

Additional file 1:

We describe our model formulation in terms of the malaria data set. Thus, let n_{itsk} denote the sum of weeks at risk of the children in each neighbourhood i ($i=1, \dots, 115$) during the period t ($t=1,2,3$) and climate season s ($s=1,2$) for a specific age group k ($k=1,2$). We assume that the number of new malaria cases per week Y_{itsk} in each neighbourhood i during the period t and climate season s and age group k has a Poisson distribution with mean $n_{itsk} \exp(\mu_{itsk})$.

The non-spatial model is defined as:

$$\log(\mu_{itsk}) = \log(n_{itsk}) + \beta_0 + \beta_t + \beta_s + \beta_{ts} + \beta_k$$

where β_t is the effect of period t , β_s , is the climate season effect, β_{ts} is the period t effect at climate season s , and β_k is the age group effect.

In the spatial model, the regional random effects b_i is incorporated into the linear predicted, thus, $\log(\mu_{itsk})$ is defined as:

$$\log(\mu_{itsk}) = \log(n_{itsk}) + \beta_0 + \beta_t + \beta_s + \beta_{ts} + \beta_k + b_i$$

For this spatial structured component, we chose a simple Gaussian intrinsic auto regression.

Thus, the conditional distribution of b_i is

$$b_i | \mathbf{b}_{-i} \sim N\left(\bar{\mathbf{b}}_i, \sigma_b^2 \mathbf{m}_i\right)$$

where $\bar{\mathbf{b}}_i$ is the corresponding mean value over the m_i neighbourhoods that are geographically contiguous to i and σ_b^2 is a spatial variance parameter.

The exponential of the regional random effects (e^{b_i}) is the neighbourhood-specific adjusted relative risk.

The spatial+ non structured model, is that which includes the regional random effects prior to b_i , and other regional random effects without spatial structure, θ_i . It is assumed that

$\theta_i \sim N(0, \sigma_\theta^2)$ where σ_θ^2 is the non-structured variance. Thus, $\log(\mu_{itsk})$ is defined as:

$$\mathbf{log}(\boldsymbol{\mu}_{it\text{sk}}) = \mathbf{log}(\mathbf{n}_{it\text{sk}}) + \beta_0 + \beta_t + \beta_s + \beta_{ts} + \beta_k + \mathbf{b}_i + \theta_i$$

Finally, in the spatial-seasonal model, the regional random effect is nested within climate season. This effect is written as $\mathbf{b}_i^{(s)}$. That is, $\mathbf{b}_i^{(s)}$ is a random effect for the i th region in climate season s .

For this spatial structured component, we also chose a simple Gaussian intrinsic auto regression. Thus, the conditional distribution of $\mathbf{b}_i^{(s)}$ is

$$\mathbf{b}_i^{(s)} | \mathbf{b}_{-i}^{(s)} \sim \mathbf{N} \left(\bar{\mathbf{b}}_i^{(s)}, \sigma_{\mathbf{b}^{(s)}}^2 \mathbf{m}_i \right)$$

where $\bar{\mathbf{b}}_i^{(s)}$ is the corresponding mean value for the climate season s over the m_i neighbourhoods that are geographically contiguous to i and $\sigma_{\mathbf{b}^{(s)}}^2$ is a spatial variance parameter for the climate season s . In this situation $\mathbf{log}(\boldsymbol{\mu}_{it\text{sk}})$ is defined as:

$$\mathbf{log}(\boldsymbol{\mu}_{it\text{sk}}) = \mathbf{log}(\mathbf{n}_{it\text{sk}}) + \beta_0 + \beta_t + \beta_s + \beta_{ts} + \beta_k + \mathbf{b}_i^{(s)}$$