

# $^{15}\text{N}$ - $^{15}\text{N}$ Proton Assisted Recoupling

## **Supporting Information**

*Józef R. Lewandowski, Gaël De Paëpe, Matthew T. Eddy, Robert G. Griffin*

Department of Chemistry and Francis Bitter Magnet Laboratory, Massachusetts Institute  
of Technology, Cambridge, Massachusetts 02139, USA.

Atom	X	Y	Z	$\delta_{\text{iso}}$ (ppm)	$\delta_{\text{aniso}}$ (ppm)	$\eta$
N <sub>35</sub> N	6.433	0.681	21.962	-5	-106	0.2
N <sub>35</sub> H	5.718	1.142	21.364	5	-110	0.2
D <sub>36</sub> N	5.419	-1.641	23.313	0	5.7	0.65
D <sub>36</sub> H	4.904	-1.32	22.468	0	5.7	0.65

**Table S11.** Atom coordinates and chemical shift values of the spin system used in the numerical simulation in the Fig. 2. The coordinates are taken from the x-ray structure of GB1 protein (PDB ID 2GI9). The <sup>1</sup>H's were added in Chimera<sup>81</sup> and NH bonds adjusted to 1.04 Å in Accelrys DS Visualizer 2.0.

Atom	X	Y	Z	$\delta_{\text{iso}}$ (ppm)	$\delta_{\text{aniso}}$ (ppm)	$\eta$
K <sub>31</sub> N	3.707	3.18	17.231	-5	-106	0.2
Q <sub>32</sub> N	2.57	1.986	19.467	5	-110	0.2
Y <sub>33</sub> N	3.579	-0.659	18.994	1	-106	0.2
A <sub>34</sub> N	6.33	-0.189	19.299	3	-110	0.2
K <sub>31</sub> H	2.982	3.7	16.696	5	5.7	0.65
Q <sub>32</sub> H	1.892	2.273	18.733	0	5.7	0.65
Y <sub>33</sub> H	3.186	-0.156	18.173	0	5.7	0.65
A <sub>34</sub> H	5.812	0.508	18.727	0	5.7	0.65

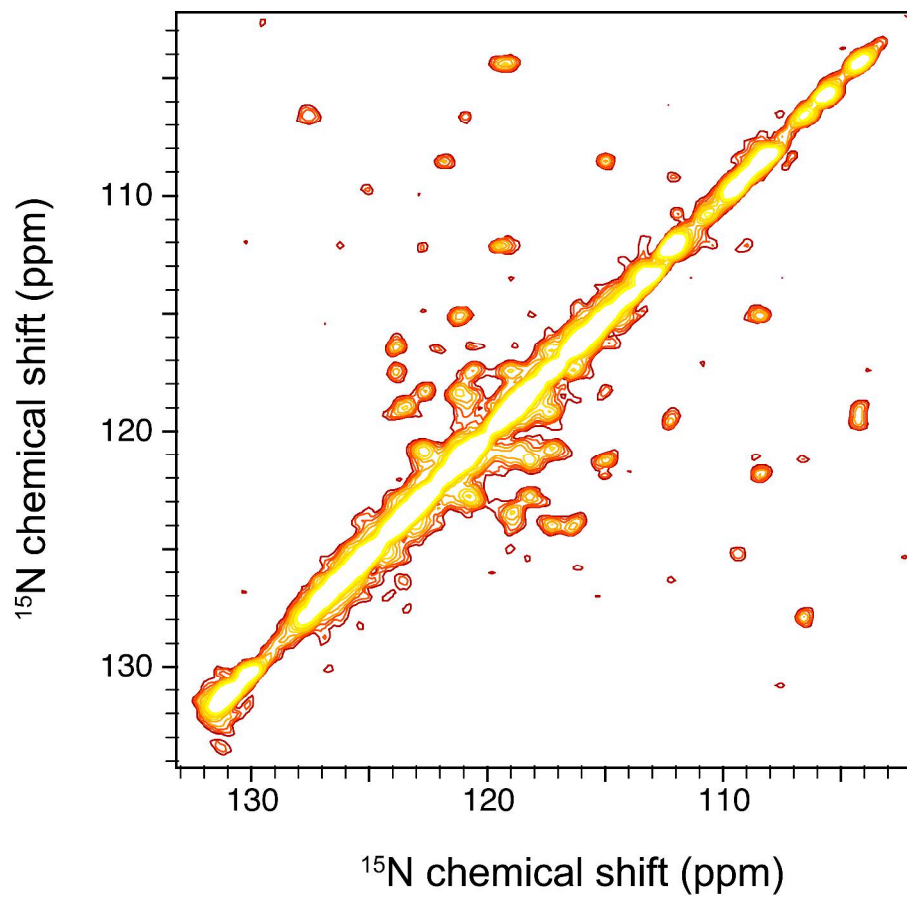
**Table S12.** Atom coordinates and chemical shift values for the  $\alpha$ -helix spin system used in simulation in Fig. 5. The coordinates are taken from the x-ray structure of protein GB1 (PDB ID 2GI9) and NH bonds adjusted to 1.04 Å in Accelrys DS Visualizer 2.0.

