

SUPPORTING MATERIAL

Bovine β -Lactoglobulin Is Dimeric under Imitative Physiological Conditions: Dissociation Equilibrium and Rate Constants over the pH Range 2.5 to 7.5

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MATERIALS AND METHODS

Protein expression and purification

The β Lg A and B variants were expressed and purified following the protocol described by Ariyaratne *et al.* (1) and Ponniah *et al.* (2). Briefly, β Lg was over expressed, along with a chaperone disulfide bond isomerase DsbC on a pETDUET-1 plasmid in *Escherichia coli* Origami (DE3) cells, which offer a more oxidizing environment than standard cell lines, such as BL21, and lysed using a French press. Following a centrifugation step, the supernatant was subjected to ion-exchange chromatography at pH 6.5 (20 mM Bis-Tris, stepwise NaCl gradient from 0.05-1.0 M). the protein was then dialyzed against 50 mM phosphate buffer, pH 7.5, before dropping the pH to 2.6, to precipitate out unwanted *E. coli* proteins and misfolded β Lg, followed by addition of NaCl to a final concentration of 30% (w/v) NaCl, which then precipitates β Lg. This procedure follows that used to purify β Lg from bovine milk (3). The β Lg A and B variants were greater than 95% pure, as judged by SDS-PAGE. The protein was then stored at 4 °C. Mass-spectrometry confirmed that our recombinant proteins, being expressed in *E. coli*, retain the N-terminal methionine, which is cleaved in wild-type β Lg. Mass-spectrometry also established that two disulfide bonds are present, as in native β Lg (2). Immediately prior to the analytical ultracentrifugation experiments, the β Lg A and B variants were further purified using size-exclusion chromatography. For each pH, a HiPrep 16/60 Sephacryl S-200 HR column (GE) was equilibrated with buffer prior to injection of the proteins. Protein fractions were collected and then quantified by measuring their absorbance at 280 nm. The buffers were chosen according to their buffering capacity at the desired pH value: 20 mM citrate buffer in 100 mM NaCl was used to study the proteins at pH 2.5, 3.5, 4.5, 5.5 and 20 mM MOPS buffer in 100 mM NaCl was used to perform the experiments at pH 6.5 and 7.5. MES buffer was used also at pH 5.5 and yielded similar results to the citrate buffer (see within). Given this and the chemical relatedness of MES and MOPS buffers, we do not consider the change of buffer from citrate to MOPS to cause any significant change in the dimer-monomer equilibrium under the constant 100 mM NaCl ionic-strength buffer employed in this study.

Analytical Ultracentrifugation Experiments

Sedimentation velocity experiments were performed using a Beckman model XL-I analytical centrifuge (Brea, CA) and a run temperature of 25 °C. β Lg A (and separately B) was pooled after gel filtration and diluted to three different concentrations for the analytical ultracentrifugation experiments [\sim 5, \sim 15 and \sim 45 μ M (\sim 0.09, \sim 0.28 and \sim 0.83 mg/mL), see Table S2 for the precise experimental concentrations]. The density and the viscosity of the buffers used in the AUC runs are shown in the Supporting Material (Table S3) and were experimentally determined using a densitometer (Anton Parr) and a viscometer (Anton Parr) or, where possible, calculated using SEDNTERP (<http://www.rasmb.bbri.org>). \bar{v} was calculated using SEDNTERP and is based on the protein's amino-acid sequence. The protein concentration was determined prior to the experiments by measuring the absorbance at 280 nm and using the extinction coefficient

(determined also by SEDNTERP) of $0.96 \text{ L g}^{-1} \text{ cm}^{-1}$ ($17,210 \text{ M}^{-1} \text{ cm}^{-1}$) for $\beta\text{Lg A}$ and for $\beta\text{Lg B}$ (4, 5).

For the sedimentation-velocity experiments, sample (380 μL) and buffer (400 μL) were loaded into the two sectors of a double-sector quartz cell and mounted in a Beckman eight-hole rotor. The samples were centrifuged at 50,000 rpm. Data were collected in continuous mode using a step size of 0.003 cm without averaging or a time lag between scans. To estimate the sedimentation parameters of the $\beta\text{Lg A}$ and B at different pH values, data were fitted to a $c(s)$ distribution or a $c(M)$ distribution using the software SEDFIT (6), available from <http://www.analyticalultracentrifugation.com>. The $c(s)$ analyses were performed with a regularization at a confidence level of 0.95 (maximum entropy), a floating frictional ratio and baseline, $S_{\min} = 0.2$ and $S_{\max} = 6$ and a resolution of 100. Weight-averaged s values for the $c(s)$ distributions were determined using SEDFIT and converted to the standardized sedimentation coefficient ($s_{20,w}$) using SEDNTERP. Sedimentation coefficients and fit statistics for $\beta\text{Lg A}$ and B are provided in Supplementary Tables S4 and S5, respectively. A van Holde-Weischet analysis (7) was performed for all runs to examine the boundary shape; the results are shown in Figs. S18–S19..

Sedimentation-equilibrium experiments were also undertaken. Sample (100 μL) and buffer (120 μL) were loaded into a six-sector quartz cell. Sedimentation-equilibrium experiments were carried out at a run temperature of 25 °C and at four rotor speeds: 12,000, 15,000, 18,000 and 24,000 rpm. Once equilibrium was obtained at each speed, the data were collected in step mode using a step size of 0.001 or 0.003 cm. Sedimentation-equilibrium and sedimentation-velocity data were globally fitted to appropriate mathematical models implemented in the software SEDPHAT (8), available at <http://www.analyticalultracentrifugation.com>. Where only a single species was observed in solution, as at pH 4.5 and 5.5, a *single interacting species* model, which uses mass conservation, best fitted the data. Where two species were detected in solution, as at pH 2.5, 3.5, 6.5 and 7.5, a *monomer-dimer self-association* model was fitted to globally fit both the sedimentation velocity and sedimentation equilibrium data. The fit was refined by alternating simulated-annealing with the Marquardt-Levenberg and Simplex algorithms and including radial-invariant (RI) and time-invariant (TI) noise correction. The default weighting estimates employed by SEDPHAT for both the sedimentation velocity and sedimentation equilibrium data were used, and all parameters and experiments were checked to ensure they influenced the fit. Since the data were collected at various wavelengths, protein concentrations were determined using the absorbance at 280 nm prior to the experiment and fixed and the extinction coefficients were instead floated when fitted with SEDPHAT. The extinction coefficients were, however, constrained across experiments collected at the same wavelength. The s_1 and s_2 species, representing the monomer and dimer, were also floated (final values are given in Table S6). Error estimates were determined using conventional F -statistics, as implemented in SEDPHAT, and represent the 68% confidence interval. The sedimentation data and residuals are provided in Figs. S1–S7 and S11–S17 in the Supporting Material.

Continuum electrostatic calculations of $\beta\text{-Lg}$ dimer formation

Continuum electrostatic calculations have been performed on the $\beta\text{Lg A}$ dimer and on its dissociated monomers by solving a linear form of the Poisson-Boltzmann equation (PBE) in order

to characterize the relationship between dimer stability and ionic strength. At pH 6.5 and less, the β Lg A dimer with the pH-gated EF loop associated with the Tanford transition at pH \sim 7.3 (9) is in the closed position with Glu89 buried (pdb code 3BLG) was used for calculations, while for calculations at pH 7.5 the β Lg A dimer with the pH-gated EF loop in the open position with Glu89 exposed (pdb code 1BSY) was used. In the preliminary set-up, the radius and charge for each atom in the structure were calculated as defined by the PARSE force field using the PDB2PQR server (10). Hydrogen atoms were added assuming the protonation states of each residue at pH 2.5 as calculated by the PROPKA (11-13). Next, the structure was minimized by performing 1000 steps of steepest descent energy minimization in explicit solvent (SPC water model), as implemented in the GROMACS package. Continuum electrostatic calculations were then carried out using APBS software (14-16). The solvent probe radius was set at 1.4 Å, the dielectric constants (ϵ) were set at the values of $4.0 \times 10^{-12} \text{ F m}^{-1}$ and $78.5 \times 10^{-12} \text{ F m}^{-1}$ for the protein and the solvent respectively and the temperature was set to 25 °C. A cubic grid having dimensions 193 x 193 x 193 Å was adopted for all calculations in a multigrid approach. A first calculation was carried out with a 1.042 Å step per grid point, employing Debye-Hückel (full coulombic) boundary conditions. In these conditions β Lg occupies approximately 50% of the grid space. The second calculation used a 0.523 Å step per grid point. In these new conditions, the β Lg dimer occupies approximately the 90-95% of the grid. The electrostatic binding energy has been calculated by subtracting the energies of a pair of solvated dissociated β Lg monomers from the energy of the solvated dimer. This work presents the results obtained by the second, more accurate calculation. To understand the ionic contribution to the binding energy, the same calculation was carried out over a range of ionic strengths spanning 0 to 500 mM by using NaCl as salt. The radii used to represent ionic species in solution were 0.95 Å and 1.81 Å for Na^+ and Cl^- ions, respectively. The distribution of the ion charge around the β Lg structure upon dimer formation at different ionic strengths has been calculated by subtracting the ion charge distribution of the monomers from the ion charge distribution of the dimer.

Electrostatic binding energy as a function of the ionic strength was analyzed assuming an extended Debye-Hückel model described by the following equation:

$$\ln K_{\text{eq}} = \frac{-|z_+z_-|A \sqrt{\text{Ionic strength}}}{1 + B \cdot \sqrt{\text{Ionic strength}}}$$

where z_+ and z_- are the positive and negative charges on the ion in solution, and A and B are temperature-dependent constants for aqueous solutions, having values of 0.5085 and 1, respectively.

Table S1: Thermodynamic parameters characterizing the monomer-dimer equilibrium of bovine β Lg at 20 °C (except where noted) and pH 1.6 to pH 8.8.

β Lg	pH	[NaCl]	ΔG_A (/kcal mol ⁻¹)	ΔH_A (/kcal mol ⁻¹)	$T\Delta S_A$ (/kcal mol ⁻¹)	K_A (20 °C) (/M ⁻¹ x 10 ⁻³)	K_D (20 °C) (/μM)	Technique	Reference
B	8.8	0.1				4.2	238	AUC	Georges et al (1962) (17)
A B	7.5	0.1				71 116	11 8.6	AUC-SE/SV (25 °C)	This work
A B C	7.5	0.1	-5.63	ND	ND	16 125 >200	63 8.0 <5	AUC-SE (20.5 °C)	McKenzie & Sawyer (1967) (18)
A B	7.0	0.1	-6.20 -6.49	-3.49 -5.77	2.71 0.72	42 69	24 14	ITC ITC	Bello <i>et al.</i> (2008) (19) Bello <i>et al.</i> (2011) (20)
A	7.0	0.1	-6.27	-15.52	-9.25	47	21	AUC-SE	Kelly & Reithel (1971) (21)
A B	6.9	0.13	-6.29 -6.9	ND	ND	49 142	20 7.0	AUC-SE/SV	Zimmerman <i>et al.</i> (1970) (22)
A B	6.5	0.1				250 400	4.0 2.5	AUC-SE/SV (25 °C)	This work
A*	6.5	0.1	-6.35	ND	ND	54	19	AUC-SE	Sakai <i>et al.</i> (2000) (23)
A*	6.5	0.02	-7.11	ND	ND	203	4.9	AUC-SE	Sakurai & Goto (2002) (24)
A	5.2	0.1	-8.08	-6.91	1.17	1120	0.89	AUC-SE	Kelly & Reithel (1971) (21)
C	4.65	0.1	-8.43	~0	85	1930	0.52	AUC-SE	Sarquis & Adams (1976) (25)
A B	3.5	0.1				250 714	4.0 1.4	AUC-SE/SV (25 °C)	This work
B ^{Prep I}	3.5	0.1	-7.3			230	4.3	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)

Table S1: Thermodynamic parameters characterizing the monomer-dimer equilibrium of bovine β Lg at 20 °C (except where noted) and pH 1.6 to pH 8.8 (follows from previous page).

