

# Supporting Information text

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**Supplementary Methods** The motion of an over-damped particle thermally fluctuating in the system described in Fig. 1 of the main text is described by the stochastic ODE:

$$\eta_x \dot{x}_i = -\omega_i(t)E'_a(x_i) - E'_e(x_i, l_i) + \sqrt{\eta_x k_B \theta} \Gamma(t), \quad (\text{S1})$$

with

$$\begin{cases} \langle \Gamma(t) \rangle = 0 \\ \langle \Gamma(t_1)\Gamma(t_2) \rangle = 2\delta(t_1 - t_2). \end{cases} \quad (\text{S2})$$

Since we are interested both in steady state and transient skeletal muscle behaviour, we approach the system of equations by direct numerical simulation using the Euler-Maruyama method [1]. Defining two subsequent times separated by the time step  $\tau_{step}$  as  $t_{n+1} = t_n + \tau_{step}$ , we recursively define  $x_i(t_n)$  as:

$$x_i(t_{n+1}) = x_i(t_n) - \eta_x^{-1}[\omega_i(t_n)E'_a(x_i(t_n)) - E'_e(x_i(t_n), l_i)]\tau_{step} + \sqrt{\eta_x^{-1}k_B\theta} \int_{t_n}^{t_{n+1}} \Gamma(t). \quad (\text{S3})$$

From the properties of  $\Gamma$  detailed in (S2), the integral in the last term is a random variable which is normally distributed with zero mean and variance  $\tau_{step}$ . Therefore we can substitute it with the function  $\sqrt{2\tau_{step}}w(0, 1)$ , where

$$\begin{cases} \langle w \rangle = 0 \\ \langle w_1 w_2 \rangle = \delta_{12}. \end{cases} \quad (\text{S4})$$

Simulations were performed with Matlab<sup>®</sup> and  $w(0, 1)$  was generated by the built-in function *randn*. Data analysis and plots were also generated by Matlab<sup>®</sup>.

The populations of attached (A) and detached (D) myosin molecules are described by the reaction:



where  $k_+$  and  $k_-$  are the first order rate constants described in Fig. 1 of the main text. At each time step the populations are updated with probabilities of switching from one state to the other:

$$\begin{cases} p_{A-D} = \frac{k_-}{k_+ + k_-} (1 - e^{-\tau_{step}(k_+ + k_-)}) \\ p_{D-A} = \frac{k_+}{k_+ + k_-} (1 - e^{-\tau_{step}(k_+ + k_-)}) \end{cases} \quad (\text{S6})$$

to a random number generated by the built-in function *rand*.

## References

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2. Marcucci L, Yanagida T (2011) Analysis of the dwell time in a bi-dimensional Brownian multi-stable system: an application to molecular motors. submitted .
3. Kitamura K, Tokunaga M, Esaki S, Iwane AH, Yanagida T (2005) Mechanism of muscle contraction based on stochastic properties of single actomyosin motors observed *in vitro*. Biophysics 1: 1-19.
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