#### Modular Coherence of Protein Dynamics in Yeast Cell Polarity

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#### **Supporting Online Material includes:**

Supplementary Methods

Figure S1 to S9

Table S1 to S11

Movie S1 to S5

Reference 1 to 8

#### **Supplementary Methods**

#### **Plasmid construction**

The GFP-Rho1 and GFP-Rho3 integrative plasmids used for the iFRAP analysis were constructed using the pRS306 vector as a template cloned with GFP-linker-myc-Rho1 or GFP-linker-myc-Rho3 inserts under the control of the Rho1 promoter. The functionality of the GFP-Rho1 and GFP-Rho3 tagged proteins was assessed in a growth dilution assay after transformation of the pRS316-based Rho1 and Rho3 plasmids in wild type and *rho1* $\Delta$  and *rho3* $\Delta$  strains with incubation at 23°C or 37°C (Fig. S4). The pRS316 Rho1 and Rho3 plasmids were constructed by cloning the amplified Rho1 and Rho3 inserts from the respective integrative plasmids, including the Rho1 promoter, into the pRS316 vector.

#### Yeast Cell wall growth rate analysis

After growing overnight at 23°C, wild type and *pea2* $\Delta$  cells were washed with 1xPBS buffer and stained for 10 min with FITC-ConA (5µg/ml, Sigma). Cells were then returned to growth at 23°C for 10 min, 20 min, 30 min and 40 min respectively, washed and fixed with 5% formaldehyde at room temperature for 20min. Thereafter cells were washed and stained with Texas Red-ConA (5µg/ml, Molecular Probes) for 10 min. Cells were washed again using 1 x PBS buffer and imaged using confocal microscopy.

#### **Identification of robust modules**

Given a network, for a certain partition P of the nodes into modules, the modularity M(P) is defined as (1):

$$M \equiv \sum_{s=1}^{N_M} \left[ \frac{l_s}{L} - \left( \frac{d_s}{2L} \right)^2 \right]$$

where  $N_M$  is the number of modules, *L* is the number of links in the network,  $l_s$  is the number of links between nodes in module *s*, and  $d_s$  is the sum of the connectivity (degrees) of the nodes in module *s*. Modules (and the optimal number of modules) are typically identified by selecting the partition  $P^*$  that maximizes M(P)(2). Two issues, however, make direct maximization of the modularity inappropriate for the identification of modules in protein interaction networks. First, protein interaction data reportedly contain numerous false positives and false negatives(3). Second, two different partitions of the same network can have very similar values of modularity, so that by only looking at the partition with the largest modularity some potentially relevant information is lost (4). To overcome these problems and obtain robust modules, we combine modularity maximization with an algorithm that enables one to identify both plausible missing interactions and observed interactions that are likely to be spurious (5).

Specifically, we repeat the following procedure 100 times (Fig. S2 A-D):

(i) From the observed cell polarity protein interaction network (which presumably contains errors and omissions with respect to the unknown *true* protein interaction network), we obtain a "reconstructed network" (2).

(ii) The reconstruction is built by adding plausible missing interactions and removing plausible spurious interactions, using the algorithm described in (4). In general, the reconstructed network has been shown to be closer to the true network than the observed network itself (5).

(iii) We obtain the modules in the reconstructed network by maximizing the modularity.

We obtain 100 reconstructed networks with maximal modularity value. Because of the stochasticity of the reconstruction algorithm, each reconstructed network is slightly different, and so are the modules. With the modules for each of the 100 reconstructed networks, we build a similarity matrix S whose element  $S_{ij}$  is the fraction of times which proteins i and j were placed in the same module (Fig. S2 A-D). From this matrix, we obtain the consensus modules by identifying groups of proteins that are consistently placed in the same module in the reconstructions (5) (Fig. 1A and Fig. S2 A-D).

#### iFRAP experiments, analysis of time-lapse movies and FRET measurements

In all iFRAP experiments, bleaching was applied on the selected area as indicated in Fig. 2 using the MicroPoint Mosaic system (Photonic Instruments, Inc., Saint Charles, IL). For proteins with  $t_{1/2}$  around or longer than 60s, such as Pea2, Pkc1, and Rho1, longer image recording (4-min videos) was needed: 9 images before iFRAP bleaching, 241 images after iFRAP bleaching with time intervals of 1 s. Pulse frequency was set to 20/s and bleaching was performed for around 2 s. Time-lapse movies (2-min videos) were produced in a standardized manner for most proteins with  $t_{1/2}$  less than 40 s: 31 images before photo bleaching, 241 images after photo bleaching, and time interval between every two images is 0.5 s (thus it takes less than 2.5 min to obtain one time-lapse movie). For Mkk1 which has  $t_{1/2}$  less than 40 s, shorter movies were made on APD confocal microscope (ZEISS): 7 images before, and 80 images after iFRAP bleaching. For each time-lapse movie, background was subtracted and at least one control cell was used for the acquisition of photobleaching correction.

From every iFRAP time-lapse movie, log file created by Metamorph to record cellular fluorescence was uploaded into IDL 7 for background subtraction and curve analysis. Correction

from photobleaching and final curve fitting were performed using OriginPro 8 with custom-made codes. ImageJ 1.4 (http://rsb.info.nih.gov/ij) was used occasionally for visualization and quantification. For image photobleaching correction, the background-subtracted fluorescence intensity in the two control cells in every time-lapse iFRAP movie was fitted to the equation

$$Y = A e^{-m}$$

where Y is the average fluorescence in the region of interest, A is the initial fluorescence value, and the factor  $e^{-m t}$  was used for correction of fluorescence intensity in the bleached cell. Only curves with the photobleaching rate lower than ~10% were selected for the next step of quantification.

For iFRAP curve fitting, equation

$$Y = A_0 + A' e^{-\omega t}$$

was used, where  $(A_0 + A')$  is the normalized initial fluorescence value and  $A_0$  is the saturation value; and  $t_{1/2} = \ln 2/\omega$ . For four strains which have low GFP expression level (Gic1, Rom2, Msb4 and Mkk1), every 5 points on iFRAP curve were averaged before iFRAP curve fitting.

For the goodness-of-fit, only the curves with R-square greater than 0.3 were kept for further analysis thus leading to the average R-square value for iFRAP curves in every strain larger than 0.5. For every strain, in order to remove the outliers in  $t_{1/2}$  data set, only the points which are in the range of mean  $\pm 2$  SD were kept.

For the measurement of Rho1 polarization rate in wild-type and  $pea2\Delta$  mutant cells, sigmoid function was used to fit the Rho1 localization curve:

$$y = \frac{A_1 - A_2}{1 + e^{(x - x_0)/k}} + A_2$$

where y is a ratio of GFP-Rho1 average intensity at the polar cortex to an average intensity in the whole cell;  $A_1$  and  $A_2$  are the initial and final value of the ratio which can be adjusted for fitting; 1/k describes GFP-Rho1 cap formation rate at the inflection point.

The acceptor photobleaching FRET experiments and analysis were performed as described in (6). The FRET efficiency image in Fig. S7 was produced by application of the following procedure using ImageJ 1.4 software:

1. Temporal binning by 4 images (before and after photobleaching) to obtain total fluorescence  $F_b$  and  $F_a$  before and after photobleaching respectively.

2. The background was subtracted and images were spatially binned by 8 pixels.

3. For each pixel the FRET efficiency ratio  $F_a / F_b$  was calculated and the result was presented in a color heat map.

The normalized FRET efficiency ratio presented in Fig. S7 was calculated by dividing all FRET efficiency ratios of each protein interacting pair by the mean of their respective negative control, therefore setting the mean of the negative control equal to 1.

#### Modeling polarity protein dynamics

Consider a protein interaction network made of n functional modules. Each module is assigned the characteristic time  $\tau_i$ , i = 1, 2, ..., n. A protein p is characterized by the integer vector  $\mathbf{N}_p = \{\mathbf{N}_{p,1}, \mathbf{N}_{p,2},..., \mathbf{N}_{p,n}\}$  where  $\mathbf{N}_{p,i}$  is the number of interactions of this protein with proteins from the i-th module and is determined by the network modular structure. The lifetime  $T_{p,i}$  of the bond created by the protein p and the protein from the i-th module is defined as the characteristic time of the i-th module, i.e.,  $T_{p,i} = \tau_i$ . We estimate  $\tau$ 's using multivariate regression as:

$$\tau_{p,j} = \sum_{i=1}^{n} \frac{N_{p,i}}{N_p} \tau_i + e_{p,j}$$

where  $\tau_{p,j}$  represents the residence time for the j-th measurement of the p<sup>th</sup> protein (experimentally obtained);  $\tau_i$  represents the residence time for the i<sup>th</sup> module;  $N_{p,i} / N_p$  represents the percentage of connections to the i<sup>th</sup> module for the p<sup>th</sup> protein;  $N_p = \sum_{i=1}^n N_{p,i}$  is the total module connection for the p<sup>th</sup> protein;  $e_{p,j}$  is the error term.

The regression analysis was performed using SAS 9.2. We first used the data from the 29 proteins to see how well the model (Eq.2) fits the data. Then, we use a set of 10 proteins (either a chosen set or randomly drawn sets from 29 proteins without replacement, see Results), each protein having at least 10 measurements to estimate the residence time for five modules. The square root of the error mean square was recorded. This Eq.2 model was used to predict the mean residence time for those proteins not included in the training set. Pearson correlation coefficients and p-value between the predicted values and the observed mean values were calculated.

