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**Supporting Material**

**Biophysically-Based Mathematical Modelling of Interstitial Cells of Cajal Slow Wave Activity Generated From a Discrete Unitary Potential Basis**

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**SLOW WAVE MODEL  
SUPPLEMENTARY MATERIALS**

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## **MODEL STATE VARIABLES**

### **Pacemaker Unit State Variables**

$C_{S1}$  – Subspace 1 [ $\text{Ca}^{2+}$ ]  
 $C_{S2}$  – Subspace 1 [ $\text{Ca}^{2+}$ ]  
 $C_{ER}$  – Endoplasmic Reticulum [ $\text{Ca}^{2+}$ ]  
 $C_{MT}$  – Mitochondrial [ $\text{Ca}^{2+}$ ]  
 $N_{S1}$  – Subspace 1 [ $\text{Na}^+$ ]  
 $H$  –  $\text{IP}_3\text{R}$  Control Variable  
 $\zeta$  –  $\text{IP}_3\text{R}$  Recovery Variable

### **Whole Cell Current Gating Variables**

$d_T - I_{\text{Ca(T)}}$  Activation Rate  
 $f_T - I_{\text{Ca(T)}}$  Inactivation Rate  
 $O_T - I_{\text{Ca(T)}}$  Open Probability  
 $d_{v1.1} - I_{\text{K(v1.1)}}$  Activation  
 $f_{v1.1} - I_{\text{K(v1.1)}}$  Inactivation  
 $d_{\text{ERG}} - I_{\text{K(ERG)}}$  Activation

### **Global Variables**

$V_m$  – Membrane Potential  
 $C_{\text{Cy}}$  – Bulk Cytoplasmic [ $\text{Ca}^{2+}$ ]

## **MODEL CONDUCTANCES**

### **Pacemaker Unit Conductances**

#### *Plasma Membrane Conductances*

$I_{Ca}$  – Inward  $Ca^{2+}$  Current

$I_{Na}$  – Inward  $Na^+$  Current

$I_{NSCC}$  – Non-Selective Cation Conductance

$I_{PM}$  – Plasma Membrane  $Ca^{2+}$ -ATPase

$I_{NaP}$  – Outward  $Na^+$  Pump

#### *Intracellular $Ca^{2+}$ Fluxes*

$J_{SERCA}$  – Sarco-Endoplasmic Reticulum  $Ca^{2+}$ -ATPase

$J_{IPR}$  –  $IP_3$  Receptor  $Ca^{2+}$  Flux

$J_{MCU}$  – Mitochondrial  $Ca^{2+}$  Uniporter

$J_{NCX}$  – Mitochondrial  $Na^+/Ca^{2+}$  Exchanger

$J_{S1S2}$  – Subspace 1/Subspace 2  $Ca^{2+}$  Diffusion

$J_{S2Cy}$  – Subspace 2/Bulk Cytoplasmic  $Ca^{2+}$  Diffusion

### **Bulk Cytoplasmic Subspace Conductances**

#### *Plasma Membrane Conductances*

$I_{Ca(T)}$  – T-Type  $Ca^{2+}$  Current

$I_{Ca(Ext)}$  –  $Ca^{2+}$  Extrusion Pump

$I_{K(v1.1)}$  –  $K(v1.1)$   $K^+$  Current

$I_{K(ERG)}$  – Ether-a-go-go  $K^+$  Current

$I_{KB}$  – Background  $K^+$  Current

$I_L$  – Non-Selective Inward Current

#### *Intracellular $Ca^{2+}$ Fluxes*

$J_{Cy}$  – Bulk Cytoplasmic Intracellular  $Ca^{2+}$  Flux

## PACEMAKER UNIT MODEL EQUATIONS

### Plasma Membrane Conductances

#### $Ca^{2+}$ Currents

$$I_{Ca} = g_{Ca}(V_m - E_{Ca}) \quad (S1)$$

$$g_{Ca} = \hat{g}_{Ca} e^{k_{Ca} V_m} \quad (S2)$$

$$I_{PM} = g_{PM} \left( \frac{C_{S1}^2}{K_{PM}^2 + C_{S1}^2} \right) \quad (S3)$$

#### $Na^+$ Currents

$$I_{Na} = g_{Na}(V_m - E_{Na}) \quad (S4)$$

$$I_{NaP} = g_{NaP} \left( \frac{N_{S1}^{h_{NaP}}}{K_{NaP}^{h_{NaP}} + N_{S1}^{h_{NaP}}} \right) (E_{NaP} - V_m) \quad (S5)$$

#### Non-Selective Cation Current

$$I_{NSCC(Z)} = g_{NSCC(Z)}(V_m - E_{NSCC}) \quad (S6)$$

$$g_{NSCC(Z)} = \hat{g}_{NSCC(Z)} \left( \frac{K_{NSCC}^{h_{NSCC}}}{K_{NSCC}^{h_{NSCC}} + C_{S1}^{h_{NSCC}}} \right) \quad (S7)$$

where  $Z = Ca$  or  $Na$

#### Nernst Potentials

$$E_{Ca} = \frac{RT}{Z_{Ca}F} \log_e \left( \frac{C_O}{C_{S1}} \right) \quad (S8)$$

$$E_{Na} = \frac{RT}{Z_{Na}F} \log_e \left( \frac{N_O}{N_{S1}} \right) \quad (S9)$$

#### Conductance Rate Scale Factor

$$V_{Scale} = \frac{n_{PU(Base)}}{n_{PU}} \quad (S10)$$

#### Aggregate Plasma Membrane Conductances

$$I_{iCa} = V_{Scale} (I_{Ca} + I_{PM} + I_{NSCC(Ca)}) \quad (S11)$$

$$I_{iNa} = V_{Scale} (I_{Na} + I_{NaP} + I_{NSCC(Na)}) \quad (S12)$$

$$I_{ion_{PU}(i)} = I_{iCa} + I_{iNa} \quad (S13)$$

### Intracellular $Ca^{2+}$ Fluxes

#### ER $Ca^{2+}$ Fluxes

$$J_{SERCA} = \frac{V_{SERCA} (C_{S1} - A_2 C_{ER})}{1 + A_4 C_{S1} + A_5 C_{ER} + A_6 C_{S1} C_{ER}} \quad (S14)$$

$$J_{IPR} = k_{IPR} \left( \frac{P\phi_1 H}{P\phi_1 + \phi_{-1}} \right)^4 (C_{ER} - C_{S2}) \quad (S15)$$