β Lg	pH	[NaCl]	ΔG_A (/kcal mol ⁻¹)	ΔH_A (/kcal mol ⁻¹)	$T\Delta S_A$ (/kcal mol ⁻¹)	$K_A(20\text{ °C})$ (/M ⁻¹ x 10 ⁻³)	$K_D(20\text{ °C})$ (/μM)	Technique	Reference
A	3.0	0.05 / 0.5	-5.1 / -7.1	-12	-6.9 / -5.0	6.9 / 162	145 / 6.2	AUC – ITC	Sakurai & Goto (2001) (4)
A		0.1				16	63		
A		0.01				0.18	5,600		
B ^{Prep II}	3.0	0.1	-5.8			18	56	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)
B	3.0	0.16				41	24	AUC-SE (25 °C)	Joss & Ralston (1996) (27)
A	2.7	0.1	-5.4	-12.4	-7.0	7.7	130	Light scatt. (25 °C)	Townend <i>et al.</i> (1961) (28)
B				-12.8	-6.8	19.6	51		
C	2.7	0.1				~17	~61	AUC (25 °C)	Townend <i>et al.</i> (1964) (29)
B	2.7	0.1				6.3	160	AUC-SE (25 °C)	Albright & Williams (1968) (30)
B ^{Prep II}	2.7	-5.7				15	67	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)
B	2.64	0.16	-5.84	-10.4	-4.47	19	53	AUC-SE (25 °C)	Visser <i>et al.</i> (1972) (31)
B	2.6	0.1				11	91	AUC-SE	Joss & Ralston (1996) (27)
B		0.16	-6.02	-15.1	-9.1	31	32		
A	2.5	0.1				66	15	AUC-SE/SV	This work
B						122	8.2	(25 °C)	
A	2.46	0.1	-4.71	-17.1	12	3.22	310	AUC-SE	Tang & Adams (1973) (32)
C	2.46	0.1	-5.39	-16.5	-11	10.5	95	AUC-SE	Sarquis & Adams (1974) (33)
B ^{Prep II}	2.2	0.1	-5.5			11	91	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)

Table S1: Thermodynamic parameters characterizing the monomer-dimer equilibrium of bovine β Lg at 20 °C (except where noted) and pH 1.6 to pH 8.8 (follows from previous page).

β Lg	pH	[NaCl]	ΔG_A (/kcal mol ⁻¹)	ΔH_A (/kcal mol ⁻¹)	$T\Delta S_A$ (/kcal mol ⁻¹)	K_A (20 °C) (/M ⁻¹ x 10 ⁻³)	K_D (20 °C) (/ μ M)	Technique	Reference
B B	2.3	0.07 0.107				0.08/0.033 5/13	12,500/30,000 200/77	Light/SAXS	Baldini <i>et al.</i> (1999) (34)
B ^{Prep II}	2.0	0.1	-4.9			3.9	260	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)
B	2.0	0.16				21	48	AUC-SE	Joss & Ralston (1996) (27)
B ^{Prep II}	1.6	0.1	-4.9			3.9	260	Light scatt. (25 °C)	Townend <i>et al.</i> (1960) (26)

**Pichia pastoris* expression, known to produce glycosylated protein

† Values of $4.9(12) \times 10^3$ and $6.4(8) \times 10^3$ M⁻¹ for pH 3, 50 mM NaCl and 20 °C are also found in this paper.

Table S2: Details of experimental conditions for analytical ultracentrifugation runs. The loading concentration was determined prior to the experiment using the absorbance at 280 nm and an extinction coefficient of $17210 \text{ M}^{-1} \text{ cm}^{-1}$. When the data were fitted using SEDPHAT, the extinction coefficient was floated, since the data were collected at various wavelengths.

Buffer	pH	β Lg A protein concentration from wavelength scans (μM)	β Lg B protein concentration from wavelength scans (μM)
Citrate	2.5	5.3	6.8
		15.7	19.2
		33.4	53.0
Citrate	3.5	4.8	5.1
		15.8	15.0
		26.7	44.1
Citrate	4.5	2.5	3.6
		14.5	13.9
		43.9	47.8
Citrate	5.5	6.5	6.5
		16.8	17.6
		47.3	50.0
MES	5.5	5.7	9.6
		16.6	17.8
		52.1	50.4
MOPS	6.5	3.5	4.3
		11.0	11.9
		33.0	36.5
MOPS	7.5	5.1	5.2
		22.6	15.4
		36.5	43.3

Table S3: Buffer density and viscosity values used for the AUC experiments at 25 °C and an ionic strength of 100 mM NaCl. The values for citrate buffer were retrieved from SEDNTERP 1.09 database (<http://www.Jphilo.mailway.com/download.htm>). The density and viscosity for MOPS buffer at the different pH values were experimentally determined using a densitometer and a viscometer (Anton Parr).

pH	Buffer (20 mM in 100 mM NaCl)	Density (ρ, g cm⁻³)	Viscosity (η, poise)
2.5-5.5	Citrate	1.0027	0.008904
5.5	MES [2-(<i>N</i> -morpholino)ethanesulfonic acid]	1.0025	0.00902
6.5-7.5	MOPS [3-(<i>N</i> -morpholino)propanesulfonic acid]	1.0022	0.00902

Table S4: Hydrodynamic properties and fit statistics for SV data of β Lg A at three concentrations over the pH range 2.5-7.5.

Sample	Model	$s_{20,w}$ peak (S)	Weight-averaged $s_{20,w}$	Mass (Da)	f/f_0	Runs-Z test score	r.m.s.d.
Citrate pH 2.5							
5.3 μ M	$c(s)$ distribution	2.1	2.2		1.26	7.6	0.005
15.7 μ M	$c(s)$ distribution	2.4	2.3		1.15	13	0.006
33.4 μ M	$c(s)$ distribution	2.6	2.5		1.17	12	0.006
Citrate pH 3.5							
4.8 μ M	$c(s)$ distribution	2.7	2.6		1.23	1.3	0.008
15.8 μ M	$c(s)$ distribution	2.7	2.7		1.24	0.5	0.009
26.7 μ M	$c(s)$ distribution	2.8	2.7		1.25	1.7	0.009
Citrate pH 4.5							
2.5 μ M	$c(s)$ distribution	2.7	2.6		1.16	4.3	0.004
14.5 μ M	$c(s)$ distribution	2.8	2.8		1.20	5.8	0.004
43.9 μ M	$c(s)$ distribution	2.8	2.8		1.23	5.5	0.006
Citrate pH 5.5							
6.5 μ M	$c(s)$ distribution	2.6	2.6		1.20	2.5	0.004
16.8 μ M	$c(s)$ distribution	2.7	2.7		1.22	4.7	0.005
47.3 μ M	$c(s)$ distribution	2.8	2.7	-	1.23	14	0.01
47.3 μ M	$c(M)$ distribution	-	-	~33,000	1.24	12	0.01
47.3 μ M	discrete species	2.7	-	33,900 \pm 1,400	-	3.9	0.005

Table S4 cont.: Hydrodynamic properties and fit statistics for SV data of β Lg A at three concentrations over the pH range 2.5-7.5 (follows from previous page).

Sample	Model	$s_{20,w}$ peak (S)	Weight-averaged $s_{20,w}$	Mass (Da)	f/f_0	Runs-Z test score	r.m.s.d.
MES pH 5.5							
5.7 μ M	$c(s)$ distribution	2.6	2.5		1.20	4.03	0.006
16.6 μ M	$c(s)$ distribution	2.7	2.6		1.22	5.73	0.006
52.1 μ M	$c(s)$ distribution	2.7	2.6		1.22	6.19	0.01
52.1 μ M	$c(M)$ distribution			~33,000	1.24	8.7	0.01
52.1 μ M	discrete species	2.7	-	33,300 \pm 1,700	-	9.0	0.007
MOPS pH 6.5							
3.5 μ M	$c(s)$ distribution	2.1	2.3		1.30	4.3	0.007
11.0 μ M	$c(s)$ distribution	2.5	2.6		1.24	4.8	0.01
33.0 μ M	$c(s)$ distribution	2.6	2.7		1.37	10	0.007
MOPS pH 7.5							
5.13 μ M	$c(s)$ distribution	2.1	2.0		1.32	1.5	0.005
22.6 μ M	$c(s)$ distribution	2.6	2.3		1.30	6.8	0.006
36.5 μ M	$c(s)$ distribution	2.9	2.4		1.31	9.6	0.007

Table S5: Hydrodynamic properties and fit statistics for SV data of β Lg B at three concentrations over the pH range 2.5-7.5.

Sample	Model	$s_{20,w}$ peak (S)	Weight-averaged $s_{20,w}$	Mass (Da)	f/f_0	Runs-Z test score	r.m.s.d.
Citrate pH 2.5							
6.8 μ M	$c(s)$ distribution	2.2	2.3		1.26	1.0	0.005
19.2 μ M	$c(s)$ distribution	2.5	2.5		1.17	0.11	0.006
53.0 μ M	$c(s)$ distribution	2.7	2.6		1.22	4.4	0.007
Citrate pH 3.5							
5.1 μ M	$c(s)$ distribution	2.7	2.7		1.27	11	0.008
15.0 μ M	$c(s)$ distribution	2.8	2.8		1.23	2.4	0.012
44.1 μ M	$c(s)$ distribution	2.8	2.8		1.26	3.5	0.008
Citrate pH 4.5							
3.6 μ M	$c(s)$ distribution	2.7	2.7		1.24	2.5	0.006
13.9 μ M	$c(s)$ distribution	2.8	2.8		1.23	2.3	0.004
47.8 μ M	$c(s)$ distribution	2.8	2.8		1.24	10.15	0.01
Citrate pH 5.5							
6.5 μ M	$c(s)$ distribution	2.7	2.7		1.21	4.6	0.004
17.6 μ M	$c(s)$ distribution	2.8	2.8		1.21	3.7	0.004
50.0 μ M	$c(s)$ distribution	2.8	2.8	-	1.23	10.16	0.02
50.0 μ M	$c(M)$ distribution	-	-	~33,000	1.25	14	0.02
50.0 μ M	discrete species	2.9	-	34,200 \pm 1,100	-	3.0	0.005

Table S5 cont.: Hydrodynamic properties and fit statistics for SV data of β Lg B at three concentrations over the pH range 2.5-7.5 (follows from previous page).

Sample	Model	$s_{20,w}$ peak (S)	Weight-averaged $s_{20,w}$	Mass (Da)	f/f_0	Runs-Z test score	<i>r.m.s.d.</i>
MES pH 5.5							
9.6 μ M	$c(s)$ distribution	2.7	2.6		1.20	1.7	0.004
17.8 μ M	$c(s)$ distribution	2.7	2.7		1.20	5.0	0.005
50.4 μ M	$c(s)$ distribution	2.7	2.7		1.22	9.81	0.009
50.4 μ M	$c(M)$ distribution	-	-	~33,000	1.24	10.7	0.01
50.4 μ M	discrete species	2.9	-	33,200 \pm 1,400	-	7.0	0.007
MOPS pH 6.5							
4.3 μ M	$c(s)$ distribution	2.5	2.6		1.33	7.8	0.007
11.9 μ M	$c(s)$ distribution	2.8	2.7		1.22	8.9	0.007
36.5 μ M	$c(s)$ distribution	2.9	2.9		1.23	7.8	0.009
MOPS pH 7.5							
5.2 μ M	$c(s)$ distribution	2.3	2.2		1.46	1.6	0.005
15.4 μ M	$c(s)$ distribution	2.6	2.4		1.29	0.69	0.006
43.3 μ M	$c(s)$ distribution	2.7	2.7		1.26	2.7	0.006

Table S6: The fitted values for monomer (s1) and dimer (s2).

	s1		s2	
	β Lg A	β Lg B	β Lg A	β Lg B
pH 2.5 citrate	1.79	1.83	2.90	2.76
pH 3.5 citrate	2.27	2.28	2.79	2.76
pH 6.5 MOPS	1.98	1.91	2.91	2.90
pH 7.5 MOPS	1.40	1.66	2.93	2.92

Table S7. Equilibrium and rate constants at 25 °C and at an ionic strength of 100 mM NaCl, calculated for β Lg A and β Lg B dimer dissociation at different pH* by global fitting of SE data for $K_D^{(2-1)}$, of SV data for $K_D^{(2-1)}$ and k_{off} , and of SE and SV data for $K_D^{(2-1)}$ and k_{off} .

Protein	Global fit - equilibrium data only	Global fit - velocity data only		Global fit – velocity and equilibrium data	
	$K_D^{(2-1)}$ (μ M)	$K_D^{(2-1)}$ (μ M)	k_{off} (s^{-1})	$K_D^{(2-1)}$ (μ M)	k_{off} (s^{-1})
β Lg A					
pH 2.5(citrate)	19.3 (14.9-26.2)	13.8 (10.1-17.7)	0.008 (0.002-0.019)	14.8 (11.2-18.4)	0.009 (0.002-0.018)
pH 3.5(citrate)	1.4 (0.2-4.4)	4.2 (1.8-7.0)	0.007 (ND) [†]	4.0 (2.3-6.0)	0.007 (ND) [†]
pH 6.5(MOPS)	11.9 (5.5-23.7)	3.9 (2.5-5.8)	Rapid equil.	4.0 (2.7-5.6)	Rapid equil.
pH 7.5(MOPS)	24 (13-43)	10.4 (6.1-15.0)	Rapid equil.	10.8 (7.6-15.8)	Rapid equil.
β Lg B					
pH 2.5(citrate)	15 (11-21)	8.3 (5.5-11.1)	0.009 (0.003-0.029)	8.2 (5.8-11.1)	0.013 (0.003-0.045)
pH 3.5(citrate)	11.6 (6.0-20.6)	1.1 (0.7-2.3)	0.041 (ND) [†]	1.4 (1.1-4.5)	0.037 (ND) [†]
pH 6.5(MOPS)	1.0 (0.3-4.8)	2.2 (1.3-3.7)	Rapid equil.	2.5 (1.0-7.1)	Rapid equil.
pH 7.5(MOPS)	17 (10-27)	8.4 (7.8-10.3)	Rapid equil.	8.6 (6.3-10.9)	Rapid equil.