#### Protein dynamics and the Kuramoto model

In adapting concepts of the Kuramoto model to explain the dynamical properties of proteins in cell polarity, we consider each protein in the PCD network as a unit oscillator (oscillating between cytoplasmic and polar cortical locations) interacting with the five modular oscillators corresponding to the five sub-functions intrinsically harbored in the PCD network. Each modular oscillator is akin to a Kuramoto's "giant oscillator", however, the original theory only deals with unimodal distribution of oscillator frequencies. Pre-defining modular oscillators based on network modularity precludes the bottom up approach used in the original theory to describe the spontaneous emergence of giant oscillators as a result of oscillator coupling, but with this assumption we aimed to explore the mathematical relationship between the dynamics of

unit oscillators with the modular oscillators once the system has evolved to a steady-state, where the behavior of the "giant oscillators" is stably established (see below).

The original Kuramoto model (7) describes the phase dynamics of N>>1 identical oscillators governed by the equations  $d\phi_i/dt = \omega_i + \epsilon/N \Sigma_{j=1} \sin(\phi_j - \phi_i)$ , where  $\epsilon$  is the strength of interaction,  $\phi_i$  (t) is the phase and  $\omega_i$  is the natural frequency of i-th oscillator. The distribution of frequencies  $g(\omega)$  is assumed to be unimodal centered around  $\omega = \omega_0$ . When the interaction strength  $\epsilon$  reaches a critical value  $2/(\pi g(\omega_0))$ , this system of oscillators self-organizes into the "giant oscillator" characterized by a single frequency to which all unit oscillators are locked. In reference (8) it was shown that for bimodal frequency distribution, one observes emergence of two "giant oscillators" with different frequencies.

Viewing the modular structure of the PCD network as a set of five "giant oscillators", one can ask: how is the dynamics of a single unit oscillator governed by the network structure. We assume that the dynamical properties of the "giant oscillators" are not affected by their interaction with unit oscillators.

Then the phase  $\phi(t)$  of the unit oscillator with a natural frequency  $\omega$  is governed by the equation  $d\phi/dt = \omega + \epsilon \Sigma_{i=1} w_i \sin(\omega_i t - \phi)$ , where  $\omega_i$  is the i-th "giant oscillator" frequency and  $w_i$  is the weight of i-th module proportional to the number of interactions of the unit oscillator with this module ( $\Sigma_{i=1} w_i = 1$ ). The numerical simulations of this model show that independently of the natural frequency  $\omega$  value of the unit oscillator, the oscillator frequency is locked to a constant value determined by the frequencies and weights of the network modules.

One can further simplify the model by replacing the nonlinear phase interaction with a linear one, so that the governing equation reads  $d\phi/dt = \omega + \epsilon \sum_{i=1} w_i (\omega_i t - \phi)$ . This equation admits

a stable steady state solution corresponding to the observed oscillator frequency equal to the weighted mean of the "giant oscillator" frequencies  $\Sigma_{i=1} w_i \omega_i$ . As we represent and measure the dynamics of proteins in the PCD by their residence times, it would be reasonable to consider a model that postulates the observed residence time  $\tau_p$  of protein p (analogous to of the observed frequency of a unit oscillator) as weighted mean of the modules characteristic kinetic parameter  $\tau_i$  (analogous to giant oscillator frequency  $\omega_i$ ) as follows  $\tau_p = \sum_{i=1} w_i \tau_i$ . The last transformation from the frequency to residence time dynamical description is not justified mathematically, but the analysis performed shows that the residence time approach describes the experimental measurements much better than the frequency-based one.

#### **Modularity Test**

To address the issue of the unimodular network structure our model predicts a single residence time t for all network components computed as simple or weighted mean of measured  $t_{1/2}$ . To compute the correlation between the predicted and observed values we used *Mathematica* 7.0.1 to generate 10000 sets of 29 random numbers with the average equal to t and standard deviation equal to that of the measured  $t_{1/2}$ . The correlation of each set with the observed values was computed and the results were averaged showing that no correlation exists, the average correlation value is 0 with the standard deviation equal to 0.07. No correlation was found greater by absolute value than 0.24.

#### **Statistics**

For the analysis comparing average  $t_{1/2}$  values for two modules (Signaling and Transport), we fitted a model including module effect and protein effect such that the protein

effect was considered as nested within the module. We also fitted a model without considering the module effect to compare the difference between all proteins. Tukey method was used for pair-wise comparison. For the analysis comparing cell wall growth between wild-type and mutant cells, we fitted a two way ANOVA model including time, genotype (wild-type and mutant), and their interaction effect. For the analysis comparing the average  $t_{1/2}$  values between a protein itself to its directly interacting proteins or to its indirectly interacting proteins (Table S8), we fitted a one way ANOVA model.

#### **Supplementary Figure Legends**

**Fig. S1**. A network of polarity protein interactions. Polarity protein network contained 99 nodes and 302 linkages obtained from BioGrid database (version 2.0.51), visualized in Cytoscape version 2.6.3.

**Fig. S2**. Identification of robust modules. From the observed protein interaction network (*A*), we build 100 reconstructions following Ref. (2) (*B*). For each of the reconstructed networks, we identify modules by maximizing modularity (4); therefore, we obtain 100 partitions of the nodes into modules (*C*). From the 100 partitions, we build a similarity matrix *S* whose element  $S_{ij}$  is the fraction of times which proteins *i* and *j* are in the same module (*D*). From this matrix, we obtain the consensus modules using the box identification procedure described in Ref.(5).

**Fig. S3.** A protein-protein similarity matrix based on the polarity protein interaction network was constructed and ordered using the network analysis scheme discussed in the text and Figure S2. Modules can be observed as distinct groups of nodes (outlined by black lines).

**Fig. S4**. Functional analysis of GFP-tagged Rho1 and Rho3 at different temperatures (23°C and 37°C). GFP-Rho1 and GFP-Rho3 plasmids were transformed into wild type, and the respective deletion mutant and growth analysis were performed using a 5 fold dilution drop test.

**Fig. S5**. A lack of correlation between  $t_{1/2}$  and node properties. Scatter plots are shown of  $t_{1/2}$  versus (*A*) Degree, (*B*) Betweenness, and (*C*) Participation coefficient for each protein. Additional correlation analysis results can be found in Table S7.

**Fig. S6**. The dynamics of two proteins in the Mitotic Exit module assessed by iFRAP. Statistical representation is the same as described in Figure 2*D* legend.

**Fig. S7**. FRET efficiency analysis of Pea2 and Rho1 interaction. (*A*) Pixel average FRET efficiency analysis of Pea2 and Rho1 interaction in cells expressing Pea2-mCherry and GFP-Rho1. The FRET efficiency (FE) is defined as the fluorescence intensity after photobleaching divided by the intensity before photobleaching. Scale bars:  $1\mu$ m. (*B*) Analysis of FE at the bud cortex in cells expressing Pea2-mCherry and GFP-Rho1 compared with cells expressing Pea2-GFP and Spa2-mcherry (as positive control for FRET). Cells expressing Spa2-GFP or GFP-Rho1 alone were used as negative control for FRET. FE values were normalized to the respective negative control average FE.

**Fig. S8**. Effects of *pea2* $\Delta$  on the dynamics of 11 polarity proteins (Spa2, Bud6, Rho1, Myo2, Rho3, Lrg1, Rga1, Cdc42, Bni1, Pkc1 and Yor304c-a). The dynamics were measured as iFRAP  $t_{1/2}$  and represented as in the legend of Figure 2*D* and *E* (p-value was obtained using t-test, equal variance assumed).

Fig. S9. Polarization of Rho1 in wild-type and  $pea2\Delta$  cells. Three representative curves obtained from time-lapse imaging of cells of each genotype showing that GFP-Rho1 polarization occurred

at a significantly lower speed in wild-type cells (A) than in *pea2* $\Delta$  mutants (B). Images of a polarized wild-type (A) and *pea2* $\Delta$  (B) cell with GFP-Rho1 and kymographs of representative movies are shown next to the graphs.

#### **Supplementary Table Legends**

**Table S1**. List of 111 polarity proteins involved in polarity establishment and maintenance.

**Table S2**. 99 proteins were assigned into 5 different modules by the stochastic search algorithm mentioned in the text.

**Table S3**. Participation coefficient and z score to determine the role for every protein in the polarity protein network. The Participation coefficient of a node is close to 1 if its links are uniformly distributed among all modules and 0 if all of its links are within its own module. The within-module degree *z*-score measures how 'well connected' node *i* is to other nodes in the module. Z-score of 0 indicates that the number of links  $\kappa_i$  of node *i* to other nodes in its module  $s_{i,j}$  is equal to the average of  $\kappa$  over all the nodes in module  $s_i$ .

**Table S4**. iFRAP  $t_{1/2}$  values for the 11 GFP tagged proteins in the Signaling module.

**Table S5**. iFRAP  $t_{1/2}$  values for the 18 GFP tagged proteins in the Transport module.

**Table S6**. There is no clear separation of  $t_{1/2}$  values for components of Signaling and Transport modules. Pairwise comparison with Tukey multiple comparison procedure followed by one-way ANOVA was performed to test if there is significant difference in any pairwise comparisons for 29 proteins from the two modules. The proteins with the same letter show non-significant difference from each other (similar to the line plot).

Except for Pea2 and Rho1 that have large  $t_{1/2}$  s, five proteins labeled with letter C (Rga1 from Signaling module, the other four from transport module) have no significant difference from each other. The majority of proteins labeled with letter D belong to either Transport or Signaling module, indicating that proteins from the same module do not always have similar  $t_{1/2}$  s.

**Table S7**. Six commonly used parameters describing network properties and analysis of their correlation with  $t_{1/2}$  values.