#### Mitochondrial $Ca^{2+}$ Fluxes

$$J_{MCU} = V_{MCU} \left( \frac{C_{S2}^2}{K_{MCU}^2 + C_{S2}^2} \right) \varepsilon_{INH} \quad (S16)$$

$$\varepsilon_{INH} = \frac{K_{INH}^{h_{INH}}}{K_{INH}^{h_{INH}} + C_{MT}^{h_{INH}}} \quad (S17)$$

$$J_{NCX} = V_{NCX} \left( \frac{C_{MT}}{K_{NCX} + C_{MT}} \right) \quad (S18)$$

#### Inter-Compartmental Volume $Ca^{2+}$ Diffusion

$$J_{S1S2(i)} = \mu_{S1S2(i)} (C_{S2(i)} - C_{S1(i)}) \quad (S19)$$

$$\mu_{S1S2(i)} = \mu_A + (\mu_B - \mu_A) \left[ \frac{i-1}{n_{PU} - 1} \right] \quad (S20)$$

$$J_{S2Cy(i)} = \mu_{S2Cy(i)} (C_{Cy} - C_{S2(i)}) \quad (S21)$$

**NB** –  $\mu_{S2Cy}$  values (for  $n_{PU} = 5-10, 15, 20$  &  $25$ ) are given in Table S5

### IP<sub>3</sub>R Rate Equations

$$\phi_1 = \frac{k_1 R_1 + r_2 C_{S2}}{R_1 + C_{S2}} \quad (S22)$$

$$\phi_{-1} = \frac{(k_{-1} + r_{-2}) R_3}{R_3 + C_{S2}} \quad (S23)$$

$$\phi_2 = \frac{k_2 R_3 + r_4 C_{S2}}{R_3 + C_{S2}} \quad (S24)$$

$$\phi_3 = \frac{g_{\phi_3} \zeta}{\left[ 1 + \left( \frac{K_{\phi_3(\text{act})}}{C_{S2}} \right)^{h_{\phi_3(\text{act})}} \right] \left[ 1 + \left( \frac{C_{S2}}{K_{\phi_3(\text{inh})}} \right)^{h_{\phi_3(\text{inh})}} \right]} \quad (\text{S25})$$

### IP<sub>3</sub>R Recovery Variable Equations

$$\frac{d\zeta}{dt} = \alpha_{\zeta}(1 - \zeta) - \beta_{\zeta}\zeta \quad (\text{S26})$$

$$\alpha_{\zeta} = g_{\alpha} \quad (\text{S27})$$

$$\beta_{\zeta} = g_{\beta} \frac{C_{S2}^{h_{\beta}}}{C_{S2}^{h_{\beta}} + K_{\beta}^{h_{\beta}}} \quad (\text{S28})$$

### Mitochondrial Ca<sup>2+</sup> Buffering Rate

$$f_m = \frac{1}{1 + \frac{K_m B_m}{(K_m + C_{MT})^2}} \quad (\text{S29})$$

### Compartmental Volume Ratio

$$\lambda_{X/Y} = \frac{\gamma_X}{\gamma_Y} \quad (\text{S30})$$

where X, Y = S<sub>1</sub>, S<sub>2</sub>, ER or MT

### State Variable Derivatives

$$\frac{dC_{S1}}{dt} = J_{S1S2} + \lambda_{MT/S1} J_{NCX} - \left( \frac{\delta_{S(\text{PU})}}{V_{\text{Scale}} Z_{\text{Ca}}} \right) I_{\text{Ca}} - \lambda_{ER/S1} J_{\text{SERCA}} \quad (\text{S31})$$

$$\frac{dC_{S2}}{dt} = J_{S2Cy} + \lambda_{ER/S2} J_{\text{IPR}} - \lambda_{S1/S2} J_{S1S2} - \lambda_{MT/S2} J_{\text{MCU}} \quad (\text{S32})$$

$$\frac{dC_{\text{ER}}}{dt} = J_{\text{SERCA}} - J_{\text{IPR}} \quad (\text{S33})$$

$$\frac{dC_{\text{MT}}}{dt} = f_m (J_{\text{MCU}} - J_{\text{NCX}}) \quad (\text{S34})$$

$$\frac{dN_{S1}}{dt} = - \left( \frac{\delta_{S(\text{PU})}}{V_{\text{Scale}} Z_{\text{Na}}} \right) I_{\text{Na}} \quad (\text{S35})$$

$$\frac{dH}{dt} = \phi_3(1 - H) - \left( \frac{P\phi_1\phi_2}{P\phi_1 + \phi_{-1}} \right) H \quad (\text{S36})$$



## BULK CYTOPLASMIC SUBSPACE MODEL EQUATIONS

### Plasma Membrane Conductances

#### $Ca^{2+}$ Currents

$$I_{Ca(T)} = g_{Ca(T)} O_T (V_m - E_{Ca(T)}) \quad (S37)$$

$$I_{Ca(Ext)} = g_{Ca(Ext)} \left( \frac{C_{Cy}}{K_{Ca(Ext)} + C_{Cy}} \right) \quad (S38)$$

#### $K^+$ Currents

$$I_{K(v1.1)} = g_{K(v1.1)} d_{v1.1} f_{v1.1} (V_m - E_K) \quad (S39)$$

$$I_{K(ERG)} = g_{K(ERG)} d_{ERG} (V_m - E_K) \quad (S40)$$

$$I_{K(B)} = g_{K(B)} (V_m - E_{K(B)}) \quad (S41)$$

#### Other Currents

$$I_L = g_L (V_m - E_L) \quad (S42)$$

#### Nernst Potentials

$$E_K = \frac{RT}{Z_K F} \log_e \left( \frac{K_O}{K_i} \right) \quad (S43)$$

#### Aggregate Currents

$$I_{ion_{cy}} = I_{Ca(T)} + I_{Ca(Ext)} + I_{K(v1.1)} + I_{K(ERG)} + I_{K(B)} + I_L \quad (S44)$$

### Intracellular $Ca^{2+}$ Fluxes

$$J_{Cy} = \mu_{Cy} (C_\infty - C_{Cy}) \quad (S45)$$

### Ionic Current Gating Differential Equations

#### $I_{Ca(T)}$ Current

$$\frac{dO_T}{dt} = \alpha_{OT} d_T f_T - \beta_{OT} O_T \quad (S46)$$

$$\frac{dX_T}{dt} = \frac{X_{T\infty} - X_T}{\tau_{XT}} \quad (\text{S47})$$

for  $X = d$  or  $f$

$$X_{T\infty} = \frac{1}{1 + e^{k_{XT}(V_m - V_{XT})}} \quad (\text{S48})$$

$$\tau_{dT} = A_{dT(1)} \quad (\text{S49})$$

$$\tau_{fT} = A_{fT(1)} + \frac{(A_{fT(2)} - A_{fT(1)})}{1 + e^{A_{fT(3)}(V_m - A_{fT(4)})}} \quad (\text{S50})$$

### $K^+$ Currents

$$\frac{dX}{dt} = \alpha_X(1 - X) - \beta_X X \quad (\text{S51})$$

for  $X = d_{v1.1}, f_{v1.1}, d_{\text{ERG}}$

$$\alpha_X = A_{X(1)} \left[ \frac{A_{X(2)}}{1 + e^{A_{X(3)}(V_m - A_{X(4)})}} + (1 - A_{X(2)}) \right] \quad (\text{S52})$$

$$\beta_X = A_{X(1)} \left[ A_{X(2)} - \frac{A_{X(2)}}{1 + e^{A_{X(3)}(V_m - A_{X(4)})}} \right] \quad (\text{S53})$$

