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Supplemental Data

A Subset-Based Approach Improves Power and

Interpretation for the Combined-Analysis of Genetic

Association Studies of Heterogeneous Traits

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Figure 1

T: number of truly associated traits (75% of the associations are in the positive direction)

Figure S1. Simulation-Based Power Comparison of Alternative Methods for Detecting an Overall Association.

the associations are in the positive direction)

In each simulation, a total of K=5 or K=10 distinct traits are analyzed, each with 2000 cases and 2000 controls. A variant with MAF=0.3 is assumed to be associated with a subset of the traits (the number of such traits is shown on the x-axis). The solid and dashed lines represent, respectively, power when all the OR-s for associated traits are fixed at a single value (1.15) (as in Figure 1) and power when the OR-s are allowed to vary around a fixed mean (1.15) witihin a given range (1.05-1.25; see Supplemental Methods, section 6 for details). The upper panel assumes that all of the associations are in the same direction and the lower panel assumes that 75% of the associations are positive and 25% are negative. In addition to two-sided (green lines) and one-sided (orange lines) subset-based tests, power curves are shown for standard meta-analysis (blue lines), Fisher's combined p-value method – a multi degree-of-freedom chi-square test (maroon line) and a "gold-standard" test (black lines) that assumes that the subset of the traits that are truly associated is known a priori. All powers are shown at a level of 0.001.

Figure S2. Simulation-Based Power Comparison of One-Sided Subset Search with Three Different p Value Estimation Procedures: Bonferroni (blue bars), DLM (orange bars) and Parametric Bootstrap (black bars)

The bootstrap method, which resamples effect size estimates for each study from a normal distribution with mean zero (assuming the null hypothesis of no association) and standard deviation equal to original standard error estimates, gives an "exact" method for computing p-values. In each simulation a total of K (5, 10,15 or 20) distinct traits are analyzed, each with equal number of cases and controls. A variant with MAF=0.3 is assumed to be associated with a subset of size T (3, 6, or 10 or 12) traits with a fixed odds ratio of 1.15. Sample sizes were chosen such that the theoretical power of the gold-standard test (not shown) is close to 95%. The total sample sizes for all traits *N* and that for the subset of associated traits $N_{_T}$ were fixed as follows: $\,$ 1) $\, \big(\! N, N_{_T} \big) \! = \! (5000, 1000)$ 3000), 2) *N*,*N^T* (10000, 6000), 3) *N*,*N^T* (15000, 9000) and 4) *N*,*N^T* (20000, 12000) for power-comparison at levels α = 0.1, 0.001, 10⁻⁵ and 10⁻⁷ respectively. In each case, the DLM method performed superior to Bonferroni. The power of the Bootstrap method was computed only at the levels α = 0.1 and 0.001 (due to compuational limitations), where it performed slightly better than DLM but considerably better than Bonferroni.

Number (proportion) of truly associated traits

Number of traits analyzed: 10

Number (proportion) of truly associated traits

Number of traits analyzed: 15

Power

Number of traits analyzed: 20

Number (proportion) of truly associated traits

Number (proportion) of truly associated traits

Figure S3. Simulation-Based Power Comparison for Combined Analysis of Heterogeneous Traits

In each simulation, a total of K (K=5, 10, 15 and 20) independent case-control studies are analyzed each with equal number of cases and controls. A variant with MAF=0.3 is assumed to be associated with a subset of the traits (non-null traits) with a fixed oddsratio of 1.1. The number of non-null traits (T) and the sample sizes for individual studies are varied such that the total number of cases/controls for associated traits is held fixed at M=10000, but the ratio π =M/N, the fraction of total sample size that contains a true association signal varies (π = 1/5, 2/5, 3/5, 4/5, or 1). In addition to the two-sided (green line) and one-sided (orange line) subset-based tests, power curves are also shown for overall meta-analysis (blue line), Fisher's combined p-value method – a multi degree-offreedom chi-square test (maroon line), and that for a "gold-standard" meta-analysis (black line) that assumes the subset of traits that are truly associated with the given SNP is known a priori. All powers are shown at a level of 10^{-7} .

Number of traits analyzed: 5

Number of traits analyzed: 10

T: number of truly associated traits (100% of the associations are in the positive direction)

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 0.8

 0.6

 0.4

 0.2

 0.0

Power

T: number of truly associated traits (100% of the associations are in the positive direction)

Number of traits analyzed: 10

the associations are in the positive direction)

Figure S4. Simulation-Based Power Comparison of Alternative Methods for Detecting an Overall Association with Homogeneous Effect Sizes

In each simulation, a total of K=5 or K=10 distinct traits are analyzed, each with 2000 cases and 2000 controls. A variant with MAF=0.3 is assumed to be associated with a subset of the traits (the number of such traits is shown on the x-axis). The OR-s for associated traits are fixed at a single value (1.15) (as in Figure 1). The upper panel assumes that all of the associations are in the same direction and the lower panel assumes that 75% of the associations are positive and 25% are negative. In addition to two-sided (green lines) and one-sided (orange lines) subset-based tests, power curves are shown for standard meta-analysis (red lines), Fisher's combined p-value method – a multi degree-of-freedom chi-square test (maroon line), the Adaptive Rank Trunkated Product (ARTP) test with K truncation points (black line) and the Adaptively Weighted (AW) statistic (blue line). All powers were calculated using empirical (simulation-based) cutoff at level 0.001.