The six global network parameters are defined as below:

*Degree*: In graph theory, the degree  $k_i$  of node (vertex) *i* is the number of edges incident to the vertex, with loops counted twice. The degree is a measure of centrality since it provides a rough indication of the importance of a node based on how well it "connects".

*Clustering coefficient*: For node *i*, clustering coefficient is the number of pairs of neighbors of *i* that are connected divided by the total number of possible pairs of neighbors  $k_i$  ( $k_i$  -1) / 2. A clustering coefficient that is higher than that of other nodes indicates greater "cliquishness". For the whole network, one can compute the average clustering coefficient and compare it to the average coefficient expected for the equivalent random network with the same number of nodes and the same degree distribution. For the network we study, the average clustering coefficient is 0.20, which is much bigger than the one in random network.

*Eccentricity*: For node *i*, eccentricity is the largest distance between node *i* and any other node in the graph (provided the other node is in the same connected component). The eccentricity provides another measure of centrality since the node with the smallest eccentricity can be considered as the "closest" one to any other node in the graph.

*Betweenness*: For a given node, betweenness is the number of shortest paths between two nodes in a graph that go through that vertex. The betweenness is also a measure of how central a node is since the higher the betweenness of a node is, the more information flows through this node.

Once nodes are grouped into modules, each node has some connections within its own module (within module degree) and some connections to other modules. In our analysis, we use two measurements of such property:

*Participation coefficient*: For node *i* in module *m*, participation coefficient measures the distribution of connections among the other modules. Nodes with all the connections within their own module have a participation coefficient equal to zero whereas nodes with more connections to several other modules than to its own module have a participation coefficient that is closer to 1.

*Within module degree z-score*: For node *i* in module *m*, within module degree z-score measures how different the number of connections to other nodes in the same modules with respect to the distribution of within module degrees for all of the nodes in the module.

**Table S8**. For most of the 29 proteins that have more than one interaction partners within the PCD network, there is no predictable trend whether their dynamics are more similar to their directly interacting partners vs indirectly-interacting proteins. In this table:

**Direct\_mean** (column B): For a given protein, **direct\_mean** refers to the mean of  $t_{1/2}$  values of all its direct interaction partners among the 29 proteins.

**Indirect\_mean** (column C): For a given protein, **indirect\_mean** refers to the mean of  $t_{1/2}$  values of its indirect interaction partners among the 29 proteins.

**Self\_mean** (clomun D): For a given protein, **self\_mean** is the mean of  $t_{1/2}$  values of this protein.

**Direct p value** (column E): measures the difference between **direct\_mean** (column B) and **self\_mean** (clomun D), that is, the difference between the mean of  $t_{1/2}$  values of a given protein and the mean of  $t_{1/2}$  values of this given protein's direct interaction partners. Colors indicate that there is significant difference (p value < 0.05).

**Indirect p value** (column F): measures the difference between **indirect\_mean** (column C) and **self\_mean** (clomun D), that is, the difference between the mean of  $t_{1/2}$  values of the given protein and the mean of  $t_{1/2}$  values of this given protein's indirect interaction partners. Colors indicate that there is significant difference (p value < 0.05).

**Table S9.** iFRAP  $t_{1/2}$  values for the two GFP-tagged proteins (Kel1 and Lte1) in the Mitotic Exit module.

**Table S10**. iFRAP  $t_{1/2}$  values for the effects of *pea2* $\Delta$  on the dynamics of 11 polarity proteins (Spa2, Bud6, Rho1, Myo2, Rho3, Lrg1, Rga1, Cdc42, Bni1, Pkc1 and Yor304c-a).

**Table S11**. Yeast strains used in this study.

#### **Supplementary Movie Legends**

Movie S1. iFRAP of GFP-Rho3. Frames were taken every 0.5 s. The cell was bleached between frame 31 and 32.

Movie S2. iFRAP of GFP-Rho1. Frames were taken every 1 s. The cell was bleached between frame 9 and 10.

Movie S3. iFRAP of Pea2-GFP. Frames were taken every 1 s. The cell was bleached between frame 9 and 10.

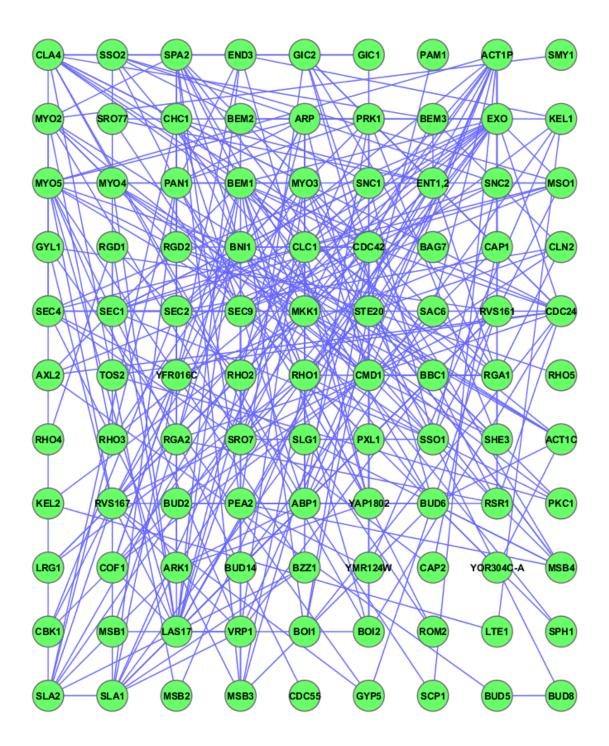
Movie S4. Polarization of GFP-Rho1 in a wild-type cell. Frames were taken every 60 s.

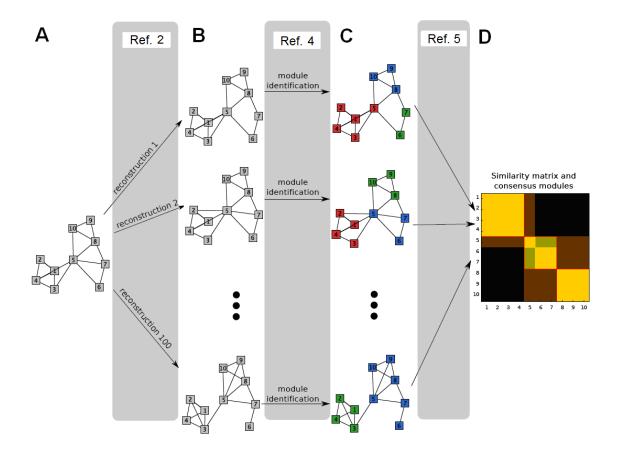
Movie S5. Polarization of GFP-Rho1 in a *pea2*⊿ mutant cell. Frames were taken every 60 s.

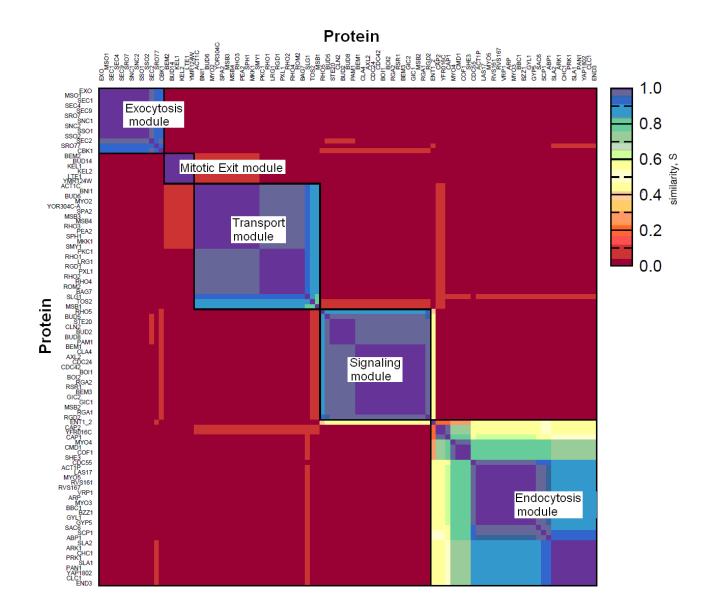
Other iFRAP movies of GFP-tagged proteins in wild type and in mutant cells are available upon request.