Atom	X	Y	Z	$\delta_{\text{iso}}$ (ppm)	$\delta_{\text{aniso}}$ (ppm)	$\eta$
T <sub>43</sub> N	11.226	9.874	16.505	-5	-106	0.2
T <sub>44</sub> N	10.639	9.569	12.975	5	-106	0.2
T <sub>45</sub> N	8.75	10.166	9.967	2	-106	0.2
T <sub>53</sub> N	10.547	5.747	11.227	-3	-106	0.2
V <sub>54</sub> N	12.114	4.79	14.309	1	-106	0.2
T <sub>43</sub> H	10.945	10.753	16.916	0	5.7	0.65
T <sub>44</sub> H	10.777	8.569	12.993	0	5.7	0.65
T <sub>45</sub> H	8.907	11.164	9.947	0	5.7	0.65
T <sub>53</sub> H	10.255	6.709	11.323	0	5.7	0.65
V <sub>54</sub> H	12.455	3.893	13.995	0	5.7	0.65

**Table SI3.** Atom coordinates and chemical shift values for the spin system used in the simulation in Fig. 6b. The coordinates are taken from the x-ray structure of protein GB1 (PDB ID 2GI9) and NH bonds adjusted to 1.04 Å in Accelrys DS Visualizer 2.0.

Atom	X	Y	Z	$\delta_{\text{iso}}$ (ppm)	$\delta_{\text{aniso}}$ (ppm)	$\eta$
D <sub>230</sub> N	-38.088	27.067	-13.66	-3	-106	0.2
I <sub>231</sub> N	-34.794	26.728	-12.382	-5	-106	0.2
R <sub>232</sub> N	-31.47	27.642	-12.164	1	-106	0.2
V <sub>267</sub> N	-34.544	21.857	-11.351	5	-106	0.2
V <sub>268</sub> N	-31.194	22.88	-11.52	2	-106	0.2
D <sub>230</sub> H	-38.252	27.981	-13.191	0	5.7	0.65
I <sub>231</sub> H	-34.757	25.695	-12.496	0	5.7	0.65
R <sub>232</sub> H	-31.714	28.643	-12.306	0	5.7	0.65
V <sub>267</sub> H	-34.665	20.829	-11.247	0	5.7	0.65
V <sub>268</sub> H	-31.439	23.889	-11.464	0	5.7	0.65

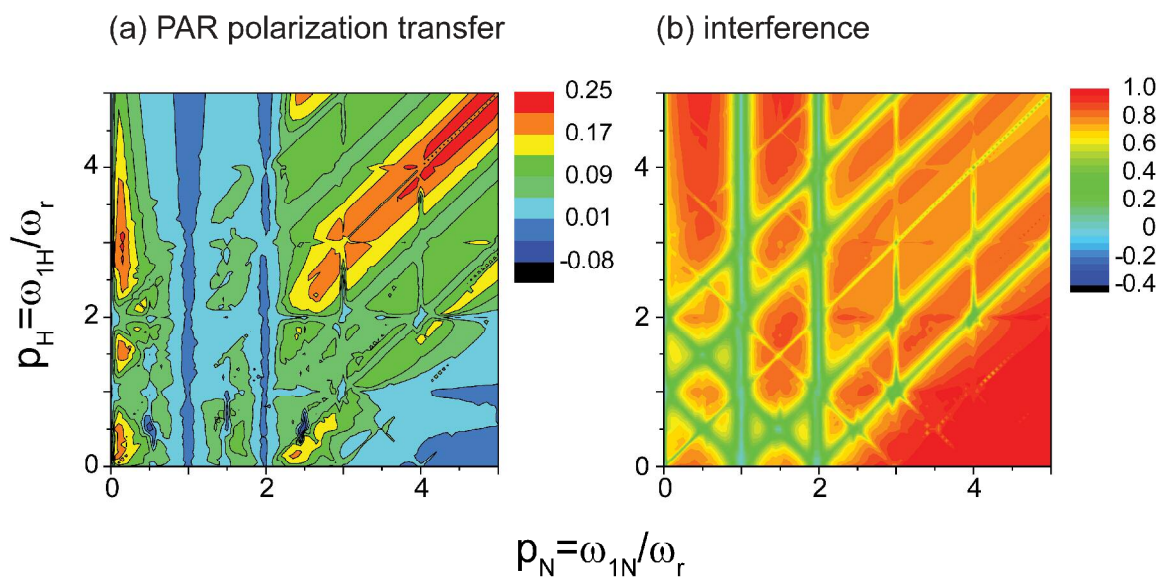
**Table SI4.** Atom coordinates and chemical shift values for the spin system used in simulation in Fig. 6d. The coordinates are taken from the model 0.1 from the SSNMR structure of HET-s (218-289) prion (PDB ID 2RNM) and NH bonds adjusted to 1.04 Å in Accelrys DS Visualizer 2.0.