### Global State Variable Derivatives

$$\frac{dV_m}{dt} = -\frac{1}{C_m} \left[ I_{\text{ion}_{\text{Cy}}} + \sum_{i=1}^{n_{\text{PU}}} I_{\text{ion}_{\text{PU}}(i)} \right] \quad (\text{S54})$$

$$\frac{dC_{\text{Cy}}}{dt} = J_{\text{Cy}} - \lambda_{\text{S2Cy}} \sum_{i=1}^{n_{\text{PU}}} J_{\text{S2Cy}(i)} - \left( \frac{\delta_{\text{S(Cy)}}}{Z_{\text{Ca}}} \right) [I_{\text{Ca(T)}} + I_{\text{Ca(Ext)}}] \quad (\text{S55})$$

**PACEMAKER UNIT MODEL PARAMETERS**

<b>Plasma Membrane Conductances</b>								
<i>Ca<sup>2+</sup> Currents</i>								
$\hat{g}_{Ca}$	0.074 pS	S2	F <sub>UP</sub> *	$k_{Ca}$	0.013 mV <sup>-1</sup>	S2	F <sub>UP</sub> **	
$g_{PM}$	675 fA	S3	F <sub>UP</sub> *	$K_{PM}$	1 μM	S3	(1)	
<i>Na<sup>+</sup> Currents</i>								
$g_{Na}$	13.5 pS	S4	F <sub>UP</sub> **	$g_{NaP}$	187.5 pS	S5	F <sub>UP</sub> *	
$E_{NaP}$	10 mV	S5	(2)**	$K_{NaP}$	1 x 10 <sup>4</sup> μM	S5	F <sub>UP</sub>	
$h_{NaP}$	4	S5	F <sub>UP</sub>					
<i>Non-Selective Cation Conductance</i>								
$E_{NSCC}$	0 mV	S6	(3)	$\hat{g}_{NSCC(Ca)}$	0.1 pS	S7	F <sub>UP</sub> *	
$\hat{g}_{NSCC(Na)}$	160 pS	S7	F <sub>UP</sub> *	$K_{NSCC}$	0.12 μM	S7	F <sub>UP</sub>	
$h_{NSCC}$	4	S7	(3)					
<b>Intracellular Ca<sup>2+</sup> Fluxes</b>								
<i>Endoplasmic Reticulum Ca<sup>2+</sup> Conductances</i>								
$k_{IPR}$	2000 s <sup>-1</sup>	S15	F <sub>UP</sub>	$V_{SERCA}$	1 x 10 <sup>5</sup> s <sup>-1</sup>	S14	F <sub>UP</sub>	
$A_2$	6 x 10 <sup>-4</sup>	S14	F <sub>UP</sub>	$A_4$	3.57 μM <sup>-1</sup>	S14	(4)	
$A_5$	2.7 x 10 <sup>-5</sup> μM <sup>-1</sup>	S14	(4)	$A_6$	2.31 x 10 <sup>-5</sup> μM <sup>-2</sup>	S14	(4)	
<i>Mitochondrial Ca<sup>2+</sup> Conductances</i>								
$V_{MCU}$	800 μM s <sup>-1</sup>	S16	F <sub>UP</sub>	$K_{MCU}$	10 μM	S16	(5)	
$K_{INH}$	10 μM	S17	F <sub>UP</sub>	$h_{INH}$	4	S17	F <sub>UP</sub>	
$V_{NCX}$	3 μM s <sup>-1</sup>	S18	F <sub>UP</sub> *	$K_{NCX}$	0.30 μM	S18	(6)	
$K_m$	0.01 μM	S29	F <sub>UP</sub>	$B_m$	1000 μM	S29	F <sub>UP</sub>	
<i>Intracellular Ca<sup>2+</sup> Diffusion Rates</i>								
$\mu_A$	0.30 s <sup>-1</sup>	S20	F <sub>UP</sub>	$\mu_B$	0.24 s <sup>-1</sup>	S20	F <sub>UP</sub>	
<b>IP<sub>3</sub>R Rate Parameters</b>								
<i>Instantaneous Rate Equations</i>								
$k_1$	0 s <sup>-1</sup>	S22	F <sub>UP</sub>	$k_{-1}$	6.4 s <sup>-1</sup>	S23	F <sub>UP</sub>	
$k_2$	4 s <sup>-1</sup>	S24	F <sub>UP</sub>	$r_2$	250 s <sup>-1</sup>	S22	F <sub>UP</sub>	
$r_{-2}$	0 μM s <sup>-1</sup>	S23	F <sub>UP</sub>	$r_4$	750 s <sup>-1</sup>	S24	F <sub>UP</sub>	
$R_1$	36 μM	S22	(7)	$R_3$	300 μM	S23,S24	(7)	
<i>φ<sub>3</sub> Rate Parameters</i>								
$g_{\phi_3}$	4.5 s <sup>-1</sup>	S25	F <sub>UP</sub>	$K_{\phi_3(act)}$	0.1 μM	S25	F <sub>UP</sub>	
$K_{\phi_3(inh)}$	0.5 μM	S25	F <sub>UP</sub>	$h_{\phi_3(act)}$	3	S25	F <sub>UP</sub>	
$h_{\phi_3(inh)}$	3	S25	F <sub>UP</sub>					
<i>ζ Rate Parameters</i>								
$g_\alpha$	0.85 s <sup>-1</sup>	S27	F <sub>UP</sub>	$g_\beta$	1.5 x 10 <sup>3</sup> s <sup>-1</sup>	S28	F <sub>UP</sub>	
$K_\beta$	0.35 μM	S28	F <sub>UP</sub>	$h_\beta$	4	S28	F <sub>UP</sub>	

**Table S1 – Pacemaker Unit Model Equation Parameters**

Numbers in parenthesis denotes literary reference. F<sub>UP</sub> denotes that parameter was fitted to reproduce unitary potential characteristics (see “Parameter Estimation” from Ref. (8)).

\* denotes parameter was modified from original model.

\*\* denotes parameter was added to model framework.