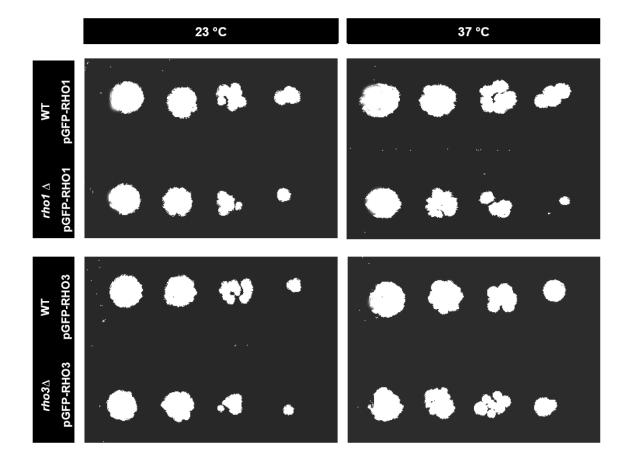
#### Reference

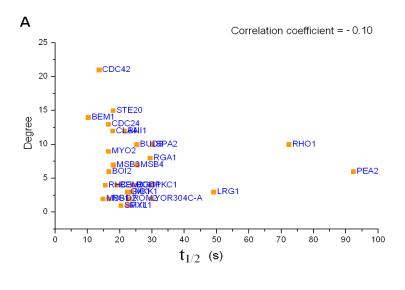
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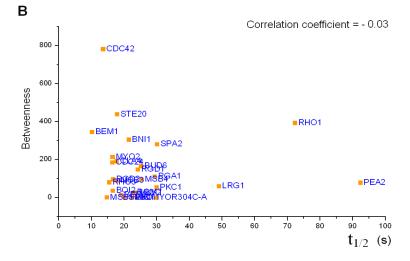