* Calculated error ranges representing an estimated 69% confidence interval are reported in parentheses.

[†] Indicative value, as no error range could be determined.

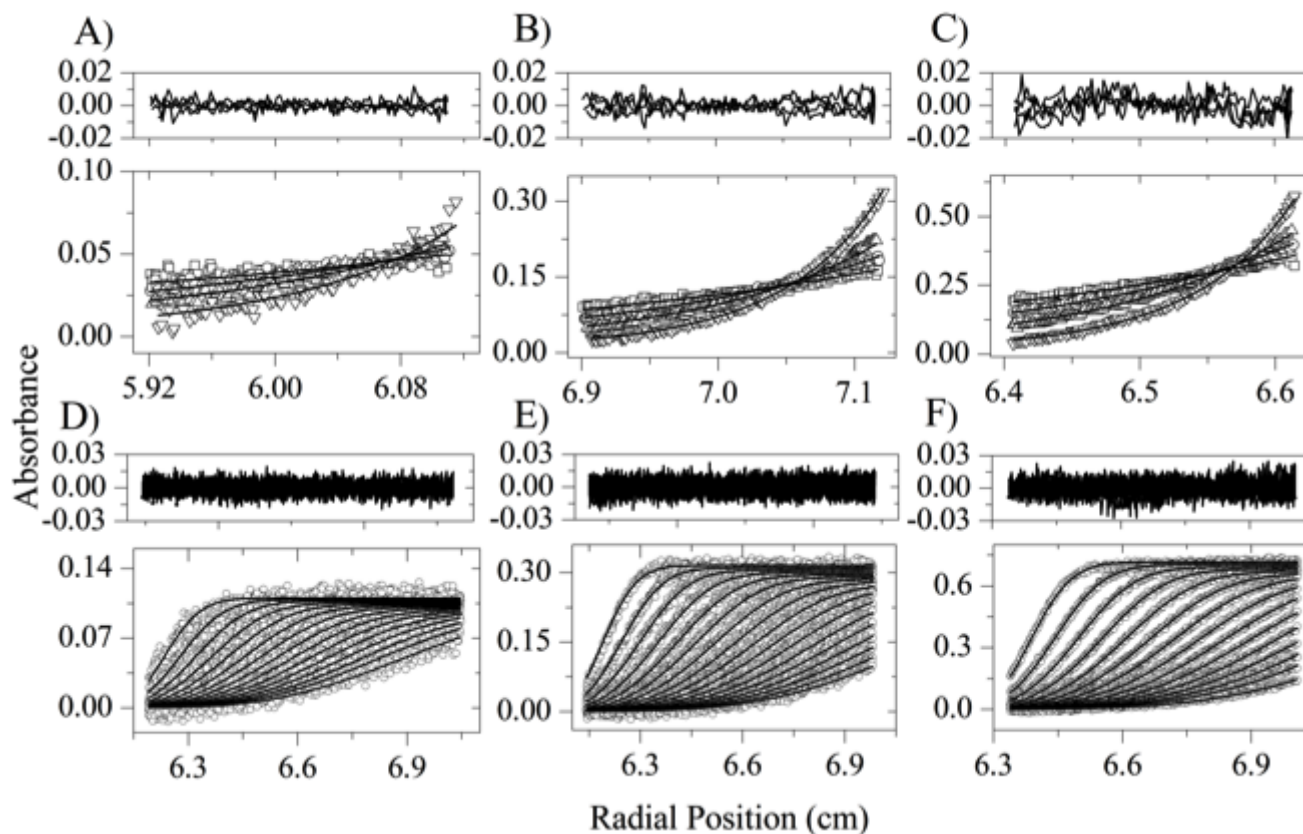


Fig. S1: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin A at pH 2.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a monomer-dimer equilibrium model, as implemented in SEDPHAT. The protein concentrations were 5.3 μ M (A and D), 15.7 μ M (B and E) and 33.4 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 250 nm. The velocity data were collected at 50,000 rpm at 280 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 2, (B) r.m.s.d. = 0.004, Z-score = 9, (C) r.m.s.d. = 0.006, Z-score = 9, (D) r.m.s.d. = 0.005, Z-score = 11, (E) r.m.s.d. = 0.006, Z-score = 3, (F) r.m.s.d. = 0.005, Z-score = 7. The global reduced chi-squared was 0.344.

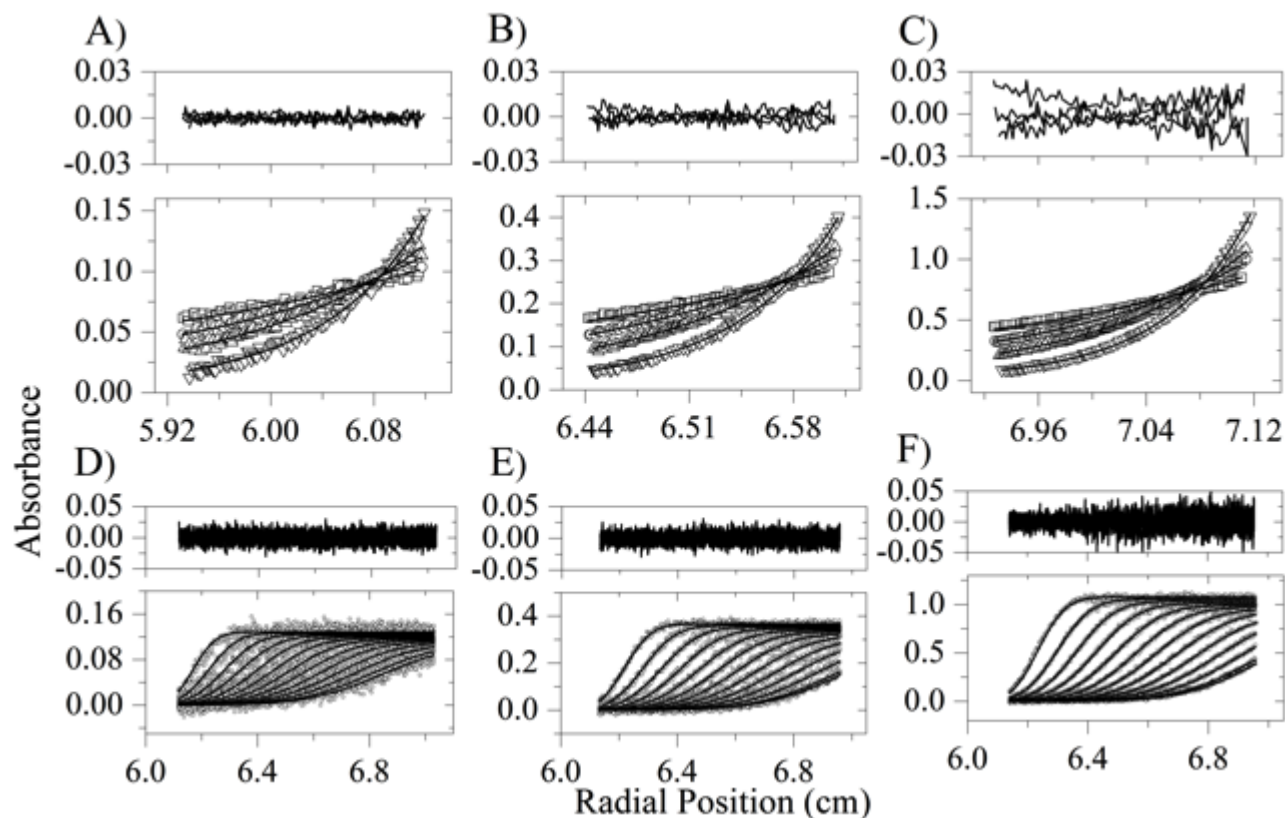


Fig. S2: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin A at pH 3.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a monomer-dimer equilibrium model, as implemented in SEDPHAT. The protein concentrations were 4.8 μ M (A and D), 15.8 μ M (B and E) and 26.7 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 260 nm. The velocity data were collected at 50,000 rpm at 237 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.002, Z-score = 2, (B) r.m.s.d. = 0.003, Z-score = 4, (C) r.m.s.d. = 0.005, Z-score = 10, (D) r.m.s.d. = 0.008, Z-score = 3, (E) r.m.s.d. = 0.009, Z-score = 0.1, (F) r.m.s.d. = 0.009, Z-score = 1.6. The global reduced chi-squared was 0.700.

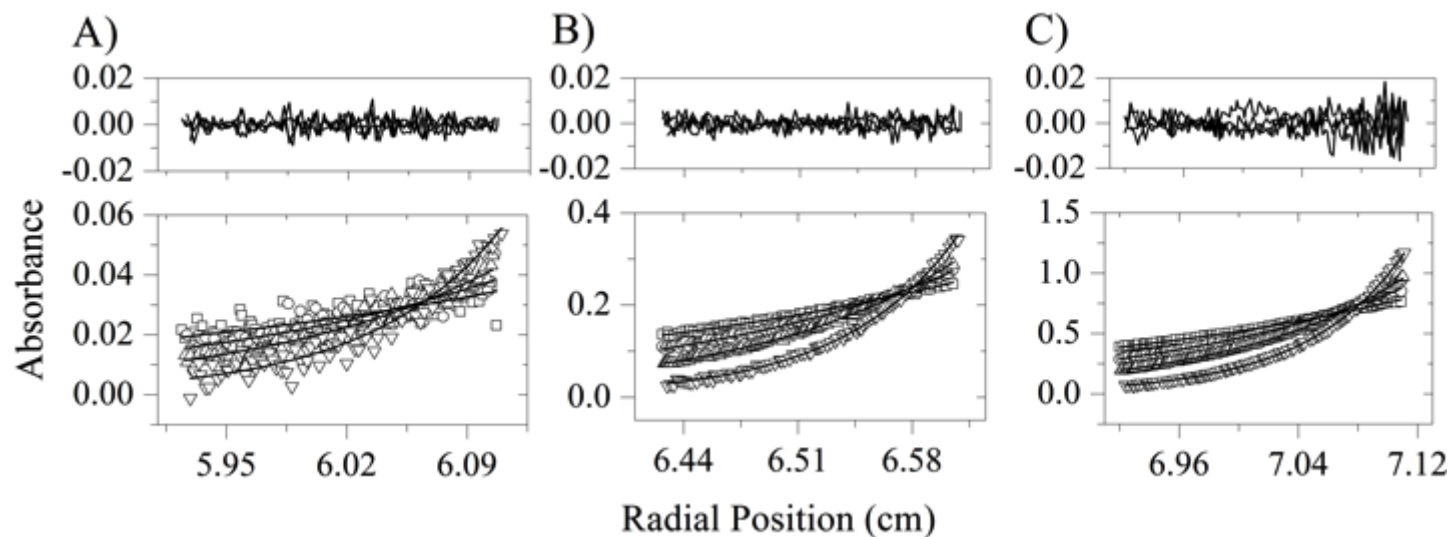


Fig. S3: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin A at pH 4.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model, as implemented in SEDPHAT. The protein concentrations were 2.5 μ M (A), 14.5 μ M (B) and 43.9 μ M (C). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 255 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 33,916 (32,130 – 34,860). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.62, (B) r.m.s.d. = 0.003, Z-score = 2.31, (C) r.m.s.d. = 0.005, Z-score = 3.4.

