Supporting Information

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SI Text

Latitudinal Distribution of Gaseous Elemental Mercury (GEM) Concentration During the Last 30 Years. Recent global modeling studies (1) suggest a latitudinal distribution of GEM concentrations in the Northern Hemisphere, with present levels slightly higher at 60°N. This present gradient is low (≈ 0.3 ng m⁻³) (1). It is likely, however, that GEM levels in the Northern Hemisphere have been more heterogeneous in the past (i.e., in the 1970s and 1980s), as suggested by limited GEM observations onboard scientific ships in the Atlantic (2–5). Higher GEM emissions from anthropogenic sources may have strongly impacted temperate areas (i.e., 40–50°N) and to a lesser extent southern latitudes (i.e., 30°N and southern).

Ship-based records of atmospheric total gaseous mercury (TGM) represent the only data available in the late 1970s. TGM includes GEM and divalent gaseous mercury species; TGM and GEM could be assimilated here, as divalent gaseous mercury species represents only a few percent of TGM (ref. 6 and references therein). [Fig. S1](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF1) presents a direct comparison of our reconstruction of atmospheric GEM inferred from firn air and the available onboard observations. Extreme caution is required when discussing ship-based records of atmospheric TGM. Such records are collected during short (i.e., multiweek) sampling periods, and thus are strongly influenced by short timescale variations of both natural and anthropogenic GEM sources. [Fig.](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF1) [S1](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF1) suggests that the evolution of GEM concentrations reconstructed above Greenland cannot be generalized to the whole Northern Hemisphere but is instead likely to be representative of middle and high northern latitudes.

Parameterization of the Diffusion Model. We used a onedimensional gas diffusion model in Eulerian coordinates (7) to infer the atmospheric record of GEM from firn air concentrations. We used firn structure parameters shown in [Fig. S2](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF2) (density and closed porosity) from the EUROCORE drilling (8).

We determined GEM diffusivity in air at Summit Station, $D_{(T,P)}^{Surface}$, using the value reported by Massman (9) corrected for Summit temperature and pressure (8):

$$
D_{(T, P)}^{Surface} = D_{T_0, P_0} \times {}^{P_0/}} \times (T_{T_0})^{1.85}
$$
 [1]

where $T_0 = 253.16$ K, $P_0 = 1013.25$ mbar, $T = 241$ K, and $P =$ 675 mbar. *T* and *P* are mean annual atmospheric values of temperature and pressure for the Summit site. Eq. **1** gives GEM diffusivity in the atmosphere above the firn surface. To obtain effective diffusivity of GEM in the firn, we used the following relation:

$$
D_{\text{eff}} = \phi_{\tau} \times D_{(T, P)}^{\text{Surface}} \tag{2}
$$

where ϕ is the snow porosity determined using the densities of snow and ice:

$$
\phi = 1 - \frac{\rho_{\text{Show}}}{\rho_{\text{Ice}}} \tag{3}
$$

and τ is the firn tortuosity.

Tortuosity of a porous medium represents the complexity of the pathway and is commonly calculated as the ratio of the mean path length to the minimum possible (straight line) path length. Effective diffusivity of GEM depends on firn tortuosity, which increases progressively with depth. A null value of the ratio $1/\tau$ at the top of the lock-in zone means that diffusion ceases at this depth. In short, GEM effective diffusivity decreases from the snow surface value to zero at the close-off depth.

We used an inverse method (7, 10) to compute the ratio at all depths in the firn from the CO_2 atmospheric trend (Fig. $S3a$) and from $CO₂$ concentrations measured in the firn at Summit [\(Fig.](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF3) [S3](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF3)*b*). In other words, we obtained a site-specific, diffusivitydepth relationship by adjusting diffusivity until the model reproduced the observed $CO₂$ firn-air profile when driven by the independently derived atmospheric $CO₂$ history. We sampled air for $CO₂$ analysis at the same depths as GEM. The $CO₂$ atmospheric scenario was derived from measured values from Alert, Canadian Arctic (11), Mauna Loa, Hawaii (12), and DE08 firn, Antarctica (13) records. We corrected records from Mauna Loa and DE08 from the difference between measured Alert and global concentrations.

Previous modeling studies (14–17) were able to reproduce accurately $CO₂$ concentrations measured in firn air at NGRIP (75°N, 42°W) using the $CO₂$ atmospheric history represented in [Fig. S3](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF3)*a*. The same studies simultaneously obtained similar results for various species (e.g., SF6, ref. 14), confirming the good parameterization of their models. NGRIP is a camp located on the Greenland ice sheet, a few hundred kilometers north of Summit, where firn air was sampled during July 2001. Thus, we considered that atmospheric evolution of $CO₂$ described previously was appropriate for parameterization of our diffusion model.

