

Supporting Information

Stylianopoulos et al. 10.1073/pnas.1213353109

SI Materials and Methods

Description of the Mathematical Model. To gain insight into the shape of tumors after releasing the stress and estimate the growth-induced stress, we constructed a 3D finite element model of an entire tumor in COMSOL and implemented an existing theory of tissue growth that has been applied successfully in arteries and brain tissue (1–3).

The tissue grows according to a specified growth deformation gradient tensor, \mathbf{F}_g , and therefore, the complete deformation gradient tensor \mathbf{F} consists of two components: the growth component \mathbf{F}_g and the elastic component \mathbf{F}_e (i.e., $\mathbf{F} = \mathbf{F}_e\mathbf{F}_g$). As a first approximation, we assumed a volumetric and isotropic growth of the tumor with $\mathbf{F}_g = \lambda_g\mathbf{I}$, where λ_g is the growth stretch ratio (3). We also made the assumption that the tumor behaves as a hyperelastic compressible neo-Hookean material with strain energy density function, W , given by (Eq. S1)

$$W = 0.5\left(\mu(-3 + \text{II}_1) + \kappa(-1 + J_e)^{-2}\right), \quad [\text{S1}]$$

where μ and κ are the shear and bulk modulus of the material, respectively, and J_e is the determinant of the elastic deformation gradient tensor \mathbf{F}_e . $\text{II}_1 = I_1 J_e^{-2/3}$, where I_1 is the first invariant of the right Cauchy–Green deformation tensor. This equation does not account for any transient poroelastic behavior. Finally, the Cauchy stress tensor is given by (Eq. S2)

$$\boldsymbol{\sigma} = J_e^{-1}\mathbf{F}_e\frac{\partial W}{\partial \mathbf{F}_e^T}. \quad [\text{S2}]$$

More details about the implementation of the model can be found in refs. 2 and 4.

In the present study, we used values of the parameters μ and κ for several tumor types measured previously and presented in Table S1 (5, 6).

Previous studies have shown a uniform compressive stress in the intratumoral region that turns to tensile stress at the margin (6, 7). Therefore, we assumed that a thin layer at the tumor periphery is in tension, whereas the intratumoral region is in compression. Furthermore, the growth and thus, the distribution of the stress are taken to be uniform throughout the intratumoral region and the periphery, but the growth stretch ratio λ between these two regions is different.

The deformation of the tumor after a cut depends on the relative growth and stiffness between the intratumoral region and the peripheral layer (i.e., $\lambda_g^* = \lambda_{gt}/\lambda_{gc}$ and $\mu^* = \mu_t/\mu_c$, where the subscripts t and c denote intratumoral region and peripheral layer, respectively). We did a parametric analysis of the simulation depicted in Fig. 1C in the text, which simulates the cutting mode that we used in our experimental procedure. We varied λ_g^* , μ^* , the thickness of the peripheral layer h , and the depth of the cut H . Because of symmetry, we performed our analysis on one-quarter of the domain. We applied a stress-free boundary condition to the outer and inner free surfaces and a symmetry boundary condition to the inner symmetry planes, and we fixed the bottom edge of the tumor to keep it in place (Fig. S1).

Fig. S2 shows the deformation of the tumor for constant λ_g^* , h , H , and four values of μ^* . In the plots, a positive deformation indicates opening of the tumor, whereas a negative deformation indicates bulging of the inner surface. As the peripheral layer becomes stiffer (i.e., μ^* decreases), the bulging of the inner surface increases, and the opening initially increases and then

drops. Notice that bulging is observed only when the peripheral tumor layer is stiffer than the intratumoral region.