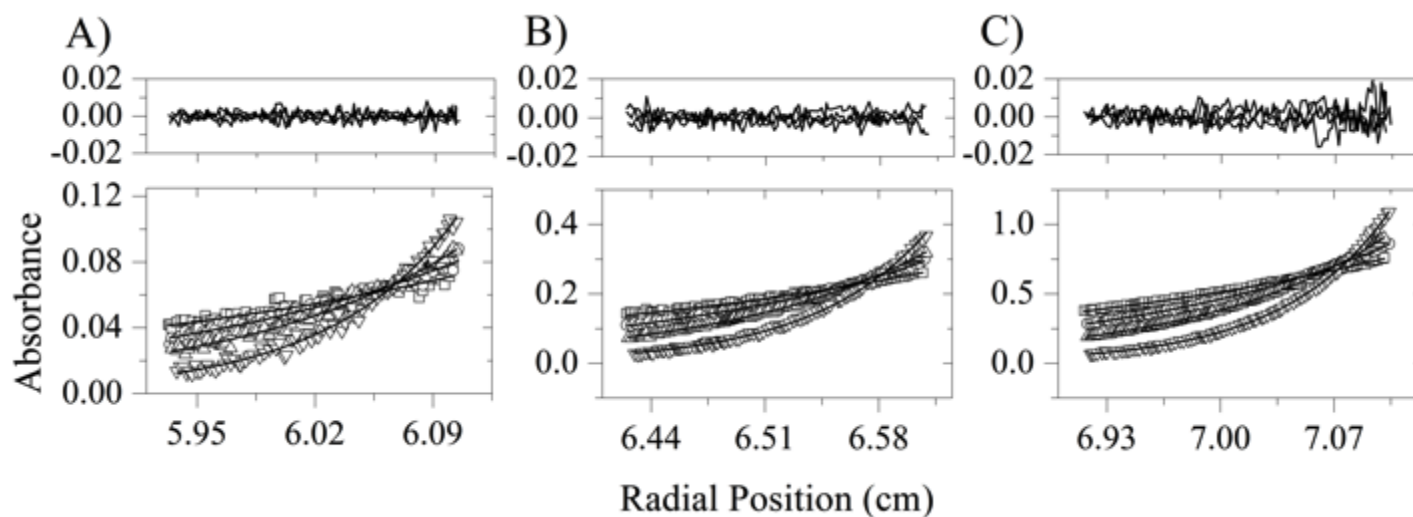


Fig. S4: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin A at pH 5.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model, as implemented in SEDPHAT. The protein concentrations were 6.5 μ M (A), 16.8 μ M (B) and 47.3 μ M (C). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 255 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 33,880 (32,521 – 35121). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 1.5, (B) r.m.s.d. = 0.003, Z-score = 2.6, (C) r.m.s.d. = 0.005, Z-score = 3.9.

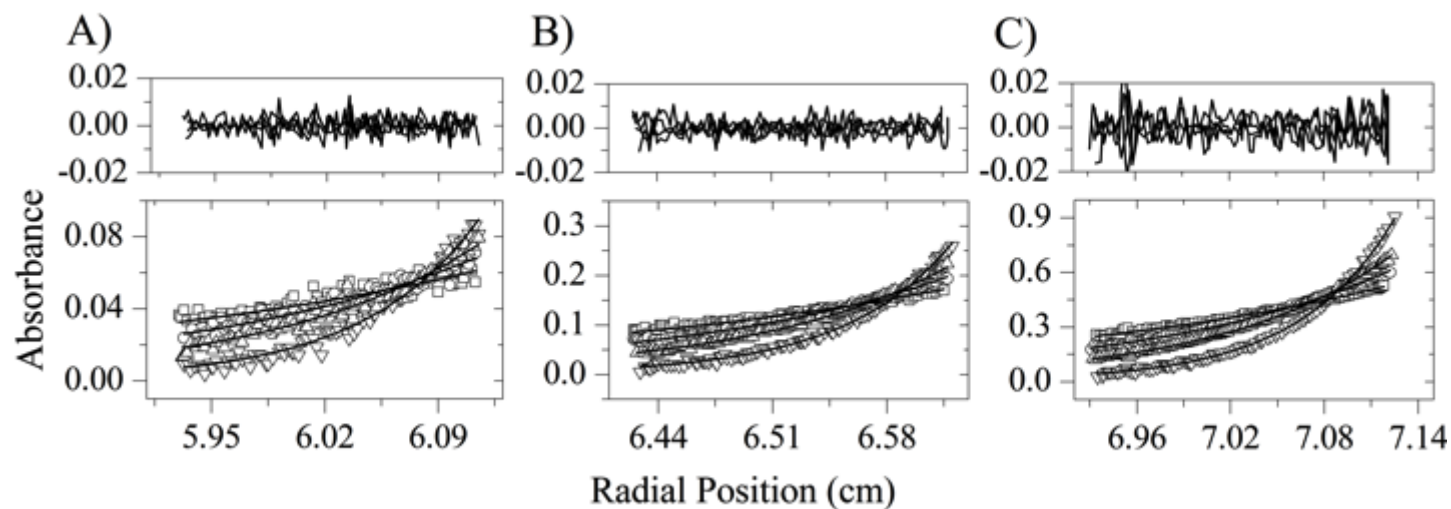


Fig. S5: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin A at pH 5.5 (20 mM MES, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model, as implemented in SEDPHAT. The protein concentrations were 5.7 μ M (A), 16.6 μ M (B) and 52.1 μ M (C). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 250 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 35808 (33,808 – 38,058). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.33, (B) r.m.s.d. = 0.004, Z-score = 5.7, (C) r.m.s.d. = 0.006, Z-score = 4.8.

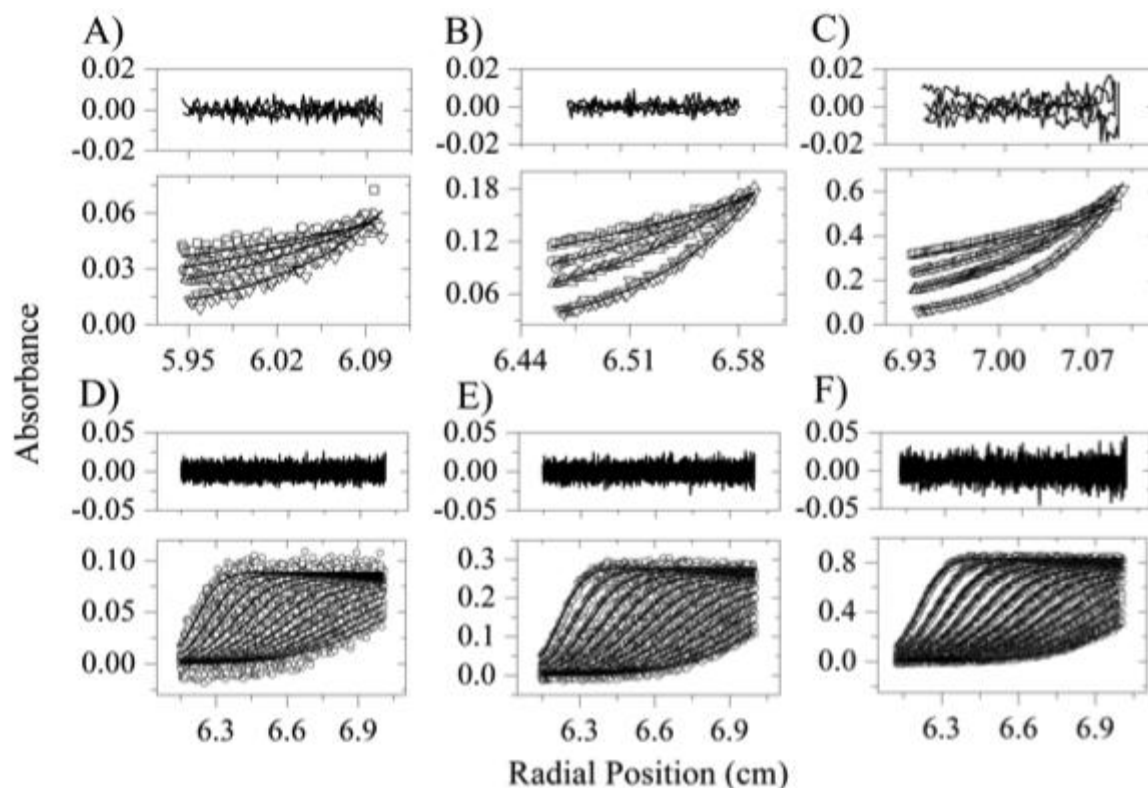


Fig. S6: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin A at pH 6.5 (20 mM MOPS, 100 mM NaCl, 25 °C), fitted to a *monomer-dimer equilibrium* model, as implemented in SEDPHAT. The protein concentrations were 3.5 μ M (A and D), 11.0 μ M (B and E) and 33.0 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 260 nm. The velocity data were collected at 50,000 rpm at 237 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.4, (B) r.m.s.d. = 0.003, Z-score = 0.4, (C) r.m.s.d. = 0.006, Z-score = 7.7, (D) r.m.s.d. = 0.007, Z-score = 2.8, (E) r.m.s.d. = 0.007, Z-score = 13, (F) r.m.s.d. = 0.01, Z-score = 38. The global reduced chi-squared was 0.7.

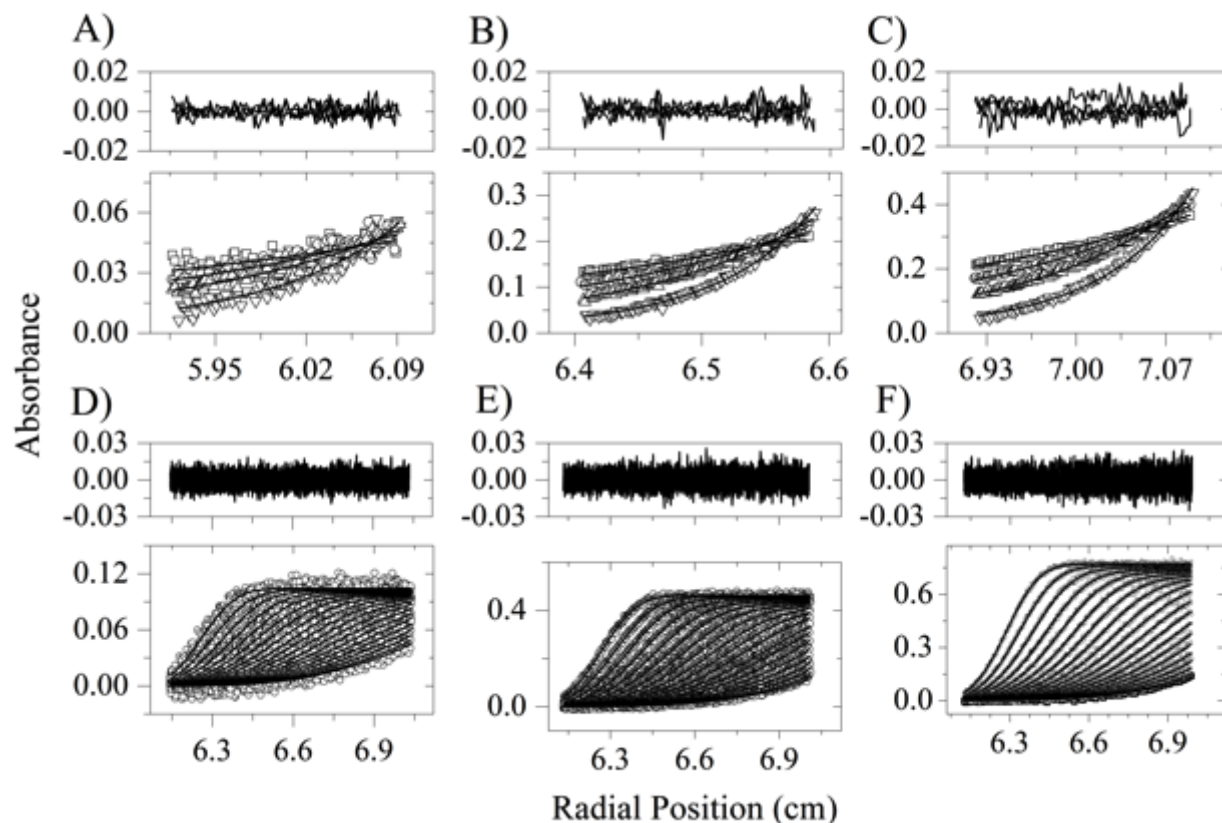


Fig. S7: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin A at pH 7.5 (20 mM MOPS, 100 mM NaCl, 25 °C), fitted to a *monomer-dimer equilibrium* model, as implemented in SEDPHAT. The protein concentrations were 5.1 μ M (A and D), 22.6 μ M (B and E) and 36.5 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 250 nm. The velocity data were collected at 50,000 rpm at 280 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.005, Z-score = 10.2, (B) r.m.s.d. = 0.004, Z-score = 6, (C) r.m.s.d. = 0.002, Z-score = 2, (D) r.m.s.d. = 0.005, Z-score = 1.6, (E) r.m.s.d. = 0.005, Z-score = 0.7, (F) r.m.s.d. = 0.006, Z-score = 2.7. The global reduced chi-squared was 0.4.