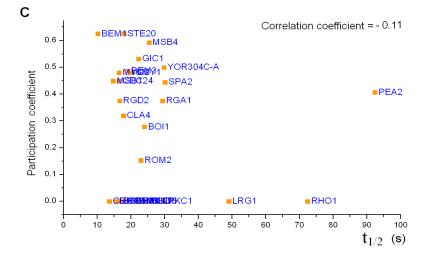


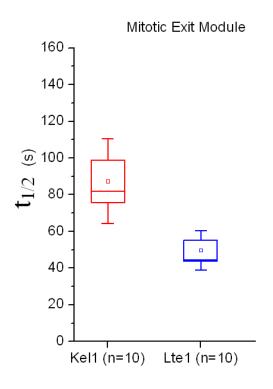


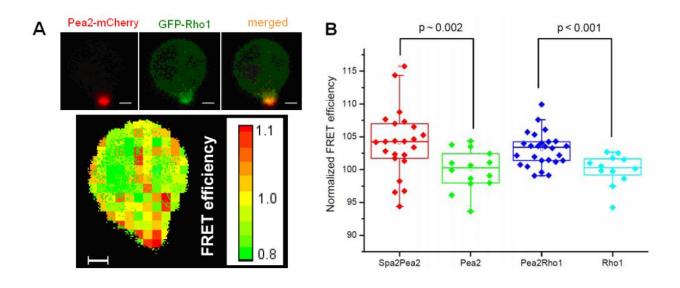


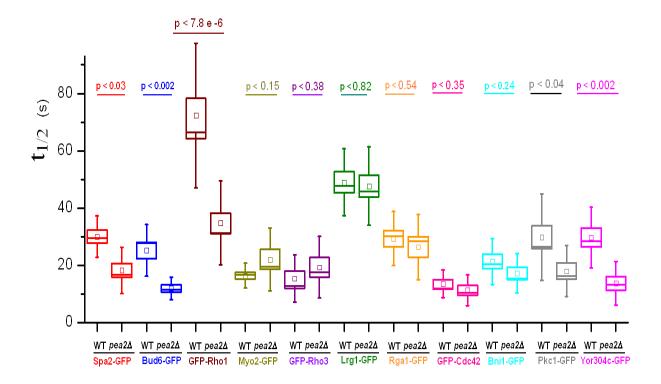


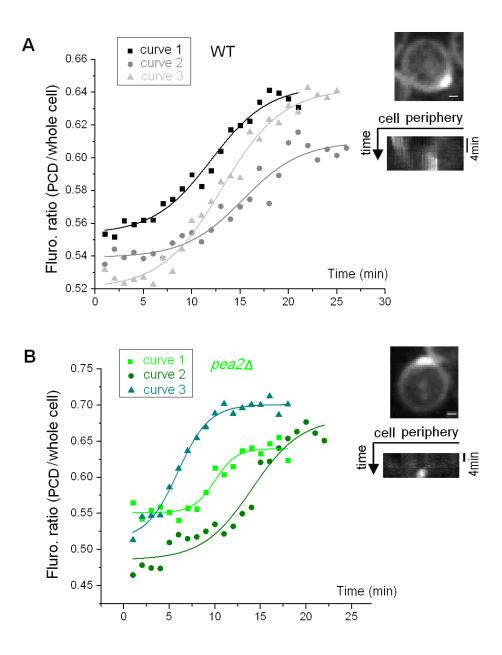












#### Table S1. 111 Proteins in the yeast PCD area

Table S	1. 111 Proteins	in the yeast PCD area	
ORF	protein name	function description	localization
YCRONIW	(as appears in BioGRID) ABP1	Activ-binding protein of the contrast actio overablehister, important for activation of the AnsD2 complex that obsers a law role actio in overablehister organization	bud
YFLODGC	ACTIC	Actin, shudural protein involved in cell polerization, endocytosis, and other cytosieletal functions	contractile ring (sensu Saccharomyces)
YFLODGC YNLODGC	ACT1P ARK1	Actin, structural protein involved in cell polarization, endocytasis, and other cytoslesistis functions Series/Interacting crostellin bitmas involved in resolution of the contral actin cytoslesistics involved in control of endocytasis	contractile ring (sensu Saccharomyces) bud
YNLODC	ARK1 ARP	Serinal/Interaction protein Kinawa insulated is regulation of the control action cytobioletics; insoluted is noticed at a serial control of endocytosis Arg232 complexes and on Acutedian control action control and endocytosis and membranes growth and polarity.	bud
Y1L140W	AXL2	Integral plasma membrane protein required for axial budding in hapkid cells, localizes to the incipient bud site and bud neck	bud neck
YOR134W	BAG7	Pito GTPsea activating protein (PitoGP), elimitates the intrinsic GTPsea activity of Rodip, which plays a rate is actin cylositekton organization and control of oil wall synthesis; intrustanaly and functionaly network to Sac2p Protein possibly involved in assumibly of actin patches; interacts with an actin assumibly boot Last2p and with the SRIG domains of Type I myoeins Myc2p and Myc2p localized predominently to control actin patches	bud
YBR200W	DEMI	Protein containing SHG-domains, involved in establishing cell polarity and morphogenesis	bud tip, bud neck
YERISSC YPL11SC	DEM2 DEM3	Pro GTPsex activating pretein (PlocAP) involved in the control of cytoskellern organization and calibler morphogenesis; required for bud emergences Pro GTPsex activating pretein (PlocAP) involved in control of the cytoskellern organization; tergets the assembly	bud
19L115C	DNH DNH	Formin, nucleates the formation of linear actin filaments, involved in cell processes such as budding and mitotic spindle orientation which require the formation of polarized actin cables, functionally redundent with DNN	bud tip, bud neck
YELDESW	BOH	Protein Implicated in polar growth, functionally redundent with BioDp	bud, bud neck
YER114C	802	Presis insplace on pair growt, functionally methodare with Bolfp Presis insplace in the solution based in subscription	bud, bud neck bud tip, bud neck
196L092C	BUD2	GTPase activating factor for RenfpBudfp required for both satial and bippler budding patients; muterin exhibit random budding in all cell types	bud
YCR038C YLR319C	BUDS	GTP/GDP exchange factor for Rarty (Burtly) required for both axial and tapolar budding patients Activ- and formin-terminolog potein, involved in actin cable nucleation and potenticed oil growth; toolated as bipolar budding muteric potential Cot/JBp substrate	bud neck bud
YLRISOW	BUDS	Acti- and termin-resentang proves, involve in actin clase inucession and possible call grown, societo as opport budging maker posimile Ceculty automate Protein involved in budging automation	butip
11R114W	8221	21G domain protein implicated in the regulation of actin polymerization, able to recruit actin polymerization machinery through its 21G domains, colocalates with control actin patches and Last7p, interacts with type I my rotins	but
YNL278W	CAF120	Part of the exclutionarily-conserved CCRH+NOT transcriptional regulatory complex limited in controlling mRHA initiation, and degradation Apha suburit of the capping protein (CP) heterodimer (Capit) and Capital which binds to the barbed ends of acin Nemets presenting further polymetration; localized predominantly to control acin patches	bud
YILOMC	CAP2	Beta subunt of the capping pretein (CP) heterodriner (CapTp and CapTp) which binds to the barbad ends of actin litements prevening further polymerization; localized predominantly to contical actin patches	bud
YNLIGIW YALOHIW	CBK1	Sanina threanina protein kinasa ihat negulatas call morphogenasis pathanya Gazarian nucleatida exchange factur (2017 or GCP-velacea factor) for Cdo-Dp	bud, bud neck bud neck
YLR229C	CDC42	Small rho-like GTPase, essential for establishment and maintenance of cell potenty	bud tip, bud neck
YGL190C	CDC55	Non-example regulatory subunit B of protein phosphataaa 2A	bud tip, bud neck
YGL206C YJL158C	CHC1 CIS3	Dathin heavy chain, subset of the major cost protein involved in inducellable protein transportand endocytosis; too heavy chains form the clathin inteleton structural component; the light chain (CLCI) is thought to regulate function Mannese-containing dycopotein constituent of the call wall	bud bud lip
174_29000	CLM	Cdc-Qp-activated signal transducing kinase of the PAK (p21-activated kinase) family, which also includes StaQp and Skrify; involved in septin ring assembly, vacuals inheritence, and cytokinesis; phosphoryleties septims Cdc2p and Cdc10p	but
YGR167W YPL256C	CLC1 CLN2	Califoni light chain, suburil of the major coal protein involved in IntraceNute protein transport and endocytoxic, thought to regulate chatrin function, two Califorin housy chains (CPC1) from the califorin tripletion structural component Cil cyclin involved in regulation of the cell cycle, activates CACIDE involved in the protein the Cil cyclin and SAP (SavEgraphic California) and SAP (SavEgraphic California)	bud
YERIOSC	CMD1	G1 cyclin included in regulation of the cell cycle, activates Cdc20(b) kinase b promote the G1 to 5 phase transition; balk G1 spacelic expression depends on transcription factor complexes, MB7 (Saldg-Mtp (s) and SB7 (Sa	bud bud tip, bud neck
Y11.050C	COP1	Collin, promotes actin litement depolarization in a pH-dependent manner; binds both actin monomers and litements and sevens litements; thought to be regulated by phosphorylation at SERH; ubiquitous and essential in eukaryotes	but
YCR017C YER166W	CWH43 DNP1	Putative sensorhansporter problem involved in cell well biogenesis Aminonhanisholishi transiscene (Tisceae) that locatives orienteels) to the searce contributes to endocritate, problem transport and cell polerity. Now 4 Prive 4/Preve	bud tip, bud neck bud
YNLODIC	ENDS	D1 domain-containing protein involved in endocytosis, actin cytoskelesis organization and cell well morphogenesis; forms a complex with Statp and Pantip	bud
	ENT1,2 EXO	Epsito-Bie protein invalued in endocytaxis and actin patch assembly and functionally redundent with Exclp binds clathrin-binding domain motif at C-terminus Essential protein with dual roles in splicescore assembly and exceptoria	bud bud tip, bud neck
114R061C	GICI	Laarena prosen ver oaa na na posoana kaarena yoo seccijotaa Protein of urkonom function insteledin initiation of budding markalitan proteination, interactie with Go-GP van he Cdo-GP van he Cdo-GP van he Cdo-GP van he	but tp, but neck but tp, but neck
YDR309C	GIC2	Protein of unknown function involved in initiation of budding and cellular polarization, interacts with Cdx42/Rac-Interactive binding (CR80) domain	bud lip
YMR192W YPL249C	GYL1 GYP5	Putates GTRees exclusing protein (GAP) that may have a role in polarized excrytonia GTRees-exclusing patient (GAP) for years Rob banky members, involved in ER to Gabi halficking	bud, bud tip, bud neck bud tip, bud neck
YMRIGIC	INP2	Perositome-specific receptor important for perositome inheritance; co-fractionales with perositome membranes and co-localizes with perositomes in vice; physically interacts with the myosin V motor Myo2; BP2 is not an essential gene	bud
YORISAC	KEL1 KEL2	Prolein required for proper cell fusion and cell morphology Prolein that functions in a complex with Netly to required in mixide cest, interacts with Temp and Liefp	bud tip, bud neck bud tip, bud neck
YORIBIW	LASI7	Present indications in a comparison want to indicate and an and a second and a	bud sp, dud neck bud
YOLDHOW	LRGI	Putation GTPsee-activating protein (GAP) involved in the Pitc1p-mediated signaling pathway that controls cell wall integrity	bud neck
YALG24C YOR231W	LTE1	Putative GZP/GTP exchange factor required for mixeds with a low temperatures. Mitogen-activated kinase kinase involved in protein Konae C signaling pathway that controls cell integrity.	bud bud to
YOR100W	MSD1	Protein involved in positive regulation of both 1,3-bets-glucan synthesis and the Pic 1p-MAPK pathway, potential Cdc2lip substrate	bud tip, bud neck
YGR014W YNL2SOW	MSB2 MSB3	Much tenty member involved in the Cdx-Dp- and MAP linear-dependent Elementous growth signaling pathway; also functions as an correspondent to the Shorlp-mediated pathway; potential CdcDp auduttatie GTP-searchwains protein for Shorlp- and MAP linear-dependent Elementous growth signaling pathway; also required for protein actin correlation	bud bud tio
YOL112W	NSD4	ucrimate-accessing present to store prote several one readour strates, and passes accopation as an accord on access, and regarded presented by the accessing acc	but tp but tp
YNROUSC	MSO1 MYO2	Probable component of the secretory vesicle docking complex, acts at a late step in secretory; shows genetic and physical interactions with Sec1p; required for prospone membrane formation during apprulation	bud
YOR326W YKL129C	MYC2 MYC2	One of two type V mycelin motions (alking with MHC4) included in activitiated transport of cargos; required for the polanized delivery of ascentory vanicies, the accusal, alta Celgi elements, pervetacemes, and the initiais apindle One of two type I myceline, localizes to activity cardinal percent of MHC3 has little effect on growth, but myc3 myc5 double deletion causes server defects in growth and activity vanices.	bud
YAL029C	MYO4	One of two type V myosin motors (along with MFO2) involved in actin-based transport of cargos; required for mRNA transport, including ASH1 mRNA, and tacilitating the growth and movement of ER tubules into the growing bud along with SheDp	bud
YMR109W YDR251W	MYOS PAMI	One of two type I myosine; contains prolew-rich tail homology 2 (THQ) and SHQ domains; MPCIS deleton has little effect on growth, but myo2 myo2 double deleton causes servere defects in growth and actin cytosleakton organization Example creater of uninnees homology	bud bud, bud neck
11R006C	PANI	Part of actin cytoteketon-regulatory complex Part p-Sattp-EndDp, associates with actin patches on the cell contex protein-protein interactions essential for endocytosis; previously thought to be a suburit of poly(A) riboractease	bud
YER149C YEL105C	PEA2 PKC1	Colled-coll potentiame protein required for potential marphogenesis, cell halon, and be allfinly Cu2+ influx; forms potentiane complex with Binlip, Budlip, and Spindly, boalase to stee of potentiand growth Protein serine/Invencine kinase essential for cell wall remodeling during growth; boaland to stee of potentiand growth and the motive-daughter bod reach; hormolog of the sights, beta, and germa ladores of marmalian protein kinase C (PKC)	bud
YILOSSW	PRC1	Protein autointrecons xusas essena to ce via introcensi guing grave, tocasanto tasse of parates grave not an intervenent xusas (a second of the approximation of the activity capability of the activity of the activity capability of the activity capability of the activity capability of the activity of the act	but
THROSOW	PKL1	LBI domain-containing protein that localizes to sites of polarized growth, required for selection and/or maintenance of polarized growth sites, may modulate signaling by the GP/ases CdoRp and Photp	bud, bud tip, bud neck
YOR127W YDR379W	RGA1 RGA2	GT7 ase-activating protein for the polarity-autibility meet protein Col-Opy, implicated in control of augein organization, pheremone response, and hepidid invasive growth GT7 ase-activating protein for the polarity-autibilityment protein Col-Opy, implicated in control of augein organization, pheremone response, and hepidid invasive growth: regulated by PholiDp and Col-Olip	bud
YBR250C	RGD1	GTPsee-activating protein (PhoGAP) for PhoSp and Pho4p, possibly involved in control of actin cytoskeleton organization	bud
YFLOI7W YFRI65W	RGD2 RHD1	GTP-bindrappotein (RhoGAP) for Cdx-Dp and Rhodp GTP-bindrappotein of the the subfamily of Rau-Hauspoteins, involved in establishment of cell soburity	bud neck bud tip, bud neck
176L090W	RHO2	Non-essential small GTPase of the PhoRac subbmilly of Pass-like proteins, involved in the establishment of cell polarity and in microtubule assembly	bud
Y1L110W	RHO3 RHO4	Non-essential small GTPase of the Rho/Rac subtamily of Ras-like proteins involved in the establishment of cell pointy; GTPase activity positively regulated by the GTPase activity positively regulated	bud
YNROSSIW YNL180C	RHQS	Non-essential small GTPase of the Rho/Roc subbrinky of Rea-Rea proteins, likely to be involved in the establishment of cell polarity Non-essential small GTPase of the Rho/Roc subbrinky of Rea-Rea proteins, likely involved in protein knows of CPIC+15/-dependent signal involvation pathway that controls cell integrity	bud
YGROTOW	ROM	CDP/GTP exchange protein (GEP) for Rhofg; mutations are synthetically lethal with mutations in rom2, which also encodes a GEP	bud
YLR371W YGR152C	ROM2 RSR1	COP/CIP exchange protein (CIP) for Rholp and Rholp CIP-bindra potein of the ma auxentramity required for bud site asticcion, montphotocical chances in response to mating physicana, and efficient cell fusion	bud tip bud neck
YCROOPC	RV5161	Amphiphysis-Re Epid rati protein; interacts with Real/67p and regulates polarization of the actin cytosteleton, endocytosis, cell polarity, cell fusion and stability following starvation or carrotic stress	bud
YDR388W YDR129C	RV5167 5AC6	Actio-associated pretein, interacts with RestRIP to regulate actin cylositeletor, endocytosis, and visibility following streatfor or cannotic stream; homolog of mammalian amphiphysin Pretoris, actio-bundling protein; cooperaties with Scylip (calponin/transgulin) in the organization and maintenance of the actin cylositeleton	bud
YOR367W	SCPI	Component of yeast control actin cyloskeleton, binds and cross links actin filtements; originally identified by its homology to calponin (contains a calponin-like repeat) but the Scopt domain structure is more similar to transgalin	bud
YDR164C	SEC1	Sm-like protein involved in docking and fusion of exceptic vesicles through binding to assembled SNARE complexes at the membrane	bud tip, bud neck
YNL272C YTL005W	5EC2 5EC4	Gasey-inacided exchange lactor for the small-Grouter Seclig, essential for pool-Golg vasiole temport, associates with the except suboril Seclig, on secretary webcies Secretary webcies field GTPuse essential for exception; associates with the except component Seclig and may republic polarized delays of transport webcies to the except at the plasma membrane	bud
YGROOPC	50.09	+SNARE protein important for fusion of secretory vasicles with the plasma membrane; similar to but not functionally redundant with Spo2Op; SNAP-25 homolog	bud
YBR130C YKR100C	5163	Protein that acts as an adaptor between My-olp and the Shelp-InRNA complex; part of the InRNA localization machinery that matrices accumulation of cartain proteine to the bud; also required for conical CR Intertances Transmittanee protein of universe function	bud bud to
YLRI87W	5KG3	Protein of unknown function	bud, bud neck
YHRIHAG YBL007C	SKG6 SLA1	Integral membrane protein that locations primarily to growing alles such as the bud to or the cell periphery; pointed CACEP publicate; (3)glp interactive with Zatrip and Zatrip Cyclosialabilit creation bindho protein required for assembly of the conflicat exclusive/and exclusion and cell contex than 3 240 domains	bud
YBL007C YNL243W	SLA1 SLA2	Cytoskeletal protein binding protein required for seasenbly of the contral actin cytoskeletor; interacts with proteins regulating actin dynamics and proteins required for endocytoxis; found in the ructious and call contex, has 3 SH3 domains Transmembrane actin-binding protein inselved in membrane cytoskeleton assembly and call polarization; adaptor protein that lacks actin to clathrin and endocytoxis; present in the actin contral patch of the emerging bud (or, dimer in vivo	bud
YOR008C	SLG1	Sensor-transducer of the stress-activated PKC1-MPK1 kinase pathway involved in maintenance of cell well integrity; involved in organization of the actin cytoslealetor; secretory pathway Wac1p is required for the annext of secretion response	bud tip, bud neck
YNLOTOW YNLOTOW	SMY1 SNC1	Proben that Interacts with MycDp, proposed to be incided in executions Vesicle membrane receptor protein (vSAVRE) incided in the tusion between Colp-denied accretory vasicies with the plasma membrane, proposed to be incided in endocytosis, member of the synophotenin/VAMP tamily of Rhype vSAVRE proteins	bud
YOR327C	SNC2	Vesicle membrane receptor protein (v-SNARE) involved in the fusion between Golgi-derived secretory vesicles with the plasma membrane; member of the synaptobrevin/VAMP tartily of R-type v-SNARE proteins	bud tip, bud neck
YLL021W	SPA2	Component of the polarisoms, which functions is actin cylosikelad organization during polarized growth	bud tip, bud neck
YURBISC YPRODZW	SPH1 SR07	Profiles involved in shmoo formation and blyoker bud site aelection Ethedor of Reb GTPase Secley, forms a complex with Secley and SWARE Secley, involved in excryteaus and docking and halon of poin-Gaigi vesicles with plasma membrane; homolog of SecTip and Dreaphile by terms magnetizer	bud
YEL105C	5R077	Protein with rokes in executories and cation homeostasis; functions in docking and fusion of post-Golgi vesicles with pleama membrane; homolog of 51x7p and Dreepphila lethal giant larvae tumor suppressor; interacts with SWARE protein Section	bud
YPL232W YMR183C	5501	Planam membrane SWRE inclued in hasion of secretary vesicies at the planam membrane and in vesich hasion during sponlation; forma a complex with Sacib that binds v SWRE Snc2p; syntexin homolog; functionally redundent with Sacib Planam membrane ISWRE inclued in hasion of secretary vesicies at the planam membrane, syntexin homolog that is Lancionally redundent with Sacib	bud
114CIELC	5502	Cdc/Gp-activated signal transducing kinase of the PAK (p21-activated kinase) family, involved in pheromone response, pasudohyphallineasive groeth, and vacuole inheritance; GBB motif (found in noncatalytic domains of PAKs) binds Steep	but but neck
YPL032C	SVLD	Protein of unknown function, mutant phenotype suggests a potential role in vacuolar function	bud
YGR221C YLR337C	TO52 VRP1	Protein involved in localization of Cdc2Ap to the site of bud growth; may act as a membrane anchor; localizes to the bud nock and bud (p; polentally phosphorylatid by Cdc2Bp Protein-rich actin-associated protein involued in cycloslestical organization and cyclolinesic; related to memmalias Wakd#-Adrich syndromy protein (WASP)-interacting protein (WAP)	bud
YAP1802	YAP1002	Protein involved in clathrin cage assembly; binds Pan to and clathrin; homologous to Yap1801p, member of the AP180 protein family	bud
YEROIGC YERAIAC	YTRDISC YLR414C	Putative protein of unknown function; green fluorescent protein (GPP)-fusion protein localizes to the cytoplasm and but, Interacts with Spatip; YTLOWC is not an essential gree Putative protein of unknown function; bouldam to bud and cytoplasm; co-localizes with Sar/b in punctible pathwe in the plasme membrane; null matter displays docreased thermoloteranor; transcription induced on cell wall damage	bud
YMR124W	YMR124W	Protein of unknown function: green fluorescent protein (GPP)-fusion protein localizes to the cell periphery, cytoplasm, bud, and bud neck: interacts with Cemfp in two-hybrid assay: YMR124W is not an essential gene	bud bud, bud neck
YMR295C	YMR295C	Protein of unknown function that associates with ribescreece green fluorescent protein (GPP) fastion protein localizes to the cell periphery and box (1987)2500 la not an essential gene	
YOR3DHC-A	YOR3MC-A	Protein of unknown function; green fluorescent protein (GPP)-fusion protein localizes to the cell periphery, cytoplasm, bud, and bud nack	

