## **Supplemental information for "Mechanical control of cation channels in the myogenic response"**

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## **1. TABLES OF FIXED PARAMETERS**



Table S1: Fixed parameters used in vessel wall mechanics model

\* Fixed parameters used here from optimized fits obtained in (8) to the data in Figure 1 of (6) for the normal control of Wistar-Kyoto rat mesenteric and femoral arterioles except for the reference values of wall thickness and diameter which are direct measurements made in original experimental study.

Fixed parameter	Units	Value <sup>*</sup>
$K_2$	1/s	0.5
$K_3$	1/s	0.4
$K_4$	1/s	0.1
$K_5$	1/s	0.5
$K_7$	1/s	0.1
$(AM+AMp)_{max}$	unitless	0.8
γ	$\mu M^3/s$	17.0
÷		

Table S2: Fixed parameters used VSM crossbridge model

\* All fixed parameter values are from (14)

Table S3: Fixed parameters used in VSM  $Ca<sup>2+</sup>$  handling and electrophysiology model

Fixed parameter	Description	Units	Value	Ref	
Standard constants and VSM cell properties					
$\overline{F}$	Faraday constant	C/mole	96485.34		
$\boldsymbol{R}$	Gas constant	$(C*mv)/(K*mole)$	8314.472		
T	Temperature	K	293		
$N_{Avo}$	Avogadro's number	$1$ /mole	$6.022 \times 10^{23}$		









\* Parameter value assumed or estimated in Kapela et al. (13)

# Parameter value determined directly in paper

§ Parameter value determined from model fits to or analysis of data presented in paper

Parameters, units and values in **bold** indicate corrections and omissions from that originally published in Kapela et al. (13).

#### **2. COMPLETE SET OF INTEGRATED MODEL EQUATIONS**

#### **Model 1: Vessel wall mechanics model**

The set of equations given below can be used to implicitly solve for a vessel diameter, *D*, as a function of the intraluminal pressure, *P*, and the activation, *Act*, as determined from running Model 2 and Model 3 to steady-state solutions. If these equations are to solve for myogenic or maximally active curves root finding is more easily performed in the stress-strain space rather than the pressure-diameter space due to hysteresis at high intraluminal pressure that often leads to multiple diameters at a given pressure but less often gives multiple strains for a given stress.

Algebraic equations:

$$
\delta_{wall} = -\frac{D}{2} + \sqrt{\left(\frac{D}{2}\right)^2 + \frac{CSA_{ref}}{\pi}}
$$
 [S1]

$$
\sigma_{total} = \frac{PD}{2\delta_{wall}}
$$
 [S2]

$$
\sigma_{pass} = \frac{C_{pass}}{\delta_{wall}} \exp\left[C'_{pass}\left(\frac{D}{D_{p100}} - 1\right)\right]
$$
 [S3]

$$
\sigma_{act}^{\max} = \frac{C_{act}}{\delta_{wall}} \exp\left[-\left(\frac{D/D_{p100} - C'_{act}}{C'_{act}}\right)^2\right]
$$
 [S4]

$$
\sigma_{total} = \sigma_{pass} + Act \sigma_{act}^{max}
$$
 [S5]

Calculation of remaining fixed parameter:

$$
CSA_{ref} = \pi \delta_{wall, ref} \left( D_{ref} + \delta_{wall, ref} \right)
$$
 [S6]

#### **Model 2: VSM crossbridge force generation model**

A dynamic VSM crossbridge model is used to determine the steady state VSM activation, *Act*, as a function of cytosolic  $Ca^{2+}$ ,  $Ca_i$ . The system of differential equations is run to steady state for a range of *Cai* and then the Hill expression given below is used to fit the simulation results. This is done to prevent a steady-state simulation to be run repeatedly in the integrated model and at this point we are not interested in the dynamic response of the system.

Algebraic and differential equations:

$$
Act = \frac{AMP + AM}{(AMP + AM)_{max}}
$$
 [S7]

$$
K_1 = K_6 = \gamma C a_i^3 \tag{S8}
$$

$$
\frac{dM}{dt} = -K_1 M + K_2 M p + K_7 A M \tag{S9}
$$

$$
\frac{\mathrm{d}Mp}{\mathrm{d}t} = K_4 A M p + K_1 M - (K_2 + K_3) M p \tag{S10}
$$

$$
\frac{\mathrm{d}AMp}{\mathrm{d}t} = K_3Mp + K_6AM - (K_4 + K_5)AMP
$$
 [S11]

$$
\frac{\mathrm{d}AM}{\mathrm{d}t} = K_s A M p - \left(K_s + K_7\right) AM \tag{S12}
$$

Setting of initial conditions:

$$
M = Mp = AMp = AM = 0.25
$$
 [S13]

Hill expression for fit of steady-state VSM activation:

$$
Act = \frac{Ca_i^{n_{XB}}}{K_{caxB}^{n_{XB}} + Ca_i^{n_{XB}}}
$$
 [S14]

# **Model 3: VSM Ca2+ handling and electrophysiology model**

Kapela et al. have made several clarifications and modifications to the original published model that are incorporated into this current model. These were determined from their model code and communications with the authors. For sGC activation, the time constant for the change in rate of cGMP formation, <sup>τ</sup>*sGC*, is determined differently as indicated below. Additionally the activation gating for the store-operated cation channel has been changed from a simple algebraic relationship to the first-order kinetics given below. Corrections have been made to fixed parameter values for  $K_{NSC}$  and *g<sub>NCX</sub>* and units on *g<sub>NCX</sub>*,  $L_{NaKCl}$  and  $\overline{I}_{IP3}$  as indicated in Table S3. A minimal set of initial conditions is specified and then the remaining initial conditions are calculated as given below. For the  $\alpha_1$ -adrenoreceptor and IP<sub>3</sub> formation equations it was not clear whether the ratio of activities of the ligand-bound to ligand-unbound receptor species,  $\delta_G$ , is a variable or fixed parameter. In this model  $\delta_G$  (here given as  $\delta_{G0}$ ) is estimated based on the initial conditions and held constant throughout the simulation as specified below. Other variables such as the rate of hydrolysis of PIP2, *rhG*, are initially estimated and then recalculated during the simulation. Standard units of concentration, time, membrane potential,vessel stress and current are mM, ms, mV, kPa and pA in this portion of the integrated model. Note that for the myogenic response both the NE stimulation and NO relaxation mechanisms are inactive and vessel diameter is driven only by step changes in pressure. The model retains these inactive pathways to remain consistent with the previous model by Kapela et al. In the simulations used in this study a single stress- or strain-controlled channel was inserted into the model at a time. The sets of equations below show all formulations of stress- and strain-controlled channels used.

