### **Supplementary Materials**

#### 0.1 Preprocessing expression data

We removed the gene expression profiles with overall small absolute values less than a percentile cutoff (60% is used here). Further, we removed the gene expression profiles with a variance less than the percentile specified by another cutoff (30% is used here). The procedure was done using the standard functions (genelowvalfilter(Data, 'Percentile',60) and genevarfilter(Data, 'Percentile',30)) in the Matlab software.

### 0.2 The SNMNMF algorithm and the discussion of its convergence

The SNMNMF algorithm minimizes the following objective function:

$$\mathcal{F}(W, H_1, H_2) = \sum_{I=1,2} \|X_I - WH_I\|_F^2$$
$$-\lambda_1 Tr(H_2 A H_2^T) - \lambda_2 Tr(H_1 B H_2^T)$$
$$+\gamma_1 \|W\|_F^2 + \gamma_2 (\sum_j \|h_j\|_1^2 + \sum_{j'} \|h_{j'}\|_1^2)$$

with the constraints  $W \ge 0$ ,  $H_I \ge 0$  and I = 1, 2, where  $h_j$  and  $h_{j'}$  are the *j*th and *j*'th column of  $H_1$  and  $H_2$  respectively.

We expand the popular multiplicative updating algorithm developed for NMF and its variants to SNMNMF. For the NMF problem, although the objective function of NMF is convex in W only or H only, it is not convex in both variables together. Therefore it is unrealistic to expect an algorithm to find the global minimum. The same applies to the SNMNMF problem. Below we detail the multiplicative updating algorithm for SNMNMF to identify the local minimum of  $\mathcal{F}$ .

Based on the simple knowledge of linear algebra, the objective function  $\mathcal{F}$  can be reformulated as follows:

$$\mathcal{F} = \sum_{I=1}^{2} \left[ Tr(X_{I}X_{I}^{T}) - 2Tr(X_{I}H_{I}^{T}W^{T}) + Tr(WH_{I}H_{I}^{T}W^{T}) \right] - \lambda_{1}Tr(H_{2}AH_{2}^{T}) - \lambda_{2}Tr(H_{1}BH_{2}^{T}) + \gamma_{1}Tr(WW^{T}) + \gamma_{2}\sum_{I=1}^{2} e_{1\times k}H_{I}H_{I}^{T}e_{1\times k}^{T}$$
(2)

. Let  $\psi_{ij}$  and  $\phi_{ij}^I$  be the Lagrange multipliers for the constraints  $W_{ij} \ge 0$  and  $(H_I)_{ij} \ge 0$ , respectively. The Lagrange  $\mathcal{L}$  is

$$\mathcal{L}(W, H_I) = \mathcal{F} + Tr(\Psi W^T) + \sum_{I=1}^{2} Tr(\Phi_I H_I^T).$$

where  $\Psi = [\psi_{ij}]$  and  $\Phi_I = [\phi_{ij}^I]$ . The partial derivatives of  $\mathcal{L}$  with respect to W and  $H_I$  are:

$$\frac{\partial \mathcal{L}}{\partial W} = \sum_{I=1}^{2} \left[ -2X_{I}H_{I}^{T} + 2WH_{I}H_{I}^{T} \right] + 2\gamma_{1}W + \Psi$$

 $\frac{\partial \mathcal{L}}{\partial H_1} = -2W^T X_1 + 2W^T W H_1 - \lambda_2 H_2 B^T + \gamma_2 2e_{k \times k} H_1 + \Phi_1,$ 

$$\frac{\partial \mathcal{L}}{\partial H_2} = -2W^T X_2 + 2W^T W H_2 - \lambda_1 2H_2 A - \lambda_2 H_1 B + \gamma_2 2e_{k \times k} H_2 + \Phi_2$$

