type 3 experiments (dephosphorylation with ATP + K⁺): for these dephosphorylation conditions, k_{-B} was initially set to 0 as a starting value, which is equivalent to saying that B and C are dephosphorylated so rapidly that the transfer of B to A is negligible. As will be discussed later, this turned out not to be true at high Na⁺.

The results of the curve fitting are given first in Figs. 1–4, where the drawn curves illustrate the efficacy of fit between the data and the three-pool model. Second, Fig. 6 shows the individual rate coefficients by which these curves were simulated, as well as the values for $[A]_o$, $[B]_o$, and $[C]_o$ as a function of Na⁺ concentration, with and without added Tris⁺. Note that the rate coefficients without Tris⁺ (closed symbols in Fig. 6) may be influenced

FIGURE 6. (*opposite*) The rate coefficients (panels 1–7) and steady state pool sizes (panels 8 and 9) of the three-pool model (S2) as a function of $[Na^+]$. Closed symbols are for experiments without Tris⁺; open symbols are for $[Na^+] + [Tris^+] = 300$ mM. The points represent the values obtained by curve fitting of the three-pool model to the data in Figs. 2–4, as described in the text. The range of variation in the rate coefficients, which will still give satisfactory curves through the data points in Figs. 1–4, is not more than $\pm 0.01 \text{ s}^{-1}$ for k_a , k_b , k_B , k_{-C} and k_c , and $\pm 0.1 \text{ s}^{-1}$ for k_A and k_{-B} . Greater variations clearly resulted in systematic differences between the computed model curves and the data. The curves in this figure are calculated from the affinity constants and the rate constants (Tables II and III) corresponding to the comprehensive model in Fig. 8.



to a certain, slight extent by the \sim 7 mM of Tris⁺ added with the ATP in experiments of types 1 and 4 (see Materials and Methods).

It is obvious that the rate coefficients of the three-pool model, with the possible exception of k_a , are very much dependent on Na⁺ concentration. Interestingly enough, the forward reaction constants k_A and k_B , as well as the hydrolysis rate coefficients k_b and k_c , are lower with Tris⁺ than without, whereas those leading in the direction of pool A, namely k_{-B} and k_{-C} , are unaffected. k_A is ~10 times higher and k_{-B} at Na⁺ ~150 mM is ~5-10 times higher than the other rate coefficients. The steady state consequence of these relationships is illustrated by the variations in the pool sizes [A]_o, [B]_o, and [C]_o with the Na⁺ and Tris⁺ concentrations shown in Fig. 6.

Comparison of Directly Measured and Calculated Na-ATPase Activity

From the hydrolysis rate coefficients and the pool sizes given in Fig. 6 one may calculate the expected overall rate of P_i production as a function of $[Na^+]$ (with or without Tris⁺) as

$$v = k_a[\mathbf{A}]_o + k_b[\mathbf{B}]_o + k_c[\mathbf{C}]_o.$$

Comparison between v (calculated) and v (measured) shows that with [Na⁺] + [Tris⁺] = 300 mM the agreement is excellent (Fig. 7A).

As regards the experiments without Tris⁺, the situation is not so clear. First of all, the measured activity with 25 μ M [³²P]ATP is 10–30% higher than that with 1 mM ATP (Fig. 7B) with Na⁺ up to 225 mM. This may be explained by the fact that our unlabeled ATP (as mentioned several times above) contains Tris⁺ and contributes ~7 mM Tris⁺ to the assay since Tris⁺ in this range of Na⁺ concentrations inhibits the hydrolysis (Fig. 7A and the hydrolysis rate constants k_b and k_c in Fig. 6). Similarly, J. C. Skou (personal communication), using Tris-ATP as substrate, has observed an inhibition above 100 μ M ATP of Na-ATPase at 37°C with Na up to 150 mM, whereas L. Plesner and I. W. Plesner (personal communication) did not observe such an inhibition, probably because they used Na₃ATP instead of Tris-ATP.

Second, for Na⁺ \geq 300 mM, the activity with 25 μ M ATP is 10–15% lower than that with 1 mM ATP. The reason for this is not clear, but it might reflect an ionic strength effect on the $K_{0.5}$ for ATP for the Na-ATPase reaction. It is obvious from Fig. 7*B*, however, that also in the experiments without Tris⁺ there is agreement between the calculated hydrolysis rate and that measured under conditions corresponding to those under which the hydrolysis rate constants were determined. This agreement might be taken as support for the validity of the computer simulation in describing the system.

A Model for Interpreting the Cation Dependence of Rate Constants

To explain and extract further information from the relationships shown in Fig. 6 between the parameters of the three-pool model and $[Na^+]$ and $[Tris^+]$, it is necessary to expand the three-pool model to a more detailed reaction scheme. Before we undertake this task, we should point out that the form of the curves through the data points in Fig. 6 immediately excludes the possibility that the interconversions in the three-pool model are simply additions (binding) of Na⁺ to or dissociation of Na⁺ from A, B, and C. In the case of binding reactions, the rate coefficients would not "saturate" with Na⁺



FIGURE 7. (A) Na-ATPase activity at 0°C with 25 μ M [³²P]ATP as the substrate (see Materials and Methods) as a function of Na⁺ concentration in the absence of Tris⁺ (O) and with [Na⁺] + [Tris⁺] = 300 mM (\Box). The values represented by a star are calculated as described in the text from the steady state pool sizes of the three-pool model (S2) and the hydrolysis rate coefficients for the Na⁺ + Tris⁺ experiment; see Fig. 6, open symbols. The activity corresponding to 100% was measured with 150 mM Na⁺, 1 mM Mg²⁺, and 30 mM imidazole (no Tris). It was 2.7 nmol·(mg protein)⁻¹·min⁻¹. (B) Na-ATPase activity at 0°C in the absence of Tris, with 25 μ M [³²P]ATP (O) or with 1 mM ATP (which contributes ~7 mM Tris⁺ to the assay) (Δ). Control activity measured as above was 1.9 nmol·(mg protein)⁻¹·min⁻¹. The values symbolized by a star are calculated as described in the text (see also above) using values for pool sizes and hydrolysis rate coefficients from Fig. 6 (no Tris⁺, closed symbols).

as do k_A and k_B , and for dissociation reactions, the coefficients are independent of Na⁺. Similarly, the observed dependence of the hydrolysis rate coefficients k_b and k_c on cation concentration is incompatible with such a simple reaction scheme.

One obvious way of explaining the data in Fig. 6 is to assume that the EP pools in the three-pool model, A, B, and C, all consist of an equilibrium mixture of EP species capable of binding Na⁺. Within a given pool of phosphoenzymes, e.g., pool B, the EP species then would differ in the degree of occupancy of their Na⁺ sites and therefore possibly also in their properties

ADP	A'3 E₁~P ¡ ^{Na} 3	1	Α 3 E ₁ -Ρ i ^{Να} 3	k _{A3} , kB3	o ^{Na} 3 E ₁ -P B3 ML	^к вз , к _{-С3}	_o Na ₃ E ₂ -P [C3] 1L
ADP	1L E ₁ ~P i ^{Na} 2 A'2	H	1L E ₁ - P ^{Na} 2 A 2	^к А 2 , ^к -В 2	o ^{Na} 2 E ₁ -P <u>B2</u> 1L	^к в2 ,	o ^{Na} 2 E ₂ -P <u>C2</u> 1L
		k k	a'3, ^k a'2 a3, ^k a2		в́1−Р в1 1L	*B1 #-C1	е́ ₂ -Р ст 1
		Pj			E ₁ -P BO	*B0 *-C0	$E_2 - P \boxed{C0}$ k_{c3}, k_{c2} k_{c1}, k_{c0}
	$\frac{A'2}{A2} = K_A$	2,	$\frac{A'3}{A3} = K_A$.3	(\mathbf{P}_i)		(\mathbf{P}_i)

FIGURE 8. Comprehensive model for the interconversion of the acid-stable EP forms of Na-ATPase. The letters i and o before bound Na signify that Na is bound to internally oriented (cytoplasmic) sites and external sites, respectively. The site binding constants (not shown in the figure) are denoted α , β , and γ for Na⁺ binding in pools A, B, and C, respectively. Within the three pools, the EP species are supposed to be in equilibrium. The model is described in further detail in the text and so is the reaction of Tris⁺ and K⁺ with the different EP forms.

in regard to hydrolysis and conversion to the corresponding species in pools A and C. The model shown in Fig. 8 is an example of the application of these principles. It further illustrates how we have broken the overall reaction scheme, the three-pool model, down into unitary processes applying the criterion that in chemical and enzymatic reactions only one event (e.g., binding or release of a ligand, conformational change in the enzyme protein, hydrolysis [or other changes] of a chemical bond) takes place at each step (Hearon et al., 1959).