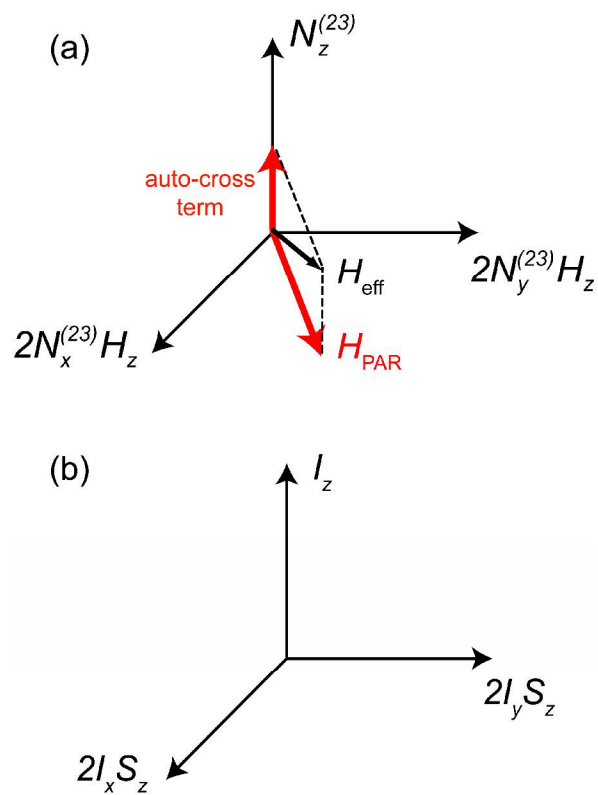
**Figure S11.** 2D  $^{15}\text{N}$ - $^{15}\text{N}$  PAR correlation spectrum on  $[1,3\text{-}^{13}\text{C},\text{U-}^{15}\text{N}]$ -protein GB1. The spectrum was obtained using 22 ms PAR mixing with  $\sim 4$  kHz  $^{15}\text{N}$  and  $\sim 52$   $^1\text{H}$  CW irradiation at  $\omega_r/2\pi=20$  kHz MAS and  $\omega_{0\text{H}}/2\pi=900$  MHz.