Algebraic and differential equations:

*Reversal potentials*:

$$
E_K = \frac{RT}{z_K F} \ln\left(\frac{K_e}{K_i}\right) \tag{S15}
$$

$$
E_{Na} = \frac{RT}{z_{Na}F} \ln\left(\frac{Na_e}{Na_i}\right)
$$
 [S16]

$$
E_{Ca} = \frac{RT}{z_{Ca}F} \ln\left(\frac{Ca_e}{Ca_i}\right)
$$
 [S17]

$$
E_{Cl} = \frac{RT}{z_{Cl}F} \ln\left(\frac{Cl_e}{Cl_i}\right)
$$
 [S18]

*Mechanically-controlled supplementary Ca2+channel:* 

Formulated as a stress-controlled channel (channel variant 4):

$$
\bar{h}_{CaoCC} = \frac{\sigma_{total}^{n_{CaoCC}}}{\sigma_{50, CaoCC}^{n_{CaoCC}} + \sigma_{total}^{n_{CaoCC}}}
$$
 [S19]

$$
I_{Ca\sigma CC} = g_{Ca\sigma CC}^{\text{max}} h_{Ca\sigma CC} (V_m - E_{Ca})
$$
 [S20]

$$
\frac{dh_{Ca\sigma CC} }{dt} = \frac{h_{Ca\sigma CC} - h_{Ca\sigma CC}}{\tau_{Ca\sigma CC}}
$$
 [S21]

Formulated as a strain-controlled channel:

$$
\overline{h}_{CaseC} = \frac{\varepsilon_{total}^{n_{CaseC}}}{\varepsilon_{50, Ca\epsilon CC}^{n_{CaseC}} + \varepsilon_{total}^{n_{CaseC}}}
$$
 [S22]

$$
I_{CacCC} = g_{CacCC}^{\text{max}} h_{CacCC} (V_m - E_{Ca})
$$
 [S23]

$$
\frac{dh_{CaseC}}{dt} = \frac{h_{CaseC} - h_{CaseC}}{\tau_{CaseC}}
$$
 [S24]

*Mechanically-controlled supplementary Na+ channel:* 

Formulated as a stress-controlled channel (channel variant 5):

$$
\overline{h}_{Na\sigma CC} = \frac{\sigma_{total}^{n_{Na\sigma CC}}}{\sigma_{50,Na\sigma CC}^{n_{Na\sigma CC}} + \sigma_{total}^{n_{Na\sigma CC}}}
$$
 [S25]

$$
I_{Na\sigma CC} = g_{Na\sigma CC}^{max} h_{Na\sigma CC} (V_m - E_{Na})
$$
 [S26]

$$
\frac{dh_{Na\sigma CC}}{dt} = \frac{h_{Na\sigma CC} - h_{Na\sigma CC}}{\tau_{Na\sigma CC}}
$$
 [S27]

Formulated as a strain-controlled channel:

$$
\overline{h}_{NacCC} = \frac{\varepsilon_{total}^{n_{NacCC}}}{\varepsilon_{50,NacCC}^{n_{NacCC}} + \varepsilon_{total}^{n_{NacCC}}}
$$
 [S28]

$$
I_{NacCC} = g_{NacCC}^{\max} h_{NacCC} (V_m - E_{Na})
$$
 [S29]

$$
\frac{dh_{NascC}}{dt} = \frac{h_{NascC} - h_{NascC}}{\tau_{NascC}}
$$
 [S30]

*L-Type voltage operated Ca2+ channel:*  Formulation from Kapela et al.:

$$
\bar{d}_{L} = \frac{1}{1 + \exp(-V_{m}/8.3)}
$$
 [S31]

$$
\overline{f}_L = \frac{1}{1 + \exp[(V_m + 42)/9.1]}
$$
 [S32]

$$
\tau_{dL} = 2.5 \exp\left[-\left(\frac{V_m + 40}{30}\right)^2\right] + 1.15
$$
 [S33]

$$
\tau_{fL} = 65 \exp\left[-\left(\frac{V_m + 35}{25}\right)^2\right] + 45
$$
 [S34]

<span id="page-9-2"></span><span id="page-9-1"></span><span id="page-9-0"></span>
$$
I_{Vocc} = 10^{6} A_{m} P_{Vocc} d_{L} f_{L} \frac{V_{m} (z_{Ca} F)^{2}}{RT} \frac{Ca_{e} - Ca_{i} \exp(V_{m} z_{Ca} F/RT)}{1 - \exp(V_{m} z_{Ca} F/RT)}
$$
 [S35]

$$
\frac{dd_L}{dt} = \frac{\overline{d}_L - d_L}{\tau_{dL}}
$$
 [S36]

$$
\frac{df_L}{dt} = \frac{\overline{f}_L - f_L}{\tau_{fL}}
$$
 [S37]

Formulated as a channel with vessel stress-control of gating voltage (channel variant 6), which is same as Kapela et al. formulation except the following three equations now replace [\[S31\]](#page-9-0)  and [\[S32\]:](#page-9-1)

$$
V_{Cal\sigma CC}^{\text{off}} = V_{Cal\sigma CC}^{\text{offmax}} \frac{\sigma_{total}^{n_{Cal\sigma CC}}}{\sigma_{50, Cal\sigma CC}^{n_{Cal\sigma CC}} + \sigma_{total}^{n_{Cal\sigma CC}}}
$$
 [S38]

$$
\overline{d}_L = \frac{1}{1 + \exp\left[-\left(V_m + V_{\text{cal}\sigma CC}^{\text{off}}\right)/8.3\right]}
$$
 [S39]

$$
\overline{f}_L = \frac{1}{1 + \exp\left[\left(V_m + V_{Cal\sigma CC}^{\text{off}} + 42\right)/9.1\right]}
$$
 [S40]

Formulated as a channel with vessel strain-control of gating voltage, which is the same as Kapela et al. formulation except the following three equations now replace [\[S31\]](#page-9-0) and [\[S32\]](#page-9-1):

$$
V_{Cal\epsilon CC}^{\text{off}} = V_{Cal\epsilon CC}^{\text{offmax}} \frac{\varepsilon_{total\epsilon CC}^{n_{Cal\epsilon CC}}}{\varepsilon_{50, Cal\epsilon CC}^{n_{Cal\epsilon CC}} + \sigma_{total}^{n_{Cal\epsilon CC}}}
$$
 [S41]

$$
\overline{d}_{L} = \frac{1}{1 + \exp\left[-\left(V_{m} + V_{\text{calcCC}}^{\text{off}}\right)/8.3\right]}
$$
 [S42]

$$
\overline{f}_L = \frac{1}{1 + \exp\left[\left(V_m + V_{Cal\epsilon CC}^{\text{off}} + 42\right)/9.1\right]}
$$
 [S43]