The design of this model (Fig. 8) is based primarily on the observations in this paper as condensed in Fig. 6. It is, for instance, necessary to have three Na⁺ binding steps in pool B to explain the Na dependence of k_{-B} , k_B , and k_b , whereas one binding reaction for Na⁺ in pool A is sufficient to explain k_a and k_A . For pool C, two or three Na⁺ binding sites are necessary. It is obvious, however, that some of the details of the model, e.g., the assignment of Na⁺binding sites to external (o) or internal (i) aspects of the enzymes, cannot be derived solely from our data since we are working with a broken membrane preparation where the cytoplasmic and the external aspects of the pump are exposed to the same medium (the same Na⁺, Tris⁺, and K⁺ concentration).

The model in Fig. 8 must therefore be considered the result of a synthesis based not only upon the results reported here but also on the many studies of Na interactions with the Na,K-ATPase performed under more physiological conditions. The relationship between our model in Fig. 8 and the results of its application in the analysis of the data in Fig. 6, and the more physiological aspects of the Na,K-ATPase, will be discussed later. It is necessary to mention here, however, that in designing this model we have correlated our analysis with the published information about Na,K-ATPase, its properties as disclosed by experiments with cells or vesicles, and its transport functions, in the following manner.

Phosphorylation by ATP in Na,K-ATPase is promoted by cytoplasmic (iNa) sodium at high-affinity sites (Blostein, 1979) and ADP-sensitive $E_1 \sim P$ is formed first (Post et al., 1975; Fukushima and Nakao, 1981). Since A is the ADP-sensitive pool, we have assigned the internal binding sites to this pool. One of the characteristics of the Na pump is that it can operate in different modes. Of particular relevance to our model is the so-called uncoupled Na efflux, extrusion of Na⁺ into a medium lacking Na⁺ and K⁺ and their congeners, and Na:Na exchange between the intra- and the extracellular medium. Since the stoichiometry of uncoupled Na efflux to ATP hydrolysis is between 2 and 3 (Glynn and Karlish, 1976) and only one Na⁺-binding reaction is necessary in pool A (see above), we suggest that the E_1P 's of pool A have bound two or three Na ions. Regarding Na:Na exchange, it is relevant to our model that it seems to be ADP dependent (Glynn et al., 1971; Glynn and Hoffman, 1971; Cavieres and Glynn, 1979), that the stoichiometry of efflux to influx is 1 (Garrahan and Glynn, 1967a; De Weer et al., 1979), and that both efflux and influx are stimulated by extracellular sodium (oNa) acting at low-affinity sites (Garrahan and Glynn, 1967a; Garay and Garrahan, 1973, 1979; Beaugé and Campillo, 1976). Also relevant to this issue is the finding that Na⁺, acting with rather low affinity, increases the ratio between ADP-sensitive and K-sensitive EP (Kuriki and Racker, 1976; Jørgensen and Karlish, 1980; Hara and Nakao, 1981; this paper). ADP:ATP exchange, which clearly involves the ADP-sensitive $E_1 \sim P$ in pool A, is also stimulated by Na acting at low-affinity sites (Tobin et al., 1973; Wildes et al., 1973; Beaugé and Glynn, 1979), and these sites are located on the external aspects of the pump (Kaplan and Hollis, 1980; Kaplan, 1982). In our analysis (see the last paragraph in this section and Table II), the binding affinities for Na⁺

binding to the species in pools B and C are found to be low, and the external Na⁺-binding sites are therefore assigned to these two pools. This makes the $A \rightarrow B$ reaction equivalent to the ion translocation process.

It is also important for the design of the model in Fig. 8 that the ADP sensitivity of EP is most probably lost at a step preceding the Na:Na exchange reaction since the latter is inhibited by oligomycin, whereas ADP:ATP exchange is stimulated (Garrahan and Glynn, 1967c; Blostein, 1970; Wildes et al., 1973), and that the concentration of the ADP-sensitive $E_1 \sim P$ is greatly increased by oligomycin (as shown by Hegyvary, 1976, and I. Klodos, unpublished data). Finally, one may ask why we have proposed that the translocation (Na:Na exchange, $A \rightleftharpoons B$) occurs before the "major" conformational change $E_1P \rightarrow E_2P$ ($B \rightarrow C$). An important argument is that the Na⁺

 TABLE II

 Site Affinity Constants for Na⁺ and Tris⁺ Corresponding to the Model in Fig. 8

	Site af	finity constant (M ⁻¹)) for
		Tris ⁺ on	Na ⁺ on
EP pool	Na ⁺ on Na ⁺ sites	Tris ⁺	site*
Α	$\alpha' = 30 (13 - 30)^{\ddagger}$	$\epsilon_A > 35$	$\rho_{\Lambda} > 20$
В	$\beta = \overline{5}(3-6)$	$\epsilon_{\rm B} > 35$	$\rho_{\rm B} > 20$
С	$\gamma = \overline{\underline{1}} (0.5 - 5)$	$\epsilon_{\rm C} > 35$	$\rho_{\rm C} > 20$

The constants were obtained as described in the text and the Appendix. Values used in the calculation of the curves in Fig. 6 are underlined, whereas the range of values giving a satisfactory fit is shown in parentheses.

* For values above those shown the simulated curves do not change significantly as long as $\epsilon/\rho = 1.75$ (see Appendix).

^{\ddagger} α' is an apparent affinity constant; see text and Appendix.

in pool B reacts at low-affinity sites [see Fig. 6 (k_{-B} as a function of [Na⁺]), and Table III], probably outside-facing sites, and that translocation therefore most likely has occurred when we go from A to B. But it should also be understood that the alternative pathway from A to C with the "major" conformational change occurring before the translocation

$$ext{intro} ONa_3$$

 $E_1 - P \rightleftharpoons E_2 - P \rightleftharpoons E_2 - P$
 iNa_3 iNa_3

would open up the possibility of a quite pronounced ADP-independent Na:Na exchange, which generally does not seem to take place to any significant extent (Glynn et al., 1971; Glynn and Hoffman, 1971; Cavieres and Glynn, 1979).

In the Appendix, the expressions relating the rate coefficients of the threepool model (S2) to the comprehensive model in Fig. 8 are presented. These expressions were fitted to the data of Fig. 6 by trial and error, and although there is a certain flexibility in this computer fitting procedure, the fact that²

² To simplify the notation, we use the general terminology k_j and k_{j0} , k_{j1} , etc., where j can stand for A, a, -B, etc., as is also shown in Table III.

 $k_j = k_{j0}$ at $[Na^+] = 0$, $k_j = k_{j3}$ at $[Na^+] \rightarrow \infty$, and that the site affinity constants $(\alpha, \beta, \gamma, \epsilon_A, \rho_A, \text{ etc.})$ are common for the rate coefficient expressions for a given pool places considerable constraints on the system. The result of the curve fitting is shown in Fig. 6 and Tables II and III and gives the range of values of the affinity constants and rate constants that allow satisfactory fits of the expressions in the Appendix (Eqs. 2A, 5A-9A, etc.) to the data.

DISCUSSION

The Necessity of the Three-Pool Model in Scheme S2

In the remarks introducing the three-pool model (S2) in the Results, we made it clear that since ADP-sensitive EP + K-sensitive EP was >100% (Table I)

j	Α	а	-В	b	В	-С	с*
	1.5 [‡] (1.5–1.7)	0.12 [‡]	4.5 (4.5–3.5)	0	0.06 (0-0.07)	0.4 (2-0.33)	0/0.24 (0-0.24)
k _{j2}	0 [‡] (0–0.3)	0.11‡	0.3 (1-0)	0.15 (0.08–0.17)	0.18	0.3 (0.4–0)	0.33/0.07 (0.4–0.07)
k _{ji}			0	0.14 (0.2–0.13)	0.12 (0.15–0.1)	0.07 (0.15–0.03)	0.11/0.04 (0.2–0.04)
k _{j0}			0	0.02 (0-0.02)	0 (0.020)	0.01 (0-0.02)	0.02
fi	0-0.1	1	1	0	0.3-0.4	1	0

 TABLE III

 Rate Constants Corresponding to the Model in Fig. 8

The constants were obtained as described in the text and the Appendix. The values used in the calculation of the curves in Fig. 6 are shown separately, whereas the range of values giving a satisfactory fit is given in parentheses. Also shown is the Tris-factor, f (see Appendix).

The values for the rate constants are connected to the values for the site affinity constants given in Table II.

* The two combinations of rate constants—0; 0.33; 0.11; 0.02 and 0.24; 0.07; 0.04; 0.02—fit the data equally well.

