

**Additional Table 3: The effect of increased false positive rate on t-test p-values.**

Alignment, Alphabet	p-value with (m,n) additional 1.0 scores in the $(i, i+4)$ and background distributions, respectively					
Tetrapod Myoglobin, charge_his.2	(0,0)	(1,82)	(10,820)	(20,1640)	(50,4100)	(100,8200)
	$5.6 \times 10^{-5}$	$0.5 \times 10^{-2}$	$2.6 \times 10^{-1}$	$3.0 \times 10^{-1}$	$3.5 \times 10^{-1}$	$3.6 \times 10^{-1}$
Chordate Myosin, orig	(0,0)	(1,539)	(10,5390)	(20,10780)	(50,26950)	(100,53900)
	$1.67 \times 10^{-6}$	$3.35 \times 10^{-6}$	$1.47 \times 10^{-4}$	$1.05 \times 10^{-3}$	$1.0 \times 10^{-2}$	$3.87 \times 10^{-2}$

To illustrate that methods with increased false positive rates achieve less significant p-values in the t-test-based analysis, for top performing method/alphabet combinations  $(i, i+4)$  score distributions are compared against background distributions, where both distributions have been modified to include additional high (i.e., positive) scores. False positives are added to both the coevolving and non-coevolving distributions, at the same rate. For example, when 1 false positive is added to the myoglobin  $(i, i+4)$ , 82 false positives are added to the background distribution because the background distribution contains 82 times more values than the  $(i, i+4)$  distribution. The additional high scores are analogous to extreme false positives (since the max value of 1.0 for NMI was added).