In Nay paper, ACTI to fadded into too groups, according to its localization and function: ACTIC (actin ca ARP2 and ARP3 are included in the same complex called **ARP**. Handingson patients IDTI' and ENIX are included in the same complex called **ENIT12**, SEC1, SEC5, SEC6, SEC6, SEC16, SEC16, EXIXT, EXIXA' are included in the same com ctin patch EXO

arres in this table are in upper case. This is to keep consistent with the protein names in Biogrid

Module name Node number in a module	Mitotic Exit 6	Endocytosis 33	Transport 25	Signaling 22	Exocytosis 13
	Bem2	Abp1	Act1C	Axl2	Cbk1
	Bud14	Act1P	Bag7	Bem1	Ехо
	Kel1	Ark1	Bni1	Bem3	Mso1
	Kel2	Arp	Bud6	Boi1	Sec1
	Lte1	Bbc1	Lrg1	Boi2	Sec2
	Ymr124w	Bzz1	Mkk1	Bud2	Sec4
		Cap1	Msb1	Bud5	Sec9
		Cap2	Msb3	Bud8	Snc1
		Cdc55	Msb4	Cdc24	Snc2
		Chc1	Myo2	Cdc42	Sro7
		Clc1	Pea2	Cla4	Sro77
		Cmd1	Pkc1	Cln2	Sso1
		Cof1	Pxl1	Gic1	Sso2
		End3	Rgd1	Gic2	
		Ent1,2	Rho1	Msb2	
		Gyl1	Rho2	Pam1	
		Gyp5	Rho3	Rga1	
		Las17	Rho4	Rga2	
		Myo3	Rom2	Rgd2	
		Myo4	Sig1	Rho5	
		Myo5	Smy1	Rsr1	
		Pan1	Spa2	Ste20	
		Prk1	Sph1		
		Rvs161	Tos2		
		Rvs167	Yor304c-a		
		Sac6			
		Scp1			
		She3			
		Sla1			
		Sla2			
		Vrp1			
		Yap1802			
		Yfr016c			

#### Table S2. Five modules in budding yeast polarity protein interaction network

#### Table S3. Participation coefficient and z-score for 99 proteins

e 55. Participation	coefficient and z-sc	ore for 99 pro
ABP1	Participation coefficient 0.17	z-score 1.06
ACT1C	0.34	1.63
ACT1P	0.50	0.3
ARK1 ARP	0.28	-0.36
AXL2	0.37 0.00	0.2 -0.28
BAG7	0.00	-0.98
BBC1	0.32	-0.64
BEM1 BEM2	0.54 0.63	1.19 -0.26
BEM3	0.00	-0.28
BNI1	0.49	2.03
BOI1 BOI2	0.00 0.28	-0.28 0.01
BUD14	0.00	-0.26
BUD2	0.00	-0.87
BUD5	0.00	-0.87 2.46
BUD6 BUD8	0.18 0.00	-0.87
BZZ1	0.00	-0.64
CAP1	0.64	0
CAP2 CBK1	0.00 0.67	0 -1.98
CDC24	0.27	1.78
CDC42	0.45	2.95
CDC55	0.00	-1.5
CHC1 CLA4	0.28 0.38	-0.36 1.19
CLC1	0.32	-0.64
CLN2	0.32	-0.28
CMD1 COF1	0.48 0.56	0.2 -0.93
END3	0.32	-0.93
ENT1,2	0.58	-0.28
EXO	0.70	0.55
GIC1 GIC2	0.00 0.53	-0.57 0.01
GYL1	0.00	-0.93
GYP5	0.00	-0.93
KEL1	0.28	2.13
KEL2 LAS17	0.00 0.28	-0.26 2.77
LRG1	0.44	-0.55
LTE1	0.00	-0.26
MKK1 MSB1	0.00	-0.12 -0.98
MSB2	0.50 0.00	-0.98
MSB3	0.45	0.74
MSB4	0.57	0.3
MSO1 MYO2	0.00 0.59	0.97 0.74
MYO3	0.40	0.77
MYO4	0.48	-0.93
MYO5 PAM1	0.15 0.00	1.34 -1.16
PAN1	0.31	0.77
PEA2	0.50	0.3
PKC1	0.38	-0.12
PRK1 PXL1	0.41 0.00	-0.07 -0.98
RGA1	0.41	0.3
RGA2	0.00	0.01
RGD1 RGD2	0.38 0.00	-0.12 -0.87
RH01	0.46	1.6
RHO2	0.00	-0.55
RHO3	0.38	-0.12
RHO4 RHO5	0.00 0.00	-0.98 -1.16
ROM2	0.00	-0.55
RSR1	0.24	0.3
RVS161 RVS167	0.00 0.15	-0.07 1.34
SAC6	0.00	-1.22
SCP1	0.00	-1.22
SEC1	0.00	0.97
SEC2 SEC4	0.63 0.47	-0.71 -0.29
SEC9	0.00	1.82
SHE3	0.32	-0.64
SLA1 SLA2	0.17 0.20	1.06 0.49
SLG1	0.50	-0.98
SMY1	0.00	-0.98
SNC1 SNC2	0.00 0.00	0.13 -0.29
SPA2	0.00	-0.29
SPH1	0.00	-0.55
SR07	0.45	-0.29
SRO77 SSO1	0.44 0.00	-1.56 0.55
SS02	0.00	0.55
STE20	0.62	0.89
TOS2	0.50	-0.98
VRP1 YAP1802	0.00 0.00	0.2 -0.07
YFR016C	0.63	0
YMR124W	0.50	-1.06
YOR304C-A	0.00	-0.55

#### Table S4 . $t_{1/2}$ values for proteins in Signaling module

(equation  $Y = A0 + A^* \exp(-\omega^* t)$  was used for iFRAP curve fitting, for details see supplementary online material.)