[‡] Apparent rate constants (see Appendix). The "true" rate constants are equal to or higher than the apparent.

and since Na⁺ added during dephosphorylation increased ADP-sensitive EP, a three-pool model is the minimum model that can explain these results. There are four other published studies from which one can extract information regarding the sum of ADP-sensitive EP and K-sensitive EP. Kuriki and Racker (1976) have published ATP, ADP, and ATP + K⁺ dephosphorylation curves at 120 mM Na⁺ (Fig. 3 in their paper) using Na,K-ATPase from the electric organ of *Electrophorus electricus*. Although the authors do not comment on this particular problem, it is obvious that ADP-sensitive EP is ~75% and K⁺-sensitive EP is ~82%, the sum being 157%. Similar results were obtained with enzymes from the same source by Yoda and Yoda (1982), who showed that the deviation from 100% of the sum of the two types of phosphoenzyme was dependent on [Na⁺]. Fukushima and Nakao (1980, 1981), studying a Ca phosphoenzyme formed with Na,K-ATPase from kidney or brain (pig or rat), also consistently observed that $E_1P + E_2P > 100\%$. The two types of EP were determined by extrapolation of the (apparently) monoexponential, slow phases of dephosphorylation curves with ADP and K^+ , respectively. To explain this observation, they suggested that both E_1P and E_2P were overestimated because the slow phases were multi- rather than monoexponential. However, if E_1P and E_2P are measured as 100% – iADP and 100% – iK, respectively, they will always be underestimated if the slow phase of dephosphorylation follows a multiexponential course. Furthermore, a multiexponential course of the slow phase means that the EP remaining after the very rapid disappearance of ADP- or K-sensitive EP must consist of at least two pools (cf. Klodos et al., 1981, for an analytical solution of this problem), which means that there must have been at least three pools initially. Regarding this point, it is of considerable interest that E_2P increased more rapidly than E_1P decreased when these components were measured as a function of time after initiation of phosphorylation (Fig. 6 in Fukushima and Nakao, 1981). This is exactly what is to be expected if A (cf. S2), formed initially, is converted relatively rapidly to B (which is both ADP and K⁺ sensitive at high Na⁺), and if C, being ADP-insensitive, is formed from B at a lower rate, as proposed here. Although these studies thus confirm our observation, Hara and Nakao (1981) reported for pig kidney Na,K-ATPase that "The sum of these fractions was nearly 1 in the range of 50 to 1,200 mM NaCl." These authors also do not concur with our observation that there is a decrease in iADP when Na⁺ is added to the dephosphorylation medium (Fig. 6 of their paper compared with Fig. 4 in this paper). Whether this discrepancy reflects species or organ differences, or whether it is due to differences in experimental conditions like the time scale of the experiments and the technique for obtaining the ordinate intercept, is not easy to determine. We should point out, however, that with 2 M Na⁺ and 40 mM K⁺ (Fig. 2, Hara and Nakao, 1981) in the K⁺ dephosphorylation experiments, a significant proportion of pool B may be converted to A (k_{-B} becomes large), escaping dephosphorylation with K^+ (see below in section 5).

The Comprehensive Model (Fig. 8) for Na⁺ and Tris⁺ Effects on EP

Although the three-pool model was necessary and sufficient to accurately describe all our data (Figs. 1–4), it must be expanded so that the dependence of its rate coefficients on $[Na^+]$, $[Tris^+]$, and $[K^+]$ can be explained. The excellent fit of the model to the data on the one hand and the dependence of the coefficients on ionic conditions on the other hand suggests that the three pools of A, B, and C must be composed of a number of EP species that are in ion-dependent equilibrium with one another. A further incentive for presenting a rather detailed model is the large amount of additional published information on the enzymological and transport properties of Na,K-ATPase in the presence of Na⁺ (and absence of K⁺). Some of this information is summarized in A Model for Interpreting the Cation Dependence of Rate Constants (see above).

Together with our results and our application of the repeatedly stated maxim that an enzymatic reaction can be divided into steps each of which represents only one event (so-called unitary processes), we have developed the model in Fig. 8 as a comprehensive but nevertheless minimal model. A simplified version of this model is discussed by Nørby and Klodos (1982) and Nørby (1983).

It should be noted that we do not operate with simultaneous Na⁺ occupancy of inner and outer sites in our model since this is not required to explain our results. In fact, simultaneous occupancy would make A3 and B3 (see Fig. 8) indistinguishable, i.e., both would equal $E_1(iNa_3, oNa_3)P$. Garrahan and coworkers (Garay and Garrahan, 1973; Garrahan and Garay, 1974; Garrahan et al., 1979) found that although simultaneous occupancy is not a requirement, it gives the simplest mathematical model for their Na-ATPase and Na:Na exchange results. Their Na-ATPase studies will be discussed below.

In the model in Fig. 8, we use the notation E_1 in pools A and B. This does not mean that we consider the enzyme protein to have exactly the same conformation in these two pools (evidently the EP's have different properties in our model). However, we do suggest that the major conformational change takes place after the translocation of Na⁺, as was suggested by Post et al. (1972) a decade ago. For a review of the conformations of Na,K-ATPase, see Jørgensen (1982). We want to indicate also that although our data can be fitted well by the expanded scheme in Fig. 8, which assumes the equivalency of the Na⁺ sites in pool B and the separate equivalency of the Na⁺ sites in pool C, this fit cannot be taken as proof of the equivalency of these sites. Rather, it reflects our limited perspective of the present pools as examined in these dephosphorylation measurements. For a separate discussion of the high affinity external Na⁺-site, see *High-Affinity External Na⁺ Site* below.

The Effect of Na⁺

It is our belief that the efficacy of fit of our model to the data presented here, together with the reasoning behind its formulation, warrants its use as a frame of reference (a biochemical and enzymological correlate) for the several properties, partial reactions, and transport modes, which, in the absence of K⁺, are influenced by the Na⁺ concentration. The reader is referred to recent reviews by Garrahan and Garay (1976), Robinson and Flashner (1979), and Cantley (1981), which cover these subjects. In this section we shall limit the discussion to the effect of Na⁺. The effect of Tris⁺, which may influence the partial reactions and transport, as it has the phosphoenzymes and Na-ATPase, is discussed below (*The Effect of Tris⁺*). We shall also assume that the substantial increase in ionic strength when Na⁺ is increased from 20 to 600 mM is responsible for the deviation between the model and the data as regards k_{α} and k_b (Fig. 6). Skou (1974, 1979) has reported a similar inhibitory effect of high ionic strength on both pNPPase and Na,K-ATPase activity.

Before we proceed with the discussion of the Na⁺ effect, we should point out that the dephosphorylation constants obtained in the present study are generally of the same magnitude as those calculated by other authors from the "linear" parts of ATP, ADP, or ATP + K⁺ dephosphorylation curves (Post et al., 1972; Kuriki and Racker, 1976; Hegyvary, 1976; Fukushima and Nakao, 1980, 1981; Klodos et al., 1981; Hara and Nakao, 1981).

Internal Na⁺ and the Properties of Pool A

The lowest Na⁺ concentration in the experiments reported in this paper is 20 mM. With 25 μ M ATP and 1 mM Mg²⁺, this gives maximum phosphorylation, in accordance with the $K_{0.5}$ for Na⁺ for phosphorylation being much lower than 20 mM, since Na⁺ is acting on high-affinity cytoplasmic sites (Blostein, 1979). Similarly, when uncoupled Na⁺ efflux (Sachs, 1970; Karlish and Glynn, 1974; Blostein, 1979), Na:Na exchange (Garrahan and Glynn, 1967*a*; Sachs, 1970; Garay and Garrahan, 1973), ATP:ADP exchange (Wildes et al., 1973; Beaugé and Glynn, 1979; Kaplan and Hollis, 1980; Kaplan, 1982), and Na-ATPase activity (Post et al., 1972; Beaugé and Glynn, 1979; Garrahan et al., 1979; Blostein, 1979) are studied, the internal Na⁺ sites have a high affinity for Na⁺ and in most cases they seem to be saturated at relatively low Na^+ concentrations. It was therefore not expected that the efflux rate constant, k_A , in S2 and Fig. 8 would increase with Na⁺ with an apparent affinity constant as low as $\sim 30 \text{ M}^{-1}$, which corresponds to a K_{diss} of \sim 30 mM. In this connection it must be remembered that the number of internally bound Na ions needed for phosphorylation is unknown (one might be sufficient, as suggested by Mårdh and Post [1977]). For ATP:ADP exchange, two might be necessary (Beaugé and Glynn, 1979), whereas Na efflux is best described by assuming that three (Garay and Garrahan, 1973) or two to three (Karlish and Pick, 1981) Na ions must be bound for maximal efflux. Our suggestion that the composition of pool A changes with Na and that $k_{A2} < k_{A3}$ (Fig. 8, Table III) agrees with these ideas.