## WHOLE CELL CURRENT EQUATION PARAMETERS

Plasma Membrane Conductances								
<i>Ca<sup>2+</sup> Currents</i>								
	$g_{Ca(T)}$	800 pS	S37	F <sub>SW</sub>	$E_{Ca(T)}$	17 mV	S37	(8)
	$g_{Ca(Ext)}$	100 fA	S38	F <sub>SW</sub>	$K_{Ca(Ext)}$	1.0 μM	S38	F <sub>SW</sub>
<i>K<sup>+</sup> Currents</i>								
	$g_{K(v1.1)}$	10 pS	S39	F <sub>SW</sub>	$g_{K(ERG)}$	6 pS	S40	F <sub>SW</sub>
	$g_{K(B)}$	13.5 pS	S41	F <sub>SW</sub>	$E_{K(B)}$	-70 mV	S41	F <sub>SW</sub>
<i>Other Currents</i>								
	$g_L$	0.8 pS	S42	F <sub>SW</sub>	$E_L$	0 mV	S42	(3)
Intracellular Ca <sup>2+</sup> Fluxes								
	$\mu_{Cy}$	1.3 s <sup>-1</sup>	S45	F <sub>SW</sub>	$C_\infty$	0.12 μM	S45	F <sub>SW</sub>
Gating Variable Rate Equations								
<i>O<sub>T</sub> Rate Equations</i>								
	$\alpha_{OT}$	240 s <sup>-1</sup>	S46	F <sub>SW</sub>	$\beta_{OT}$	72 s <sup>-1</sup>	S46	F <sub>SW</sub>
<i>d<sub>T</sub> Rate Equations</i>								
	$k_{dT}$	-0.60 mV <sup>-1</sup>	S48	(9)	$V_{dT}$	-53 mV	S48	(9)
	$A_{dT(1)}$	0.0025 s	S49	(9)				
<i>f<sub>T</sub> Rate Equations</i>								
	$k_{fT}$	1 mV <sup>-1</sup>	S48	(9)	$V_{fT}$	-65 mV	S48	(9)
	$A_{fT(1)}$	0.019 s	S50	(9)	$A_{fT(2)}$	6.75 s	S50	(9)
	$A_{fT(3)}$	2 mV <sup>-1</sup>	S50	(9)	$A_{fT(4)}$	-40 mV	S50	(9)
<i>d<sub>v1.1</sub> Rate Equations</i>								
	$A_{dv(1)}$	1000 s <sup>-1</sup>	S52,S53	(10)	$A_{dv(2)}$	0.80	S52,S53	(10)
	$A_{dv(3)}$	-0.13 mV <sup>-1</sup>	S52,S53	(10)	$A_{dv(4)}$	25 mV	S52,S53	(10)
<i>f<sub>v1.1</sub> Rate Equations</i>								
	$A_{fv(1)}$	333 s <sup>-1</sup>	S52,S53	(10)	$A_{fv(2)}$	0.10	S52,S53	(10)
	$A_{fv(3)}$	0.23 mV <sup>-1</sup>	S52,S53	(10)	$A_{fv(4)}$	44.8 mV	S52,S53	(10)
<i>d<sub>ERG</sub> Rate Equations</i>								
	$A_{dERG(1)}$	1000 s <sup>-1</sup>	S52,S53	(10)	$A_{dERG(2)}$	0.70	S52,S53	(10)
	$A_{dERG(3)}$	-0.56 mV <sup>-1</sup>	S52,S53	(10)	$A_{dERG(4)}$	30 mV	S52,S53	(10)

**Table S2 – Whole Cell Current Model Equation Parameters**

Numbers in parenthesis denotes literary reference. FSW denotes that parameter was fitted to reproduce slow wave characteristics (see “Parameter Estimation” section in manuscript).

**CELL CONSTANTS AND GLOBAL PARAMETERS**

<b>Universal Constants</b>					
$R$	$8.31 \times 10^3 \text{ aJ zmol}^{-1} \text{ K}^{-1}$	S8,S9,S43	$T$	310.16 K	S8,S9,S43
$F$	$9.649 \times 10^{-2} \text{ fC zmol}^{-1}$	S8,S9,S43			
<b>Ion/Metabolite Concentrations</b>					
$C_O$	$1.8 \times 10^3 \text{ } \mu\text{M}$	S8	$N_O$	$140 \times 10^3 \text{ } \mu\text{M}$	S9
$K_O$	$5.4 \times 10^3 \text{ } \mu\text{M}$	S43	$K_i$	$145 \times 10^3 \text{ } \mu\text{M}$	S43
$P$	$1 \text{ } \mu\text{M}$	S15,S36			
<b>Ion Valency</b>					
$Z_{Ca}$	2	S8,S31,S55	$Z_{Na}$	1	S9,S35
$Z_K$	1	S43			
<b>Compartmental Volume Ratios</b>					
$\gamma_{S1}$	100	S30	$\gamma_{S2}$	1	S30
$\gamma_{ER}$	20	S30	$\gamma_{MT}$	200	S30
$\gamma_{Cy}$	1000	S30			
<b>Cell Constants</b>					
$\delta_{S(Cy)}$	$2 \times 10^{-3} \text{ } \mu\text{M C}^{-1}$	S55	$\delta_{S(PU)}$	$9.25 \text{ } \mu\text{M C}^{-1}$	S31,S35
$C_m$	20 pF	S54	$n_{PU(Base)}$	50	S10

**Table S3 – Model Cell Constants and Other Global Parameters**

**INITIAL STATE VARIABLE VALUES**

<b>Pacemaker Unit State Variables</b>			
$C_{S1}$	0.120 $\mu\text{M}$	$C_{S2}$	0.023 $\mu\text{M}$
$C_{ER}$	200 $\mu\text{M}$	$C_{MT}$	0.200 $\mu\text{M}$
$N_{S1}$	$1.01 \times 10^4 \text{ } \mu\text{M}$	$H$	0.200
$\zeta$	0.300		
<b>Whole Cell Current Gating Variables</b>			
$d_T$	0.010	$f_T$	0.001
$O_T$	0.000	$d_{v1.1}$	0.000
$f_{v1.1}$	1.000	$d_{ERG}$	0.000
<b>Global Variables</b>			
$V_m$	-70 mV	$C_{Cy}$	0.12 $\mu\text{M}$

**Table S4 – Model State Variable Initial Values**

**SUBSPACE 2/BULK CYTOPLASM  $\text{Ca}^{2+}$  DIFFUSION RATES**

PU #	$n_{\text{PU}} = 5$	$n_{\text{PU}} = 6$	$n_{\text{PU}} = 7$	$n_{\text{PU}} = 8$	$n_{\text{PU}} = 9$	$n_{\text{PU}} = 10$	$n_{\text{PU}} = 15$	$n_{\text{PU}} = 20$	$n_{\text{PU}} = 25$
1	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000
2	0.4788	0.4133	0.4071	0.3662	0.3520	0.3361	0.2150	0.1544	0.1136
3	0.6843	0.5577	0.4752	0.4253	0.3850	0.3658	0.4367	0.3260	0.2489
4	0.9335	0.7464	0.6244	0.5441	0.4829	0.4357	0.5096	0.4981	0.3872
5	1.1673	0.9389	0.7818	0.6750	0.5935	0.5351	0.4565	0.4844	0.5217
6		1.1184	0.9388	0.8062	0.7095	0.6366	0.5033	0.4455	0.5672
7			1.0827	0.9357	0.8240	0.7386	0.5390	0.4628	0.4886
8				1.0545	0.9325	0.8361	0.6042	0.5127	0.4790
9					1.0336	0.9320	0.6642	0.5458	0.5179
10						1.0185	0.7348	0.5831	0.5282
11							0.7977	0.6366	0.5536
12							0.8619	0.6802	0.5883
13							0.9241	0.7256	0.6200
14							0.9812	0.7694	0.6541
15							1.0344	0.8221	0.6935
16								0.8690	0.7305
17								0.9096	0.7684
18								0.9550	0.8036
19								0.9965	0.8343
20								1.0347	0.8712
21									0.9092
22									0.9435
23									0.9768
24									1.0079
25									1.0361

