

Figure S1: *Direct validation of MIST MI approximation.* To evaluate the MIST framework, we simulated 100 randomly generated networks with analytically computable joint entropies and applied the metrics using a range of sample sizes. Half of each network was randomly chosen and the MI between one half and the other was computed analytically or using the MIST approximation of various orders. When the analytical entropies are known exactly (A), the higher-order approximations performing increasingly well. When the entropies are estimated from a finite sample, however (C–E), the approximations provide the best estimates, with the higher-order approximations performing better as more data become available. This behavior is quantified by computing the sum-of-squared error of each metric as a function of the sampling regime (B). The best approximation to use depends upon the amount of data available, but for all cases examined with finite sample size, the approximations outperform direct estimation and the second-order approximation provides a good estimate.

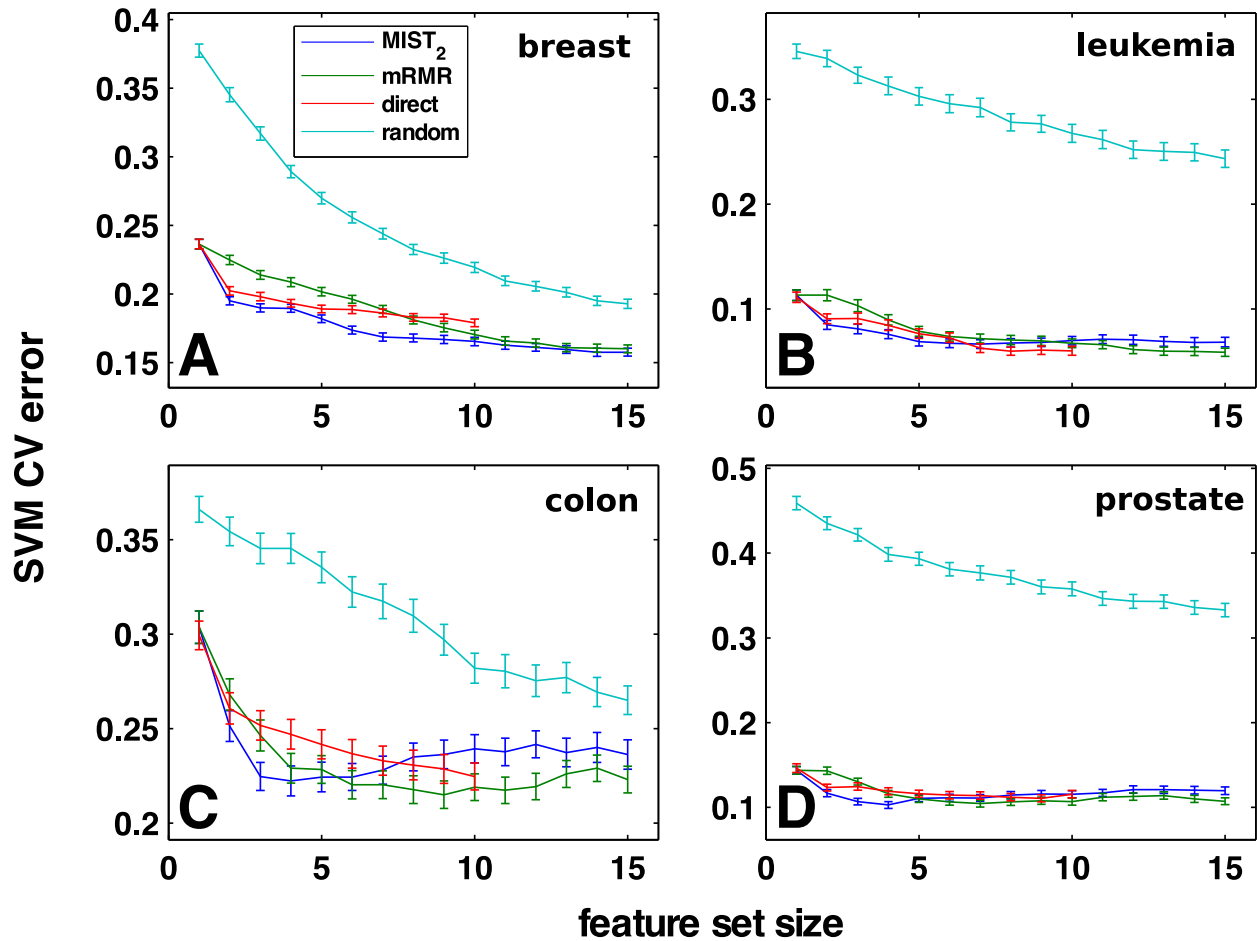


Figure S2: **Gene subset selection for cancer classification.** Subsets of gene expression levels were chosen incrementally to maximize the information content with the cancer class variable according to MIST₂, direct estimation of MI, mRMR, or at random and the chosen sets were scored by the cross-validation error of an SVM classifier trained to discriminate the cancer type. For all data sets, 75% of the data was separated and used to select features and train the model; the classifier was then used to classify the remaining 25% of the samples. The mean classification error and standard error of the mean for 200 such training/testing partitioning are reported. Genes were selected for data sets relating to (A) breast, (B) leukemia, (C) colon, and (D) prostate cancer.