Comparing quantitative aspects such as apparent $K_{\rm m}$ or $K_{0.5}$ values requires that species differences, temperature, etc., be taken into consideration. However, although a $K_{0.5}$ of ~30 mM (1/ α' , Table II) suggests a rather lowaffinity site to be in operation, it must be noted (see Appendix and Fig. 8) that the "true" affinity constant, α , is $\alpha'(1 + K_{A2})/(1 + K_{A3})$, so that the "true" $K_{\rm diss}$ for Na⁺ may be considerably lower than 30 mM.

Our model in Fig. 8 sets some constraints on the mechanism by which oligomycin can simultaneously inhibit Na:Na exchange (Garrahan and Glynn, 1967c; Sachs, 1980) and stimulate ATP:ADP exchange (Blostein, 1970; Wildes et al., 1973) and $E_1 \sim P$ formation (Hegyvary, 1976; I. Klodos, unpublished data) in a reversible manner. The simplest possibility is that oligomycin binds to $iNa_2E_1 \sim P$ and/or $iNa_3E_1 \sim P$ in such a manner that the ADP sensitivity of these forms is stabilized (conversion to iNa_3E_1P is inhibited). Oligomycin may also bind to all the species in pool A and inhibit translocation of Na⁺ ($k_A \rightarrow 0$, as with Tris⁺ or K⁺; see below) without changing drastically the equilibria within the A pool.

External Na⁺ and the Properties of Pools B and C

Na⁺ in concentrations higher than that needed to saturate the high-affinity internal sites is important for a number of properties and partial reactions of

the Na,K-ATPase. We propose that these effects of Na⁺, which are elicited on rather low-affinity sites, may be due to interactions of Na⁺ with pools B and C. First, our model provides a detailed mechanistic explanation of the role of Na⁺ in increasing the E_1P/E_2P ratio. Here it must be borne in mind that not only does pool A increase with [Na⁺] at the expense of pool C (Fig. 6), but also that more and more of pool B becomes ADP-sensitive because of the increasing ratio of k_{-B}/k_B at higher Na⁺. This effect of Na⁺ is clearly a low-affinity phenomenon (and Tris dependent [Fig. 6]; see also Kuriki and Racker, 1976; Jørgensen and Karlish, 1980; Hara and Nakao, 1981; Yoda and Yoda, 1982), and it is parallel to a similar low-affinity effect of Na⁺ on ATP:ADP exchange (Wildes et al., 1973; Beaugé and Glynn, 1979; Kaplan and Hollis, 1980). Presumably, it is Na⁺ bound to external sites that promotes this phenomenon (Kaplan and Hollis, 1980; Kaplan, 1982), which shows little or no tendency to saturate in the region of 20 to 140–200 mM Na⁺, as with k_{-B} (or k_{-C}).

Our model also indicates part of the route that must be followed when ATP is synthesized from inorganic phosphate and ADP in what is called the backwards-running or reversal of the pump. In pump reversal (Glynn et al., 1970), K^+ efflux and the simultaneous ATP synthesis by red blood cells (Glynn and Lew, 1970) increases linearly with external [Na⁺]. Similarly, when E_2P is formed from $E + P_i$, synthesis of ATP can be invoked by adding ADP and high concentrations of Na⁺, the apparent $K_{0.5}$ for Na⁺ being 0.3–1 M (Post et al., 1974; Taniguchi and Post, 1975). This is what one would expect from Fig. 8 and the affinities and rate constants in Tables II and III: driving E_2P toward iNa₃ $E_1 \sim P$ is possible only with very high Na⁺ concentrations. A similar relation has been observed between Na:Na exchange and external [Na⁺] by several laboratories, e.g., Garrahan and Glynn (1967a), Garay and Garrahan (1973), and there is ample evidence that two to three sites must be occupied before Na⁺ influx can take place (Garay and Garrahan, 1973). This is equivalent to our observation that k_{-B0} and k_{-B1} are both zero (Fig. 8, Table III).

As regards the Na-ATPase activity, the effect of Na⁺ on the redistribution of the three pools and on the dephosphorylation constants does not provide a simple kinetic formula for the relationship between Na-ATPase activity, v, and [Na⁺] observed by us and by Glynn and Karlish (1976), Beaugé and Glynn (1979), and Garrahan et al. (1979). The versatility of our model in accounting also for this relationship is apparent from the agreement between the calculated and the directly observed v's in Fig. 7. Note that here the lowaffinity sites of pools B and C play a role. Two further points regarding Na-ATPase activity need to be emphasized. First, our data are best simulated if it is assumed that k_{b3} (and perhaps k_{c3}) is zero, which would suggest inhibition (lower rate constants) at very high [Na⁺]. This is in line with the measurements shown in Fig. 7B and the findings of Hara and Nakao (1981) and Forgac and Chin (1982), but it was not observed by Mårdh and Post (1977) (or by P. Ottolenghi, personal communication), probably because the latter authors used Tris⁺ to keep [Tris⁺] + [Na⁺] constant (see also Fig. 7A and The Effect of Tris⁺ below). Second, the suggestion by Glynn and Karlish (1976) and Lee and Blostein (1980) that on the low-affinity sites Na⁺ acts like K⁺ in promoting dephosphorylation is also consistent with the result that only occupation of one or two sites is necessary for instituting hydrolysis. This is the type of Na⁺ interaction that may result in Na:Na exchange in the absence of ADP, and, accompanied by ATP hydrolysis, the Na⁺ influx proceeding via $E_2P(Na)_o \rightarrow$ $E_2(Na)_o \rightarrow E_1(Na)_i$. It is clear, however, that at saturating external Na⁺ and with ADP in the cells, Na:Na exchange in our model will be accompanied by little hydrolysis because (a) k_{b3} and k_{c3} are 0, and (b) k_A and k_{-B} will both be at least one order of magnitude higher than k_a , as shown in Fig. 6.

High-Affinity External Na⁺ Site

One feature of the interaction between Na,K-ATPase and Na⁺ is the inhibition by low extracellular [Na⁺] (<5 mM) of (a) uncoupled Na⁺ efflux (Garrahan and Glynn, 1967a; Sachs, 1970; Lew et al., 1973; Karlish and Glynn, 1974; Beaugé and Campillo, 1976), (b) the ATP hydrolysis associated herewith (Karlish and Glynn, 1974; Glynn and Karlish, 1976), and (c) ATP:ADP exchange (Beaugé and Glynn, 1979; Kaplan and Hollis, 1980; Kaplan, 1982). Although our experiments are performed at [Na⁺] > 20 mM, and although the inhibition by Na⁺ at the high-affinity extracellular site is reversed at higher [Na⁺] concentrations, this phenomenon may nevertheless be important for the interpretation of our model at 0–20 mM Na⁺.

It has been suggested that the inhibition results from high-affinity binding of one Na⁺ (Cavieres and Ellory, 1975; Garay and Garrahan, 1979) to E_2P , which inhibits the dephosphorylation of this compound (Lew et al., 1973; Cavieres and Ellory, 1975; Glynn and Karlish, 1976), thereby disrupting the cycle before the formation of E_1P , which plays a crucial role in the processes mentioned. Now, if this high-affinity site is one of the three external Na⁺ sites, the three sites cannot have the same affinity for Na⁺ as assumed in our model (Appendix). The consequence of this is that our data at $[Na^+] = 20$ -600 mM, where the high-affinity site is saturated, must be described by a two-site model. When such a model, assuming two equal, independent, lowaffinity sites in each of the pools B and C ($\beta = 2$ and $\gamma = 0.5$ M⁻¹), is fitted to our data, the results given in Fig. 9 and Table IV are obtained. Comparison of Figs. 6 and 9 will reveal that the fit to k_b (and perhaps k_B) is best with the equal three-site model, whereas k_{-C} and k_{c} fit equally well. One may speculate whether this reflects the presence of a high-affinity external site on E₂P in pool C only and not on the species in pool B.

The Effect of Tris+

The original purpose of adding Tris⁺ in the series of experiments where $[Na^+] + [Tris^+]$ was kept constant at 300 mM was to see whether the Na⁺ effect at $[Na^+] = 20-300$ mM was influenced by ionic strength. The profound difference between the hydrolysis curves (Fig. 7A) with and without Tris⁺ might well be thought of as an ionic strength effect, especially as the rate of hydrolysis declines when $[Na^+]$ is increased from 300 to 600 mM. However,

on the basis of our analysis of all the data, we shall argue in favor of a specific effect of Tris⁺ on what we shall call a "Tris site."

It is clear from the simulation of the three-pool model (Fig. 6) that k_{-B} and k_{-C} (and probably also k_a) are independent of the presence of Tris⁺. When these coefficients are evaluated according to the comprehensive model in



FIGURE 9. The result of fitting a model with one high-affinity external Na⁺ site ($K_{diss} < 5$ mM) and two equal and independent low-affinity external Na⁺ sites to the rate coefficients for pools B and C (see Fig. 6 for further details on the data points). The constants used in the calculation of the curves are given in Table IV and in the text (*High-Affinity External Na⁺ Site* in the Discussion).

