Rate-Independent Constructs for Chemical Computation

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Appendix: Exponentiation Reactions

We present chemical reactions that implement the pseudo-code presented in the text.

System Initialization As with our multiplication module, we have a small set of reactions to control the overall timing.

$$x + x'_{ab} + y'_{ab} \xrightarrow{\text{slow}} x + g^P$$
 (1)

$$g^P + x' \xrightarrow{\text{fast}} x'$$
 (2)

$$g^P + y' \xrightarrow{\text{fast}} y'$$
 (3)

$$g^P \xrightarrow{\text{slow}} g^1 + g^2$$

$$\tag{4}$$

Doubling We use a slight variation of our copier module to implement the line of pseudo-code y = 2 * y.

$$g^1 + y \xrightarrow{\text{slow}} g^1 + y'$$
 (5)

$$g^1 + y_{\rm ab} \xrightarrow{\text{slow}} \varnothing$$
 (6)

$$g_{\rm ab}^1 + y' \xrightarrow{\rm slow} 2y$$
 (7)

Decrement As with our multiplication module, we decrement \mathbf{x} once each loop.

$$x + g^2 \xrightarrow{\text{slow}} x' + g^2$$
 (8)

$$g^2 + x_{\rm ab} \xrightarrow{\rm slow} \varnothing$$
 (9)

$$2 x' + g_{\rm ab}'^2 \xrightarrow{\text{fast}} x' + x + x^{\rm rx}$$
(10)

$$x^{\mathrm{rx}} \xrightarrow{\mathrm{slow}} \varnothing$$
 (11)

$$x' + x_{ab}^{rx} + g_{ab}'^2 \xrightarrow{\text{slow}} \varnothing$$
 (12)

Absence Indicators Four absence indicators are needed by this system; they are of the same form as all others described in this paper.