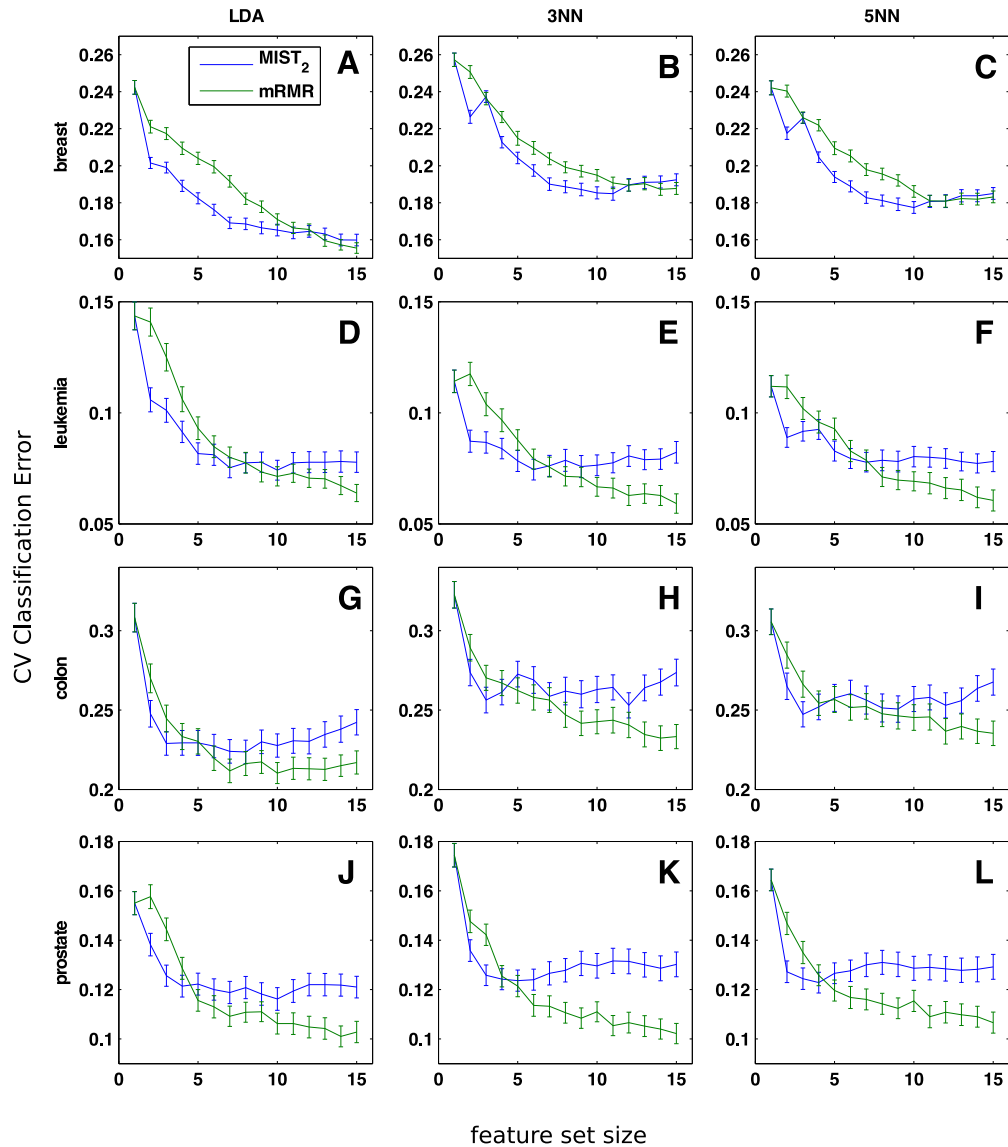


Figure S3: *Gene subset selection for cancer classification.* Subsets of gene expression levels were chosen incrementally to maximize the information content with the cancer class variable according to MIST₂ or mRMR and the chosen sets were scored by the cross-validation error of an LDA (A,D,G,J), 3NN (B,E,H,K), or 5NN (C,F,I,L) classifier trained to discriminate the cancer type. For all data sets, 75% of the data was separated and used to select features and train the model; the classifier was then used to classify the remaining 25% of the samples. The mean classification error and standard error of the mean for 200 such training/testing partitioning are reported. Genes were selected for four data sets relating to (A,B,C) breast, (D,E,F) leukemia, (G,H,I) colon, and (J,K,L) prostate cancer. Results using an SVM classifier and including direct estimation-based feature selection are shown in Figure 4.