The deformation of the center line of the tumor is the dashed line in Fig. S3. We separately varied the parameters λ_g^* , h , H , or μ^* while keeping the other three constant. Fig. S4 depicts the predictions of the mathematical model. Increase in the growth stretch ratio λ_g^* increases the opening of the tumor but does not affect the bulging of the inner surface (Fig. S4A). In contrast, changes in the stiffness of the peripheral layer can significantly affect both bulging and opening (Fig. S4B). Importantly, there is a maximum in tumor opening as μ^* decreases (peripheral layer stiffens). This intriguing finding is the result of two competing effects: the tension at the margin and the compression at the interior of the tumor. Hence, increase in the thickness of the peripheral layer would decrease opening and increase bulging (Fig. S4C). Finally, the depth of the cut affects both bulging and opening (Fig. S4D).

The parameter λ_g^* describes the relative cell proliferation between the tumor periphery and interior. Measurements of the spatial distribution of cancer cell proliferation (8, 9) have shown that the proliferation rate is higher at the periphery of the tumor, where there are more blood vessels. The proliferation rate at the periphery can be two times as much as the rate at the center. In Fig. S5, we plot the circumferential compressive growth-induced stress at the interior of the tumor as a function of the relative growth, λ_g^* . As the relative growth increases, growth-induced stress increases as well.

In addition, we performed simulations keeping λ_g^* constant and varying the relative stiffness μ^* between the interior and the periphery of the tumor (Fig. S6). Fig. S6 shows that stiffening of the tumor periphery has little effect on the intratumoral compressive growth-induced stress.

Model Limitations. Our mathematical approach to quantify stress in tumors is subject to several assumptions and limitations. The magnitude of the stress given by the model depends on the specified material properties and growth. The material properties that we used were based on previous measurements in our laboratory (5, 6), which are in the same range as in other published studies (10, 11). However, when depleting tumor constituents, the material properties change. Thus, as discussed in the text, in many cases, we compared normalized tumor openings rather than stress magnitudes because of the uncertainty of the material properties. In addition, we assumed an isotropic and uniform growth of the tumor and peripheral layer, which might not be true given its heterogeneous structure. This assumption is an approximation that we had to make because of the lack of any experimental findings of growth patterns in our tumor models. Also, we used the neo-Hookean constitutive equation to describe the mechanical behavior of tumors. Tumors, like most biological tissues, are complex, heterogeneous, and poroelastic structures, and an isotropic, continuum-level constitutive equation might not be sufficient to describe their mechanical response. Nonetheless, the model predictions were consistent with our cutting experiments, which suggest that our assumptions are reasonable. As more data become available, they can be easily incorporated into our current framework. Finally, another limitation of the model is that many different growth fields or combinations of growth patterns and material properties can give rise to similar residual stress distributions. Added to this information is the fact that the cutting experiment only eliminates most and not all of the stress, making it difficult to come up with a unique growth

pattern. Hence, the current results provide an estimate of the growth-induced stress in tumors.

Quantification of Growth-Induced Stress Using the Mathematical Model. To quantify the growth-induced stress from the opening measurements, we used the mathematical model, which was implemented in COMSOL using the finite element method. The tumors were represented as ellipsoids. The lengths of the three axes of the tumors, which we incorporated into the model, were measured after the tumors were excised and before performing the cutting experiment. We simulated the experiment using the material properties shown in Table S1. Although bulging of the inner surface was evident in all types of tumors, it was not possible to perform accurate measurements of the bulging. To estimate the compressive stress of the intratumoral region, we varied μ^* from 1/10, where bulging is first observed (Fig. S2), to 1/40, where the two inner surfaces are almost in contact, and we calculated the value of λ_g^* that matched the experimentally measured tumor opening. Subsequently, knowing the growth stretch ratio, λ_g^* , we used our model to convert this stretch to growth-induced stress. The thickness, h , of the peripheral layer was set to 5% based on previous studies (6), and the depth of our cuts was 80% of tissue thickness. We followed the same methodology to quantify the compressive, growth-induced stress of the human tumors presented in Table S3. Human tumors were modeled as ellipsoids based on the dimensions in the three coordinate directions, and we used the material properties of the stiffest tumor shown in Table S1.

