

Supplementary methods

Center of rotation

It might seem intuitive to calculate the translation from $|\mathbf{t}|$, the displacement of c_S , the center of mass of S. However, except for translation parallel to \mathbf{u} , \mathbf{t} may arise from rotation about a physically meaningful axis that does not pass through c_S . We define an axis as physically meaningful if this axis passes near the interface between L and S, that is, the residues that define the 6 Å contacts between L and S. We define an axis as passing near a set of residues if the C_α atom of any residue in the set is no more than 5.0 Å from the axis. To assess this, we first find a center of rotation c_R , such that the motion can be described as a rotation by θ about \mathbf{u} , centered at c_R , and a translation T_u parallel to \mathbf{u} .

To do this, we first find the basis vectors \mathbf{e}_x , \mathbf{e}_y , and \mathbf{e}_z of a right-handed orthogonal coordinate system centered at c_R describing the counterclockwise motion from state A to state B. Let s_1 and s_2 be the centers of S_A and S'_B , and let \mathbf{s} be the vector between the two centers. Let $\mathbf{e}_z = \mathbf{u}$, and let \mathbf{e}_x lie in a plane defined by \mathbf{e}_z and the midpoint of \mathbf{s} such that s_1 and s_2 are in the $(\mathbf{e}_x, -\mathbf{e}_y)$ and $(\mathbf{e}_x, \mathbf{e}_y)$ quadrants, respectively. Then, $\mathbf{e}_x = \text{unit}(\mathbf{s} \times \mathbf{e}_z)$, where $\text{unit}(\mathbf{v}) = \frac{\mathbf{v}}{|\mathbf{v}|}$, and $\mathbf{e}_y = \mathbf{e}_z \times \mathbf{x}$.

Then, we find the distance of s_1 from the origin in the \mathbf{e}_y and \mathbf{e}_x directions. Since \mathbf{e}_x lies in a plane bisecting \mathbf{s} , s_1 is $y = \frac{1}{2}(\mathbf{s} \cdot \mathbf{e}_y)$ from the origin in the $-\mathbf{e}_y$ direction. Next, we triangulate to find x , the distance of s_1 from the origin in the \mathbf{e}_x direction:

$$x = \frac{y}{\tan\left(\frac{1}{2}\theta\right)}.$$

To find c_R , we simply extrapolate back:

$$c_R = s_1 - x\mathbf{e}_x + y\mathbf{e}_y.$$