**Table S5 – Subspace 2/Bulk Cytoplasmic ( $\mu_{\text{S2Cy}}$ )  $\text{Ca}^{2+}$  Diffusion Rates**

## **DOSE-RESPONSE SIMULATIONS**

The following is of the dose-response simulations that have been included in the supplementary materials:

- Figure 1 – Decreased  $[\text{Ca}^{2+}]_o$
- Figure 2 – Decreased  $[\text{Na}^+]_o$
- Figure 3 – Increased  $[\text{K}^+]_o$
- Figure 4 – Varying  $[\text{IP}_3]$
- Figure 5 –  $J_{\text{NCX}}$  Inhibition
- Figure 6 –  $I_{\text{K(ERG)}}$  Inhibition

The format of each dose-response simulation figure is comprised of 9 subplots (*A-I*). The subplots *A-H* are separated into two columns, the first column illustrating the simulated  $V_m$  response and the second the pacemaker unit discharge rastergram. Each row, within this subplot group, is the response generated by the proportional change in the target parameter (see Table 5 of the manuscript) which indicated by the key given in subplot *I*. The final subplot (*I*) shows the change in the slow wave characteristic values from control conditions, a list of which is given below:

- MDP (mV) ,
- Amplitude (mV) ,
- $\{dV_m/dt\}_{\text{max}}$  (mV s<sup>-1</sup>) , and
- Frequency (cpm)