Interstitial Fluid Pressure Measurement. Interstitial fluid pressure (IFP) was measured with the wick-in-needle technique (12) before tumor excision. For each tumor, IFP was measured in at least two different tumor locations.

Piezoelectric Probe Measurement. We measured the combination of IFP and some component of solid stress using a piezoelectric probe (13). Briefly, we connected a Millar Mikro-Tip pressure catheter transducer (0.33-mm diameter, SPR-1000) to a PCU-2000 Pressure Control Unit and an ADInstruments PowerLab data acquisition system. After calibration, we placed the catheter using a 25-gauge needle to create a space in the tissue to insert the probe after needle withdrawal.

Tumor Growth Rate Measurement. Tumor planar dimensions (x, y) were measured with a digital caliper every 2 d. The volume of the tumor was estimated by the expression $V = \frac{\pi}{6}(xy)^{3/2}$. Tumor doubling time, T , was calculated by fitting the equation $V = V_0 2^{t/T}$ to the experimental data.

Collagenase, Hyaluronidase, and Diphtheria Toxin Treatment. Bacterial collagenase from *Clostridium histolyticum* (C0773; Sigma-Aldrich) was prepared by dissolving 1 mg collagenase in 10 mL 50 mM TES buffer containing 0.36 mM calcium chloride, pH 7.4, at 37 °C. After excision, the tumor was placed in the collagenase

solution remaining at 37 °C for 2 h before measurement. Hyaluronidase (H3506; Sigma-Aldrich) was administered i.p. 24 and 1 h before tumor excision; each time, it was administered in a volume of 0.1 mL/20 g body weight to provide an enzyme activity of 100,000 IU/kg (14).

Human cells are 1,000 times more sensitive to diphtheria toxin than murine cells and thus, can be depleted by diphtheria toxin in vivo in mice (15, 16). Mice were injected one time i.p. with 1 μ g diphtheria toxin in 0.3 mL PBS (15). After 24 h, the tumor was excised to perform the measurement.

Saridegib Treatment. Male FVB and male SCID mice bearing orthotopic human pancreatic adenocarcinomas AK4.4 and Capan-2 were treated as described previously (17). Saridegib was dissolved in a 5% aqueous solution of hydroxypropyl- β -cyclodextran. Accounting for the potency of the batch received, the resulting solution was 5 mg/mL. After sonication and vortexing, the solution was sterile-filtered; 40 mg/kg resulting drug were administered daily by gavage for 8 or 10 d in mice bearing AK4.4 or Capan-2, respectively.

Immunofluorescence Staining, Imaging, and Analysis. For frozen sections, staining was performed according to a previously described protocol (18, 19). Human vimentin staining was done only on frozen tissues according to a previously described protocol (16). After retro-orbital injection of biotinylated lectin 5 min before tumor removal (100 μ L; Vector Labs), tissues were excised, fixed for 2–3 h in 4% formaldehyde in PBS, incubated in 30% sucrose in PBS overnight at 4 °C, and frozen in optimal cutting temperature compound (Tissue-Tek). Transverse tumor sections (40- μ m thick) were immunostained with antibodies to endothelial marker CD31 and counterstained by mounting with DAPI-containing medium (Vectashield; Vector Labs). Collagen I staining was done on both frozen and paraffin embedded tissues. In both cases, collagen I was detected using the LF-67 antibody provided by Larry Fisher (National Institute of Dental Research, Bethesda, MD). For paraffin sections, slides were treated with 3% hydrogen peroxide before antigen retrieval with Target Retrieval Solution, pH 9 (DAKO). The slides were further treated with 0.05% trypsin before the primary antibody was applied.