Validation of Model Parameterization. We validated parameterization of the ratio ϕ/τ using CH₄ and three halocarbon species (CFC11, CFC113, and CCl₄) for which atmospheric histories have been estimated from emission scenarios and real-time measurements (11, 18, 19). Concentration-depth profiles were determined for these four species using the adjusted ϕ/τ -depth profile in the diffusion model, and good agreement with concentration-depth profiles actually measured in the Summit firn was obtained [\(Figs. S4 and S5\)](http://www.pnas.org/cgi/data/0905117106/DCSupplemental/Supplemental_PDF#nameddest=SF4).

Changes in atmospheric concentrations of CFC11, CFC113, and CCl₄ during recent decades were $\approx 7\%$, $\approx 6\%$, and $\approx 11.5\%$, respectively, and these species poorly constrain the diffusivity profile in shallow firn. GEM concentrations have not exhibited important changes during the last 15 years, however, and our results were not sensitive to errors in diffusivity in the shallow firn.

Monte Carlo Modeling. We chose a mathematical parameterization of atmospheric GEM history from 1940 to 2006 (firn air model input)—which allowed for the possibility of a constant level, monotonic increase, or decrease, or peak concentration of GEM concentration during this timeframe, depending on the choice of parameter values. Specifically, we combined two log-normal functions to represent a potential peak in concentrations. We tested a wide range of parameter values with the forward firn air model previously described (Monte Carlo approach), representing widely varying scenarios for the atmospheric evolution of GEM concentrations. We then modeled a profile of GEM concentrations in the firn from each atmospheric history tested. Agreement between a modeled firn profile *j* and the experimental firn profile (Fig. 1) was estimated using the χ^2 parameter defined by the following relation:

$$
\chi_j^2 = \sum_{i=1}^n \left(\frac{(Hg^{\circ}_{\text{Measured}})_i - (Hg^{\circ}_{\text{Modeled},j})_i}{\sigma_i} \right)^2 \tag{4}
$$

where σ_i represents the measurement error associated with (Hg°*Measured*)*i*. According to Tarantola theory (20), we were able to associate a probability density *pj* with each atmospheric scenario tested (Eq. 5), using the χ^2 _j value previously determined:

$$
p_j \propto \exp\left[-\frac{\chi_j^2}{2}\right] \tag{5}
$$

We finally assessed probability distributions for GEM concentrations with a 1-year time resolution. Such distributions were obtained by a statistical analysis of all GEM atmospheric histories tested for any 1-year time interval:

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$$
p(x, x + dx) \propto \sum_{j=0}^{N} p_j \times \delta_j(x, x + dx)
$$
 [6]

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where $p(x,x, +dx)$ is the probability that the atmospheric concentration of GEM is in the interval $[x, x+dx]$ and $\delta_j(x, x, +dx)$ is a function whose value is one when the concentration of scenario j is in the interval $[x, x+dx]$ and zero otherwise. We calculated means and standard deviations from all distributions (i.e., every year from 1940 to 2006). The envelope of atmospheric GEM concentrations presented in this study corresponds to the mean concentrations plus or minus one standard deviation. Our Monte Carlo approach led to high quality results, but was timeconsuming due to the large number of tested scenarios. Thus, inverse modeling should be considered as a potential improvement for further studies involving modeling of GEM diffusion processes in polar firn.

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Fig. S1. Intervals of modeled concentrations for atmospheric GEM inferred from Summit firn air (gray stripes), and latitudinal distributions of total gaseous mercury (TGM) over the Atlantic for the years 1977, 1978, 1979, and 1980 (18), 1990 (17), 1995 (16), 1996, and 1999/2000 (19). TGM includes GEM and divalent gaseous mercury species.

Fig. S2. Evolution of density and closed porosity with depth at Summit, Greenland (from ref. 8).

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Fig. S3. (*a*) Atmospheric evolution of CO2 during the last century, and (*b*) CO2 concentrations measured in firn at Summit in June 2006 (red dots). The blue line represents the CO₂ firn profile modeled after adjustment of the ratio ϕ/τ (*b*).

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Fig. S4. (*a*) Atmospheric concentrations of CH4 during the last century; (*b*) CH4 concentrations measured (red dots) and modeled (blue line) in the firn at Summit after parameterization of the model.

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Fig. S5. Atmospheric concentrations of CFC11(*a*), CFC113 (*c*), and CCl4 (*e*) (13); concentrations of these halocarbons measured (red dots) and modeled (blue line) in the firn at Summit after parameterization of the model (*b*, *d*, and *f*).

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