Formulated as a channel with vessel stress-control of conductance (channel variant 7), which is the same as Kapela et al. formulation except for the following 2 equations now replace [\[S35\]](#page-9-2):

$$
\rho_{Cal\sigma CC} = 1 + (\rho_{\rho Cal\sigma CC}^{\text{max}} - 1) \frac{\sigma_{total}^{\text{n}_{\rho Cal\sigma CC}}}{\sigma_{50,\rho Cal\sigma CC}^{\text{n}_{\rho Cal\sigma CC}} + \sigma_{total}^{\text{n}_{\rho Cal\sigma CC}}}
$$
 [S44]

$$
I_{vocc} = 10^{6} A_{m} P_{vocc} \rho_{Caloc} d_{L} f_{L} \frac{V_{m} (z_{Ca} F)^{2}}{RT} \frac{C a_{e} - C a_{i} \exp(V_{m} z_{Ca} F/RT)}{1 - \exp(V_{m} z_{Ca} F/RT)}
$$
 [S45]

Formulated as a channel with vessel strain-control of conductance, which is the same as Kapela et al. formulation except for the following 2 equations now replace [\[S35\]:](#page-9-2)

$$
\rho_{Cal\epsilon CC} = 1 + (\rho_{\rho Cal\epsilon CC}^{\text{max}} - 1) \frac{\varepsilon_{total}^{\text{p}_{\text{total}\epsilon CC}}}{\varepsilon_{50,\rho Cal\epsilon CC}^{\text{p}_{\text{total}\epsilon CC}} + \varepsilon_{total}^{\text{p}_{\text{total}\epsilon CC}}}
$$
 [S46]

$$
I_{Vocc} = 10^{6} A_{m} P_{Vocc} \rho_{Cal\_acc} d_{L} f_{L} \frac{V_{m} (z_{Ca} F)^{2}}{RT} \frac{Ca_{e} - Ca_{i} \exp(V_{m} z_{Ca} F/RT)}{1 - \exp(V_{m} z_{Ca} F/RT)}
$$
 [S47]

*Large conductance Ca2+-activated K+ channel:*

Formulation from Kapela et al.:

$$
P_{KCa} = 0.17 p_f + 0.83 p_s \tag{S48}
$$

$$
R_{NO} = \frac{NO}{NO + 0.2 \times 10^{-3}}
$$
 [S49]

$$
R_{cGMP} = \frac{cGMP^2}{cGMP^2 + (1.5 \times 10^{-3})^2}
$$
 [S50]

<span id="page-10-0"></span>
$$
V_{50,KCa} = -41.7 \log(Ca_i) - 128.2 - (dV_{50,KCaNO}R_{NO}) - (dV_{50,KCaCGMP}R_{cGMP})
$$
 [S51]

$$
\overline{p}_o = \frac{1}{1 + \exp\left[-\left(V_m - V_{50, KCa}\right)/18.25\right]}
$$
 [S52]

<span id="page-10-1"></span>
$$
I_{B K C a} = 10^{6} A_{m} N_{B K C a} P_{B K C a} P_{K C a} \frac{V_{m} (z_{K} F)^{2}}{RT} \frac{K_{e} - K_{i} \exp(V_{m} z_{K} F/RT)}{1 - \exp(V_{m} z_{K} F/RT)}
$$
 [S53]

$$
\frac{\mathrm{d}p_f}{\mathrm{d}t} = \frac{\overline{p}_o - p_f}{\tau_{pf}}\tag{S54}
$$

$$
\frac{\mathrm{d}p_s}{\mathrm{d}t} = \frac{\overline{p}_o - p_s}{\tau_{ps}} \tag{S55}
$$

Formulated as a channel with vessel stress-control of gating voltage (channel variant 8), which is same as Kapela et al. formulation except the following two equations now replace [\[S52\]:](#page-10-0)

$$
V_{BKG\sigma CC}^{\text{off}} = V_{BKG\sigma CC}^{\text{offmax}} \frac{\sigma_{total}^{n_{BKG\sigma CC}}}{\sigma_{50, BKG\sigma CC}^{n_{BKG\sigma CC}} + \sigma_{total}^{n_{BKG\sigma CC}}}
$$
 [S56]

$$
\overline{p}_o = \frac{1}{1 + \exp\left[-\left(V_m + V_{B K C a \sigma C C}^{\text{off}} - V_{50, K C a}\right) / 18.25\right]}
$$
 [S57]

Formulated as a channel with vessel strain-control of gating voltage, which is same as Kapela et al. formulation except the following two equations now replace [\[S52\]](#page-10-0):

$$
V_{BKGacCC}^{\text{off}} = V_{BKGacCC}^{\text{offmax}} \frac{\varepsilon_{total}^{n_{BKGacCC}}}{\varepsilon_{50, BKGacCC}^{n_{BKGacCC}} + \varepsilon_{total}^{n_{BKGacCC}}}
$$
 [S58]

$$
\overline{p}_o = \frac{1}{1 + \exp\left[-\left(V_m + V_{BKGacCC}^{\text{off}} - V_{50,KCa}\right)/18.25\right]}
$$
 [S59]

Formulated as a channel with vessel stress-control of conductance (channel variant 9), which is same as Kapela et al. formulation except the following two equations now replace [\[S53\]](#page-10-1):

$$
\rho_{B K Ca\sigma CC} = 1 - (1 - \rho_{\rho B K Ca\sigma CC}^{\max}) \frac{\sigma_{total}^{n_{\rho B K Ca\sigma CC}}}{\sigma_{50, \rho B K Ca\sigma CC}^{n_{\rho B K Ca\sigma CC}} + \sigma_{total}^{n_{\rho B K Ca\sigma CC}}
$$
 [S60]

$$
I_{B K C a} = 10^{6} A_{m} N_{B K C a} P_{B K C a} \rho_{B K C a \sigma C C} P_{K C a} \frac{V_{m} (z_{K} F)^{2}}{RT} \frac{K_{e} - K_{i} \exp(V_{m} z_{K} F/RT)}{1 - \exp(V_{m} z_{K} F/RT)}
$$
 [S61]

Formulated as a channel with vessel strain-control of gating voltage, which is same as Kapela et al. formulation except the following two equations now replace [\[S53\]:](#page-10-1)

$$
\rho_{BKCacCC} = 1 - (\rho_{\rho BKCacCC}^{\max} - 1) \frac{\varepsilon_{total}^{n_{\rho BKCacCC}}}{\varepsilon_{50, \rho BKCacCC}^{n_{\rho BKCacCC}} + \varepsilon_{total}^{n_{\rho BKCacCC}}}
$$
 [S62]

$$
I_{B K C a} = 10^{6} A_{m} N_{B K C a} P_{B K C a} O_{B K C s C C} P_{K C a} \frac{V_{m} (z_{K} F)^{2}}{RT} \frac{K_{e} - K_{i} \exp(V_{m} z_{K} F/RT)}{1 - \exp(V_{m} z_{K} F/RT)}
$$
[S63]