Fig. 8 (see the Appendix), it appears that only those species with three Na⁺, B3 and C3, are converted to A3 and B3, respectively, since k_{j0} , k_{j1} , and k_{j2} (j = -B or -C) are close to zero (Table III). From these premises we can conclude that Tris⁺ does not alter the composition of pool B or C and it

seems to be without influence on the site affinity constant for Na^+ . It is thus unlikely that Tris reacts on the Na^+ sites. There is no indication of a Na^+ effect of Tris⁺.

On the other hand, k_A , k_b , k_B , and k_c are all dramatically decreased by Tris⁺, and this, together with the indifference of the other constants, is most easily explained as follows: within a given pool—A, B, or C—Tris⁺ reacts with all species on a Tris site with the same affinity, ϵ_A , ϵ_B , or ϵ_C , and the EP complexes with Tris⁺ have in some but not all respects properties different from those without Tris⁺. The close correlation between the observed and calculated hydrolysis rates (Fig. 7A) supports this analysis. Finally, with the above assumptions and the additional feature of a competition (Appendix) between Na⁺ and Tris⁺ on the Tris site, we were also able to simulate satisfactorily the rate-constant curves for the Tris experiments in Fig. 6.

According to what we have just said, the discrepancy between the Na-ATPase curves with and without Tris⁺ is the result of a specific Tris⁺ effect rather than an effect of variation in ionic strength. This should be taken into consideration in the interpretation of several published Na-ATPase curves:

 TABLE IV

 Rate Constants Corresponding to a Model Like That in Fig. 8 But with One High

 Affinity Na⁺ Site in Pools B and C

	50	-			
j	-В	b	В	-C	с
$k_{i3} (s^{-1})$	6	0	0	1	0
k _{i2}	0	0.25	0.25	0.25	0.37
k _{j1}	0.1	0.04	0.02	0	0.02
fj	1	0	0.4	1	0

The rate constants are those used in the calculation of the curves in Fig. 9. See the Discussion.

Post et al. (1972) had no Tris⁺ in their Na-ATPase assay (but measured dephosphorylation rate constants as a function of $[Na^+]$ in the presence of up to 720 mM Tris⁺); Mårdh and Post (1977) used 30 mM Tris and varied $[Na^+]$. Both Beaugé and Glynn (1979) and Garrahan et al. (1979) kept $[Na^+]$ + $[Tris^+]$ constant, at 180 and 150 mM, respectively. Choline has also been used to keep ionic strength constant (Glynn and Karlish, 1976; Lee and Blostein, 1980), but we do not know whether choline has a specific effect on Na,K-ATPase.

Besides inhibiting the hydrolysis by decreasing k_b and k_c , Tris⁺ also inhibits the conversion of A to B (the ion translocation step in Fig. 8), since it decreases k_A toward zero (Fig. 6 and Table III; $f_A \sim 0$). Tris⁺, so to say, keeps the EP on the true E₁P form with high-affinity internal sites for Na⁺. This effect of Tris⁺ may be analogous to that observed for the dephosphoenzymes by Skou and Esmann (1980), who found that Tris⁺ (and certain other protonated buffers) favored the formation of a sodium-like conformation of the enzyme. Of equal interest is the report by Jensen and Ottolenghi (1984) that Na,K-ATPase at low ionic strength occurs in a form with a high affinity for K⁺, a low affinity for ATP, and presumably a low affinity for Na⁺. Addition of 15–75 mM Tris⁺ (Nørby and Jensen, 1971; Jensen et al., 1983) converts the enzyme to a form with a high affinity for ATP, and presumably a high affinity for Na⁺. The affinity for Tris⁺ in these experiments seems to be higher than 100 M⁻¹ (J. C. Skou, personal communication), and our value for the affinity to the phosphoenzymes, $\epsilon > 35$ M⁻¹ (Table II), thus seems to be comparable to that for the dephosphoenzymes.

The Effect of K^+

The dephosphorylation experiments in the presence of 1 mM ATP and 20 mM K⁺ are best simulated by setting a high value for the hydrolysis rate constants of B and C in scheme S2, e.g., $k_b = 2 \text{ s}^{-1}$ and $k_c = 5 \text{ s}^{-1}$; for $[Na^+] < 300$ mM, we assume that k_A (see below) and k_{-B} are 0. For $[Na^+] =$ 600 mM, the following coefficients were used (s⁻¹): $k_b = 1$, $k_c = 0.8$, $k_A =$ 0.075, and $k_{-B} = 0.5$. The other coefficients were those shown in Fig. 6 for the appropriate Na⁺ concentration.³ This is equivalent to a situation where external K⁺ competes with Na⁺ in pools B and C, and by binding to the EP species in both pools, it speeds up dephosphorylation of K⁺-sensitive EP, as is generally accepted. After a short time, then, only pool A is left, and one might expect the slope of this slow dephosphorylation phase to correspond to $k_a + k_A$ (remember [Fig. 6] that for $[Na^+] = 20-300 \text{ mM}, k_a \approx 0.12 \text{ s}^{-1}$ and $k_{\rm A} = 0.7 - 1.2 \text{ s}^{-1}$). However, the observed slope (Figs. 2 and 3) corresponds in all cases to a rate coefficient of only 0.1 s⁻¹ and thus is close to k_a (and not $k_a + k_A$). This means that k_A must be drastically reduced by K⁺. We interpret this to show that K^+ reacts with the species in pool A (the ADP-sensitive EP) and blocks the translocation of Na⁺ from inside sites to outside sites (i.e., $k_{\rm A} = 0$ and we conclude that K⁺ has very much the same effect as Tris⁺ on this step (see above). This effect of K^+ on k_A was unexpected, but a survey of the literature for the relatively few K⁺ dephosphorylation curves revealed that this may not have been a unique observation, although it has not really been commented on before. Thus, with enzyme preparations from different sources, Kuriki and Racker (1976), Foster and Ahmed (1977), Fukushima and Nakao (1980, 1981) (with Ca²⁺ phosphoenzyme), and Hara and Nakao (1981) all demonstrated that dephosphorylation with CDTA (or ATP) + K^+ is biphasic and that the slope of the second, slow phase is comparable to that of the dephosphorylation curves in the absence of K^+ , as observed in the present paper (Figs. 1–3; note that k_a , k_b , and k_c are of the same magnitude; Fig. 6). We should like further to emphasize that the rate constant for the decay of the second component of the ATP + K^+ curve is independent of Na⁺ and Tris⁺ (this paper), and therefore, like k_a , it is probably not influenced by Na⁺ on outside sites. The implications of these findings for the reaction mechanism of Na- and Na,K-ATPase are discussed below.

³ Under these circumstances the curves are simulated equally well by assuming that k_b and k_c , or k_b and k_c , or k_b and k_{-C} are large. In all three cases B and C will disappear rapidly.

Are the Phosphointermediates of the Na-ATPase Cycle Common to Both the Na-ATPase and the Na,K-ATPase Cycles?

In a recent paper (Plesner et al., 1981), we addressed this question and arrived at a negative answer. The arguments were based on a kinetic analysis using the classic two-pool model, as well as a critical review of the papers by Mårdh and his colleagues (for references, see Plesner et al., 1981). In our opinion, the experiments discussed in the preceding section clearly indicate that at least the EP species of pool A (classic E_1P or ADP-sensitive EP) cannot be intermediates of the Na,K-ATPase cycle: according to what has been said above, the rate of metabolism of A in the presence of 20 mM K⁺ in steady



FIGURE 10. Directly measured Na-ATPase activity with 1 mM ATP (O) and Na,K-ATPase activity (Δ) with 1 mM ATP, 20 mM K⁺, and the Na⁺ concentrations shown (t = 0-1°C; circumstances correspond to type 3 experiments). The dotted line represents the calculated maximal Na,K-ATPase activity under these conditions, assuming that at steady state (a) almost 100% of the enzyme is located in pool A (scheme S2, Fig. 8) and (b) that the rate constant for the metabolism of pool A is close to k_a under these conditions. See above for a discussion regarding the discrepancy between the measured (Δ) and the calculated (--) maximum Na,K-ATPase activity.

state is close to $k_a \cdot [A]_o$, and this must be equal to the rate of P_i production (ATP hydrolysis) via the intermediates of the scheme in Fig. 8. Since $[A]_o$ cannot exceed $[E]_{tot}$, the calculated, maximal rate of ATP hydrolysis is $k_a \cdot [E]_{tot}$. When the ATPase activity is measured with or without K⁺ (Fig. 10), it appears that 20 mM K⁺ at all Na⁺ concentrations almost doubles the activity. However, the maximum Na,K-ATPase activity, calculated as described, is clearly lower than that measured at most Na⁺ concentrations. The difference between the measured and the calculated Na,K-ATPase activity becomes even more pronounced if one takes into account that the steady state value

of $[EP]_{tot}$ in the presence of 20 mM K⁺, and therefore of $[A]_o$, is definitely lower than $[E]_{tot}$, as demonstrated, for instance, by Klodos and Nørby (1979).