Eight random images (four interior and four periphery images) at 20 \times magnification at a resolution of 1.3 pixels to micrometers were taken from each slide. Images of collagen- and vimentin-stained sections were analyzed by thresholding based on the average image intensity. The fraction of pixels above threshold was used as a measure of the content in each tumor. Nonviable tissue area was excluded from the analysis. For vascular analysis, vessels were segmented using a custom semiautomated tracing program developed in MATLAB (MathWorks), allowing the removal of structures under 30 pixels and regions of autofluorescence.

Statistical Analysis. The data are presented as means with SEs. Groups were compared using a Student t test.

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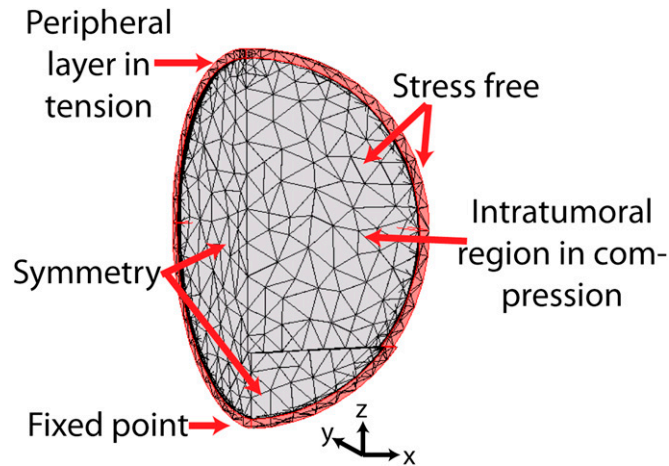


Fig. S1. Boundary conditions of the model. Because of symmetry, we solved for one-quarter of the domain; we applied symmetry boundary conditions at the planes of symmetry and stress-free boundary conditions at the free surfaces.

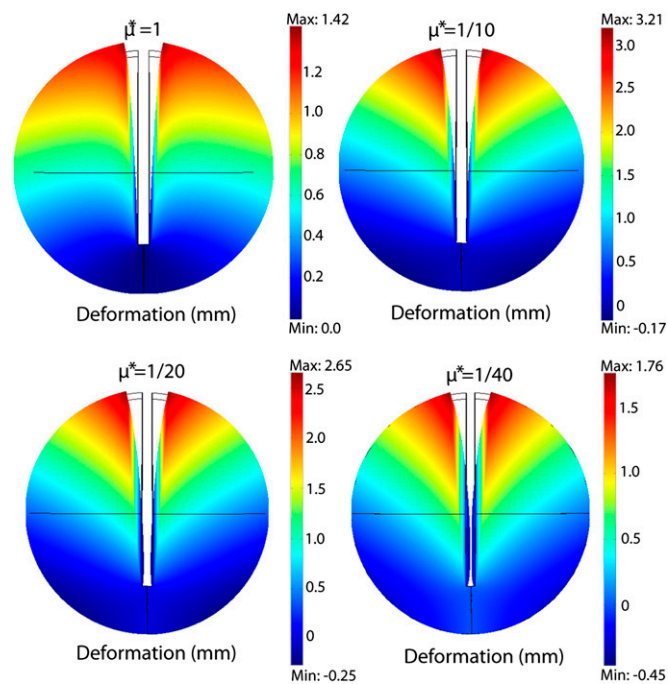


Fig. S2. Model predictions of the tumor shape after making a cut for four values of μ^* . The value of λ_0^* was 1.2, the peripheral layer occupied 5% of the thickness, and the depth of the cut was 0.8 cm.