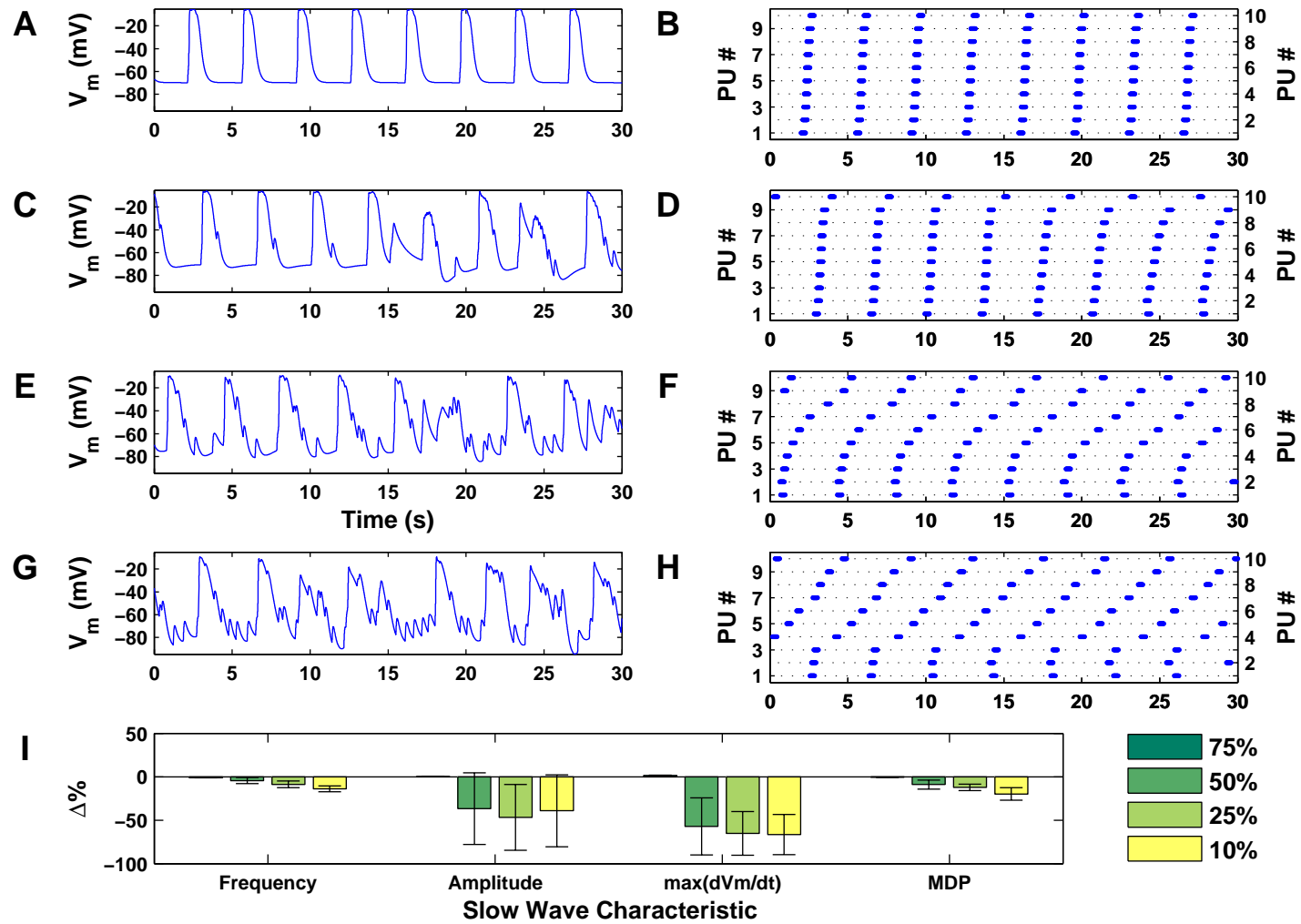


Figure S1 – Decreased Extracellular  $[Ca^{2+}]$  Dose Response Simulation



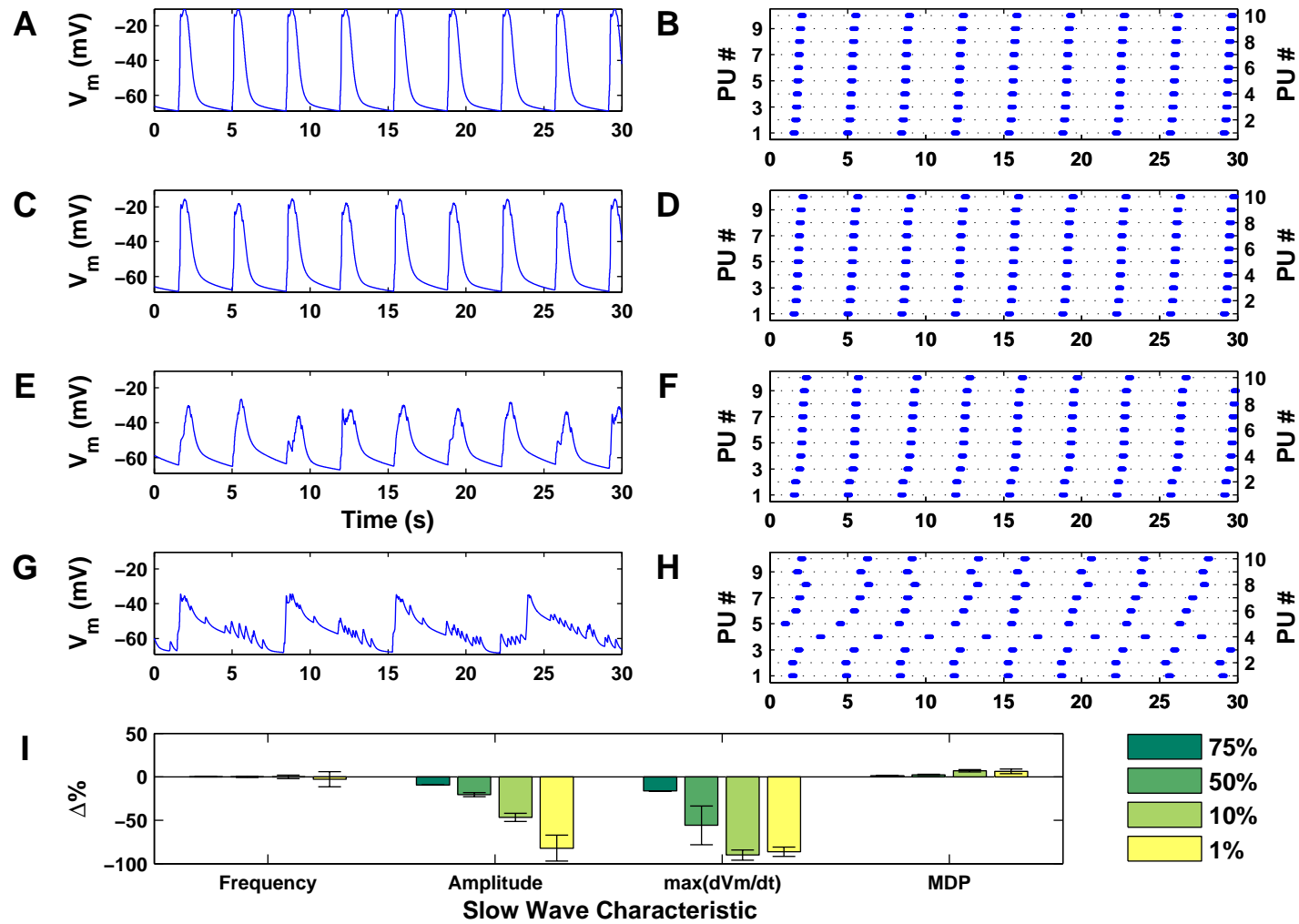


Figure S2 – Decreased Extracellular  $[Na^+]$  Dose Response Simulations

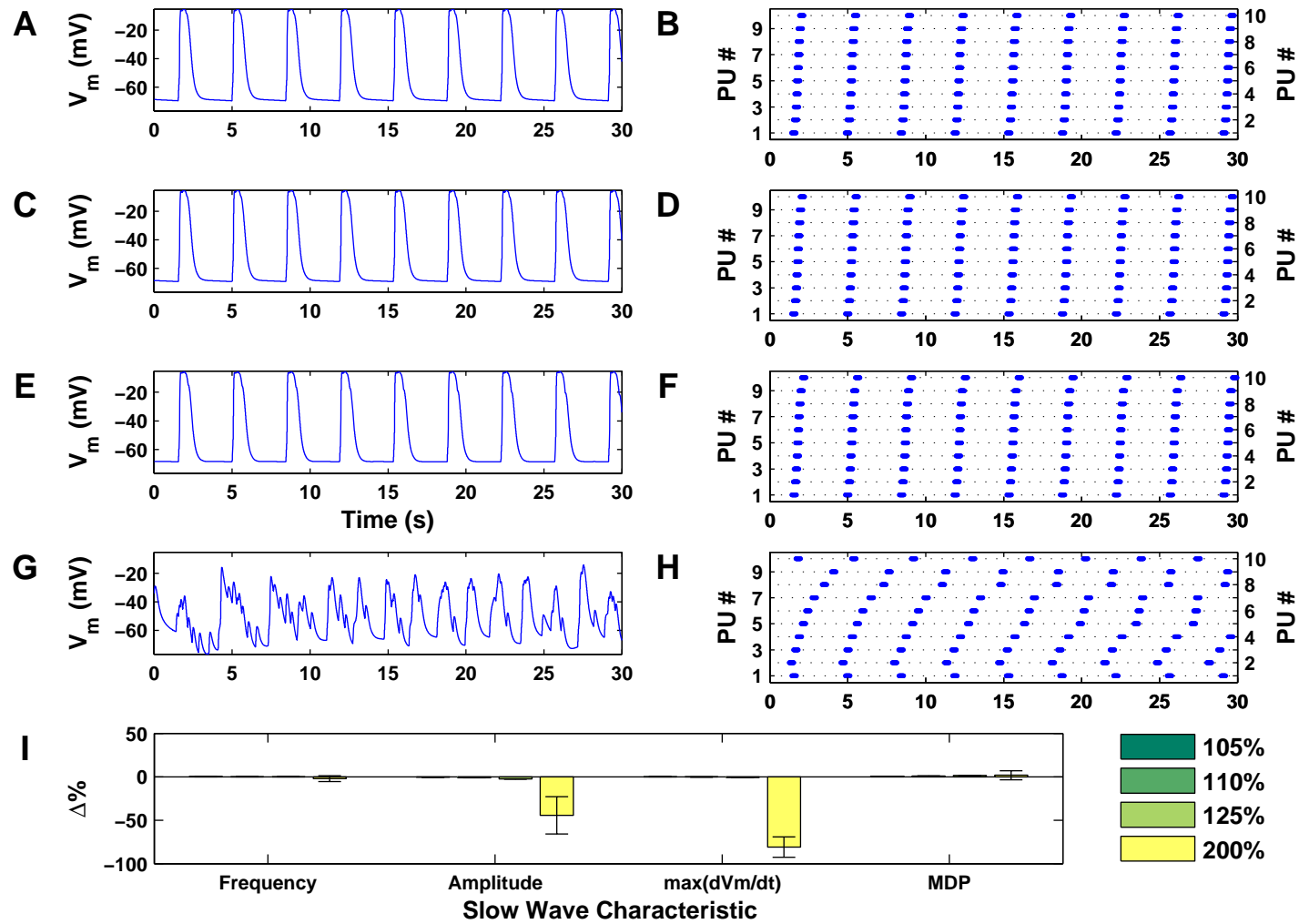


Figure S3 – Increase Extracellular  $[K^+]$  Dose Response Simulations

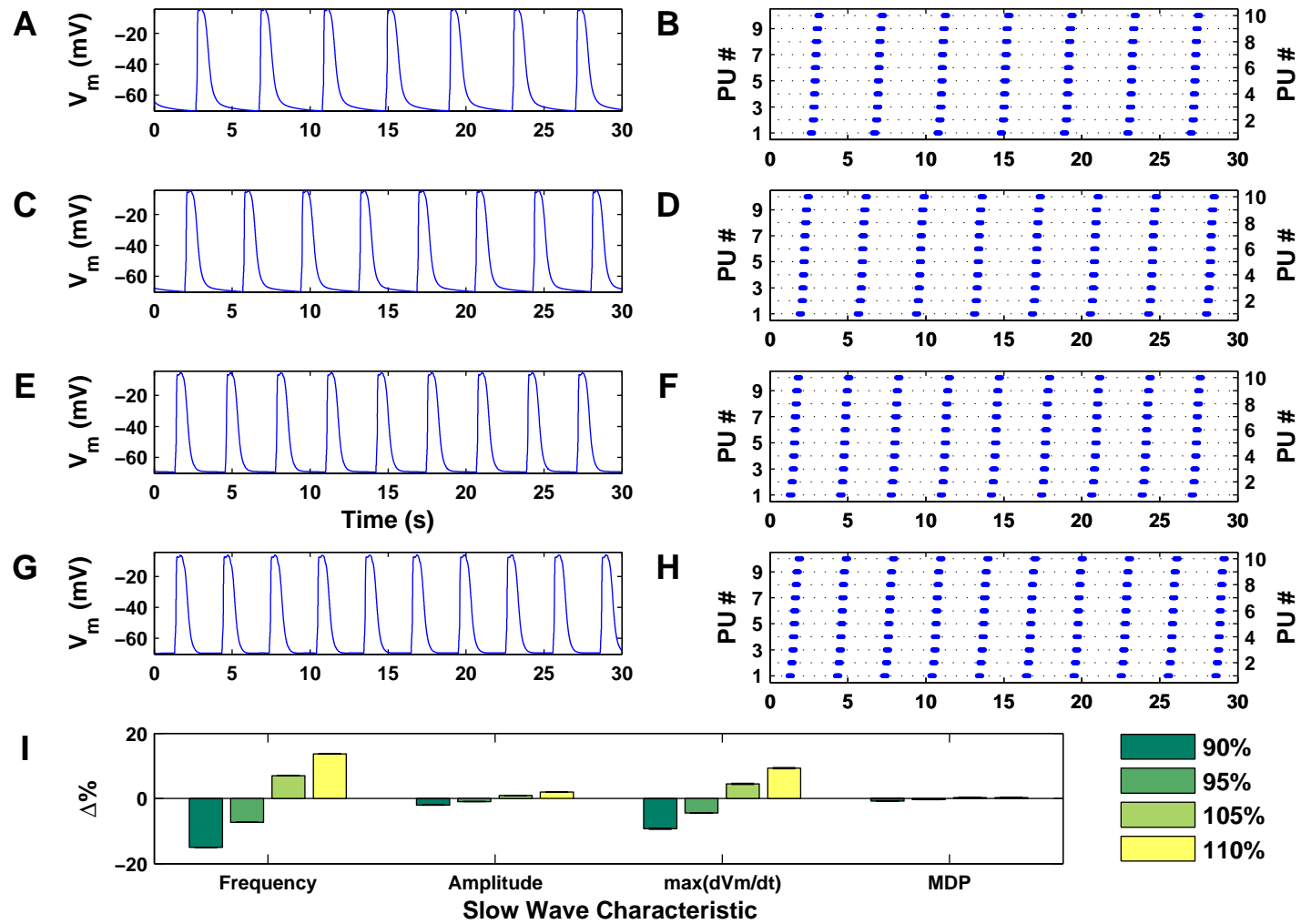


Figure S4 – Varying [IP<sub>3</sub>] Dose Response Simulations

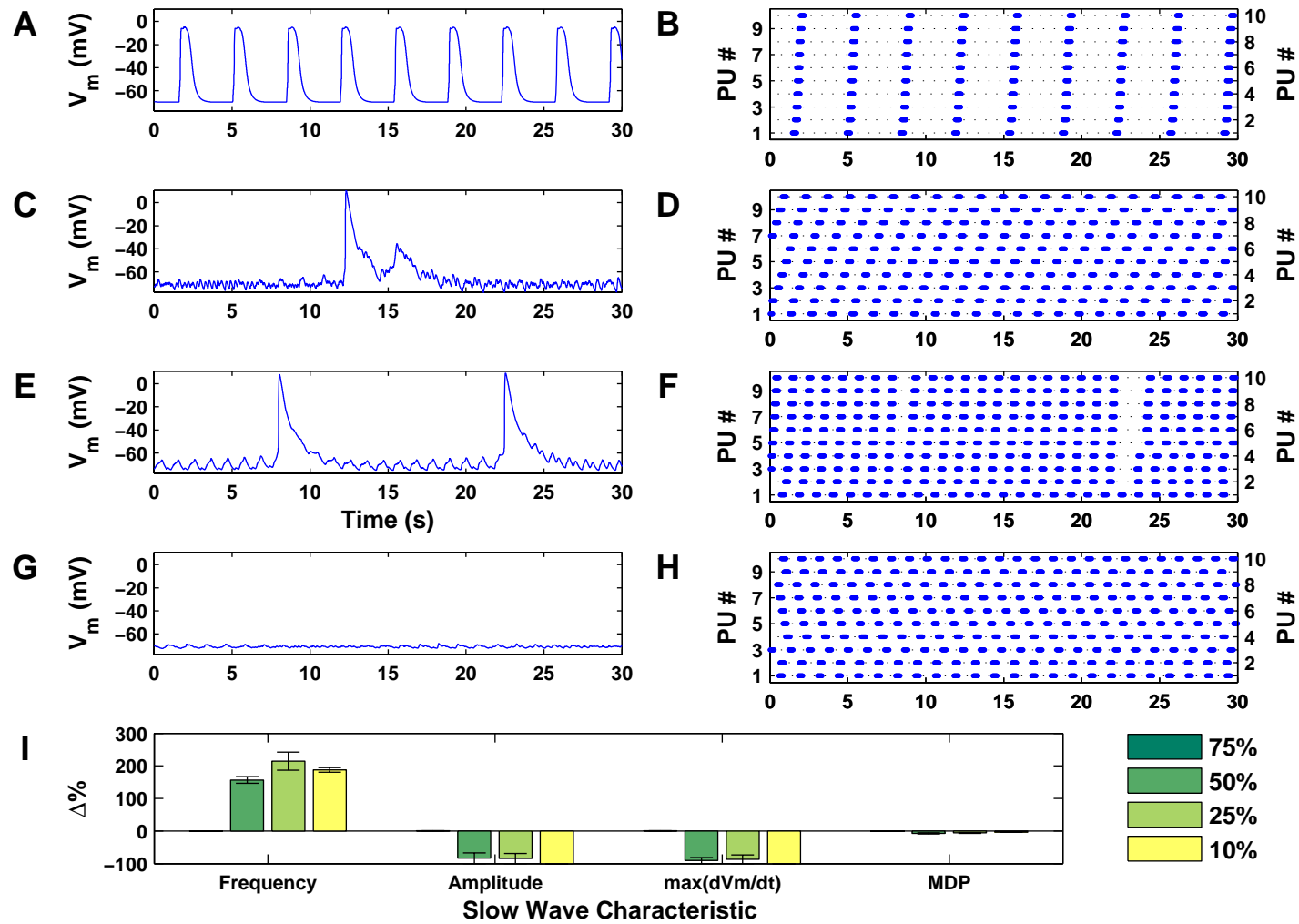


Figure S5 –  $J_{NCX}$  Inhibition Dose Response Simulations

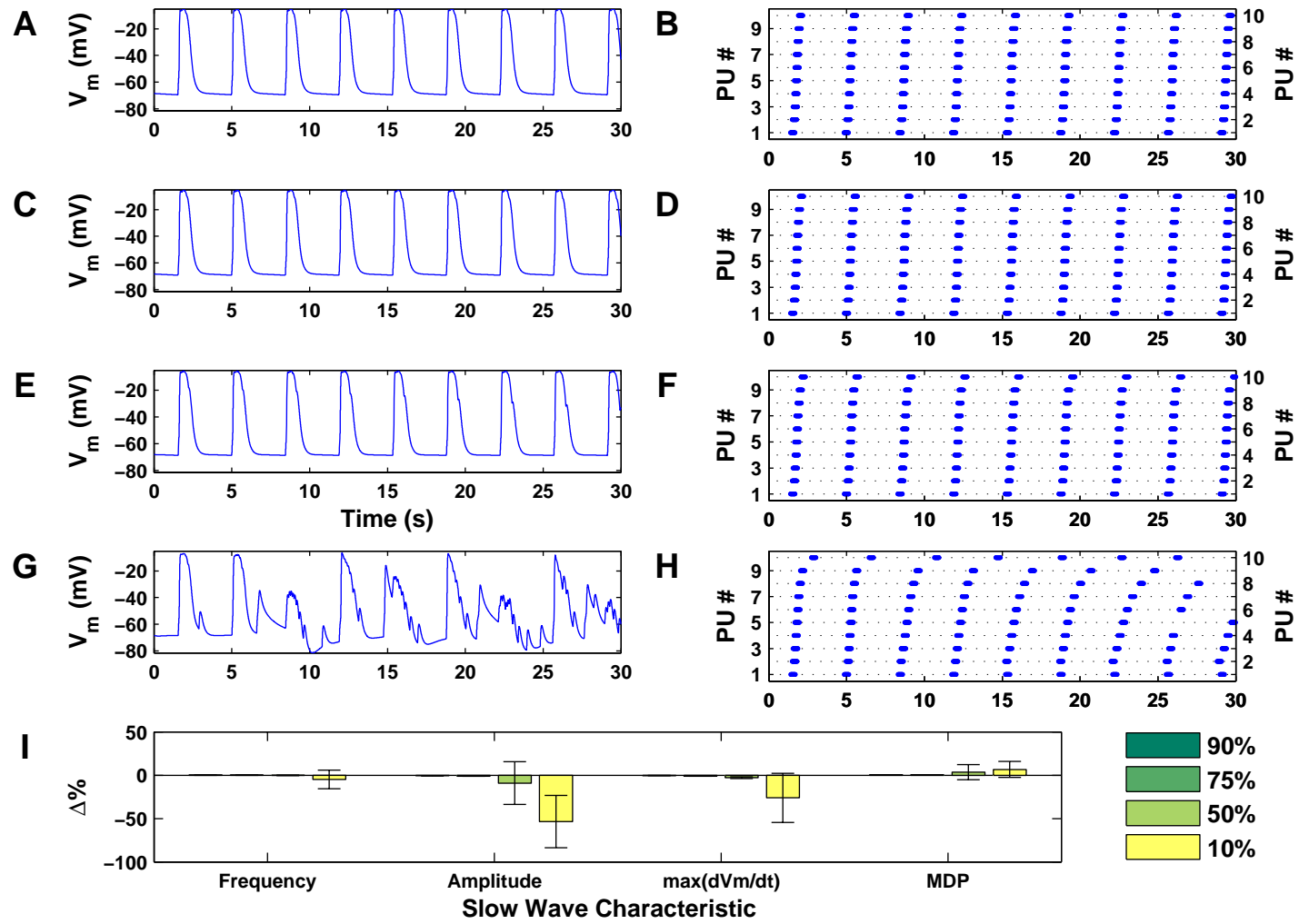


Figure S6 –  $I_{K(ERG)}$  Inhibition Dose Response Simulations

## PACEMAKER UNIT FIRING DISTRIBUTION

### Inverse Distribution Function

The cumulative distribution function,  $\psi(t)$  that describes pacemaker unit discharge over time is given by the 2-parameter Boltzmann function as follows:

$$\psi(t) = \frac{1}{1 + e^{-k_\psi(t-T_\psi)}} \quad (\text{S.A1})$$

Therefore, in order to determine the time at which a proportion,  $P_x$ , of the pacemaker unit population has fired, we invert  $\psi(t)$  as follows:

$$t = \psi^{-1}(P_x) = T_\psi - \frac{1}{k_\psi} \log_e \left( \frac{1}{P_x} - 1 \right) \quad (\text{S.A2})$$

### Pacemaker Unit Firing Probability

If a pacemaker unit population is comprised of  $n_{PU}$  units, then each pacemaker unit represents a proportion of  $1/n_{PU}$  of the entire population. Therefore, the proportion of the population which has fired after the discharge of  $i$  pacemaker units is given by the equation:

$$P_{x(i)} = \frac{i}{n_{PU}} \quad (\text{S.A3})$$

Note that as we are making a discrete approximation to a continuous distribution, this proportion is fixed as the midpoint of the interval over which it represents (i.e.,  $1/n_{PU}$ ).

$$\text{i.e. } P_{x(i)} = \frac{i}{n_{PU}} - \frac{1}{2n_{PU}} = \frac{2i-1}{2n_{PU}} \quad (\text{S.A4})$$

Substituting eqn. (S.A4) into eqn. (S.A2) therefore gives the time at which the  $i^{\text{th}}$  pacemaker unit will discharge:

$$t_i = T_\psi - \frac{1}{k_\psi} \log_e \left( \frac{2n_{PU}}{2i-1} - 1 \right) \quad (\text{S.A5})$$