Based on the KKT conditions  $\psi_{ij}W_{ij} = 0$  and  $\phi_{ij}^{I}(H_{I})_{ij} = 0$ , we get the following equations for  $W_{ij}$ ,  $(H_{1})_{ij}$  and  $(H_{2})_{ij}$ :

$$-2\sum_{I=1}^{2} (X_{I}H_{I}^{T})_{ij}W_{ij} + [2\sum_{I=1}^{2} (WH_{I}H_{I}^{T}) + 2\gamma_{1}W]_{ij}W_{ij} = 0,$$
  
$$-W^{T}X_{1} - \frac{\lambda_{2}}{2}H_{2}B^{T})_{ij}W_{ij} + (W^{T}WH_{1} + \gamma_{2}e_{k\times k}H_{1})_{ij}W_{ij} = 0,$$
  
$$-W^{T}X_{2} - \lambda_{1}H_{2}A - \frac{\lambda_{2}}{2}H_{1}B)_{ij}W_{ij} + (W^{T}WH_{2} + \gamma_{2}e_{k\times k}H_{2})_{ij}W_{ij} = 0.$$

Then we can get the following updating rules:

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$$w_{ij} \leftarrow w_{ij} \frac{(X_1H_1^T + X_2H_2^T)_{ij}}{(WH_1H_1^T + WH_2H_2^T + \gamma_1W)_{ij}},$$

$$h_{ij}^1 \leftarrow h_{ij}^1 \frac{(W^TX_1 + \frac{\lambda_2}{2}H_2B^T)_{ij}}{[(W^TW + \gamma_2e_{k\times k})H_1]_{ij}},$$

$$h_{ij}^2 \leftarrow h_{ij}^2 \frac{(W^TX_2 + \lambda_1H_2A + \frac{\lambda_2}{2}H_1B)_{ij}}{[(W^TW + \gamma_2e_{k\times k})H_2]_{ij}},$$
(3)

We have the following theorem to guarantee the convergence of the above updating rules to a local optimum.

**Theorem 1** The objective function  $\mathcal{F}$  of the SNMNMF problem is nonincreasing under the above updating rules. The objective function is finite and invariant under these updates if and only if W,  $H_1$  and  $H_2$  are at a stationary point.

The principle of convergence proof of NMF can be easily expanded to prove this theorem. A difference to NMF is that the objective function  $\mathcal{F}$  here can be unbounded below. Only the objective is finite, the SNMNMF can get a stable local solution. Here, we show that  $\mathcal{F}$  is nonincreasing under the updating rules. In particular, here we prove that the  $\mathcal{F}$  is nonincreasing under the updating rule for  $H_1$ , and same feature under the updating rule for W can be similarly proved. We will adopt the same strategy used in (Lee and Seung, 2001) that introduced an auxiliary function in the Expectation-Maximization algorithm. The following is the definition of the auxiliary function.

**Definition** G(h,h') is an auxiliary function for F(h) if the conditions  $G(h,h') \ge F(h)$ , G(h,h) = F(h) are satisfied.

Due to the following property, the auxiliary function is very useful for the proof.

**Lemma 1** If G is an auxiliary function of F, then F is nonincreasing under the update  $h^{(t+1)} = \arg\min(G(h, h^{(t)}))$ .

With a proper auxiliary function, the updating rule for  $H_1$  is exactly the update in this Lemma. Taking into account any element  $(H_1)_{ab}$  in  $H_I$ , we use the  $F_{ab}$  to denote the part of  $\mathcal{F}$  that is only relevant to  $(H_1)_{ab}$ . It is easy to see that

$$F_{ab}^{'} = \left(\frac{\partial \mathcal{F}}{\partial H_1}\right)_{ab} = (-2W^T X_1 + 2W^T W H_1 - \lambda_2 H_2 B^T + \gamma_2 2e_{k \times k} H_1)_{ab}$$
$$F_{ab}^{''} = 2(W^T W + \gamma_2 e_{k \times k})_{aa}$$

Because the update is essentially element-wise, it is sufficient to show that each  $F_{ab}$  is nonincreasing under the updating rule for  $H_1$ .

#### Lemma 2 Function

$$G(h, (H_1)_{ab}^{(t)}) = F_{ab}((H_1)_{ab}^{(t)}) + F_{ab}'((H_1)_{ab}^{(t)})(h - (H_1)_{ab}^{(t)}) + \frac{[(W^T W + \gamma_2 e_{k \times k})H_1]_{ab}}{(H_1)_{ab}^{(t)}}(h - (H_1)_{ab}^{(t)})^2$$
(4)

is an auxiliary function for  $F_{ab}$ .