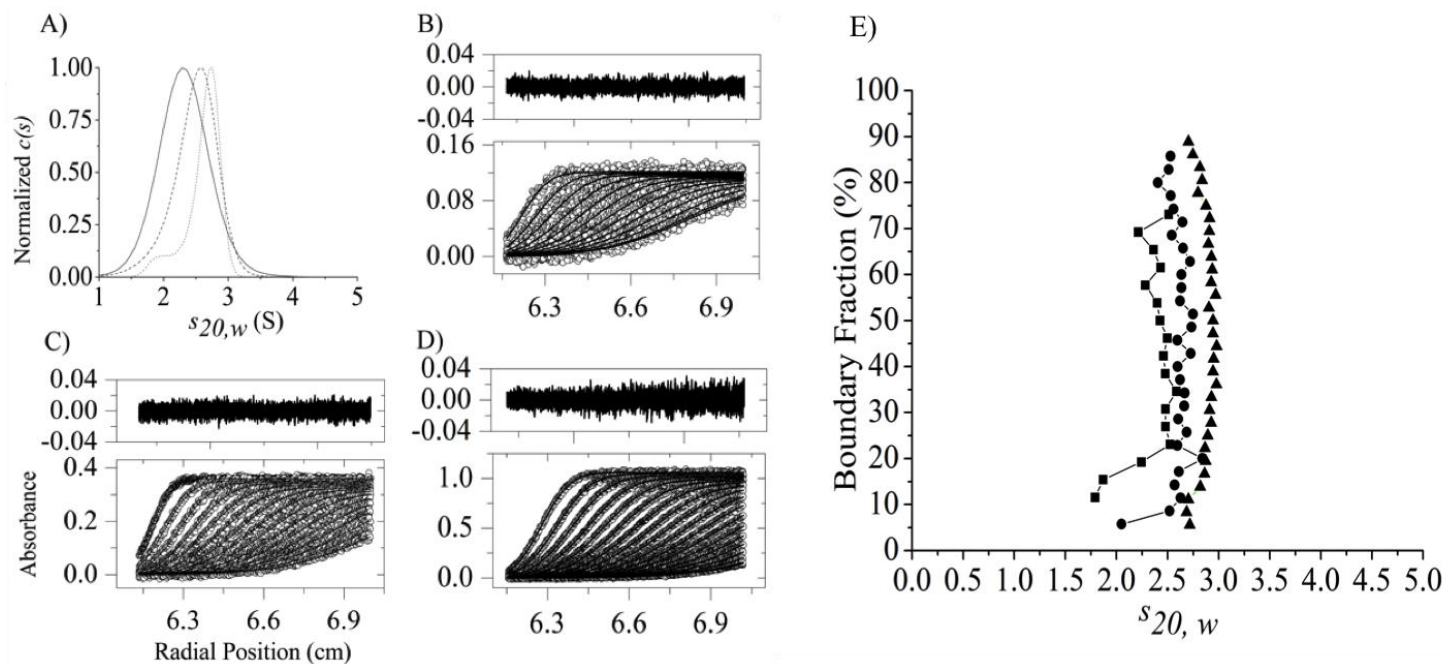


Fig. S8. Sedimentation velocity data for β -lactoglobulin B at pH 2.5 (20 mM citrate, 100 mM NaCl, 25 °C). (A) Continuous $c(s)$ analysis derived from SV data for β -lactoglobulin B at loading concentrations of 6.8 μM (solid line; SV data and least-squares fits and residuals shown in panel B), 19.2 μM (dashed line; panel C) and 53.0 μM (dotted line; panel D). Statistics for the non-linear least-squares fits: (B) r.m.s.d. = 0.005, test-Z-score = 0.95; (C) r.m.s.d. = 0.006, Z-score = 0.11; (D) r.m.s.d. = 0.007, Z-score = 4.4. In (E) the van Holde-Weischet full integration plot is shown at the three different loading concentrations of 6.8, 19.2 and 53.0 μM represented respectively using squares, circles and up-triangles.

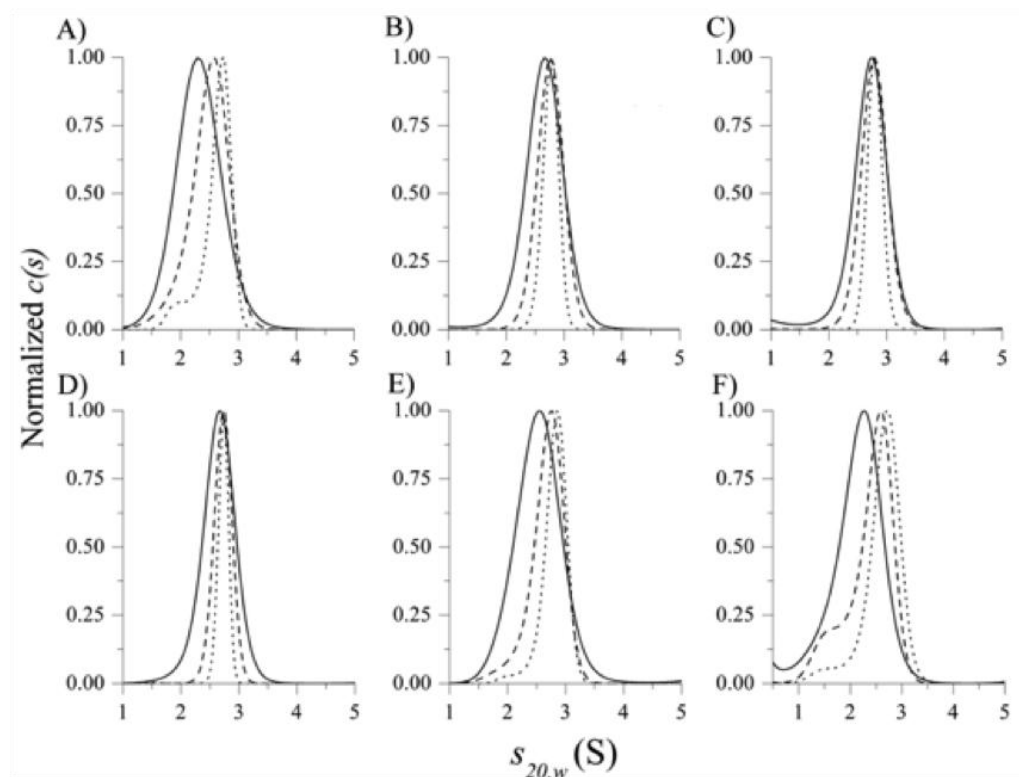
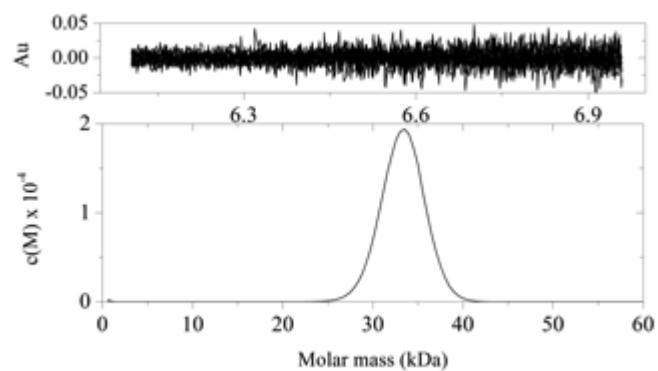


Fig. S9. Normalized $c(s_{20,w})$ distribution plots for β -lactoglobulin B over the pH range of 2.5 to 7.5. Figures show the distribution plots for β -lactoglobulin B obtained from the fitting of sedimentation velocity isotherms using a continuous $c(s)$ distribution model. The three protein concentrations explored are approximately 5 μM (*solid line*), 15 μM (*dashed line*) and 45 μM (*dotted line*); actual concentrations are given in parentheses. In 20 mM citrate and 100 mM NaCl: (A) pH 2.5 (6.76, 19.2, 53.0 μM), (B) pH 3.5 (5.1, 15.0, 44.1 μM), (C) pH 4.5 (3.6, 13.9, 47.8 μM) and (D) pH 5.5 (6.5, 17.6, 50.0 μM). In 0.0200 M MOPS and 100 mM NaCl: (E) pH 6.5 (4.3, 11.9, 36.5 μM) and (F) pH 7.5 (5.22, 15.4, 43.3 μM). Statistics for the fits can be found in the supporting material (Figs. S11-S17).

A)



B)

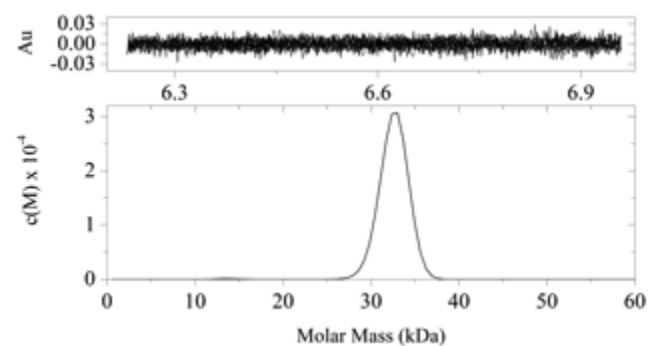


Fig. S10. Continuous mass distribution $c(M)$ obtained from the fitting of SV data at pH 5.5 (20 mM citrate, 100 mM NaCl) for (A) β Lg A at 47.3 μ M and (B) β Lg B at 50.4 μ M. The apparent molar mass of the species represented by the peak has been found to be $33,900 \pm 1,300$ Da for β Lg A and $34,200 \pm 900$ for β Lg B.

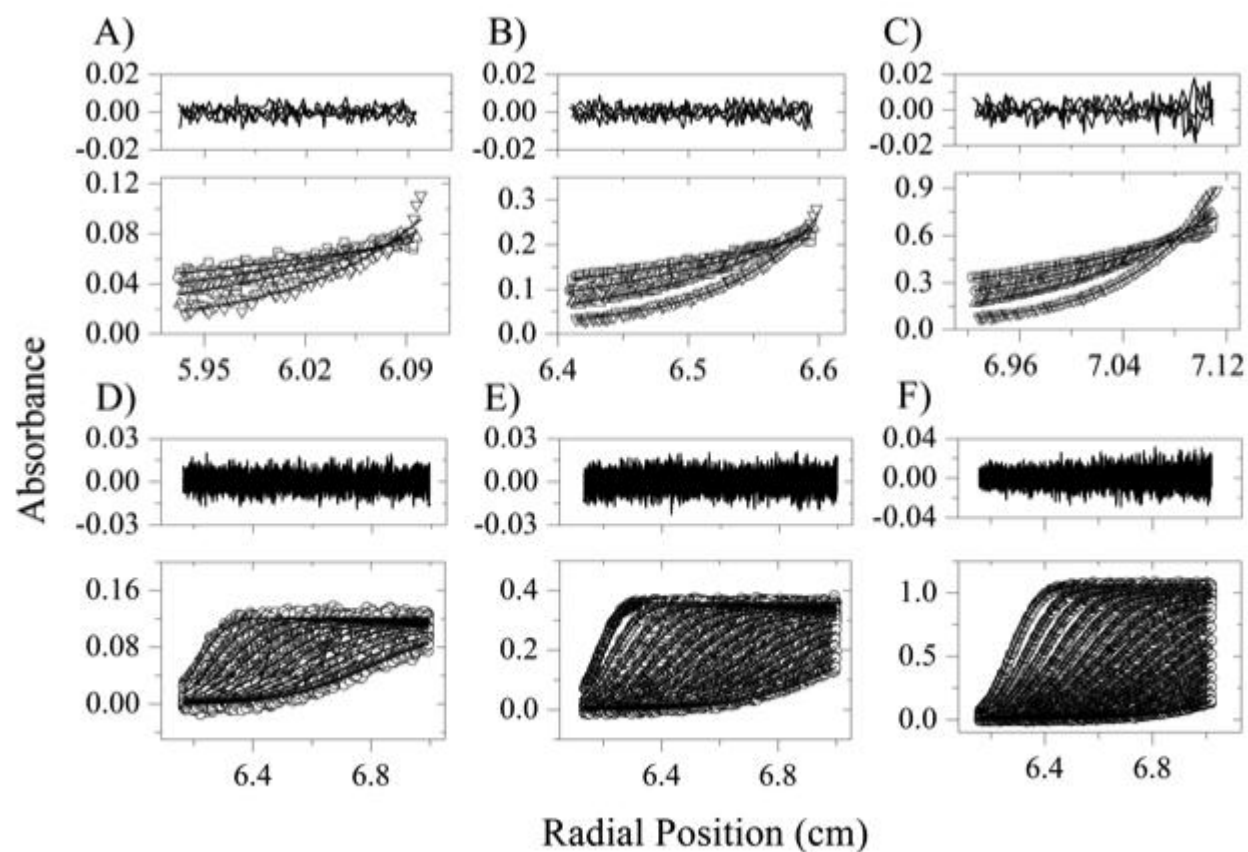


Fig. S11: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin B at pH 2.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a *monomer-dimer equilibrium* model, as implemented in SEDPHAT. The protein concentrations were 6.76 μ M (A and D), 19.2 μ M (B and E) and 53.0 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 250 nm. The velocity data were collected at 50,000 rpm at 280 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.7, (B) r.m.s.d. = 0.003, Z-score = 4.6, (C) r.m.s.d. = 0.005, Z-score = 4.1, (D) r.m.s.d. = 0.005, Z-score = 0.9, (E) r.m.s.d. = 0.006, Z-score = 0.2, (F) r.m.s.d. = 0.007, Z-score = 5. The global reduced chi-squared was 0.394.