*Voltage dependent K+ channel:* 

$$
\overline{p}_K = \frac{1}{1 + \exp[-(V_m + 11)/15]}
$$
 [S64]

$$
\overline{q} = \frac{1}{1 + \exp\left[\left(V_m + 40\right)/14\right]}
$$
 [S65]

$$
\tau_{pK} = 61.49 \exp(-0.0268 V_m)
$$
 [S66]

$$
I_{Kv} = g_{Kv} p_k \left( 0.45 q_1 + 0.55 q_2 \right) \left( V_m - E_K \right) \tag{S67}
$$

$$
\frac{\mathrm{d}p_K}{\mathrm{d}t} = \frac{\overline{p}_K - p_K}{\tau_{pK}}\tag{S68}
$$

$$
\frac{dq_1}{dt} = \frac{\overline{q} - q_1}{\tau_{q1}} \tag{S69}
$$

$$
\frac{dq_2}{dt} = \frac{\overline{q} - q_2}{\tau_{q2}}
$$
 [S70]

Unspecified  $K^+$  leak channel including ATP-sensitive  $K^+$  channel:

$$
I_{Kleak} = g_{Kleak} \left( V_m - E_k \right) \tag{S71}
$$

<span id="page-12-2"></span>*Non-selective cation channel:* 

<span id="page-12-1"></span>Formulation from Kapela et al.:

$$
DAG = IP_3 \tag{S72}
$$

$$
Po_{NSC} = 0.4344 + \frac{0.5656}{1 + \exp[-(V_m - 47.12)/24.24]}
$$
 [S73]

$$
I_{NaNSC} = 10^6 A_m P_{NANSC} \left( \frac{DAG}{DAG + K_{NSC}} + d_{NSC}^{\min} \right) Po_{NSC}
$$
  
\$\downarrow\$  $V_m (z_{Na}F)^2 Na_e - Na_i \exp(V_m z_{Na}F/RT)$  [S74]

$$
V_m \left(z_{Na}F\right)^2 N a_e - N a_i \exp\left(V_m z_{Na} F / RT\right)
$$
  
RT 
$$
1 - \exp\left(V_m z_{Na} F / RT\right)
$$
  

$$
I_{KNSC} = 10^6 A_m P_{KNSC} \left(\frac{DAG}{DAG + K_{NSC}} + d_{NSC}^{\min}\right) Po_{NSC}
$$
  

$$
V_m \left(z - E\right)^2 K_m V_{NSC} \left(V_{K} - E / PT\right)
$$
 [S75]

$$
*\frac{V_m(z_K F)^2}{RT}\frac{K_e - K_i \exp(V_m z_K F/RT)}{1 - \exp(V_m z_K F/RT)}
$$

$$
I_{\text{cansc}} = 10^6 A_m P_{\text{cansc}} d_{\text{NSC}}^{\min} P_{\text{O}_{\text{NSC}}} \frac{V_m (z_{\text{c}a} F)^2}{RT} \frac{C a_e - C a_i \exp(V_m z_{\text{c}a} F/RT)}{1 - \exp(V_m z_{\text{c}a} F/RT)} \tag{S76}
$$

$$
I_{NSC} = I_{NANSC} + I_{KNSC} + I_{CANSC}
$$
 [S77]

<span id="page-12-0"></span>Formulated as a channel with vessel stress-control of  $Ca^{2+}$  conductance (channel variant 1), which is same as Kapela et al. formulation except the following two equations now replace [\[S76\]](#page-12-0):

$$
\rho_{\text{CaNSC}\sigma CC} = 1 + (\rho_{\text{CaNSC}\sigma CC}^{\text{max}} - 1) \frac{\sigma_{\text{total}}^{\text{n}_{\text{caNSC}\sigma CC}}}{\sigma_{\text{50},\text{CaNSC}\sigma CC}^{\text{n}_{\text{CaNSC}\sigma CC}} + \sigma_{\text{total}}^{\text{n}_{\text{CaNSC}\sigma CC}}
$$
 [S78]

$$
I_{\text{cansc}} = 10^6 A_m P_{\text{cansc}} d_{\text{NSC}}^{\text{min}} \rho_{\text{cansc}\sigma\text{c}} P o_{\text{NSC}} \frac{V_m (z_{\text{c}a} F)^2}{RT} \frac{C a_e - C a_i \exp(V_m z_{\text{c}a} F/RT)}{1 - \exp(V_m z_{\text{c}a} F/RT)} \text{[S79]}
$$

Formulated as a channel with vessel strain-control of  $Ca^{2+}$  conductance, which is same as Kapela et al. formulation except the following two equations now replace [\[S76\]:](#page-12-0)

$$
\rho_{\text{CaNSC} \epsilon CC} = 1 + (\rho_{\text{CaNSC} \epsilon CC}^{\text{max}} - 1) \frac{\varepsilon_{\text{total}}^{\text{R}_{\text{CaNSC} \epsilon CC}}}{\varepsilon_{\text{50},\text{CaNSC} \epsilon CC}^{\text{R}_{\text{caNSC} \epsilon CC}} + \varepsilon_{\text{total}}^{\text{R}_{\text{CaNSC} \epsilon CC}}}
$$
[S80]

$$
I_{\text{cansc}} = 10^6 A_m P_{\text{cansc}} d_{\text{NSC}}^{\text{min}} \rho_{\text{cansc}c\epsilon C} P o_{\text{NSC}} \frac{V_m (z_{c_a} F)^2}{RT} \frac{C a_e - C a_i \exp(V_m z_{c_a} F/RT)}{1 - \exp(V_m z_{c_a} F/RT)} \text{ [S81]}
$$