**Proof** Obviously,  $G(h, h) = F_{ab}(h)$ . Here we only show that  $G(h, (H_1)_{ab}^{(t)}) \geq F_{ab}(h)$ . To achieve this, we compare the Taylor series expansion of  $F_{ab}(h)$ 

$$F_{ab}(h) = F_{ab}((H_1)_{ab}^{(t)}) + F_{ab}^{'}((H_1)_{ab}^{(t)})(h - (H_1)_{ab}^{(t)}) + (W^T W + \gamma_2 e_{k \times k})_{aa}(h - (H_1)_{ab}^{(t)})^2$$
(5)

with the auxiliary function  $G(h, (H_I)_{ab}^{(t)})$  to find that  $G(h, (H_1)_{ab}^{(t)}) \ge$  $F_{ab}(h)$  is equivalent to

$$\frac{\left[\left(W^TW + \gamma_2 e_{k \times k}\right)H_1\right]_{ab}}{\left(H_1\right)_{ab}^{(t)}} \ge \left(W^TW + \gamma_2 e_{k \times k}\right)_{aa}.$$

Obviously, we have

$$((W^{T}W + \gamma_{2}e_{k\times k})H_{1})_{ab} = \sum_{k} (W^{T}W + \gamma_{2}e_{k\times k})_{ak}(H_{1})_{kb}^{(t)}$$
$$\geq (H_{1})_{(ab)}^{(t)}(W^{T}W + \gamma_{2}e_{k\times k})_{aa}.$$
(6)

Thus  $G(h, (H_1)_{ab}^{(t)}) \ge F_{ab}(h)$  holds. **Proof of Theorem 1** We can get the the following updating rule based on the auxiliary function  $G(h, (H_1)_{ab}^{(t)})$ :

$$(H_1)_{ab}^{(t+1)} = (H_1)_{ab}^{(t)} - (H_1)_{ab}^{(t)} \frac{F_{ab}^{'}((H_1)_{ab}^{(t)})}{2((W^TW + \gamma_2 e_{k\times k})H_1)_{ab}}$$
$$= (H_1)_{ab}^{(t)} \frac{(W^TX_1 + \frac{\lambda_2}{2}H_2B^T)_{ab}}{((W^TW + \gamma_2 e_{k\times k})H_1)_{ab}}.$$
(7)

Due to the property of the auxiliary function  $G(h, (H_1)_{ab}^{(t)})$  for  $F_{ab}$ ,  $F_{ab}$  is nonincreasing under this updating rule.

#### 0.3 Initialization of the algorithm

We initialize the W,  $H_1$  and  $H_2$  matrices by assigning the uniformly distributed values ranging from 0 to 1 to their entries. We note that, under different runs of the algorithm, the objective function only have minor changes.

#### 0.4 Parameter selection

The method proposed here requires setting of several parameters. Given that 41 miRNAs in the data sets have been previously reported to be related with ovarian cancer (Koturbash et al., 2010), and which can have multiple regulatory combination with other miRNAs and the 57 miRNA clusters contained in the data sets (miRNA cluster data from the miRBase website [http://www.mirbase.org/] with a genomic cutoff distance of 50kb, see Materials and Methods), we set the number of co-module to 50. As to the parameters  $\lambda_1$ ,  $\lambda_2$ ,  $\gamma_1$ ,  $\gamma_2$ , they were empirically determined by relative size of each corresponding term of the objective function (Figure S1A). To test

the robustness of our result with respect to the initial parameters, we ran our method using several different combinations. We found that more than 60% of the genes were consistently grouped together and most of the enriched terms are the same for these different settings (Figure S1B). Here the consistency measure is defined as the ratio of gene pairs present in the same modules across different results under different settings.