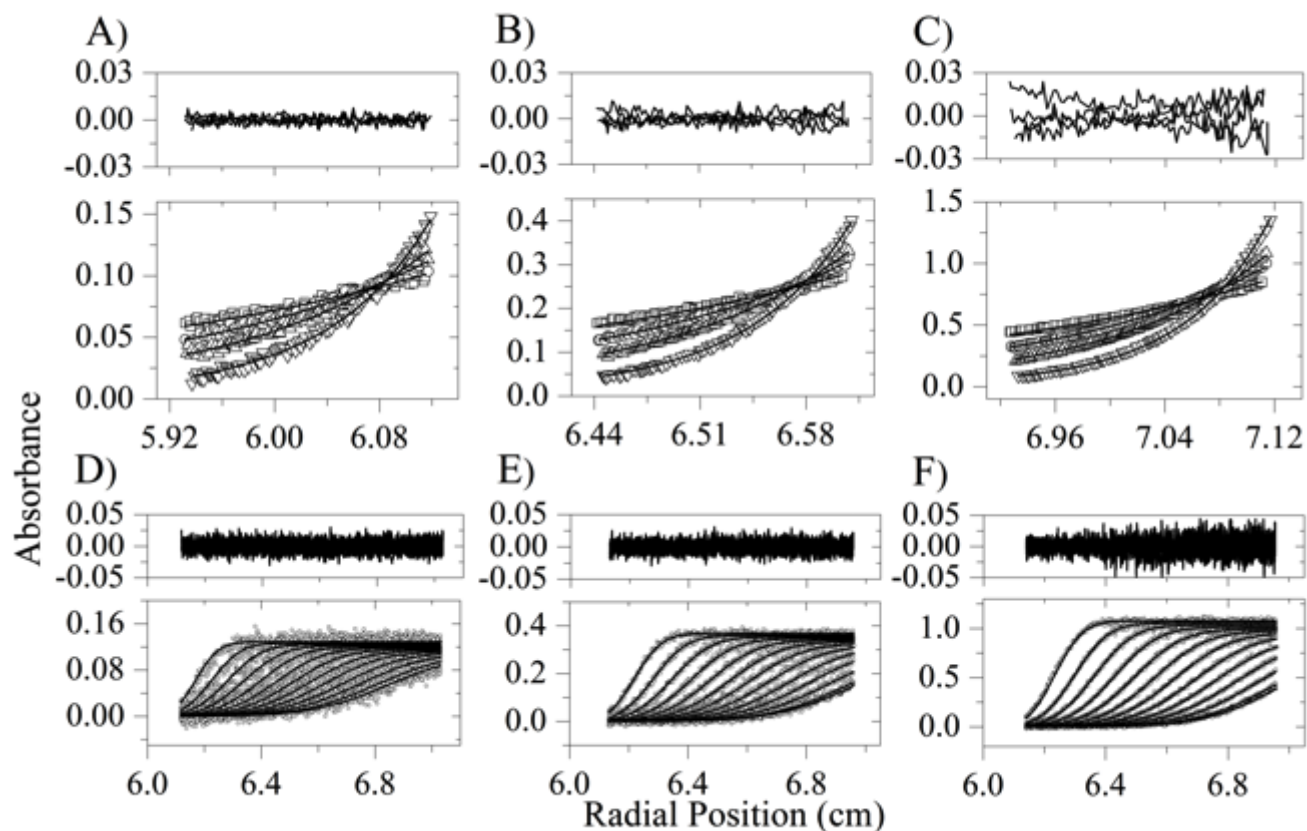


Fig. S12: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin B at pH 3.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a monomer-dimer equilibrium model, as implemented in SEDPHAT. The protein concentrations were 5.1 μ M (A and D), 15.0 μ M (B and E) and 44.1 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 260 nm. The velocity data were collected at 50,000 rpm at 237 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.002, Z-score = 0.15, (B) r.m.s.d. = 0.004, Z-score = 5.7, (C) r.m.s.d. = 0.009, Z-score = 13, (D) r.m.s.d. = 0.008, Z-score = 11, (E) r.m.s.d. = 0.008, Z-score = 3.6, (F) r.m.s.d. = 0.011, Z-score = 3. The global reduced chi-squared was 0.9.

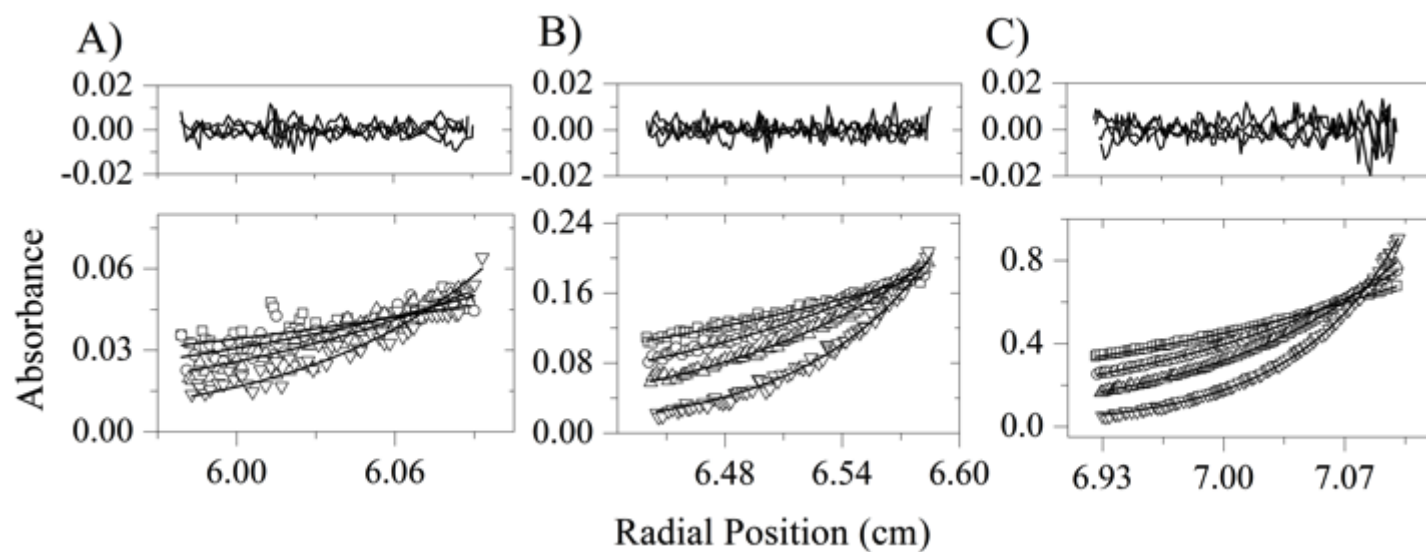


Fig. S13: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin B at pH 4.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model as implemented in SEDPHAT. The protein concentrations were 3.6 μ M (A), 13.9 μ M (B) and 47.8 μ M (C). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 255 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 33,270 (32,070 – 34,570). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 1.24, (B) r.m.s.d. = 0.003, Z-score = 1.19, (C) r.m.s.d. = 0.005, Z-score = 7.38.

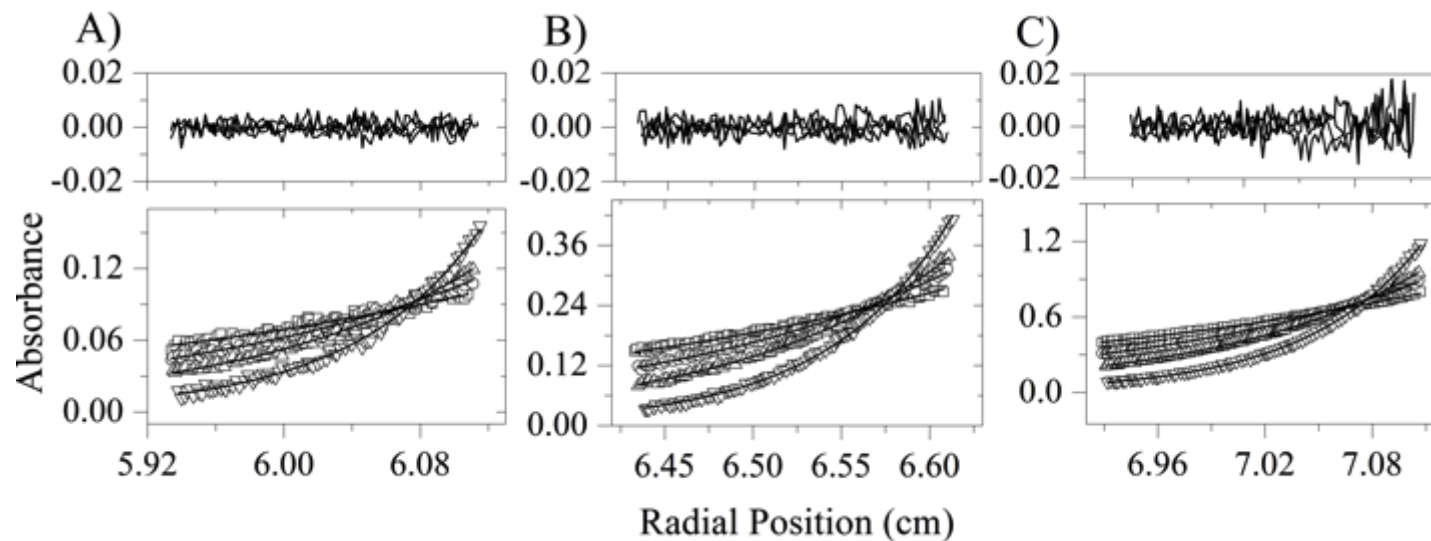


Fig. S14: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin B at pH 5.5 (20 mM citrate, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model as implemented in SEDPHAT. The protein concentrations were 6.5 μ M (A), 17.6 μ M (B) and 50.0 μ M (C). The equilibrium data (A-C) was collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 255 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 34,162 (33,262 – 35,261). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.002, Z-score = 0.85, (B) r.m.s.d. = 0.003, Z-score = 4.35, (C) r.m.s.d. = 0.005, Z-score = 2.98.

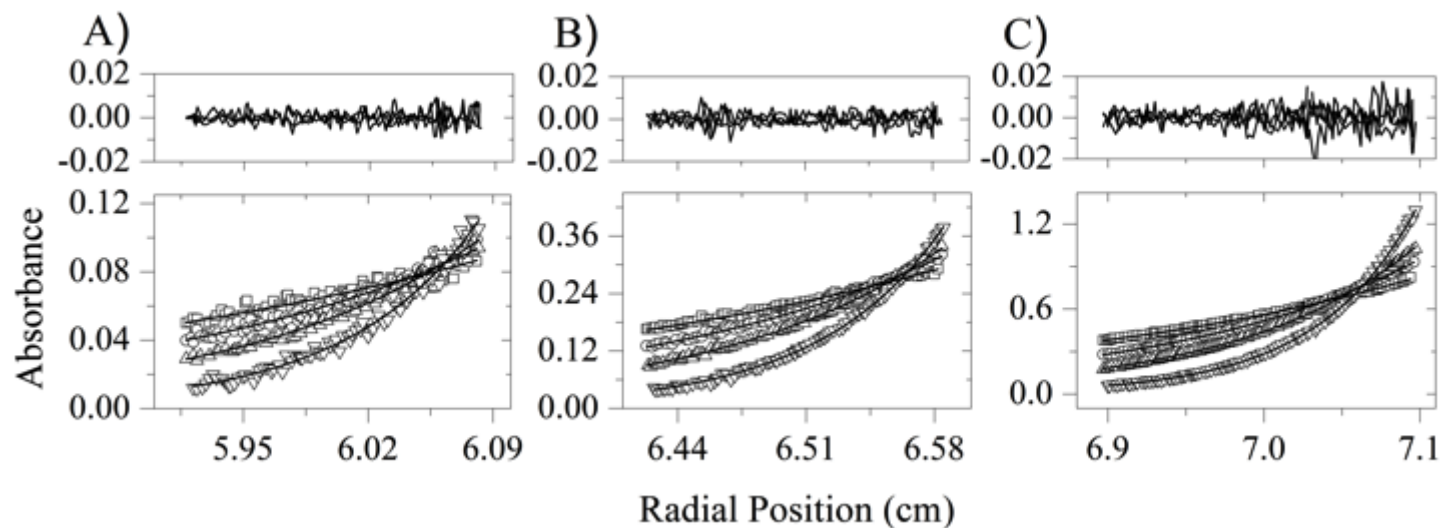


Fig. S15: Single species analysis of sedimentation equilibrium (A-C) data for β -lactoglobulin B at pH 5.5 (20 mM MES, 100 mM NaCl, 25 °C), fitted to a *single species of interacting system* model as implemented in SEDPHAT. The protein concentrations were 9.6 μ M (A), 17.8 μ M (B) and 50.4 μ M (C). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 255 nm. Residual plots of the fit are shown above. The derived molecular weight (and range) is 34939 (33,808 – 36,039). Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.27, (B) r.m.s.d. = 0.003, Z-score = 4.6, (C) r.m.s.d. = 0.005, Z-score = 3.8.