It is thus obvious that the hydrolysis of ATP under these conditions (with K^+) proceeds via other intermediates than those represented in Fig. 8. This strongly argues against the commonly accepted Post-Albers scheme (Post et al., 1972; Karlish et al., 1978), in which the intermediates of Na-ATPase are also intermediates in the presence of K^+ (Na,K-ATPase activity), and it supports our earlier notion that the two types of ATP hydrolysis proceed via separate cycles (Plesner et al., 1981).

It remains to be discussed by which mechanism K^+ might block the conversion of A to B. To do this, K^+ must react with one or more of the EP's of pool A, but since the effect of (20 mM) K^+ is completely independent of $[Na^+]$ from 20 to almost 600 mM (Fig. 2) and of $[Tris^+]$ (Fig. 3), it is unlikely that K^+ binds to a Na⁺ or Tris⁺ site in pool A. It has been shown that low external K^+ even at high external Na⁺ will inhibit Na:Na exchange (Garrahan and Glynn, 1967*a*, *b*; De Weer et al., 1979) and the ATP hydrolysis associated with uncoupled Na⁺ efflux (Glynn and Karlish, 1976). This might indicate binding to external sites in pool A, but it could just as well be a result of a competition between Na⁺ and K⁺ in pool B and a subsequent accumulation of E_2K (Glynn and Karlish, 1976).

One hypothesis, purely speculative, regarding the effect of K⁺, is that K⁺ binds to a high-affinity, external K⁺ site on the E_1P species of pool A (is this the site that later becomes the high-affinity external Na⁺ site? see above), and by sitting there it blocks the A \rightarrow B conversion by preventing the movement of Na⁺ from the inside sites (through a channel?) to the outside sites.

Concluding Remarks

The model presented in scheme S2 and Fig. 8 has a necessary and sufficient number of reaction steps to explain most, if not all, the properties of Na,K-ATPase known to involve the acid-stable phosphorylated intermediates. In the light of the foregoing discussion, we want especially to emphasize the following points.

First, the phosphorylated intermediates are distributed among three major pools (and not just the classic E_1P and E_2P pools), each consisting of EP complexes which are in rapid equilibrium. The EP species of pool A have Na⁺ bound to two or three (probably internal) high-affinity sites, whereas the EP's of pools B and C are characterized by a binding of Na⁺ to three (probably external) low-affinity sites. A simultaneous effect of Na⁺ on internal and external sites is thus not a feature of our model. It is noteworthy that Na⁺ is translocated before the (presumably slow) major conformation change (from E_1P to E_2P). Second, at 100–600 mM Na⁺ (in the absence of K⁺ and Tris⁺), the rate coefficients for the interconversion $A \rightleftharpoons B$ are one order of magnitude higher than those for the $B \rightleftharpoons C$ interconversion and for dephosphorylation. This might allow for a ratio of ~10:1 or larger between the rate of Na:Na exchange and ATP hydrolysis. Third, pool A reacts rapidly with ADP (is ADP sensitive), and at relatively high [Na⁺] also a part of pool B will disappear upon addition of ADP, because of the relatively fast $A \rightleftharpoons B$ interconversion (see above). Fourth, we suggest that the most likely explanation of the inhibitory effect of low external [Na⁺] on (uncoupled) Na⁺ efflux and on ATP:ADP exchange is the existence of a high-affinity, external Na⁺ site on the E₂P of pool C. This site might be one of the three Na sites on E₂P. Fifth, Tris⁺ has dramatic effects: it blocks the A \rightarrow B conversion and reduces drastically the dephosphorylation rate of B and C. Finally, whereas pools B and C are both rapidly dephosphorylated after addition of K⁺ to the medium, the dephosphorylation of A is not affected, but its conversion to B is apparently blocked. Furthermore, the calculated rate of ATP hydrolysis in the presence of K⁺ is considerably smaller than the observed and we conclude that the EP species in pool A are only intermediates of the Na-ATPase but not of the Na,K-ATPase activity.

APPENDIX

Derivation of the Relationship of the Rate Coefficients of the Three-Pool Model (S2) to the Rate Constants of the Comprehensive Model (Fig. 8), $[Na^+]$, and $[Tris^+]$

The derivation of these relationships is performed under the assumption (see also legend to Fig. 8) that (a) there is equilibrium within the pools and (b) the site affinity constant within a pool is independent of the degree of occupancy by sodium and independent of the presence of Tris⁺. The Na⁺-site affinity constants are α , β , and γ in pools A, B, and C, respectively. Furthermore, Tris⁺ binds to a separate Tris⁺ site with the same affinity to all species in a pool, the binding constants being ϵ_A , ϵ_B , and ϵ_C for the three pools. As discussed in the main text, it is necessary for obtaining a good fit of the Tris data to assume that Na⁺ competes with Tris⁺ on the Tris site, but that only the presence of Tris⁺ on the site has effect. The binding constants for Na⁺ to that site are ρ_A , ρ_B , and ρ_C .

Experiments with Na⁺ Alone (No Tris⁺)

By definition, [A] = [A2] + [A'2] + [A3] + [A'3], and the rate of dephosphorylation of pool A is

$$k_{a}[\mathbf{A}] = k_{a2}[\mathbf{A}2] + k_{a'2}[\mathbf{A}'2] + k_{a3}[\mathbf{A}3] + k_{a'3}[\mathbf{A}'3].$$

Using the equilibrium constants in Fig. 8 and the binding constant, α , defined above, we get

$$k_a = \frac{(k_{a2} + k_{a'2} \cdot K_{A2}) + (k_{a3} + k_{a'3} \cdot K_{A3})\alpha[\mathrm{Na}^+]}{(1 + K_{A2}) + (1 + K_{A3}) \cdot \alpha \cdot [\mathrm{Na}^+]}.$$

This equation can be rearranged to

$$k_{a} = \frac{\frac{(k_{a2} + k_{a'2} \cdot K_{A2})}{1 + K_{A2}} + \frac{(k_{a3} + k_{a'3} \cdot K_{A3})}{1 + K_{A3}} \cdot \alpha'[\text{Na}^{+}]}{1 + \alpha'[\text{Na}^{+}]}$$
(1A)

$$k_a = \frac{k'_{a2} + k'_{a3} \cdot \alpha' [\text{Na}^+]}{1 + \alpha' [\text{Na}^+]},$$
(2A)

where α' is an "apparent" affinity:

$$\alpha' = \alpha \cdot \frac{1 + K_{\Lambda 3}}{1 + K_{\Lambda 2}} \tag{3A}$$

and the meaning of the apparent rate constants k'_{a2} and k'_{a3} is evident from comparison of Eqs. 1A and 2A. Using the same line of reasoning,

$$k_{\rm A} = \frac{k_{\rm A2} + k_{\rm A3} \cdot \alpha \cdot [\rm Na^+]}{(1 + K_{\rm A2}) + (1 + K_{\rm A3})\alpha[\rm Na^+]}; \tag{4A}$$

$$k_{\rm A} = \frac{k'_{\rm A2} + k'_{\rm A3} \cdot \alpha' \cdot [\rm Na^+]}{1 + \alpha' [\rm Na^+]},$$
(5A)

where α' is defined in Eq. 3A and k'_{A2} and k'_{A3} are apparent constants equal to $k_{A2}/(1 + K_{A2})$ and $k_{A3}/(1 + K_{A3})$.

By similar arguments we can write the equations for the other five rate coefficients of scheme S2:

$$k_{j} = \frac{k_{j0} + k_{j1} \cdot 3\beta[Na^{+}] + k_{j2} \cdot 3\beta^{2}[Na^{+}]^{2} + k_{j3} \cdot \beta^{3}[Na^{+}]^{3}}{(1 + \beta[Na^{+}])^{3}},$$
(6A)

where j = b, -B, or B and, similarly,

$$k_{\rm n} = \frac{k_{\rm n0} + k_{\rm n1} \cdot 3\gamma [\rm Na^+] + k_{\rm n2} \cdot 3\gamma^2 [\rm Na^+]^2 + k_{\rm n3} \cdot \gamma^3 [\rm Na^+]^3}{(1 + \gamma [\rm Na^+])^3},$$
(7A)

where n = c or -C.