Formulated as a channel with vessel stress-control of  $Na<sup>+</sup>$  conductance (channel variant 2), which is same as Kapela et al. formulation except the following two equations now replace [\[S74\]](#page-12-1):

$$
\rho_{\scriptscriptstyle NaNSC\sigma CC} = 1 + (\rho_{\scriptscriptstyle NaNSC\sigma CC}^{\scriptscriptstyle \text{max}} - 1) \frac{\sigma_{\scriptscriptstyle \text{total}}^{\scriptscriptstyle n_{\scriptscriptstyle NaNSC\sigma CC}}}{\sigma_{\scriptscriptstyle 50, NaNSC\sigma CC}^{\scriptscriptstyle n_{\scriptscriptstyle NaNSC\sigma CC}} + \sigma_{\scriptscriptstyle \text{total}}^{\scriptscriptstyle n_{\scriptscriptstyle NaNSC\sigma CC}}}
$$
 [S82]

$$
I_{NaNSC} = 10^{6} A_{m} P_{NaNSC} \left( \frac{DAG}{DAG + K_{NSC}} + d_{NSC}^{\min} \right) \rho_{NaNSC\sigma CC} P o_{NSC}
$$
\n
$$
* \frac{V_{m} (z_{Na}F)^{2}}{RT} \frac{Na_{e} - Na_{i} \exp(V_{m} z_{Na}F/RT)}{1 - \exp(V_{m} z_{Na}F/RT)}
$$
\n[S83]

Formulated as a channel with vessel stress-control of  $Na<sup>+</sup>$  conductance, which is same as Kapela et al. formulation except the following two equations now replace [\[S74\]:](#page-12-1)

$$
\rho_{NaNSC\epsilon CC} = 1 + (\rho_{NaNSC\epsilon CC}^{\max} - 1) \frac{\varepsilon_{total}^{n_{NaNSC\epsilon CC}}}{\varepsilon_{50, NaNSC\epsilon CC}^{n_{NaNSC\epsilon CC}} + \varepsilon_{total}^{n_{NaNSC\epsilon CC}}}
$$
\n[S84]  
\n
$$
I_{NaNSC} = 10^6 A_m P_{NaNSC} \left( \frac{DAG}{DAG + K_{NSC}} + d_{NSC}^{\min} \right) \rho_{NaNSC\epsilon CC} P o_{NSC}
$$
\n[S85]  
\n\*  $\frac{V_m (z_{Na}F)^2}{RT} \frac{Na_e - Na_i \exp(V_m z_{Na}F/RT)}{1 - \exp(V_m z_{Na}F/RT)}$ 

Formulated as a channel with vessel stress-control of  $Ca^{2+}$  and Na<sup>+</sup> gating voltage (channel variant 3), which is same as Kapela et al. formulation except the following two equations now replace [\[S73\]](#page-12-2):

$$
V_{NSC\sigma CC}^{off} = V_{NSC\sigma CC}^{off \max} \frac{\sigma_{total}^{n_{NSC\sigma CC}}}{\sigma_{50,NSC\sigma CC}^{n_{NSC\sigma CC}} + \sigma_{total}^{n_{NSC\sigma CC}}}
$$
 [S86]

$$
Po_{NSC} = 0.4344 + \frac{0.5656}{1 + \exp[-\left(V_m + V_{NSC\sigma CC}^{off} - 47.12\right)/24.24]}\tag{S87}
$$

Formulated as a channel with vessel strain-control of  $Ca^{2+}$  and Na<sup>+</sup> gating voltage, which is same as Kapela et al. formulation except the following two equations now replace [\[S73\]:](#page-12-2)

$$
V_{NSC\epsilon CC}^{off} = V_{NSC\epsilon CC}^{off \max} \frac{\varepsilon_{total}^{n_{NSC\epsilon CC}}}{\varepsilon_{50,NSC\epsilon CC}^{n_{NSC\epsilon CC}} + \varepsilon_{total}^{n_{NSC\epsilon CC}}}
$$
 [S88]

$$
Po_{NSC} = 0.4344 + \frac{0.5656}{1 + \exp[-(V_m + V_{NSC\epsilon CC}^{off} - 47.12)/24.24]}
$$
 [S89]

*Store-operated non-selective cation channel:* 

$$
\overline{P}_{SOC} = \frac{1}{1 + Ca_{SRu}/K_{SOC}}
$$
 [S90]

$$
I_{NaSOC} = g_{NaSOC} P_{SOC} (V_m - E_{Na})
$$
 [S91]

$$
I_{CasOC} = g_{CasOC} P_{SOC} (V_m - E_{Ca})
$$
 [S92]

$$
I_{SOC} = I_{NasOC} + I_{casOC}
$$
 [S93]

$$
\frac{\mathrm{d}P_{SOC}}{\mathrm{d}t} = \frac{\overline{P}_{SOC} - P_{SOC}}{\tau_{SOC}}
$$
 [S94]

*Ca2+-activated Cl- channel:* 

$$
\alpha_{\text{Cl}} = \frac{cGMP^{n_{\text{ClcGMP}}}}{cGMP^{n_{\text{ClcGMP}}} + K_{\text{ClcGMP}}^{n_{\text{ClcGMP}}}}
$$
 [S95]

$$
K_{\text{ClCacGMP}} = 4 \times 10^{-4} \left( 1 - 0.9 \alpha_{\text{Cl}} \right) \tag{S96}
$$

$$
P_{Cl} = R_{ClcGMP}^{\min} \frac{C a_i^{n_{ClCa}}}{C a_i^{n_{ClCa}} + K_{ClCa}^{n_{ClCa}}} + \alpha_{Cl} \frac{C a_i^{n_{ClCa}}}{C a_i^{n_{ClCa}} + K_{ClCacGMP}^{n_{ClCa}}}
$$
 [S97]

$$
I_{ClCa} = C_m g_{ClCa} P_{Cl} (V_m - E_{Cl})
$$
 [S98]

*Plasma membrane Ca2+-ATPase:* 

$$
I_{PMCA} = \overline{I}_{PMCA} \frac{Ca_i}{Ca_i + K_{mPMCA}}
$$
 [S99]

*Plasma membrane Na+ -Ca2+ exchanger:* 

$$
R_{NCXcGMP} = 1 + 0.55 \frac{cGMP}{cGMP + 4.5 \times 10^{-2}}
$$
 [S100]

$$
\phi_F = \exp\left(\frac{\gamma_{\text{NCX}} V_m F}{RT}\right) \tag{S101}
$$

$$
\phi_R = \exp\left[\frac{(\gamma_{NCX} - 1)V_m F}{RT}\right]
$$
 [S102]

$$
I_{NCX} = g_{NCX} R_{NCXcGMP} \frac{Na_i^3 Ca_e \phi_F - Na_e^3 Ca_i \phi_R}{1 + d_{NCX} \left( Na_e^3 Ca_i + Na_i^3 Ca_e \right)}
$$
 [S103]

*Na+ -K+ pump:* 

$$
I_{\text{Nak}} = C_m \overline{I}_{\text{Nak}} Q_{\text{Nak}} \frac{K_e^{n_{\text{HKe}}} - N a_i^{n_{\text{HNa}}} N a_i^{n_{\text{HNa}}}}{K_e^{n_{\text{HKe}}} + K_{dKe}^{n_{\text{HNa}}} N a_i^{n_{\text{HNa}}} + K_{d\text{Nai}}^{n_{\text{HNa}}} V_m + 200}
$$
 [S104]