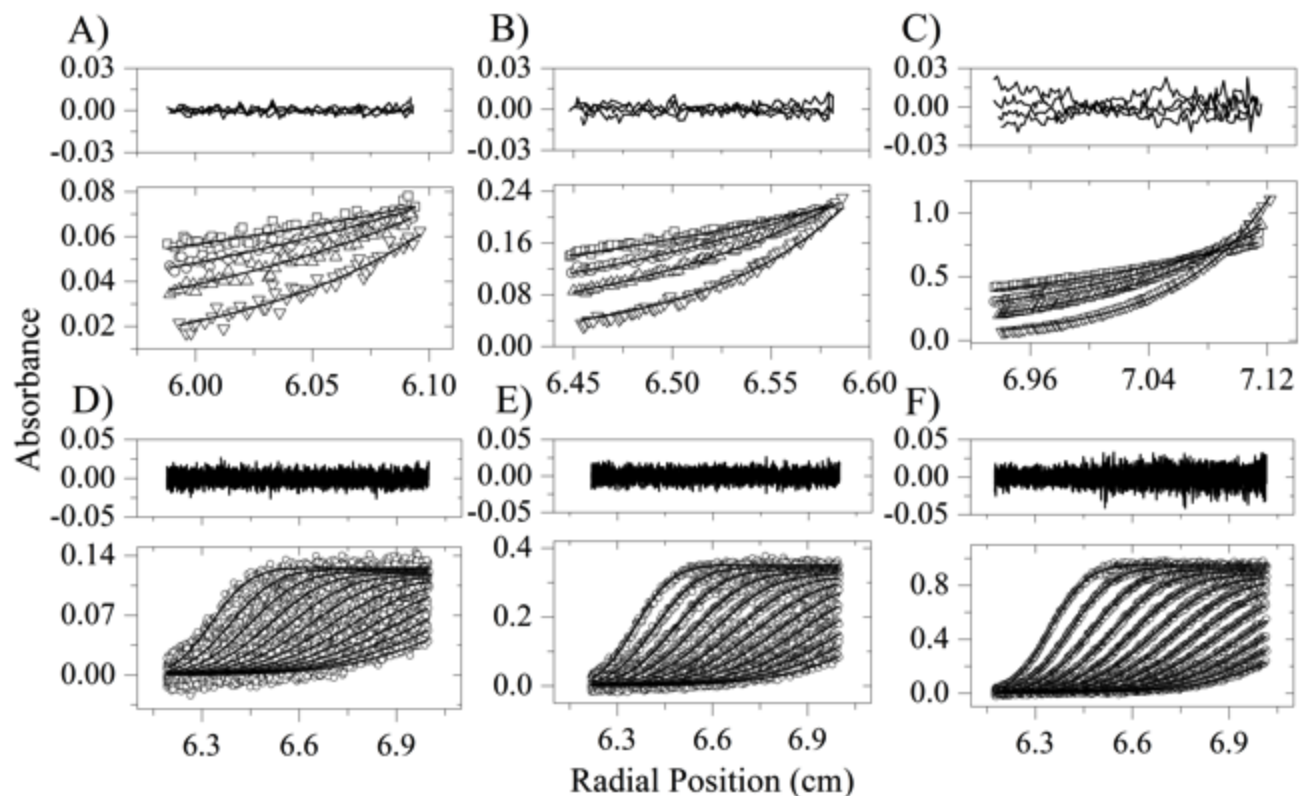


Fig. S16: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin B at pH 6.5 (20 mM MOPS, 100 mM NaCl, 25 °C), fitted to a *monomer-dimer equilibrium* model as implemented in SEDPHAT. The protein concentrations were 4.3 μ M (A) and 5.5 μ M (D), 11.9 μ M (B) and 15.4 μ M (E), and 36.5 μ M (C) and 42.0 μ M (F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 260 nm. The velocity data were collected at 50,000 rpm at 237 nm wavelength. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.002, Z-score = 0.08, (B) r.m.s.d. = 0.004, Z-score = 5.6, (C) r.m.s.d. = 0.008, Z-score = 10.7, (D) r.m.s.d. = 0.007, Z-score = 7.8, (E) r.m.s.d. = 0.007, Z-score = 12, (F) r.m.s.d. = 0.009, Z-score = 6.6. The global reduced chi-squared was 0.733.

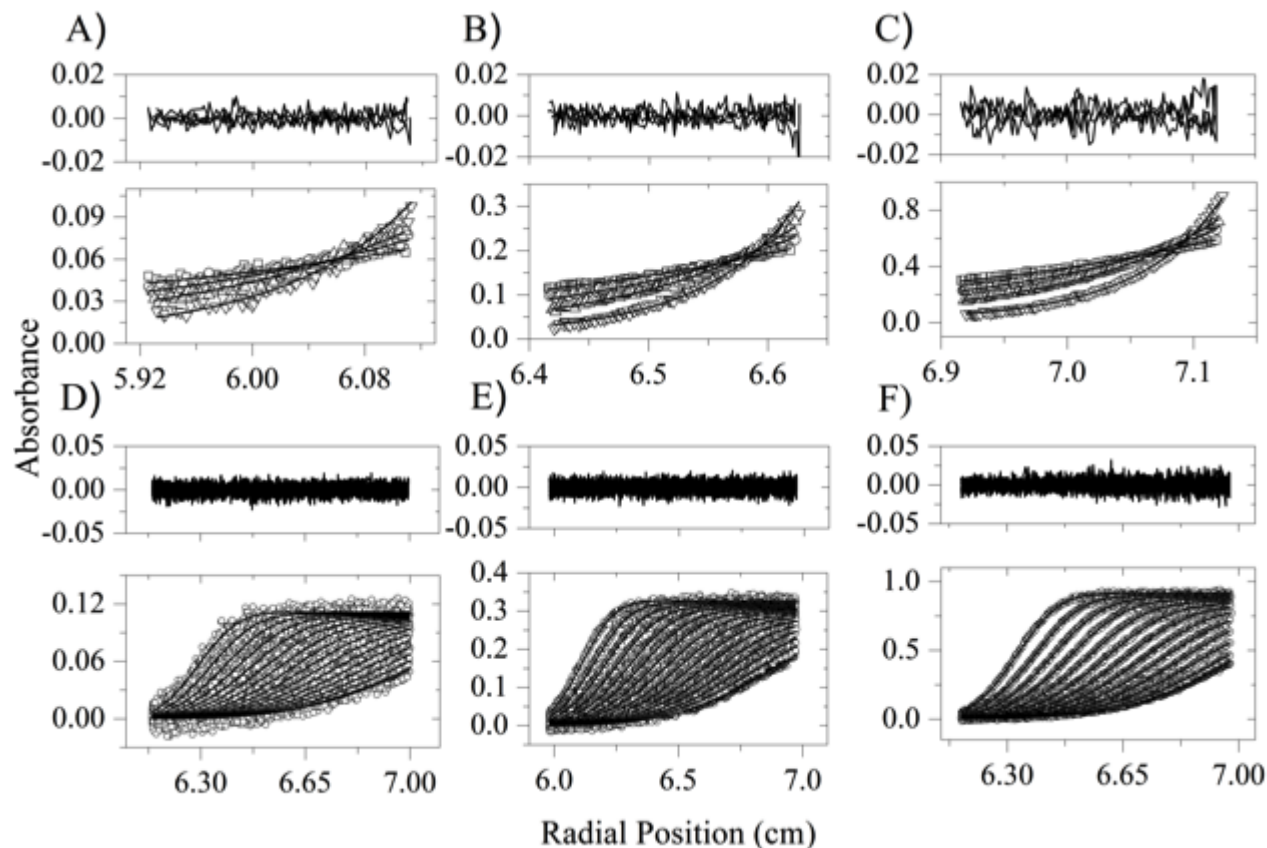


Fig. S17: Global fit of sedimentation equilibrium (A-C) and velocity (D-F) data for β -lactoglobulin B at pH 7.5 (20 mM MOPS, 100 mM NaCl, 25 °C), fitted to a *monomer-dimer equilibrium* model as implemented in SEDPHAT. The protein concentrations were 5.22 μ M (A and D), 15.4 μ M (B and E) and 43.3 μ M (C and F). The equilibrium data (A-C) were collected at 4 speeds (12,000 – triangle down, 15,000 – triangle up, 18,000 – circle, and 24,000 – square, rpm) at a wavelength of 250 nm. The velocity data were collected at 50,000 rpm at a wavelength of 280 nm. Residual plots of the fit are shown above. Statistics for the non-linear least-squares fits were: (A) r.m.s.d. = 0.003, Z-score = 0.6, (B) r.m.s.d. = 0.004, Z-score = 3, (C) r.m.s.d. = 0.005, Z-score = 3.4, (D) r.m.s.d. = 0.006, Z-score = 10, (E) r.m.s.d. = 0.006, Z-score = 5.6, (F) r.m.s.d. = 0.007, Z-score = 9.7. The global reduced chi-squared was 0.375.

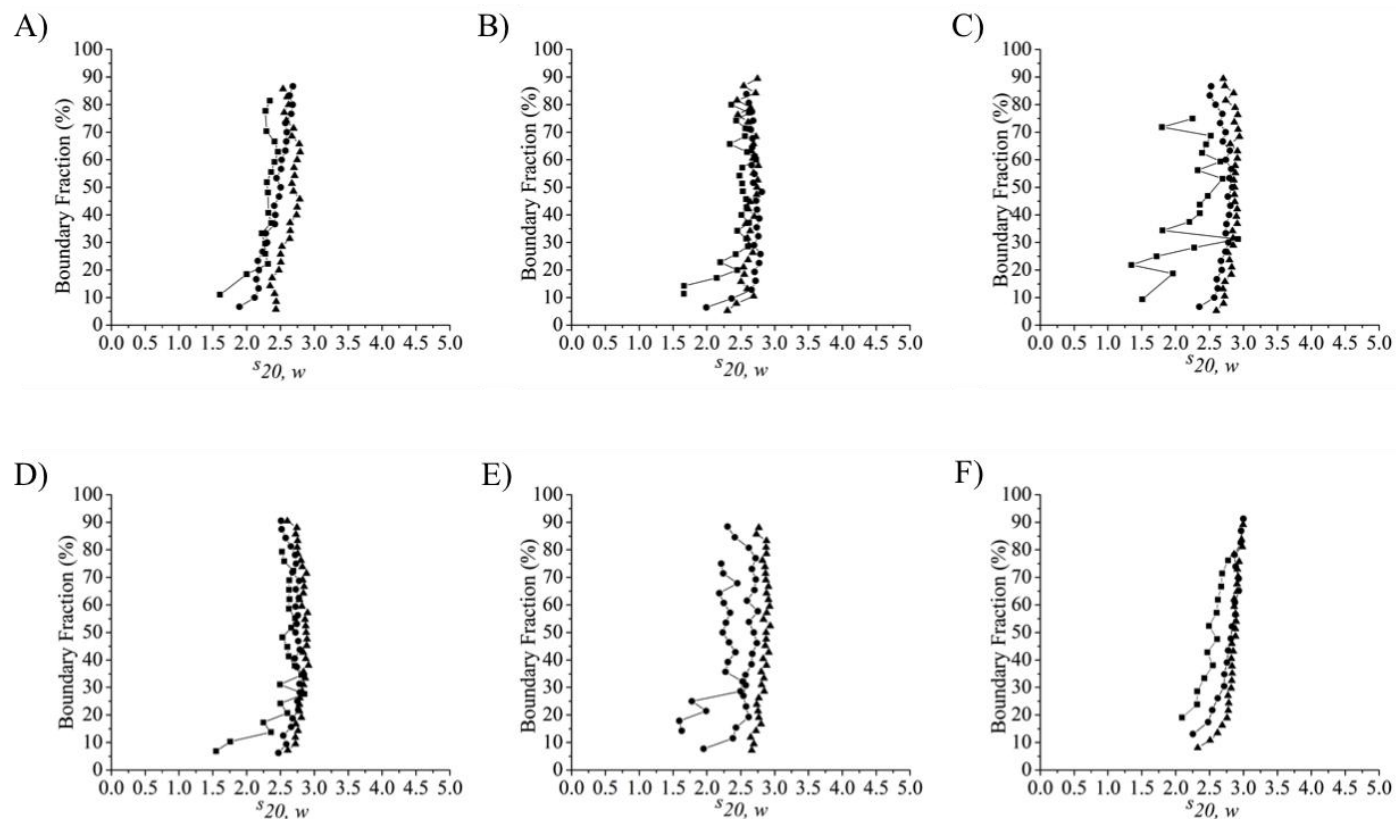


Fig. S18: van Holde-Weischet integral distribution plots for β Lg A over the pH range of 2.5 to 7.5: (A) pH 2.5 in 20 mM citrate, 100 mM NaCl, (B) pH 3.5 in 20 mM citrate, 100 mM NaCl, (C) pH 4.5 in 20 mM citrate, 100 mM NaCl, (D) pH 5.5 in 20 mM citrate, 100 mM NaCl, (E), pH 6.5 in 20 mM MOPS, 100 mM NaCl, (F) pH 7.5 in 20 mM MOPS, 100 mM NaCl. The van Holde-Weischet analysis is shown in each graph at three different loading concentrations of approximately 5, 15 and 45 μ M represented respectively as squares, circles and triangles. Precise concentrations are given in the captions to Figures S1–S4 and S6–S7, respectively.