Experiments with Na⁺ and Tris⁺

The rate coefficients with Tris⁺ bear the extra subscript T, e.g., k_{BT} , k_{B2T} , etc. According to the assumptions laid out in the first paragraph of this appendix, and taking pool B as an example for the method of deriving the Tris rate coefficients, we can write

$$[B] = [B0](1 + \beta Na)^{3}(1 + \rho_{B}[Na^{+}] + \epsilon_{B}[Tris^{+}]).$$

If we also make the simple assumption that the rate constant for a particular type of reaction is changed by the same factor for all species involved, e.g., $k_{B3T} = f_B \cdot k_{B3}$, $k_{B2T} = f_B \cdot k_{B2}$, or $k_{b3T} = f_b \cdot k_{b3}$ and $k_{b2T} = f_b \cdot k_{b2}$, it is easy to show that, for example,

$$k_{\rm BT} = k_{\rm B} \cdot \frac{1 + \rho_{\rm B}[\rm Na^+] + f_{\rm B} \cdot \epsilon_{\rm B}[\rm Tris^+]}{1 + \rho_{\rm B}[\rm Na^+] + \epsilon_{\rm B}[\rm Tris^+]}; \tag{8A}$$

$$k_{bT} = k_b \cdot \frac{1 + \rho_{\rm B}[{\rm Na}^+] + f_b \cdot \epsilon_{\rm B}[{\rm Tris}^+]}{1 + \rho_{\rm B}[{\rm Na}^+] + \epsilon_{\rm B}[{\rm Tris}^+]}.$$
(9A)

Analogous expressions for the effect of Tris⁺ on k_a , k_A , k_{-B} , k_{-C} , and k_c have exactly the same form. An explanatory note: if f = 1, Tris⁺ is obviously without effect. Since the Tris⁺ coefficients of the three-pool model are always equal to or lower than those in the absence of Tris⁺, f is always between 1 and 0.

The authors wish to thank Mrs. Inge Raungaard for her excellent technical assistance, and Dr. Robert B. Gunn, Department of Physiology, Emory University, Atlanta, GA, for his help and

755

critical assessment of the manuscript. Thanks are also due to Adrienne L. McLean for typing this article.

This work was supported in part by grants 512-10806, 512-21027, and 12-3556 from The Danish Medical Research Council.

Received for publication 14 January 1983 and in revised form 3 June 1983.

REFERENCES

Albers, R. W. 1967. Biochemical aspects of active transport. Annu. Rev. Biochem. 36:727-756.

- Beaugé, L. A., and E. D. Campillo. 1976. The ATP dependence of an ouabain-sensitive sodium efflux activated by external sodium, potassium and lithium in human red cells. *Biochim. Biophys. Acta.* 433:547-554.
- Beaugé, L. A., and I. M. Glynn. 1979. Sodium ions, acting at high-affinity extracellular sites, inhibit sodium-ATPase activity of the sodium pump by slowing dephosphorylation. *J. Physiol.* (*Lond.*). 289:17-31.
- Blostein, R. 1970. Sodium-activated adenosine triphosphatase activity of the erythrocyte membrane. J. Biol. Chem. 245:270-275.
- Blostein, R. 1979. Side-specific effects of sodium on Na,K-ATPase. Studies with inside-out red cell membrane vesicles. J. Biol. Chem. 254:6673-6677.
- Cantley, L. C. 1981. Structure and mechanism of the Na,K-ATPase. Curr. Top. Bioenerg. 11:201-237.
- Cavieres, J. D., and J. C. Ellory. 1975. Allosteric inhibition of the Na-pump by external Na. *Nature (Lond.)*. 255:338-340.
- Cavieres, J. D., and I. M. Glynn. 1979. Sodium-sodium exchange through the sodium pump: the roles of ATP and ADP. J. Physiol. (Lond.). 297:637-645.
- De Weer, P., B. G. Kennedy, and R. F. Abercrombie. 1979. Relationship between the Na:K exchanging and Na:Na exchanging modes of operation of the sodium pump. *In* Na,K-ATPase: Structure and Kinetics. J. C. Skou and J. G. Nørby, editors. Academic Press, Inc., London. 503-515.
- Forgac, M., and G. Chin. 1982. Na⁺ transport by the (Na⁺)-stimulated adenosine-triphosphatase. J. Biol. Chem. 257:5652-5655.
- Foster, D., and K. Ahmed. 1977. Solvent effects on hydrolysis of the phosphoenzyme intermediate in sodium- and potassium-dependent adenosine triphosphatase: correlation and stimulation of potassium-dependent *p*-nitrophenyl phosphatase. *Mol. Pharmacol.* 13:142–149.
- Fukushima, Y., and M. Nakao. 1980. Changes in affinity of Na⁺- and K⁺-transport ATPase for divalent cations during its reaction sequence. J.Biol. Chem. 255:7813-7819.
- Fukushima, Y., and M. Nakao. 1981. Transient state in the phosphorylation of sodium- and potassium-transport adenosine triphosphatase by adenosine triphosphate. J. Biol. Chem. 256:9136-9143.
- Garay, R. P., and P. J. Garrahan. 1973. The interaction of sodium and potassium with the sodium pump in red cells. J. Physiol. (Lond.). 231:297-325.
- Garay, R. P., and P. J. Garrahan. 1979. The effect of external Na⁺ on the different types of Na⁺ extrusion catalyzed by the Na-pump in human red cells. *In* Na,K-ATPase: Structure and Kinetics. J. C. Skou, and J. G. Nørby, editors. Academic Press, Inc., London. 247–259.
- Garrahan, P. J., and R. P. Garay. 1974. A kinetic study of the Na pump in red cells. Its relevance to the mechanism of active transport. Ann. NY Acad. Sci. 242:445-458.
- Garrahan, P. J., and R. P. Garay. 1976. The distinction between sequential and simultaneous models for sodium and potassium transport. Curr. Top. Membr. Transp. 8:29-97.

- Garrahan, P. J., and I. M. Glynn. 1967a. The behavior of the sodium pump in red cells in the absence of external potassium. J. Physiol. (Lond.). 192:159-174.
- Garrahan, P. J., and I. M. Glynn. 1967b. Factors affecting the relative magnitude of the sodium:potassium and sodium:sodium exchanges catalyzed by the sodium pump. J. Physiol. (Lond.). 192:189-216.
- Garrahan, P. J., and I. M. Glynn. 1967c. The stoichiometry of the sodium pump. J. Physiol. (Lond.). 192:217-235.
- Garrahan, P. J., A. Horenstein, and A. F. Rega. 1979. The interaction of ligands with the Na,K-ATPase during Na-ATPase activity. *In* Na,K-ATPase: Structure and Kinetics. J. C. Skou, and J. G. Nørby, editors. Academic Press, Inc., London. 261-274.
- Glynn, I. M., and J. F. Hoffman. 1971. Nucleotide requirements for sodium-sodium exchange catalyzed by the sodium pump in human red cells. J. Physiol. (Lond.). 218:239–256.
- Glynn, I. M., J. F. Hoffman, and V. L. Lew. 1971. Some "partial reactions" of the sodium pump. *Philos. Trans. R. Soc. Lond. B Biol. Sci.* 262:91-102.
- Glynn, I. M., and S. J. D. Karlish. 1976. ATP hydrolysis associated with an uncoupled sodium flux through the sodium pump: evidence for allosteric effects of intracellular ATP and extracellular sodium. *J. Physiol. (Lond.)*. 256:465–496.
- Glynn, I. M., and V. L. Lew. 1970. Synthesis of adenosine triphosphate at the expense of downhill cation movements in intact human red cells. J. Physiol. (Lond.). 207:393-402.
- Glynn, I. M., V. L. Lew, and U. Lüthi. 1970. Reversal of the potassium entry mechanism in red cells, with and without reversal of the entire pump cycle. J. Physiol. (Lond.). 207:371-391.
- Hara, Y., and M. Nakao. 1981. Sodium ion discharge from pig kidney Na,K-ATPase. Na⁺-dependency of the E1P E2P equilibrium in the absence of KCl. J. Biochem. (Tokyo). 90:923–931.
- Hearon, J. Z., S. A. Bernhard, S. L. Friess, D. J. Botts, and M. F. Morales. 1959. Enzyme kinetics. *In* The Enzymes. P. D. Boyer, H. Lardy, and K. Myrbäck, editors. Academic Press, Inc., New York. 1:49-142.
- Hegyvary, C. 1976. Ouabain-binding and phosphorylation of Na,K-ATPase treated with *N*-ethylmaleimide or oligomycin. *Biochim. Biophys. Acta.* 422:365–379.
- Jensen, J., J. G. Nørby, and P. Ottolenghi. 1984. Sodium and potassium binding to the sodium pump of pig kidney: stoichiometry and affinities evaluated from nucleotide-binding behaviour. J. Physiol. (Lond.). In press.
- Jensen, J., and P. Ottolenghi. 1983. Binding of Rb⁺ and ADP to a potassium-like form of Na,K-ATPase. Curr. Top. Membr. Transp. 19:223-227.
- Jørgensen, P. L. 1982. Mechanism of the Na⁺,K⁺ pump. Protein structure and conformations of the pure Na,K-ATPase. *Biochim. Biophys. Acta.* 694:27-68.
- Jørgensen, P. L., and S. J. D. Karlish. 1980. Defective conformational response in a selectively trypsinized Na,K-ATPase studied with tryptophan fluorescence. *Biochim. Biophys. Acta.* 597:305-317.
- Kaplan, J. H. 1982. Sodium pump-mediated ATP:ADP exchange. The sided effects of sodium and potassium ions. J. Gen. Physiol. 80:915-937.
- Kaplan, J. H., and R. J. Hollis. 1980. External Na dependence of ouabain-sensitive ATP:ADP exchange initiated by photolysis of intracellular caged-ATP in human red cell ghosts. *Nature* (Lond.). 288:587-589.
- Karlish, S. J. D., and I. M. Glynn. 1974. An uncoupled efflux of sodium ions from human red cells, probably associated with Na-dependent ATPase activity. Ann. NY Acad. Sci. 242:461– 470.

