## **Dynamic Role of Cross-Linking Proteins in Actin Rheology**

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## **Supporting Material**



FIGURE S1 Hysteresis of actin networks with various strain rates ( $\dot{\gamma}_{eff}$ ). Colors indicate different  $\dot{\gamma}_{eff}$ , and solid lines represent a stretching phase with dashed ones indicating a restoring phase (*legend*). The control case (*magenta*) has no unbinding event, corresponding to very large  $\dot{\gamma}_{eff}$ .



FIGURE S2 Differential modulus, *K*, with various (*A*)  $\dot{\gamma}_{\text{eff}}$  and (*B*) *R*. (*A*)  $\dot{\gamma}_{\text{eff}}$  is varied at 0.001-1 s<sup>-1</sup>. Darker and thicker lines indicate greater  $\dot{\gamma}_{\text{eff}}$ . (*B*) Symbols and colors indicate different *R* (*legend*).



FIGURE S3 Aging of actin networks. (*A*) A stress relaxation curve of an actin network after shearing to  $\gamma = 0.5$  without unbinding. Networks were extracted at t = 0 (*magenta circles*), 10 (*green triangles*), 20 (*blue inverted-triangles*), and 30 s (*cyan diamonds*). (*B*) *G*' (*solid*) and *G*'' (*open*) of the networks extracted from (*A*).



FIGURE S4 (*A*) *G*' (*solid*) and *G*'' (*open*) at 10 Hz with various  $k_{ub}^0 (= n \times k_{ub,r}^0)$ . (*B*) Density of active ACPs bound to two filaments,  $R^{act}$ , (*open*) and the sum of energy dissipated by unbinding of ACPs bearing more than 1 pN (*solid*).



FIGURE S5 *G*' depending on prestress ( $\tau_0$ ) level with various *R* (*legend*). The black line indicates linear scaling, *G*' ~  $\tau_0$ .