### Pacemaker Cycle Landmark

As  $\psi(t)$  can be shifted in time to coincide with any arbitrary landmark point within the slow wave cycle, then the value of  $T_\psi$  is also arbitrary. Therefore,  $\psi(t)$  was fixed such that the firing of the first pacemaker unit was set at  $t = 0$ . This is due to the fact that this is

a landmark point which is common to any pacemaker unit population, independent of size. Substituting  $t = 0$  into eqn. (S.A5) and rearranging gives:

$$T_{\psi} = \frac{1}{k_{\psi}} \log_e \left( \frac{1}{P_{x(1)}} - 1 \right) \quad (\text{S.A6})$$

From eqn. (S.A4), we know that  $P_{x(1)} = 1/(2n_{PU})$ . Therefore, substituting eqn. (S.A4) into (S.A6) gives the following equation which describes  $T_{\psi}$  as a function of  $n_{PU}$ :

$$T_{\psi} = \frac{1}{k_{\psi}} \log_e (2n_{PU} - 1) \quad (\text{S.A7})$$

### **Pacemaker Unit Firing Time Distribution**

Substituting eqn. (S.A7) into eqn. (S.A5) gives the final equation describing the time at which the  $i^{\text{th}}$  pacemaker unit, from a population of  $n_{PU}$  units, will discharge as follows:

$$t_i = \frac{1}{k_{\psi}} \left[ \log_e (2n_{PU} - 1) - \log_e \left( \frac{2n_{PU}}{2i - 1} - 1 \right) \right] \quad (\text{S.A8})$$

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