*Na+ -K+ -Cl- cotransporter:* 

$$
R_{\text{NaKClcGMP}} = 1 + 3.5 \frac{cGMP}{cGMP + 6.4 \times 10^{-3}}
$$
 [S105]

$$
I_{\text{CINaKCl}} = -A_{m} R_{\text{NaKClcGMP}} L_{\text{NaKCl}} z_{\text{Cl}} FRT \ln \left[ \left( \frac{N a_{e}}{N a_{i}} \right) \left( \frac{K_{e}}{K_{i}} \right) \left( \frac{C l_{e}}{C l_{i}} \right)^{2} \right]
$$
 [S106]

$$
I_{\text{NaNaKCl}} = -\frac{I_{\text{ClNaKCl}}}{2} \tag{S107}
$$

$$
I_{\text{KNaKCl}} = -\frac{I_{\text{CINaKCl}}}{2} \tag{S108}
$$

*Sarcoplasmic reticulum IP3 receptor:* 

$$
I_{IP3} = \overline{I}_{IP3} Vol_{Ca} z_{Ca} F \left( \frac{IP_3}{IP_3 + K_{IP3}} \frac{Ca_i}{Ca_i + K_{IP3}^{act}} h_{IP3} \right)^3 \left( Ca_{SRu} - Ca_i \right)
$$
 [S109]

$$
\frac{dh_{IP3}}{dt} = k_{IP3}^{on} \left[ K_{IP3}^{inh} - \left( Ca_i + K_{IP3}^{inh} \right) h_{IP3} \right]
$$
 [S110]

*Sarcoplasmic reticulum SERCA, internal diffusion and release:* 

$$
I_{SERCA} = \overline{I}_{SERCA} \frac{Ca_i}{Ca_i + K_m^{up}}
$$
 [S111]

$$
I_{tr} = \frac{Vol_{SRu} z_{Ca} F}{\tau_{tr}} (Ca_{SRu} - Ca_{SRr})
$$
 [S112]

$$
I_{rel} = \frac{Vol_{SRr} z_{Ca} F}{\tau_{rel}} \left( R_{10}^2 + R_{leak} \right) \left( Ca_{SRr} - Ca_i \right)
$$
 [S113]

$$
\frac{\mathrm{d}Ca_{SRu}}{\mathrm{d}t} = \frac{I_{SERCA} - I_{tr} - I_{IP3}}{Vol_{SRu} z_{Ca} F}
$$
 [S114]

$$
\frac{dCa_{SRr}}{dt} = \frac{I_{tr} - I_{rel}}{\left(Vol_{SRr}z_{Ca}F\right)\left[1 + \frac{\overline{CSQN}K_{CSQN}}{\left(K_{CSQN} + Ca_{SRr}\right)^2}\right]}
$$
 [S115]

*Sarcoplasmic reticulum ryanodine receptor:* 

$$
R_{00} = 1 - R_{10} - R_{11} - R_{01}
$$
 [S116]

$$
\frac{dR_{10}}{dt} = K_{r1}Ca_i^2R_{00} - (K_{mr1} + K_{r2}Ca_i)R_{10} + K_{mr2}R_{11}
$$
 [S117]

$$
\frac{dR_{11}}{dt} = K_{r2}Ca_iR_{10} - (K_{mr1} + K_{mr2})R_{11} + K_{r1}Ca_i^2R_{01}
$$
 [S118]

$$
\frac{dR_{01}}{dt} = K_{r2}Ca_iR_{00} + K_{mr1}R_{11} - (K_{mr2} + K_{r1}Ca_i^2)R_{01}
$$
 [S119]

<sup>α</sup>*1-adrenoreceptor activation and IP3 formation:* 

$$
\rho_{rG} = \frac{NER_G^S}{\xi_G R_{rG} \left( K_{1G} + NE \right)} \tag{S120}
$$

$$
r_{hG} = \alpha_G G \frac{Ca_i}{Ca_i + K_{cG}} \tag{S121}
$$

$$
\frac{dR_G^S}{dt} = k_{rG}\xi_G R_{TG} - \left(k_{rG} + \frac{k_{pG}NE}{K_{1G} + NE}\right)R_G^S - k_{rG}R_{PG}^S
$$
 [S122]

$$
\frac{dR_{PG}^S}{dt} = NE \left( \frac{k_{PG} R_G^S}{K_{1G} + NE} - \frac{k_{eG} R_{PG}^S}{K_{2G} + NE} \right)
$$
 [S123]

$$
\frac{\mathrm{d}G}{\mathrm{d}t} = k_{aG} \left( \delta_{G0} + \rho_{rG} \right) \left( G_{TG} - G \right) - k_{dG} G \tag{S124}
$$

$$
\frac{\text{dIP}_3}{\text{d}t} = \frac{r_{hG}PIP_2}{\gamma_G} - k_{\text{deg }G}IP_3
$$
 [S125]

$$
\frac{dPIP_2}{dt} = -\left(r_{hG} + r_{rG}\right)PIP_2 - r_{rG}\gamma_GIP_3 + r_{rG}PIP_{2T}
$$
 [S126]

### *sGC activation and cGMP formation:*

$$
\overline{V}_{cGMP} = V_{cGMP}^{\text{max}} \frac{B5_{sGC}NO + NO^2}{AO_{sGC} + A1_{sGC}NO + NO^2}
$$
 [S127]

$$
\tau_{sGC} = \begin{cases}\n\frac{1}{k_{3sGC}NO + k_{DrsGC}} & \text{if } \bar{V}_{cGMP} - V_{cGMP} \ge 0 \\
\frac{1}{k_{m2sGC} + k_{DrsGC}} & \text{otherwise}\n\end{cases}
$$
\n[S128]

$$
\frac{dV_{cGMP}}{dt} = \frac{\bar{V}_{cGMP} - V_{cGMP}}{\tau_{sGC}}
$$
 [S129]

$$
\frac{\text{dcGMP}}{\text{d}t} = V_{cGMP} - k_{pdecGMP} \left( \frac{cGMP^2}{cGMP + K_{mpde}} \right)
$$
 [S130]

*Ionic balances:* 

Note: For vessel stress-controlled supplementary  $Ca^{2+}$  channel (channel variant 4 with stress),  $I_{CaoCC}$  is calculated from equation [S20], otherwise it is 0. For vessel strain-controlled supplementary  $Ca^{2+}$  channel (channel variant 4 with strain),  $I_{CaeCC}$  is calculated from equation [S23], otherwise it is 0. For vessel stress-controlled supplementary  $Na<sup>+</sup>$  channel (channel variant 5 with stress),  $I_{NaoCC}$  is calculated from equation [S26], otherwise it is 0. For vessel straincontrolled supplementary Na<sup>+</sup> channel (channel variant 5 with strain),  $I_{NacCC}$  is calculated from equation [S29], otherwise it is 0.