Number of traits analyzed: 5

Number of traits analyzed: 10

Figure S5. Simulation-Based Power Comparison of Alternative Methods for Detecting an Overall Association with Heterogeneous Effect Sizes

In each simulation, a total of K=5 or K=10 distinct traits are analyzed, each with 2000 cases and 2000 controls. A variant with MAF=0.3 is assumed to be associated with a subset of the traits (the number of such traits is shown on the x-axis). The OR-s for associated traits are allowed to vary around a fixed mean (1.15) witihin a given range (1.05-1.25; see Supplemental Methods, section 6 for details). The upper panel assumes that all of the associations are in the same direction and the lower panel assumes that 75% of the associations are positive and 25% are negative. In addition to two-sided (green lines) and one-sided (orange lines) subset-based tests, power curves are shown for standard meta-analysis (red lines), Fisher's combined p-value method – a multi degree-of-freedom chi-square test (maroon line), the Adaptive Rank Trunkated Product (ARTP) test with K truncation points (black line) and the Adaptively Weighted (AW) statistic (blue line). All powers were calculated using empirical (simulation-based) cutoff at level 0.001.

Table 1. Performance of the Subset-Based Test for Detection of the Truly Associated Subset of Traits in Presence of Heterogeneity of Odds Ratios

In each simulation, a total of K=5 or K=10 distinct traits are analyzed, each with 2000 cases and 2000 controls. A variant with MAF=0.3 is assumed to be associated with a subset of size T (< K) traits with odds ratios varying within the range 1.05-1.25 with a mean value of 1.15 (see Methods for Details). For each K (i.e., 5 or 10 traits), Panel A assumes that all of the associations are in the same direction and Panel B assumes that 75% of the associations are positive and 25% are negative. Two measures of performance are shown; (1) sensitivity: the average proportion of associated traits detected and (2) specifity: the average proportion of null traits discarded.

- $§ K = Total number of traits analyzed (5 or 10).$
	- T_1 = Number of traits that are truly associated in the positive direction.
	- T_2 = Number of traits that are truly associated in the negative direction.

Table S2. The Number of Cases and Controls and Their Overlaps† in the NCI GWAS Studies of Six Cancer Sites

There were a total of 21,473 cases and 25,891 controls.

† Numbers along the diagonals equal total sample size for that study. Numbers outside the diagonal represent shared cases (upper panel) and shared controls (lower panel).

Table S3. Details of the 18 GliomaScan Studies Included in the Glioma Subtype Analysis Example

There were a total of 1,856 cases and 4,955 controls.

§ Cancer incidence data for the CLUE study have been provided by the Maryland Cancer Registry. We acknowledge the State of Maryland, the Maryland Cigarette Restitution Fund, and the National Program of Cancer Registries of the Centers for Disease Control and Prevention for the funds that helped support the availability of the cancer registry data.

† The findings and conclusions in this report are those of the author(s) and do not necessarily represent the views of the National Institute for Occupational Safety and Health.

Table 4. Simulation-Based Estimates of Type I Error for Combined Analysis of Heterogenous Traits

In each simulation, a total of K=5 or K=10 distinct traits are analyzed, each with N=2000 cases and N=2000 controls. A variant with MAF=0.3 unrelated to all the traits is tested for association in each case. Type I errors are shown for the standard meta-analysis and the proposed one-sided and two-sided methods based on subset search, at three different nominal significance levels.

- § N = Number of cases from each study corresponding to a single trait (fixed at 2000).
	- $K =$ Total number of traits analyzed (either 5 or 10).

Table S5. Simulation-Based Estimates of Type I Error for the Analysis of a Case-Control Study with Geterogeneous Disease Subtypes

Each simulation includes N=2000 cases for each of K=7 subtypes. Rows labeled A and B correspond to designs with N_0 =14000 and N_0 =3000 shared controls respectively. A variant with MAF=0.3 unrelated to all disease subtypes is tested for association in each case. Type I errors are shown for an overall case-control analysis and the two alternative subset-based tests, namely "Case-control" and "Case-complement," at three different nominal significance levels.

- § N = Number of cases from corresponding to each disease subtype (fixed at 2000).
	- $K =$ Total number of traits analyzed (fixed at 7).
	- N_0 = Number of controls available (either 14000 or 3000).

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