	Bem1	Bem3	Boi1	Boi2	Cdc24	Cdc42	Cla4	Gic1	Rga1	Rgd2	Ste20
curve 1	4.32	21.34	21.89	25.22	13.31	10.44	13.94	16.82	30.11	11.74	9.00
curve 2	19.08	23.08	27.13	29.81	8.08	17.75	10.67	26.11	18.99	21.20	30.83
curve 3	9.22	14.04	22.01	8.86	24.80	19.91	14.92	27.74	33.10	15.70	19.61
curve 4	5.62	21.38	15.34	14.94	15.17	14.71	17.89	17.85	26.19	14.02	10.92
curve 5	15.74	10.24	26.41	6.68	17.40	7.86	18.36	15.05	42.90	16.68	15.32
curve 6	15.92	16.52	30.35	9.25	24.11	12.61	8.91	19.70	17.07	23.06	22.48
curve 7	8.75	27.77	23.75	7.98	14.44	21.92	21.34	21.87	41.14	18.08	14.44
curve 8	14.13	14.23	28.84	19.28	11.57	8.98	20.56	20.16	28.59	18.29	14.28
curve 9	8.37	18.94	18.61	11.83	14.31	10.49	30.60	36.56	39.15	21.59	18.40
curve 10	4.58	22.52	21.61	31.31	20.60	10.86	25.32	20.20	15.45	12.17	23.20
curve 11	5.98		27.85		10.49		12.57		30.32	9.93	
curve 12					16.48						
curve 13					28.24						
curve 14					10.72						

### Table S5 . $t_{1/2}$ values for proteins in Transport module (equation $Y = A0 + A^* exp(-\omega^* t)$ was used for iFRAP curve fitting, for details see supplementary online material.)

	Bni1	Bud6	Lrg1	Msb1	Msb3	Myo2	Pea2	Pkc1	Pxl1
curve 1	20.37	26.57	52.87	18.73	15.44	17.47	41.73	49.18	29.07
curve 2	15.42	14.11	44.18	14.67	13.00	12.36	79.33	48.27	15.83
curve 3	33.07	18.26	60.98	20.32	24.47	19.85	65.38	45.79	33.36
curve 4	29.75	29.14	30.29	5.60	8.35	24.45	143.99	57.63	18.73
curve 5	26.81	30.14	49.84	10.68	15.18	17.79	64.72	13.91	13.74
curve 6	14.36	30.19	38.97	11.31	13.00	19.00	148.54	12.84	18.20
curve 7	18.79	13.82	61.24	14.70	22.29	17.37	121.05	11.64	15.53
curve 8	27.87	16.13	38.75	8.08	20.13	16.75	133.65	20.17	32.28
curve 9	6.93	34.91	45.76	14.12	22.50	13.01	69.65	29.07	29.37
curve 10	20.39	39.10	67.18	28.74	27.03	11.57	54.91	26.87	17.98
curve 11					10.77	16.12		16.32	
curve 12					23.06	11.67		26.12	
curve 13						23.70		25.04	
curve 14						16.14		35.58	
curve 15						9.22			

	Rgd1	Rho1	Rho3	Smy1	Spa2	Yor304c-a	Mkk1	Msb4	Rom2
curve 1	33.70	91.15	26.37	12.01	25.04	18.36	23.30	14.15	16.22
curve 2	26.45	101.67	24.18	14.41	19.42	28.85	18.00	45.78	32.52
curve 3	33.06	101.73	12.83	12.94	28.76	28.20	22.96	38.90	16.85
curve 4	21.89	123.08	6.99	17.43	31.85	18.12	35.25	20.00	17.18
curve 5	26.32	56.96	11.24	20.87	28.99	16.27	18.99	16.01	38.54
curve 6	38.75	52.51	4.89	34.66	30.25	33.70	13.26	16.83	26.03
curve 7	15.95	95.08	23.43	14.03	42.95	27.23	31.61	16.39	21.71
curve 8	10.98	45.28	24.11	24.83	31.61	39.75	28.09	25.79	13.32
curve 9	14.62	46.51	10.17	23.26	22.18	48.74	26.28	16.68	28.83
curve 10	20.14	39.87	10.09	28.25	39.58	38.13	17.54	42.71	17.94
curve 11		72.65							
curve 12		57.36							
curve 13		94.75							
curve 14		94.65							

	34.03
curve 15	60.81
curve 16	58.28
curve 17	67.88
curve 18	41.14

#### Table S6. There is no clear separation of $t_{1/2}$ values between two modules

<b>module</b> column A	<b>protein</b> column B	<b>LSMean</b> column C	Line2 column D	<b>Line1</b> column E
transport	Pea2	92.2958	А	
transport	Rho1	72.2976	В	
transport	Lrg1	49.0053	С	
transport	Spa2	30.0618	С	D
transport	Pkc1	29.8887	С	D
transport	Yor304c-a	29.7346	С	D
signaling	Rga1	29.3638	С	D
transport	Msb4	25.3230		D
transport	Bud6	25.2383		D
transport	Rgd1	24.1865		D
signaling	Boi1	23.9802		D
transport	Mkk1	23.5280		D
transport	Rom2	22.9140		D
transport	Px11	22.4097		D
signaling	Gic1	22.2062		D
transport	Bni1	21.3748		D
transport	Smy1	20.2712		D
signaling	Bem3	19.0057		D
transport	Msb3	17.9355		D
signaling	Ste20	17.8486		D
signaling	Cla4	17.7356		D
signaling	Rgd2	16.5862		D
signaling	Boi2	16.5163		D
transport	Myo2	16.4315		D
signaling	Cdc24	16.4087		D
transport	Rho3	15.4310		D
transport	Msb1	14.6941		D
signaling	Cdc42	13.5537		D
signaling	Bem1	10.1558		D

LSMean: Least Square Mean

	<b>t</b> 1 /2	degree	clustering coefficient		betweenness	Participation coefficient	z-score
BEM1	10.16	14	0.27	4	346.74	0.63	-0.26
BEM3	19.00	4	0.17	5	14.23	0.49	2.03
BNI1	21.38	12	0.18	4	306.16	0.00	-0.28
BOI1	23.98	4	1.00	4	0.00	0.28	0.01
BOI2	16.52	6	0.60	4	37.05	0.00	-0.26
BUD6	25.20	10	0.29	4	166.66	0.00	-0.87
CDC24	16.41	13	0.33	4	186.42	0.45	2.95
CDC42	13.55	21	0.17	4	782.91	0.00	-1.5
CLA4	17.74	12	0.21	4	192.70	0.32	-0.64
GIC1	22.21	3	1.00	5	0.00	0.53	0.01
LRG1	<b>49.00</b>	3	0.00	5	61.64	0.00	-0.12
MKK1	23.53	3	0.00	5	26.66	0.00	-0.87
MSB1	14.69	2	0.00	5	1.72	0.45	0.74
MSB3	17.90	7	0.33	4	90.14	0.00	0.97
MSB4	25.32	7	0.33	4	96.46	0.59	0.74
MYO2	16.43	9	0.14	5	214.33	0.48	-0.93
PEA2	92.30	6	0.40	5	79.47	0.41	-0.07
PKC1	<b>29.90</b>	4	0.00	5	54.16	0.00	-0.98
PXL1	22.40	1	0.00	6	0.00	0.00	0.01
RGA1	29.36	8	0.14	4	111.55	0.38	-0.12
RGD1	24.19	4	0.00	5	148.46	0.00	-0.55
RGD2	1 <b>6.59</b>	2	0.00	5	97.00	0.38	-0.12
RHO1	72.30	10	0.04	5	394.13	0.00	-0.98
RHO3	15.43	4	0.00	5	81.50	0.00	-0.55
ROM2	<b>22.91</b>	2	0.00	5	27.72	0.15	1.34
SMY1	20.27	1	0.00	6	0.00	0.48	1.6
SPA2	30.06	10	0.20	4	281.58	0.44	-1.56
STE20	17.85	15	0.16	4	439.29	0.63	0
YOR304C-A	29.73	2	1.00	5	0.00	0.50	-0.98
average	26.08	6.86	0.24	4.62	146.16	0.26	-0.04
Correlation coefficient between t1/2 and							
global parameters:		-0.10	0.02	0.21	-0.03	-0.11	-0.17
		А	В	С	D	E	F
A completion between t	مار ار مر م						

#### Table S7. Global parameters for 29 proteins in Transport module and Signaling module

A: correlation between  $t_{1/2}$  and degree B: correlation between  $t_{1/2}$  and clustering coefficient