$$
I_{\text{Caatom}} = I_{\text{CaSOC}} + I_{\text{VOCC}} - 2I_{\text{NCX}} + I_{\text{PMCA}} + I_{\text{CaNSC}} + I_{\text{Ca}\sigma CC} + I_{\text{Ca}\sigma CC}
$$
 [S131]

$$
I_{\text{Natom}} = I_{\text{NaN} \text{AKCl}} + I_{\text{Na} \text{SOC}} + 3I_{\text{Nak}} + 3I_{\text{NCX}} + I_{\text{Na} \text{NSC}} + I_{\text{Na} \text{OCC}} + I_{\text{Na} \text{EC}}
$$
 [S132]

$$
I_{K\text{totm}} = I_{K\text{NakCl}} + I_{B\text{KCa}} + I_{Kv} + I_{K\text{NSC}} + I_{K\text{leak}} - 2I_{\text{Nak}}
$$
 [S133]

$$
I_{\text{Cltotm}} = I_{\text{ClNaKCl}} + I_{\text{ClCa}} \tag{S134}
$$

$$
\frac{dCa_{i}}{dt} = -\frac{I_{\text{Catotm}} + I_{\text{SERCA}} - I_{\text{rel}} - I_{\text{IP3}}}{Vol_{Ca} z_{Ca} F} \left( \frac{1}{1 + \frac{\overline{S}_{\text{CM}} K_{\text{dCM}}}{(K_{\text{dCM}} + Ca_{i})^{2}} + \frac{\overline{B}_{\text{F}} K_{\text{dB}}}{(K_{\text{dB}} + Ca_{i})^{2}}} \right) \quad [S135]
$$

$$
\frac{dNa_i}{dt} = -\frac{I_{\text{Natom}}}{Vol_i z_{\text{Na}} F}
$$
 [S136]

$$
\frac{\mathrm{d}K_i}{\mathrm{d}t} = -\frac{I_{\text{Ktotm}}}{Vol_i z_K F} \tag{S137}
$$

$$
\frac{\mathrm{d}CI_{i}}{\mathrm{d}t} = -\frac{I_{\text{Cltotm}}}{Vol_{i} z_{Cl} F}
$$
 [S138]

### *Membrane potential:*

Note: Mechanically controlled supplementary channel currents ( $I_{CaoCC}$ ,  $I_{CaoCC}$ ,  $I_{NaoCC}$  and  $I_{NaeCC}$ ) are calculated as for the ionic balances as noted above.

$$
\frac{dV_m}{dt} = -\frac{1}{C_m} (I_{vocc} + I_{B K C a} + I_{K v} + I_{K le a k} + I_{N SC} + I_{S OC} + I_{C I C a}
$$
\n
$$
+ I_{P M C A} + I_{N C X} + I_{N a K} + I_{C a \sigma CC} + I_{C a \sigma CC} + I_{N a \sigma CC} + I_{N a \sigma CC} - I_{s tim})
$$
\n(S139)

Calculation of remaining fixed parameters:

*Na+ -K+ pump:* 

$$
Q_{Nak} = Q_{10}^{\frac{T-309.15}{10}}
$$
 [S140]

<sup>α</sup>*1-adrenoreceptor activation and IP3 formation:* 

$$
\gamma_G = 10^{-15} N_{Av} Vol_i
$$
 [S141]

$$
\delta_{G0} = \frac{k_{dG} G_0}{k_{dG} (G_{TG} - G_0)}
$$
 [S142]

*sGC activation and cGMP formation:* 

$$
B5_{sGC} = k_{2sGC} / k_{3sGC}
$$
 [S143]

$$
A0_{sGC} = \frac{(k_{m1sGC} + k_{2sGC})k_{DsGC} + k_{m1sGC}k_{m2sGC}}{k_{1sGC}k_{3sGC}}
$$
 [S144]

$$
A1_{sGC} = \frac{(k_{1sGC} + k_{3sGC})k_{DsGC} + (k_{2sGC} + k_{m2sGC})k_{1sGC}}{k_{1sGC}k_{3sGC}}
$$
 [S145]

Setting and calculation of initial conditions:

Vessel wall stress- or strain-activated 
$$
Ca^{2+}
$$
 channel:  
\n $h_{CaoCC} = 0$  or  $h_{CaccC} = 0$  [S146]

*Vessel wall stress- or strain-activated Na+ channel:* 

$$
h_{Na\sigma CC} = 0 \quad or \quad h_{Na\epsilon CC} = 0 \tag{S147}
$$

*L-Type voltage operated Ca2+ channel:* 

$$
d_{L0} = \frac{1}{1 + \exp(-V_{m0}/8.3)}
$$
 [S148]

$$
f_{L0} = \frac{1}{1 + \exp\left[\left(V_{m0} + 42\right)/9.1\right]}
$$
 [S149]

*Large conductance Ca2+-activated K+ channel:* 

$$
R_{NO0} = \frac{NO_0}{NO_0 + 0.2 \times 10^{-3}}
$$
 [S150]

$$
R_{cGMP0} = \frac{cGMP_0^2}{cGMP_0^2 + (0.55 \times 10^{-3})^2}
$$
 [S151]

$$
V_{50,KCa0} = -41.7 \log(Ca_{i0}) - 128.2 - dV_{50,KCaNO}R_{NO0} - dV_{50,KCaC(MP)}R_{cGMP0}
$$
 [S152]

$$
p_{f0} = \frac{1}{1 + \exp\left[-\left(V_{m0} - V_{50, KCa0}\right)/18.25\right]}
$$
 [S153]

$$
p_{s0} = \frac{1}{1 + \exp[-(V_{m0} - V_{50, KCa0})/18.25]}
$$
 [S154]

*Voltage dependent K+ channel:* 

$$
p_{K0} = \frac{1}{1 + \exp[-(V_{m0} + 11)/15]}
$$
 [S155]

$$
q_{10} = \frac{1}{1 + \exp\left[\left(V_{m0} + 40\right)/14\right]}
$$
 [S156]

$$
q_{20} = \frac{1}{1 + \exp\left[\left(V_{m0} + 40\right)/14\right]}
$$
 [S157]

*Store-operated non-selective cation channel:* 

$$
P_{\text{SOC}0} = 0 \tag{S158}
$$

*Sarcoplasmic reticulum IP3 receptor:* 

$$
h_{I P 30} = \frac{K_{I P 3}^{\text{inh}}}{C a_{i0} + K_{I P 3}^{\text{inh}}}
$$
 [S159]