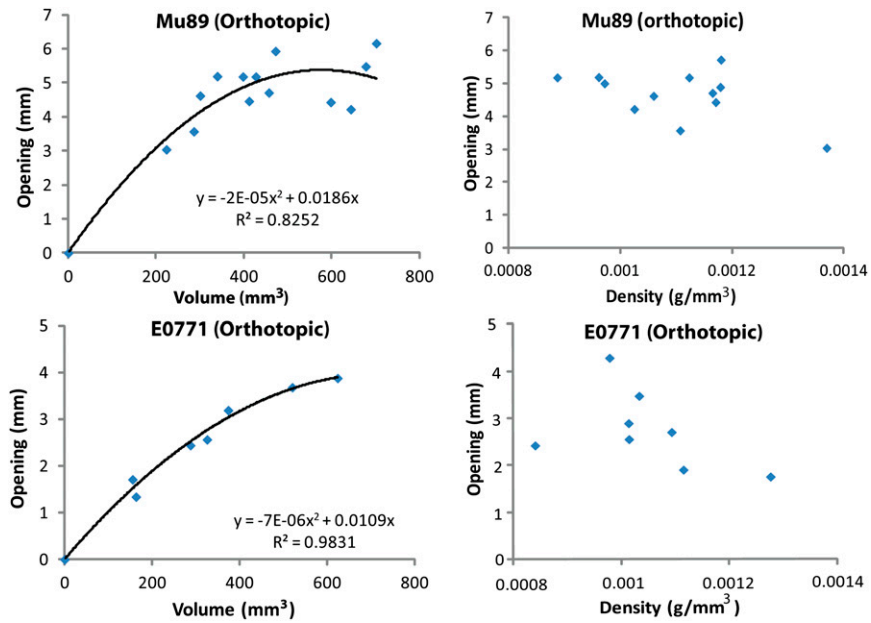


Fig. S8. Tumor opening as a function of tumor volume and mass density for two orthotopic cancer cell lines: Mu89 melanomas and E0771 mammary adenocarcinomas. Tumor opening increases linearly with volume before reaching a plateau. Higher volumes are usually correlated with increased necrosis, which is likely to reduce the interior swelling and thus, reduce the opening. No dependence of tumor opening on density was observed.

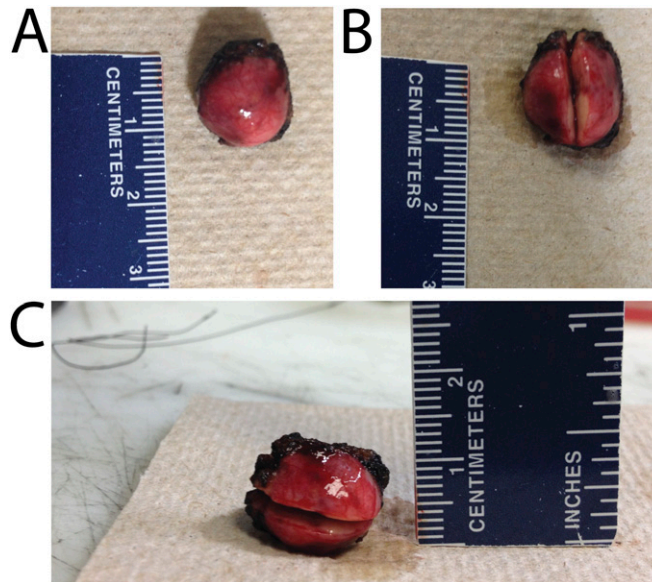


Fig. S9. Tumor opening of human pancreatic neuroendocrine tumors. A human pancreatic neuroendocrine tumor after it is excised from a patient before processing for histology (A) opens after a partial cut (B). The tumor opening is not affected after the tumor is placed on its side (C) or the tumor is closed manually.

Table S1. Mechanical material properties of the tumor types used in the study

Tumor type	Cancer cell line	Bulk modulus κ		Shear modulus μ	
		mmHg	kPa	mmHg	kPa
Epithelial					
Breast	MCalV, 4T1, E0771	50	6.7	37.5	5.0
Colon	LS174T	30	4.0	22.5	3.0
Pancreatic	Pan02, Capan-2, AK4.4	Not available	Not available	Not available	Not available
Mesenchymal					
Sarcoma	HT1080	Not available	Not available	Not available	Not available
Melanoma	Mu89, B16F10	19	2.5	14.25	1.9
Glioma	U87	200	26.7	150	20.0

The shear modulus, μ , is a measure of the stiffness of the tumor (the higher the value of the shear modulus, the stiffer the tumor). The values of μ and κ shown here were measured experimentally in our previous work (1, 2). mmHg, millimeter of mercury; kPa, kilopascal.