Assignment	$\omega_1$ (ppm)	$\omega_2$ (ppm)	Assignment	$\omega_1$ (ppm)	$\omega_2$ (ppm)	Assignment	$\omega_1$ (ppm)	$\omega_2$ (ppm)
M1N-Q2N	40.1	125.3	V29N-F30N	119.0	118.3	D46N-D47N	126.8	123.4
L5N-T16N	126.9	115.2	F30N-V29N	118.2	119.0	D46N-T51N	126.4	112.2
L7N-G14N	127.0	105.6	F30N-K31N	118.7	120.6	D47N-D46N	123.3	126.4
N8N-G9N	125.2	109.5	K31N-F30N	120.7	118.6	D47N-A48N	123.5	119.0
G9N-N8N	109.7	125.0	Q32N-K31N	121.2	119.9	A48N-D47N	119.0	123.3
K10N-T11N	121.1	106.6	Y33N-A34N	121.0	122.6	A48N-T49N	118.9	104.1
T11N-K10N	106.5	121.0	A34N-Y33N	122.5	121.0	T49N-A48N	104.4	119.1
T11N-L12N	106.6	127.6	A34N-N35N	122.5	118.1	T49N-K50N	104.4	119.5
L12N-T11N	127.8	106.6	N35N-A34N	118.5	122.7	K50N-T49N	119.4	104.3
G14N-L7N	105.6	127.1	N35N-D36N	118.3	121.2	K50N-T51N	119.5	112.2
T16N-L5N	115.3	126.8	N35N-N37N	118.3	115.0	T51N-D46N	112.3	126.4
A23N-A24N	122.8	120.6	D36N-A34N	121.3	122.5	T51N-K50N	112.3	119.5
A24N-A23N	120.6	122.8	D36N-N35N	121.2	118.2	T51N-F52N	112.3	130.1
A24N-T25N	120.7	117.2	D36N-N37N	121.2	115.0	F52N-T51N	130.3	112.2
A24N-A26N	120.8	123.8	N37N-N35N	115.0	118.1	T53N-T44N	112.2	109.0
T25N-A24N	117.4	120.5	N37N-D36N	115.1	121.1	T53N-V54N	112.3	118.5
T25N-A26N	117.4	123.8	N37N-G38N	115.1	108.4	V54N-T53N	118.5	112.1
A26N-A24N	124.0	120.6	G38N-N37N	108.5	115.0	T55N-E42N	124.1	119.1
A26N-T25N	124.0	117.2	G38N-V39N	108.6	121.7			
A26N-E27N	123.9	116.4	V39N-G38N	121.8	108.4			
E27N-A26N	116.5	123.9	D40N-V39N	131.2	121.6			
E27N-K28N	116.5	117.2	D40N-G41N	131.0	108.2			
K28N-E27N	117.5	116.3	G41N-D40N	108.4	131.2			
K28N-V29N	117.4	118.8	E42N-T55N	119.3	124.0			
V29N-K28N	119.1	117.3	T44N-T53N	109.1	112.1			

**Table SI5.** Cross-peaks observed in the spectra in Fig. 4. The sequential cross-peaks in the loop regions are highlighted in red, sequential cross-peaks in the  $\alpha$ -helix are highlighted in green, and interstrand cross-peaks within the antiparallel  $\beta$ -sheets are highlighted in blue.



**Figure SI2.** Comparison of the  $^{15}\text{N}$ - $^{15}\text{N}$  PAR polarization transfer map (a) and the interference map (b). Simulation was performed for the spin system described in Table SI1 using 20 ms of PAR mixing at  $\omega_r/2\pi=20$  kHz MAS and  $\omega_{0H}/2\pi=750$  MHz. In the PAR optimization map the polarization transfer between the nitrogens is monitored as a function of nitrogen ( $p_N$ ) and proton ( $p_H$ ) irradiation in units of spinning frequency. In the interference map the decay of the magnetization on the nitrogens after the PAR mixing is monitored as a function of nitrogen ( $p_N$ ) and proton ( $p_H$ ) irradiation in units of spinning frequency. The initial magnetization is prepared on the x-axis on one of the nitrogens in (a) and on both nitrogens in (b).