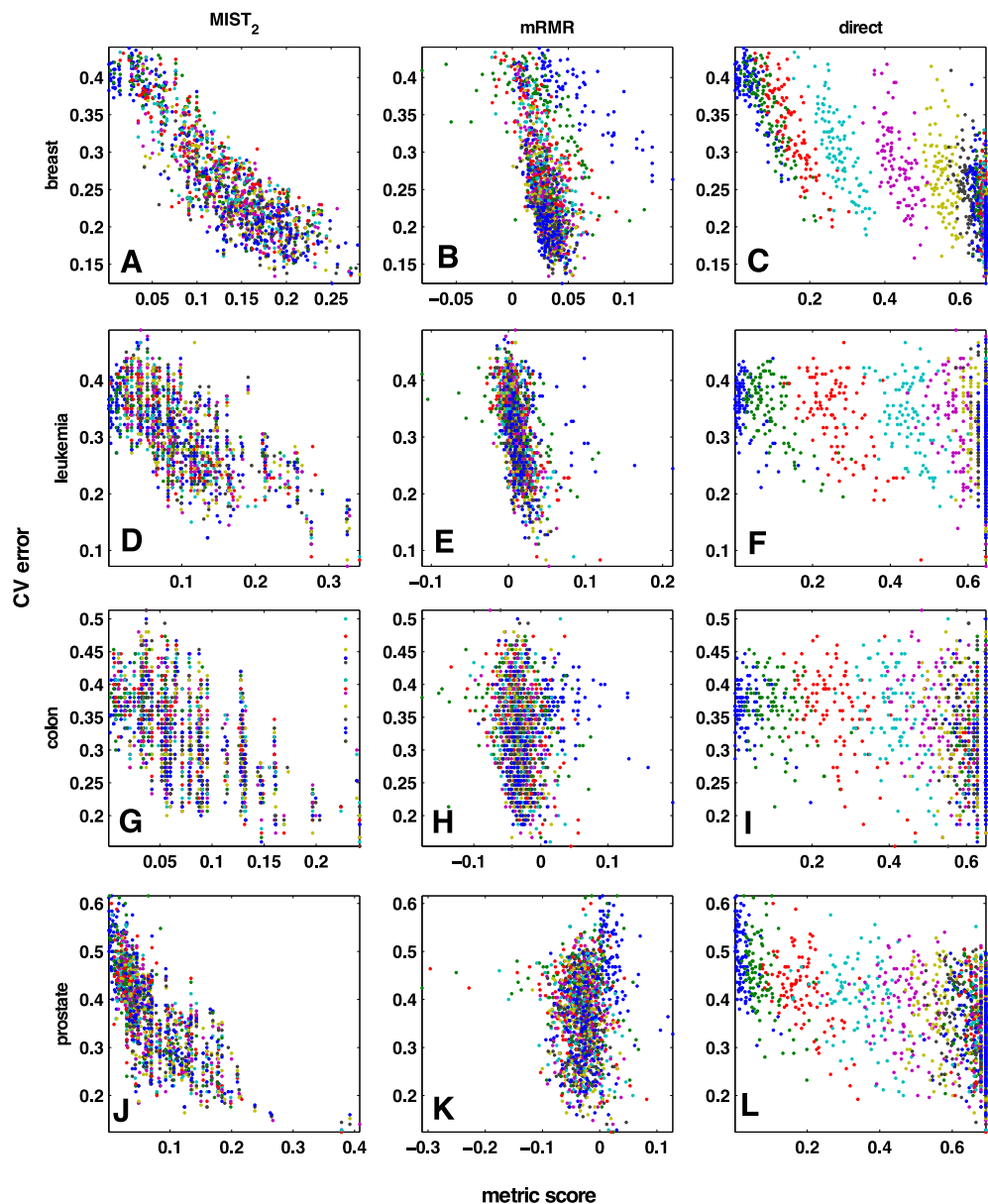


Figure S4: *Correlation of classification error and MI metrics.* The classification error of randomly chosen subsets of 1–15 genes was computed through cross-validation with an SVM based classifier. The same sets were then scored by MIST₂ (A,D,G,J), MI computed with direct estimation (B,E,H,K), and mRMR (C,F,I,L) and these metrics are shown plotted against the CV classification error. The color of the points relates to the size of the feature set, cycling through blue, green, red, cyan, magenta, yellow, black for increasing set size. The correlation coefficients between metrics as a function of set size is shown in Figure 3. Notably, MIST₂ has strong negative correlation across all feature set sizes.

Table S1: Microarray data sets for cancer classification

Tissue	# Samples	# Genes	Class Type	Ref
breast	295	70	good/bad prog	[24]
leukemia	72	7070	AML/ALL	[11]
colon	62	2000	normal/tumor	[2]
prostate	102	12600	normal/tumor	[20]

Table S2: Genes selected by MIST₂

Tissue	#	Gene ID	Reproduce %	Cancer Relevance	Other Studies