Fig. S1. A. The objective value for current setting. B. Comparison of current parameter setting with other three based on enrichment analysis. The -log(p-value) is shown on x- and y-axis for different parameter settings. There three setting are  $(K = 50, \lambda_1 = 0.0001, \lambda_2 = 0.01, \gamma_1 = 10, \text{ and}$  $\gamma_2 = 10$ ),  $(K = 50, \lambda_1 = 0.0001, \lambda_2 = 0.01, \gamma_1 = 10$ , and  $\gamma_2 = 5$ ) and  $(K = 60, \lambda_1 = 0.0001, \lambda_2 = 0.01, \gamma_1 = 10, \text{ and } \gamma_2 = 5)$ , respectively.

We have run the programs with different initializations with other fixed parameters, we found that the 90% of the genes were consistently grouped together, indicating the robustness of the method to different initializations.

To select the proper threshold T, we assess the enrichment rate of gene modules with respect to GO biological process. For comparison, the mean rate of functional enrichment for 100 corresponding random runs was also calculated. In Figure S2, we show the ratio of real enrichment rate against the mean of 100 random ones for different cutoff T. The highest peak shows that the T = 7 is a good threshold.

#### 0.5 Permutation test for between correlations

We show the sum of Pearson's correlation coefficients (PPCs) for the miRNA-gene modules 32 and 40 and their distributions of 1000 random chosen miRNA-gene modules respectively (Figure S3).

#### 0.6 Module size distribution

We run the proposed method on the ovarian cancer dataset and obtained 50 'co-modules' which are composed by a set of miRNAs and a set of genes which are denoted as miRNAs modules and gene modules respectively. We show the module size distribution in Figure S4 and each co-module contains 3.8 miRNAs and 78 genes



Fig. S2. The distribution of the enrichment ratio of gene modules against the mean of that for modules of 100 random runs under different cutoff T.



Fig. S3. Distribution of the sum of PCCs of randomly chosen miRNA-gene modules estimated by 1000 random samplings for co-module 32 and 40 respectively.

on average. Note that three miRNAs and one genes modules are empty.

# 0.7 The literature review support for the overlapping miRNAs

We search any two miRNAs of the overlapping miRNAs for each comodule and see if they are related with the same biological processes uncovered by other studies. The ones supported by literature review were listed in Table S1.

# 0.8 The co-modules are highly enriched with cancer genes

We listed the modules that are enriched with ovarian cancer genes based on the IPA system in Table S2.



Fig. S4. Module size distribution for miRNA modules and gene modules respectively.

#### 0.9 Illustration of the signals of W basis vectors

Based on the basis matrix W, we can divide the samples into three groups. We show the signals of co-module 39 and 40 with corresponding dividing lines (Figure S5).



Fig. S5. The signals of W basis vectors for co-module 39 and 40 respectively. The same figure for other co-modules can be similarly plotted.

#### 0.10 The EBC method

The EBC method integrated two types of information to identify miRNA-gene regulatory module. The method has the following major steps (Figure S6): (1) Calculate miRNA-gene correlation matrix based on the (inverse) correlations in the expressions across samples, and convert the correlation matrix into a miRNAgene correlation network. (2) Construct a miRNA-gene regulatory network by combining the constructed miRNA-gene correlation network and the corresponding predicted miRNA-gene regulatory network. (3) Enumerate all maximal bicliques as candidate regulatory modules, remove the ones with genes less than ten, and postprocess candidate modules.

The maximal bicliques in a bipartite network can have quite big overlap. For example, the maximal biclique 1 and 2 have a large number of overlapping genes, and their combinations and maximal biclique 3 only have two genes difference (Figure S7).

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Fig. S6. Workflow of the EBC method for co-module identification.



Fig. S7. Examples of maximal bicliques.

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### Table S1. Summary of collected function roles of the enriched overlapping miRNAs based on literature search.