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2. Roose T, Netti PA, Munn LL, Boucher Y, Jain RK (2003) Solid stress generated by spheroid growth estimated using a linear poroelasticity model small star, filled. *Microvasc Res* 66: 204–212.

Table S2. Experimentally measured doubling time and model estimates of the growth stretch ratio and growth-induced solid stress in the interior of the transplanted tumors used in the study

Cancer cell line	Doubling time (days)	Growth stretch ratio λ_g^* ($\mu^* = 1/10-1/40$)	Compressive circumferential stress ($\mu^* = 1/10-1/40$)	
			mmHg	kPa
U87 (ectopic)	5.18	1.17–1.32	38.0–60.1	5.07–8.01
Mu89	2.13	1.15–1.29	3.2–5.3	0.43–0.71
B16F10	0.94	1.13–1.25	2.8–4.7	0.37–0.63
LS174T	1.88	1.11–1.20	5.0–8.4	0.67–1.12
E0771 (ectopic)	2.21	1.08–1.14	4.9–8.2	0.65–1.09
E0771 (orthotopic)	—	1.13–1.25	7.4–12.4	0.99–1.65
MCalV (ectopic)	2.50	1.07–1.13	4.5–7.4	0.60–0.99
MCalV (orthotopic)	—	1.19–1.34	8.4–14.5	0.67–1.99
4T1 (ectopic)	2.25	1.09–1.16	5.3–8.8	0.71–1.17
4T1 (orthotopic)	—	1.11–1.20	6.3–10.5	0.84–1.40

Doubling time is a measure of tumor growth rate. High doubling times correspond to slow-growing tumors. The growth-induced solid stress in the tumor interior is compressive. The table shows the estimates of the growth-induced solid stress in the circumferential direction of the tumor. Material properties of pancreatic tumors and HT1080 soft-tissue sarcoma are not available, and analysis was not performed. mmHg, millimeter of mercury; kPa, kilopascal.

Table S3. Dimensions and model estimates of the growth-induced solid stress developed in the interior of surgically excised human tumors along the circumferential direction

Tumor type	Tumor dimensions (cm)	Compressive circumferential stress	
		mmHg	kPa
Breast tumor	2.2 × 2.5 × 2.0	75.1–97.2	10.0–12.9
Breast tumor	2.6 × 2.7 × 1.6	99.5–142.4	13.3–19.0
Pancreatic neuroendocrine tumor	1.4 × 1.6 × 1.2	54.9–81.2	7.3–10.8
Pancreatic neuroendocrine tumor	1.3 × 1.8 × 0.9	16.4–31.2	2.2–4.2
Osteosarcoma	13.0 × 15.7 × 9.8	35.3–48.3	4.7–6.4
Soft-tissue sarcoma	5.0 × 5.9 × 3.1	73.7–107.6	9.8–14.3
Soft-tissue sarcoma	6.5 × 10.5 × 4.0	42.9–57.2	5.7–7.6
Soft-tissue sarcoma	12.0 × 15.0 × 6.0	50.8–58.5	6.7–7.8
Liposarcoma	6.2 × 6.9 × 6.8	41.8–58.7	5.6–7.8
Neurofibrosarcoma	8.5 × 12.0 × 8.0	45.6–62.3	6.1–8.3

The growth-induced solid stress in the tumor interior is compressive. The table shows the estimates of the growth-induced solid stress in the circumferential direction of the tumor. We used the mechanical properties of U87 tumors, the stiffest tumor in Table S1. mmHg, millimeter of mercury; kPa, kilopascal.