*Sarcoplasmic reticulum SERCA, internal diffusion and release:* 

$$
Ca_{SRu0} = 0.66
$$
 [S160]

$$
Ca_{SRr0} = 0.57
$$
 [S161]

*Sarcoplasmic reticulum ryanodine receptor:* 

$$
R_{100} = 0.0033 \tag{S162}
$$

$$
R_{110} = 4 \times 10^{-6} \tag{S163}
$$

$$
R_{010} = 0.9955 \tag{S164}
$$

α*1-adrenoreceptor activation and IP3 formation:* 

$$
r_{hG0} = \frac{k_{\text{deg }G} \gamma_G I P_{30}}{P I P_{20}}
$$
 [S165]

$$
R_{G0}^S = R_{TG}\xi_G \tag{S166}
$$

$$
R_{PG0}^S = 0 \tag{S167}
$$

$$
G_0 = \frac{r_{hG0} (K_{cG} + Ca_{i0})}{\alpha_G Ca_{i0}}
$$
 [S168]

$$
IP_{30} = 0 \tag{S169}
$$

$$
PIP_{20} = PIP_{2T} - (1 + k_{\text{deg }G}/r_{rG})\gamma_{G}IP_{30}
$$
 [S170]

*sGC activation and cGMP formation:* 

$$
V_{cGMP0} = 0
$$
 [S171]  

$$
cGMP_0 = 0
$$
 [S172]

*Ionic balances:* 

$$
Ca_{i0} = 68 \times 10^{-6}
$$
 [S173]

$$
Na_{i0} = 8.4
$$
 [S174]  

$$
K = 140
$$
 [S175]

$$
K_{i0} = 140 \tag{S175}
$$

$$
Cl_{i0} = 59.4
$$
 [S176]

*Membrane potential:* 

$$
V_{m0} = -59.4
$$
 [S177]

# **3. TABLES OF OPTIMIZED PARAMETERS**



Table S4: Optimized parameters to fit of steady-state VSM crossbridge activation

Table S5: Optimized parameters of myogenic response fits with nine different hypothetical vessel stress-controlled channel variants



L-type  $Ca^{2+}$  channel with stress-controlled gating voltage (CaL $\sigma CC$ )



#### **4. COMPARISON OF THIN AND THICK WALL FORMULATION**



The thin wall vessel formulation for calculating average vessel wall stress (also known as the Law of Laplace) assumes the vessel wall is thin enough compared to the internal radius to have roughly constant circumferential stress across the vessel wall. In many cases this is true however when the arterioles analyzed in this study contract to very small internal diameters the circumferential stress on the inner and outer surfaces of the vessel wall may deviate from that approximated with the thin wall formulation. To estimate the error between the thin and thick walled

circumferential stress formulation for each steady state diameter reached in these experimental studies we first cast the two formulations as follows:

Thick wall circumferential stress formulation:

$$
\sigma_{\theta, TkW}(\rho) = \frac{P_1}{1 - r_1^2/r_2^2} \left( \frac{r_1^2}{r_2^2} + \frac{r_1^2}{\rho^2} \right)
$$
 [S178]

where  $\sigma_{\theta,TkW}$  is the thick wall formulation circumferential stress,  $P_l$  is the intraluminal pressure,  $r_1$  is the inner radius,  $r_2$  is the outer radius and  $\rho$  is the vessel wall position where we are calculating the stress. If we let:

$$
r_1 = R - \delta/2; \quad r_2 = R + \delta/2; \quad \rho = R + \varepsilon
$$
 [S179]

where *R* is the midline radius,  $\delta$  is the vessel wall thickness and  $\varepsilon$  varies from  $-\delta/2$  to  $\delta/2$  then we have for the thick walled stress at the normalized distance  $\varepsilon$  from the midwall radius,  $\varepsilon/R$ :

$$
\frac{\sigma_{\theta,TRW}\left(\frac{\mathcal{E}}{R}\right)}{P_1} = \frac{\left[1 - \frac{\delta}{R} + \frac{1}{4}\left(\frac{\delta^2}{R^2}\right)\right] + \left[1 - \frac{\delta}{R} + \frac{1}{4}\left(\frac{\delta^2}{R^2}\right)\right]}{1 + 2\left(\frac{\mathcal{E}}{R}\right) + \left(\frac{\mathcal{E}^2}{R^2}\right)}\right]}{1 - \left[\frac{1 - \frac{\delta}{R} + \frac{1}{4}\left(\frac{\delta^2}{R^2}\right)}{1 + \frac{\delta}{R} + \frac{1}{4}\left(\frac{\delta^2}{R^2}\right)}\right]}\tag{S180}
$$

Thin wall circumferential stress formulation:

$$
\sigma_{\theta, \text{Inv}} = \frac{P_1 r_1}{\delta} = \frac{P_1 (R - \delta/2)}{\delta}
$$
 [S181]

where  $\sigma_{\theta TnW}$  is the thin wall formulation circumferential stress. Rearranging we have:

$$
\frac{\sigma_{\theta, TnW}}{P_1} = \frac{1}{\delta \frac{Z}{R}} - \frac{1}{2}
$$
 [S182]

The standard rule of thumb for the thin walled approximation to be valid is a radius to wall thickness ratio, R/δ of 20. In the mesenteric arteriole dataset the R/δ ranges from 5 to 12 and with the femoral arteriole dataset the range is 2.5 to 5.25 so the thin walled approximation appears to be not valid in this case. However in our problem we are trying to estimate the stress across the VSM cell that spans the midline of the vessel wall where the error between thin wall and thick wall stress formulations is much smaller. Shown below in Figure S2A, B we see the error between the thick walled and thin walled vessel formulation for each data point in the mesenteric and femoral datasets. Error is given for inner wall, at 25%, at 50%, at 75% and outer vessel wall stress for each steady state diameter. If we assume the VSM cell occupies the middle 50% of the vessel wall we see that the average stress over the VSM cell varies by less than 0.5% and 2% between the two formulations over the mesenteric and femoral datasets respectively. More accurate stress values can be obtained with the thick walled vessel formulation if more detailed knowledge about how and where the stress is sensed in VSM cells. Additionally even if in this study we are underestimating or overestimating the circumferential stress we are not altering the trend in circumferential stress with changes in intraluminal pressure. Therefore free parameters in the model may change but the conclusions remain unaltered concerning which stress-controlled channel variants are able to describe the steady state myogenic response.



Figure S2. Relative error of thin wall circumferential stress formulation compared to thick wall stress formulation for A. mesenteric and B. femoral arteriole steady-state data points. Bottom graph shows average relative error across entire VSM assuming it occupies the middle 50% of the vessel wall.

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