- Karlish, S. J. D., and V. Pick. 1981. Sidedness of the effects of sodium and potassium ions on the conformational state of the sodium-potassium pump. J. Physiol. (Lond.). 312:505-529.
- Karlish, S. J. D., D. W. Yates, and I. M. Glynn. 1978. Conformational transitions between Na⁺bound and K⁺-bound forms of Na,K-ATPase, studied with formycin nucleotides. *Biochim. Biophys. Acta.* 525:252-264.
- Klodos, I., and J. G. Nørby. 1979. Effect of K⁺ and Li⁺ on intermediary steps in the Na,K-ATPase reaction. In Na,K-ATPase: Structure and Kinetics. J. C. Skou and J. G. Nørby, editors. Academic Press, Inc., London. 331-342.
- Klodos, I., J. G. Nørby, and N. O. Christiansen. 1983. Three (at least) consecutive phosphointermediates of Na-ATPase. Curr. Top. Membr. Transp. 19:573–576.
- Klodos, I., J. G. Nørby, and I. W. Plesner. 1981. The steady-state mechanism of ATP hydrolysis catalyzed by membrane-bound Na,K-ATPase from ox brain. II. Kinetic characterization of phosphointermediates. *Biochim. Biophys. Acta*. 643:463–482.
- Klodos, I., P. Ottolenghi, and A. A. Boldyrev. 1975. Large-scale preparation of Na,K-ATPase from ox brain. *Anal. Biochem.* 67:397-403.
- Kuriki, Y., and E. Racker. 1976. Inhibition of (Na⁺,K⁺) adenosine triphosphatase and its partial reactions by quercetin. *Biochemistry*. 15:4951–4956.
- Lee, K. H., and R. Blostein. 1980. Red cell sodium fluxes catalyzed by the sodium pump in the absence of K⁺ and ADP. *Nature (Lond.)*. 285:338–339.
- Lew, V. L., M. A. Hardy, and J. C. Ellory. 1973. The uncoupled extrusion of Na⁺ through the Na⁺ pump. *Biochim. Biophys. Acta.* 323:251-266.
- Lindberg, O., and L. Ernster. 1956. Determination of organic phosphorous compounds by phosphate analysis. *Methods Biochem. Anal.* 3:1-22.
- Mårdh, S., and R. L. Post. 1977. Phosphorylation from adenosine triphosphate of sodium and potassium-activated adenosine triphosphatase. Comparison of enzyme-ligand complexes as precursors to the phosphoenzyme. J. Biol. Chem. 252:633–638.
- Nørby, J. G. 1983. Ligand interactions with the substrate site of Na,K-ATPase: nucleotides, vanadate and phosphorylation. Curr. Top. Membr. Transp. 19:281-314.
- Nørby, J. G., and J. Jensen. 1971. Binding of ATP to brain microsomal ATPase. Determination of the ATP-binding capacity and the dissociation constant of the enzyme-ATP complex as a function of K⁺ concentration. *Biochim. Biophys. Acta.* 233:104–116.
- Nørby, J. G., and I. Klodos. 1982. The phosphorylated intermediates of Na,K-ATPase. The role of Na⁺ and K⁺ in their interconversion and hydrolysis. *EBEC (Eur. Bioenerg. Conf.) Rep.* LBTM-CNRS edition. 2:35-36.
- Ottolenghi, P. 1975. The reversible delipidation of a solubilized sodium-plus-potassium iondependent adenosine triphosphatase from the salt gland of the spiny dogfish. *Biochem. J.* 151:61-66.
- Plesner, L., and I. W. Plesner. 1981a. The steady-state kinetic mechanism of ATP hydrolysis catalyzed by membrane-bound Na,K-ATPase from ox brain. I. Substrate identity. *Biochim. Biophys. Acta.* 643:449-462.
- Plesner, L., and I. W. Plesner. 1981b. The steady-state kinetic mechanism of ATP hydrolysis catalyzed by membrane-bound Na,K-ATPase from ox brain. IV. Rate constant determination. Biochim. Biophys. Acta. 648:231-246.
- Plesner, I. W., L. Plesner, J. G. Nørby, and I. Klodos. 1981. The steady-state kinetic mechanism of ATP hydrolysis catalyzed by membrane-bound Na,K-ATPase from ox brain. III. A minimal model. *Biochim. Biophys. Acta*. 643:483-494.
- Post, R. L., C. Hegyvary, and S. Kume. 1972. Activation by adenosine triphosphate in the

phosphorylation kinetics of sodium and potassium ion transport adenosine triphosphatase. J. Biol. Chem. 247:6530-6540.

- Post, R. L., K. Taniguchi, and G. Toda. 1974. Synthesis of adenosine triphosphate by Na, K-ATPase. Ann. NY Acad. Sci. 242:80-91.
- Post, R. L., G. Toda, S. Kume, and K. Taniguchi. 1975. Synthesis of adenosine triphosphate by way of potassium-sensitive phosphoenzyme of sodium, potassium adenosine triphosphatase. J. Supramol. Struct. 3:479-487.
- Robinson, J. D., and M. S. Flashner. 1979. The (Na⁺ + K⁺)-activated ATPase. Enzymatic and transport properties. *Biochim. Biophys. Acta.* 549:145–176.
- Sachs, J. R. 1970. Sodium movements in the human red blood cell. J. Gen. Physiol. 56:322-341.
- Sachs, J. R. 1980. The order of release of sodium and addition of potassium in the sodiumpotassium pump reaction mechanism. J. Physiol. (Lond.). 302:219-240.
- Skou, J. C. 1957. The influence of some cations on an adenosine triphosphatase from peripheral nerves. *Biochim. Biophys. Acta.* 23:394–401.
- Skou, J. C. 1965. Enzymatic basis for active transport of Na⁺ and K⁺ across cell membranes. *Physiol. Rev.* 45:596–617.
- Skou, J. C. 1974. Effect of ATP on the intermediary steps of the reaction of the (Na⁺ + K⁺)dependent enzyme system. III. Effect on the *p*-nitrophenylphosphatase activity of the system. *Biochim. Biophys. Acta.* 339:258–273.
- Skou, J. C. 1975. The (Na⁺ + K⁺) activated enzyme system and its relationship to transport of sodium and potassium. Q. Rev. Biophys. 7:401–434.
- Skou, J. C. 1979. Effect of ATP on the intermediary steps of the reaction of the $(Na^+ + K^+)$ -dependent enzyme system. IV. Effect of ATP on $K_{0.5}$ for Na⁺ and on hydrolysis at different pH and temperature. *Biochim. Biophys. Acta.* 567:421-435.
- Skou, J. C., and M. Esmann. 1980. Effects of ATP and protons on the Na:K selectivity of the Na,K-ATPase studied by ligand effects on intrinsic and extrinsic fluorescence. *Biochim. Biophys. Acta.* 601:386-402.
- Taniguchi, K., and R. L. Post. 1975. Synthesis of ATP and exchange between inorganic phosphate and ATP in sodium and potassium transport ATPase. J. Biol. Chem. 250:3010-3018.
- Tobin, T., T. Akera, S. I. Baskin, and T. M. Brody. 1973. Calcium ion and sodium- and potassium-dependent adenosine triphosphatase: its mechanism of inhibition and identification of the E1-P intermediate. *Mol. Pharmacol.* 9:336–349.
- Whittam, R., and A. R. Chipperfield. 1975. The reaction mechanism of the sodium pump. *Biochim. Biophys. Acta.* 415:149-171.
- Wildes, R. A., H. J. Evans, and J. Chiu. 1973. Effects of cations on the adenosine diphosphateadenosine triphosphate exchange catalyzed by rat brain microsomes. *Biochim. Biophys. Acta.* 307:162-168.
- Yoda, A., and S. Yoda. 1982. Formation of ADP-sensitive phosphorylated intermediates in the electric eel Na, K-ATPase preparation. *Mol. Pharmacol.* 22:693-699.