No	Function description according to literature abstract	Reference
10	Tumor suppressor function through regulating Rb/E2F1 activity (miR-449a/449b)	Yang et al. (2009)
	Targets of p53 and control of cell proliferation and adhesion-independent growth (mir-34b/34c)	Corney et al. (2007)
14	Repression of the (miR-143/145 cluster) by oncogenic Ras initiates a tumor-promoting feed-forward pathway	Kent et al. (2010)
	Smooth muscle cell (SMC) differentiation and vascular pathogenesis (miR-143/145 cluster)	Elia et al. (2009)
	(miR-143/145) modulate cytoskeletal dynamics and responsiveness of smooth muscle cells to injury.	Xin et al. (2009)
16	Might be important biomarkers for the early detection and prognostic assessment of prostate cancer	Yin et al. (2010)
	Repress FOXO1 expression, affect cell cycle control and apoptotic responses in endometrial cancer	Myatt et al. (2010)
	Expression depending on mismatch repair status and characteristic of undifferentiated proliferative states	Sarver et al. (2009)
	Upregulated in prostate cancer and useful diagnostic and prognostic indicators	Schaefer et al. (2010)
	Differential expressed, related with peculiar tumourigenetic pathways and be potential biomarkers	Cho et al. (2009)
	The development of the cochlea (from the patterning to the differentiation of the cochlear structures)	Sacheli et al. (2009)
17	Both partners of the (miR-144/451 cluster) confer protection against simulated I/R-induced	Zhang et al. (2010)
	cardiomyocyte death via targeting CUGBP2-COX-2 pathway	
	(miR-144/451 cluster) tunes gene expression to impart a robustness to erythropoiesis	Rasmussen et al. (2010)
19	Amplification and overexpression of (miR-30b, miR-30d and KHDRBS3) at 8q24.22-q24.23 in medulloblastoma	Lu et al. (2009)
20	See 16	See 16
42	Deffiential expressed signature associated with Renal ischemia reperfusion injury (IRI)	Godwin et al. (2010)
	miR-199a/miR-214 cluster is down-regulated in both murine and human cytomegalovirus infection and	Santhakumar et al. (2010)
	Manifests similar antiviral properties in mouse and human cells	
	Through mir-199a/214, TWISTing stemness, inflammation and proliferation of epithelial ovarian cancer cells	Yin et al. (2010)
	Altered microRNA Expression Patterns in Hepatoblastoma Patients	Magrelli et al. (2009)
	Deregulation of miRNAs is a recurrent event in human ovarian cancer and that miR-214 induces cell survival	Yang et al. (2008)
	and cisplatin resistance primarily through targeting the PTEN/Akt pathway	
46	See 17	See 17

Table S2. Summary of gene modules that are enriched with ovarian cancer genes based on the IPA system. q-value, the B-H multiple test corrected p-value.

No.	Ovarian cancer genes	genes	q-value
2	FN1, INHBA, MMP3, MMP1, POSTN, PTGS2, SERPINE1, VCAN	8	2.87e-02
4	C11ORF9, EFNB2, FGF18, KLK6, KLK8, KLK10, KLK11, SCGB2A1	8	6.06E-02
6	DACH1, EEF1A2, MMP3, S100P, SLIT2, WT1	6	5.73E-02
14	ABCA8, DIRAS3, GSTM5, HSD11B1, ITLN1, MUM1L1	6	4.89E-03
22	DACH1, FAM54A, KPNA2, RRM2, S100P, TOP2A, TYMS	7	5.75E-03
23	CALB2, CFH, CXCL14, FABP4, FGF1, INHBA, PDGFRB, PEG3, POSTN, SLIT2, TIMP3, VCAM1, VCAN	13	1.62E-03
28	DUSP4, EYA2, IFI27, IGFBP1, KLK5, KLK7, KLK8, MMP3, MMP7, PRKCB, S100P, SCGB2A1, VTCN1, WFDC2, WT1	15	4.49E-07
34	CCL4, CSF1R, GPR65, IGFBP1, KLK7, LCN2, MMP7, SCGB2A1	8	2.29E-02
39	FOLR1, HMGA2, HOXB6, KLK11, PROM1, S100A2, TACSTD2, VAV3	8	5.66E-02
40	FAM54A, HIST2H2AA3, KRT23, PAEP, SLPI, TIMP1, TOP2A, VTCN1	8	4.88E-02
42	FLRT2, HOXA4, IGFBP4, KIT, PDGFRA, PEG3, SEMA3C, SERPINA5, TUBB2A	9	3.32E-02
48	CXCL14, FLT1, IL6, INHBA, PLAU, POSTN, TIMP3, VCAN	8	2.20E-03
49	CEACAM6, GPX3, LCN2, PEG3, S100A2, VAV3	6	4.34E-02