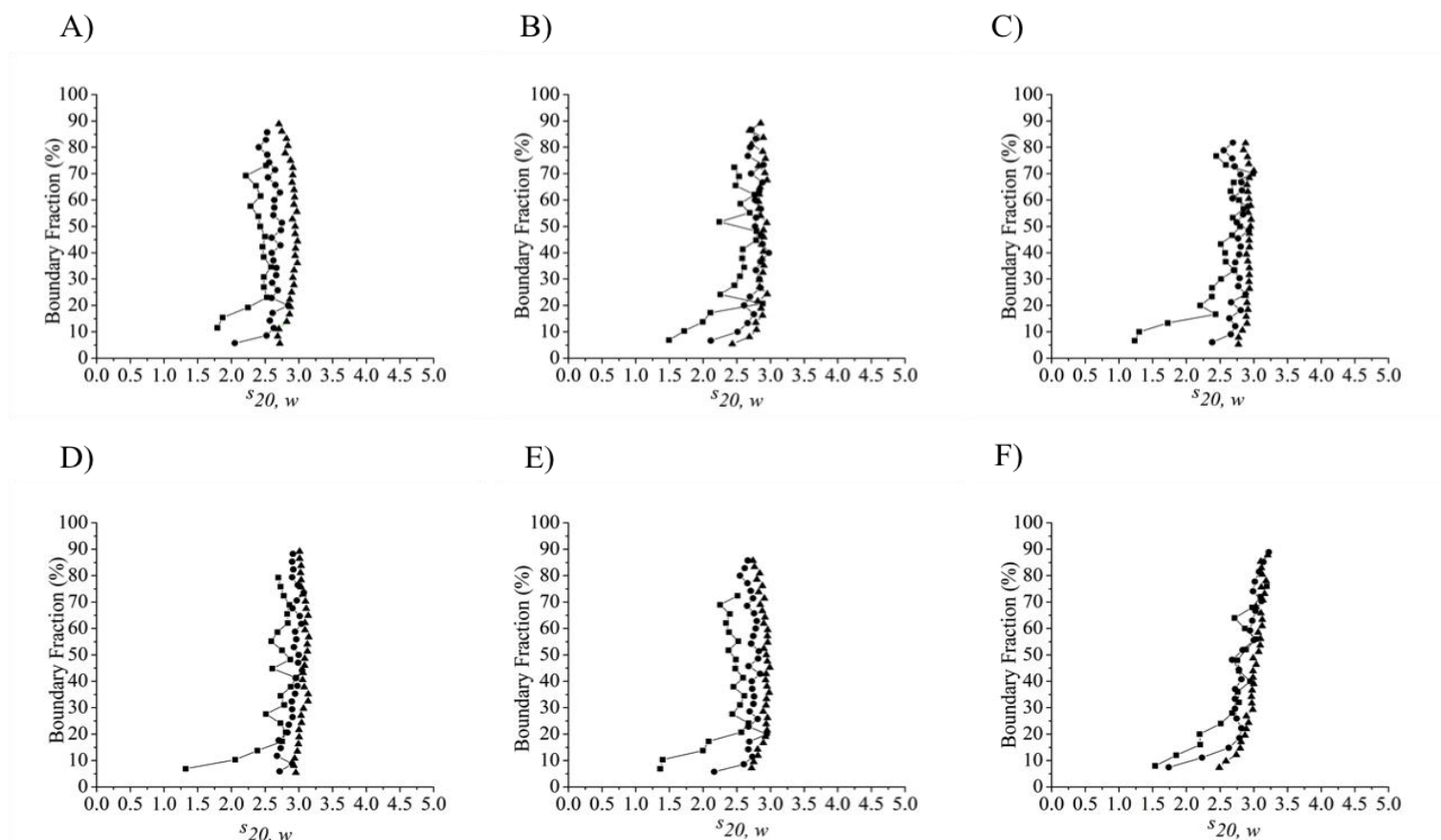


Fig. S19: van Holde-Weischet integral distribution plots for β Lg B over the pH range of 2.5 to 7.5: (A) pH 2.5 in 20 mM citrate, 100 mM NaCl, (B) pH 3.5 in 20 mM citrate, 100 mM NaCl, (C) pH 4.5 in 20 mM citrate, 100 mM NaCl, (D) pH 5.5 in 20 mM citrate, 100 mM NaCl, (E), pH 6.5 in 20 mM MOPS, 100 mM NaCl, (F) pH 7.5 in 20 mM MOPS, 100 mM NaCl. The van Holde-Weischet analysis is shown in each graph at three different loading concentrations of approximately 5, 15 and 45 μ M represented respectively using squares, circles and triangles. Precise concentrations are given in the captions to Figures S11–S14 and S16–S17, respectively.

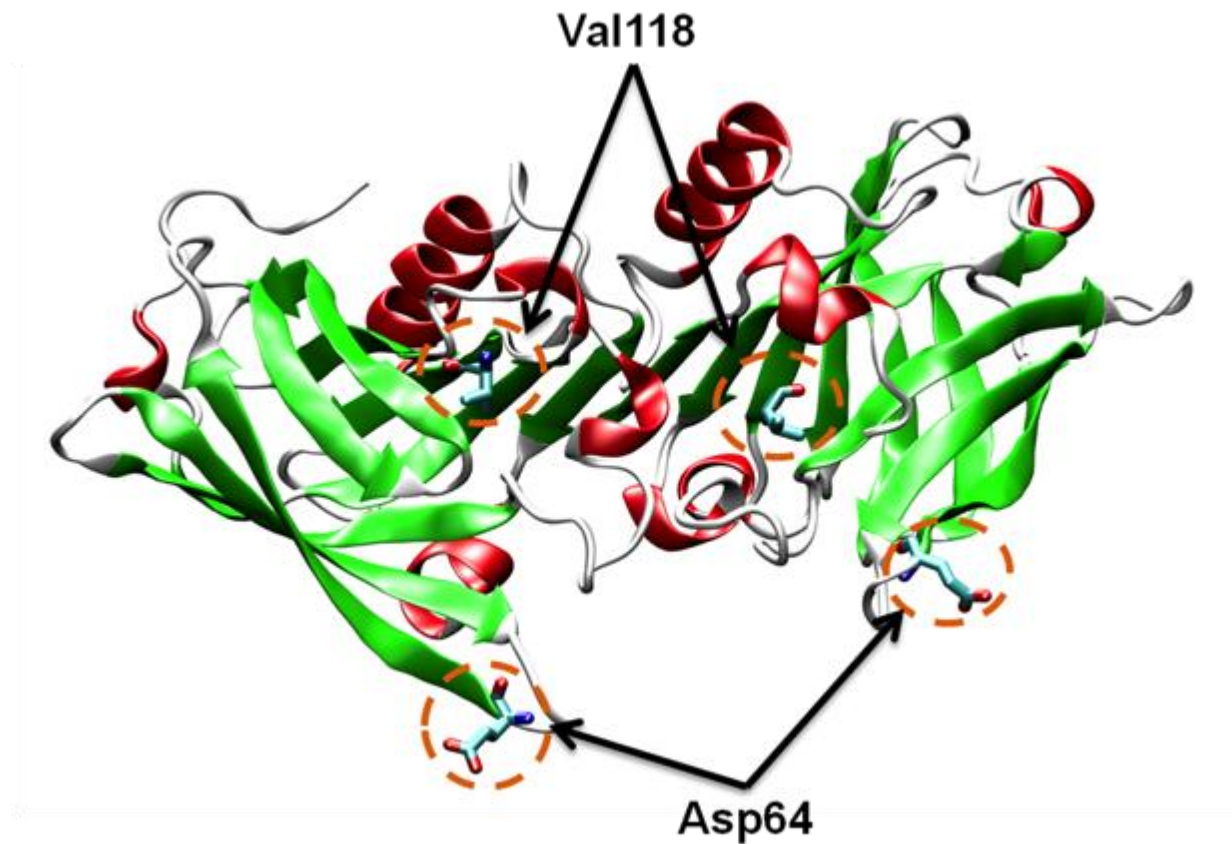


Fig. S20. Cartoon representation of the β Lg A dimer. Color code is the same as that used for Fig. 1. The residues Asp64 and Val118 are represented within orange circles on both monomers in licorice and colored by atom type. These residues are substituted by Gly64 and Ala118 in β Lg B.

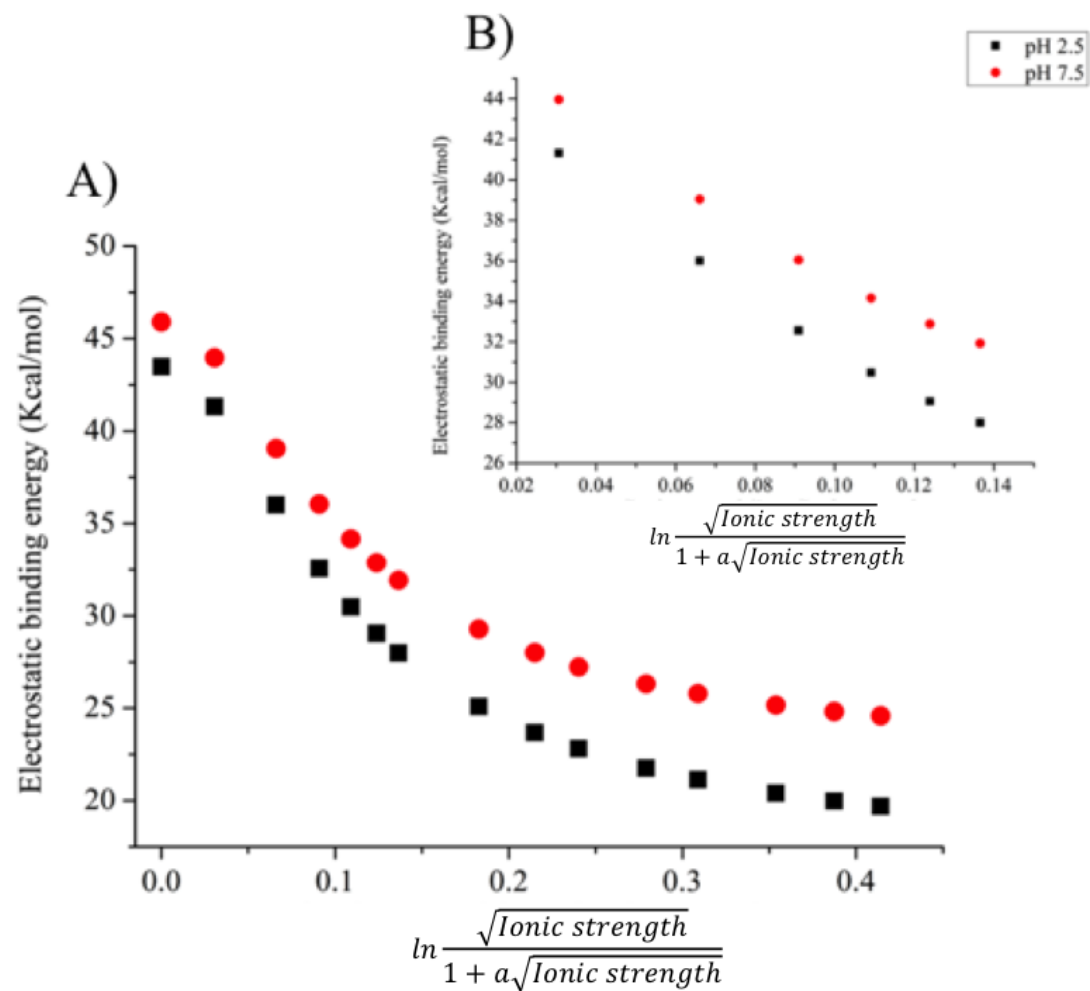


Fig. S21. (A) Calculated electrostatic binding energy for the β LgA dimer as a function of the ionic strength in NaCl solutions at pH 2.5 (*squares*) and 7.5 (*circles*). (B) Close up of (A) in the ionic strength range 1 to 25 mM NaCl showing the linear fit to the extended Debye-Hückel law.

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