C: correlation between  $t_{1/2}$  and eccentricity D: correlation between  $t_{1/2}$  and betweenness

E: correlation between  $t_{1/2}$  and Participation Coefficient

F: correlation between t<sub>1/2</sub> and Z-score

## Table S8. For most of the 29 proteins, there is no significant differenceof the dynamics between interaction partners and non-interaction partners

protein name	direct_mean	indirect_mean	self_mean	direct p value	indirect p value
Bem1	35.18579313	20.4200025	20.29053677	0.029284367	0.999453147
Bem3	22.16449378	25.47004966	25.4260303	0.848077688	0.999957955
Bni1	25.17449117	25.54996367	14.31911051	0.148577758	0.128636953
Boi1	20.36943696	26.08663267	29.78392211	0.244261402	0.736717846
Boi2	18.12387658	28.0709584	20.83555692	0.829057016	0.384624999
Bud6	24.77557506	25.50010166	18.2009402	0.430359221	0.360273805
Cdc24	21.68480089	26.86861351	21.43040874	0.998191532	0.534614185
Cdc42	23.41198322	28.45603099	18.05252687	0.539930096	0.233742151
Cla4	24.30578123	25.70635726	23.91960297	0.996351782	0.936990943
Gic1	22.34634008	25.28820336	28.80837161	0.56330568	0.780396886
Lrg1	49.57247335	22.27711449	42.89716174	0.449156949	0.001364365
Mkk1	22.85327422	25.57026714	16.42044772	0.54070119	0.245110205
Msb1	18.9455585	26.12290547	7.637098795	0.224553284	0.008691618
Msb3	42.61289748	21.45390865	13.16625143	1.22873E-06	0.186960233
Msb4	31.15164233	23.99075189	18.59142598	0.099604194	0.512872609
Myo2	13.9622052	27.25109492	7.64310228	0.404214413	0.000541832
Pea2	18.57977452	24.2033472	86.55516366	9.99978E-13	9.99978E-13
Pkc1	50.12688838	23.21575298	25.13566874	0.000153343	0.881134011
Pxl1	23.45519429	25.52291169	15.54061371	0.559010985	0.208813964
Rga1	42.48827801	21.6535067	37.71609318	0.60168499	0.014368333
Rgd1	8.042241793	25.85148207	16.79776579	0.490386237	0.264994085
Rgd2	17.981655	25.83284746	23.03816779	0.678636315	0.833611673
Rho1	23.62373005	23.01751404	67.63079073	9.99978E-13	9.99978E-13
Rho3	11.46697195	27.05533248	6.838391381	0.652504284	0.003111965
Rom2	67.44807956	23.31229875	18.06443312	9.99978E-13	0.506595814
Smy1	8.717449835	26.17674736	12.5571785	0.818679808	0.061952758
Spa2	23.06601882	25.77718193	22.74732693	0.996867955	0.780361927
Ste20	21.35687704	26.7160152	23.29223319	0.90599407	0.758440988
Yor304c-a	18.27848111	25.42256076	22.77475211	0.817038227	0.874000593

Table S9. t<sub>1 /2</sub> values for 2 proteins in Mitotic Exit module (equation  $Y = A0 + A^* \exp(-\omega^* t)$  was used for iFRAP curve fitting, for details see supplementary online material.)

	Kel1	Lte1
curve 1	45.74	44.01
curve 2	85.76	43.59
curve 3	146.20	69.98
curve 4	149.13	37.11
curve 5	83.57	68.72
curve 6	55.93	31.97
curve 7	63.05	46.87
curve 8	80.19	39.01
curve 9	57.39	80.16
curve 10	106.90	36.37

# Table S10. t<sub>1/2</sub> values for 11 proteins in *pea2* $\Delta$ (equation Y = A0 + A\* exp(- $\omega$ \* t) was used for iFRAP curve fitting, for details see supplementary online material.)

	∆pea2 Rga1-GFP	∆pea2 GFP-Cdc42p	∆pea2 Bni1-GFP	∆pea2 Pkc1p-GFP
curve 1	12.78	17.40	14.29	21.92
curve 2	32.83	10.07	13.39	17.83
curve 3	42.38	11.19	16.83	19.96
curve 4	11.95	20.98	12.53	14.15
curve 5	14.33	16.40	27.54	38.32
curve 6	37.17	7.08	20.19	24.49
curve 7	18.70	10.95	30.32	9.49
curve 8	24.15	5.26	16.49	14.89
curve 9	34.15	5.09	10.25	11.18
curve 10	35.92	8.88	10.43	8.11
	∆pea2 GFP-Rho3p	∆pea2 Yor304c-a-GFP	∆pea2 Bud6-GFP	∆pea2 Myo2-GFP
curve 1	23.21	12.66	. 19.46	17.92
curve 2	13.97	11.39	11.50	19.63
curve 3	18.49	14.03	11.33	11.46
curve 4	8.35	10.56	15.94	15.78
curve 5	18.24	14.04	8.20	27.21
curve 6	16.64	16.83	10.09	31.55
curve 7	17.00	17.47	11.11	46.32
curve 8	32.52	31.40	12.84	8.28
curve 9	4.26	4.49	5.20	23.42
curve 10	40.75	4.82	14.19	19.64
	∆pea2 Spa2-GFP	∆pea2 Lrg1-GFP	∆pea2 GFP-Rho1p	
curve 1	13.30	, 41.16	59.49	
curve 2	10.45	63.31	26.08	
curve 3	11.84	24.51	28.66	
curve 4	25.05	61.02	43.68	
curve 5	18.99	75.17	26.08	
curve 6	22.79	31.87	38.04	
curve 7	14.15	45.78	37.98	
curve 8	16.80	45.50	28.94	
curve 9	30.53	56.13	33.64	
curve 10	30.66	38.09	33.24	
curve 11	6.44	48.35	27.22	
curve 12		48.87	22.83	
curve 13		40.39	26.68	
curve 14			13.94	
curve 15			69.61	
curve 16			58.15	
curve 17			19.13	
curve 18			33.39	

#### Table S11. Yeast strains used in this study

Strain	Mat	Relevant genotype (*)	Source
RLY4555	а	pea2∆::KanR BNI1-GFP::HIS3	from this paper
RLY4526	а	pea2∆::KanR BUD6-GFP::HIS3	from this paper
RLY4528	а	pea2Δ::KanR MYO2-GFP::HIS3	from this paper
RLY4530	а	pea2∆::KanR SPA2-GFP::HIS3	from this paper
RLY4553	а	pea2Δ::KanR PKC1-GFP::HIS3	from this paper
RLY4851	а	pea2∆::KanR YOR304C-A-GFP::URA3	from this paper
RLY4852	а	pea2∆::KanR RGA1-GFP::URA3	from this paper
RLY4853	а	pea2Δ::KanR LRG1-GFP::URA3	from this paper
RLY4531	а	pea2Δ::KanR RHO1::GFP-RHO1-myc6::URA3	from this paper
RLY4533	а	pea2A::KanR RHO3::GFP-RHO3-myc6::URA3	from this paper
RLY4535	а	pea2∆::KanR CDC42::GFP-CDC42 -myc6::URA3	from this paper
RLY3479	а	BNI1-GFP::HIS3	Huh et al., Nature 2003.
RLY2912	а	CLA4-GFP::HIS3	Huh et al., Nature 2003.
RLY2550	а	LRG1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2908	а	GIC1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2907	а	BOI2-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2766	а	BEM1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2913	а	MSB4-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2910	а	BOI1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2544	а	RGA1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2556	а	RGD2-GFP::HIS3	Huh et al., Nature 2003.
RLY2557	а	RGD1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2558	а	BUD6-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2769	а	PKC1-GFP::HIS3	Huh et al., Nature 2003.
RLY2916	а	STE20-GFP::HIS3	Huh et al., Nature 2003.
RLY2767	а	CDC24-GFP::HIS3	Huh et al., Nature 2003.
RLY2877	а	MYO2-GFP::HIS3	Huh et al., Nature 2003.
RLY2770	а	MSB1-GFP::HIS3	Huh et al., Nature 2003.
RLY3090	а	BEM3-GFP::HIS3	Huh et al., Nature 2003.
RLY3243	а	SMY1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY3239	а	PXL1-GFP::HIS3	Huh et al., Nature 2003.
RLY3119	а	SPA2-GFP::HIS3	Huh et al., Nature 2003.
RLY4606	а	PEA2-GFP::HIS3	Huh et al., Nature 2003.
RLY4608	а	MKK1-GFP::HIS3	Huh et al., Nature 2003.
RLY4610	а	ROM2-GFP::HIS3	Huh et al., Nature 2003.
RLY4613	а	YOR304C-A-GFP::HIS3	Huh et al., Nature 2003.
RLY4609	а	MSB3-GFP::HIS3	Huh et al., Nature 2003.
RLY3238	а	BEM2-GFP::HIS3	Huh et al., Nature 2003.
RLY2914	а	LTE1-GFP::HIS3	Huh <i>et al.</i> , Nature 2003.
RLY2768	а	KEL1-GFP::HIS3	Huh et al., Nature 2003.
RLY3387	а	RHO3::GFP-Rho3-myc6::URA3	from this paper
RLY3385	a	RH01::GFP-Rho1-myc6::URA3	from this paper
RLY2902	a	CDC42::GFP-Cdc42-myc6::URA3	from this paper
RLY4547	a	SPA2-mCherryOPT::URA3 PEA2-GFP::HIS3	from this paper
RLY4548	а	PEA2-mCherryOPT::HIS3 RH01::GFP-RH01-myc6::URA3	from this paper

All strains are of S288C background and others with same type of genotype (markers)