breast	1	NM_003981	91.0*	[17]	[14, 5, 21]
	2	AI918032	91.0*		[5]
	3	NM_003239	85.5*	[9]	[5]
	4	AW024884	52.0*		
	5	AA404325	68.5*		
	6	AF055033	77.0*		[5, 21]
	7	AW014921	77.0*		
	8	AL080059	49.5*		[26]
	9	AI738508	1.5		
	10	AK000745	17.0		
leukemia	1	M27891	33.0*		[10, 3, 6, 26, 4, 8]
	2	U29175	3.5*		[3, 8]
	3	U72621	19.0*	[1]	[3]
	4	U88047	7.5*		[8]
	5	M92287	24.0*	[19]	[3, 4, 8]
	6	M19507	2.0		[3, 6, 4, 8]
	7	D84294	0.5		
	8	HG3549-HT3751	6.5*		
	9	M32304	6.5*		[3]
	10	AF005043	1.0		
colon	1	M63391	22.0*	[7]	[3, 4, 8]
	2	U30825	3.5		[3, 8]
	3	T57468	4.5*		[8]
	4	T47377	21.5*		[3, 4, 8]
	5	M26383	19.0*		[3, 4, 8]
	6	R39209	24.5*		[8]
	7	M76378	5.5*		[3, 4, 8]
	8	M80815	3.0		[3, 8]
	9	Y00097	4.5*	[18]	
	10	X90858	1.0	[12]	[3]
prostate	1	X07732	90.0*	[13]	[6, 25, 22]
	2	U24577	33.0*		
	3	M62895	6.0*	[16]	
	4	U12472	14.0*		
	5	D80010	17.5*		
	6	AB014545	15.0*		
	7	AB023204	27.0*		
	8	U67615	23.5*		
	9	M21536	12.5*	[15]	
	10	AF038451	4.0*	[23]	

*Bonferroni adjusted $p \leq 0.01$ for gene occurring this often in 200 random 10-feature selection runs.

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