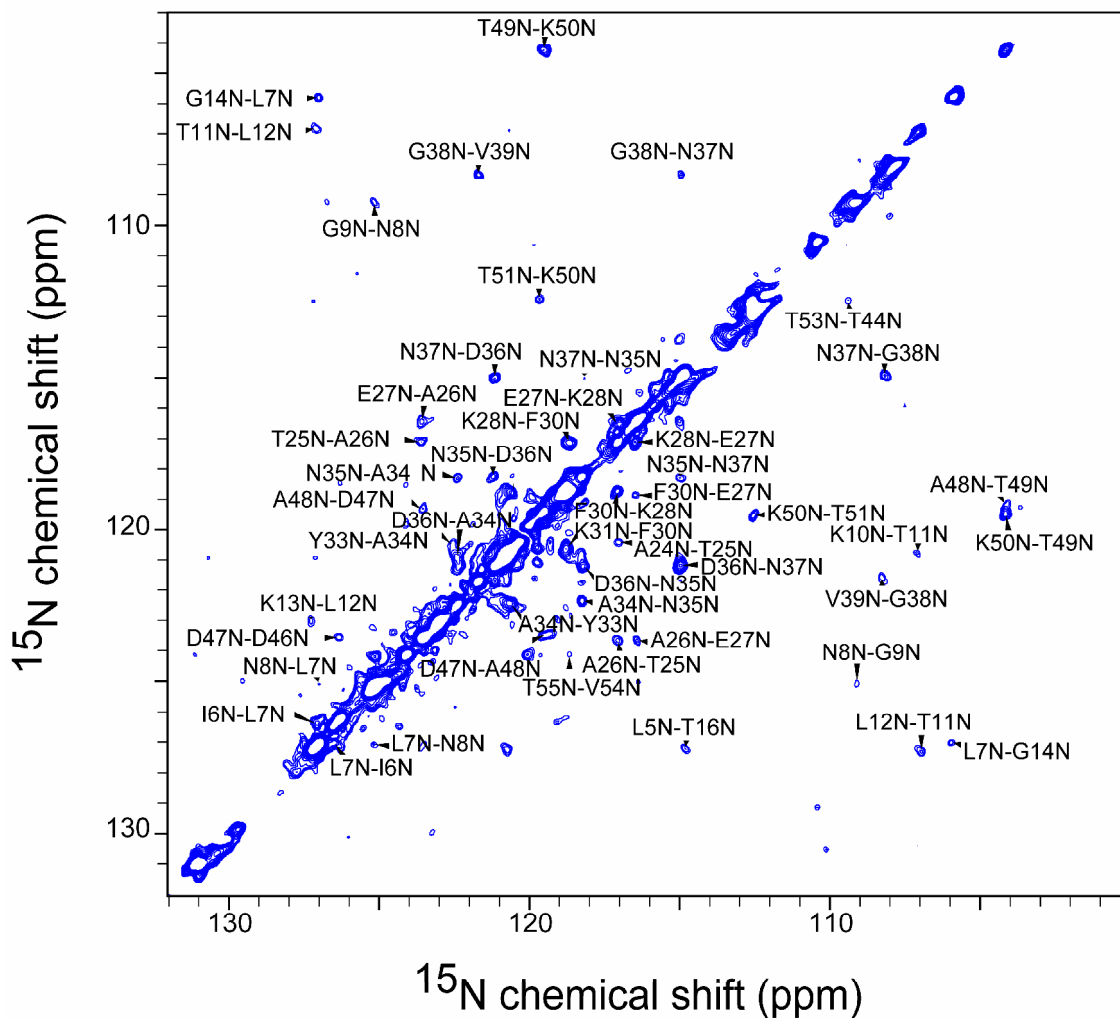


**Figure S13.** Visualization of the PAR subspace. The space can be seen as a coupled basis between a fictitious ZQ operator involving the two carbons (or nitrogens) and a proton spin. The red arrows indicate PAR recoupling axis and longitudinal tilting field resulting from auto-cross terms. Panel (b) depicts the coupled basis encountered in solution NMR.

Atom	X	Y	Z	$\delta_{\text{iso}}$ (ppm)	$\delta_{\text{aniso}}$ (ppm)	$\eta$
T <sub>44</sub> N	10.639	9.569	12.975	-5	-106	0.2
T <sub>53</sub> N	10.547	5.747	11.227	5	-106	0.2
W <sub>43</sub> H <sub><math>\alpha</math></sub>	10.835	8.369	15.129	0	5.7	0.65
W <sub>4</sub> H <sub><math>\beta</math>3</sub>	8.402	9.135	14.812	0	5.7	0.65
W <sub>43</sub> H <sub><math>\epsilon</math>3</sub>	7.851	6.796	14.29	0	5.7	0.65
T <sub>44</sub> H	10.781	8.539	12.994	0	5.7	0.65
T <sub>44</sub> H <sub><math>\alpha</math></sub>	10.044	11.236	11.893	0	5.7	0.65
T <sub>44</sub> H <sub><math>\gamma</math>2</sub>	13.117	10.317	12.407	0	5.7	0.65
T <sub>53</sub> H	10.246	6.738	11.326	0	5.7	0.65
T <sub>53</sub> H <sub><math>\gamma</math>1</sub>	14.093	7.513	11.659	0	5.7	0.65

**Table SI6.** Atom coordinates and chemical shift values for the spin system used in simulation in Fig. 7. The coordinates are taken from the x-ray structure of protein GB1 (PDB ID 2GI9) and NH bonds adjusted to 1.04 Å in Accelrys DS Visualizer 2.0.





**Figure S14.** 2D  $^{15}\text{N}$ - $^{15}\text{N}$  PAR correlation spectrum on  $[\text{U-}^{13}\text{C}, ^{15}\text{N}]$ - protein GB1. The spectrum was obtained using 20 ms PAR mixing with  $\sim 71$  kHz  $^{15}\text{N}$  and  $\sim 69$   $^1\text{H}$  CW irradiation at  $\omega_r/2\pi=11.11$  kHz MAS and  $\omega_{0\text{H}}/2\pi=500$  MHz. The acquisition time was 46.1 ms in  $t_1$  and 46.1 ms in  $t_2$ . The temperature (as read by thermocouple) was maintained at  $-5^\circ\text{C}$  using 50 scfh flow of nitrogen.