

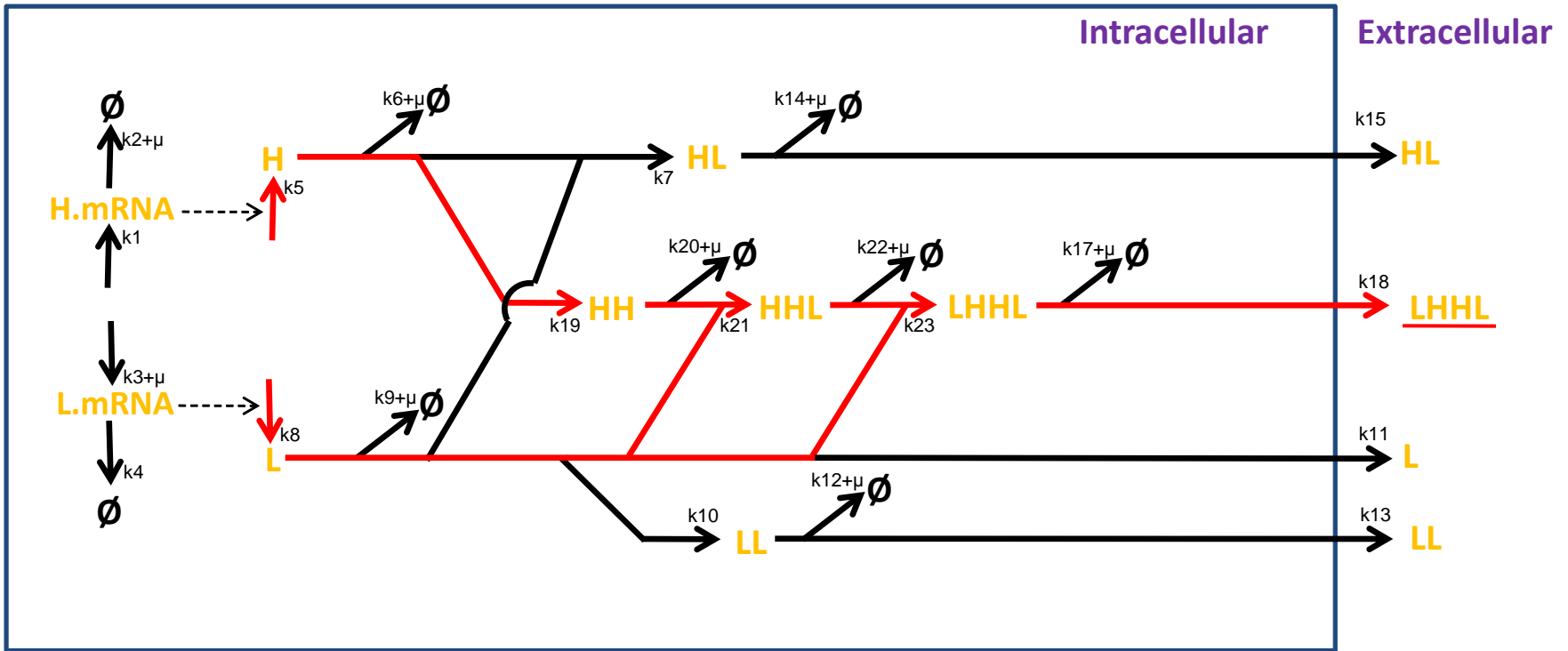
Mead *et al.*

Supplementary file 3

Pathway diagrams and differential equation systems for the different antibody assembly models considered in this study.

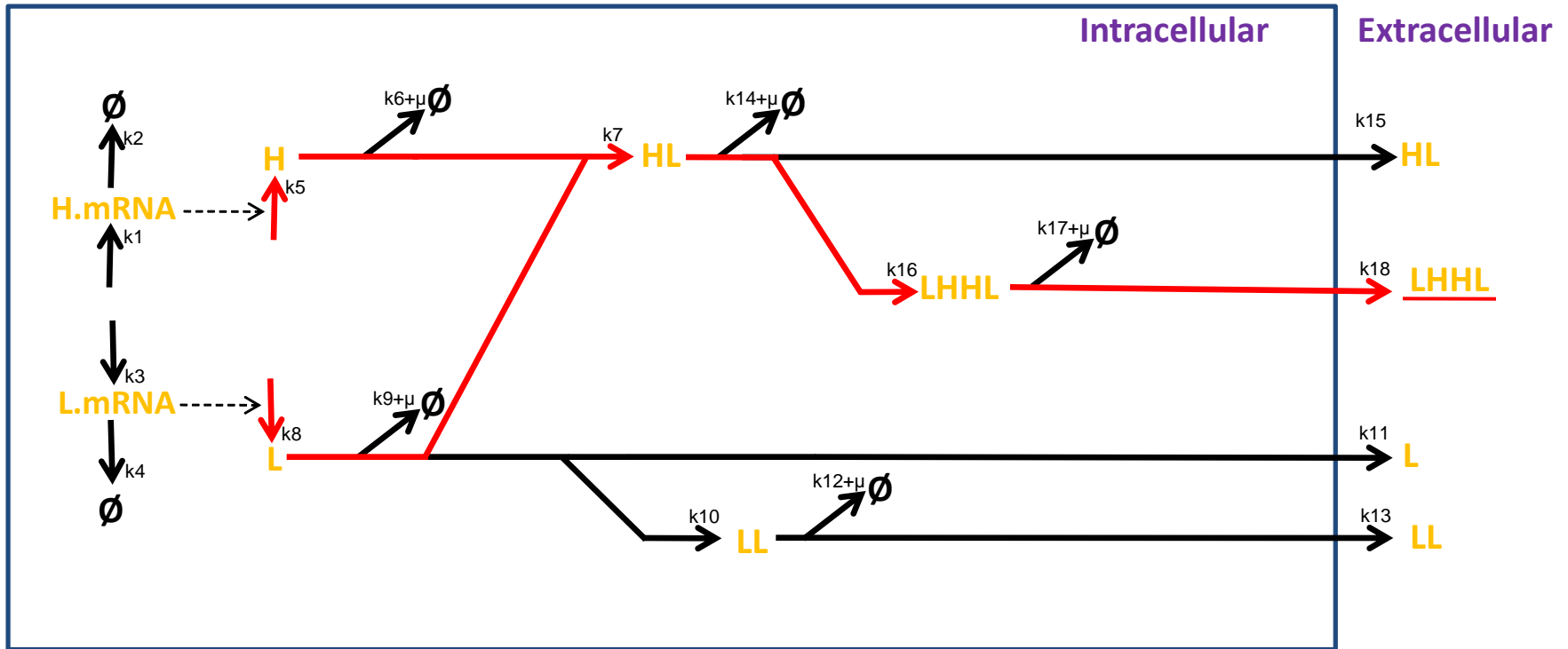
In pathway diagrams, productive reactions (leading to secreted full antibody) are shown in red.

HH model



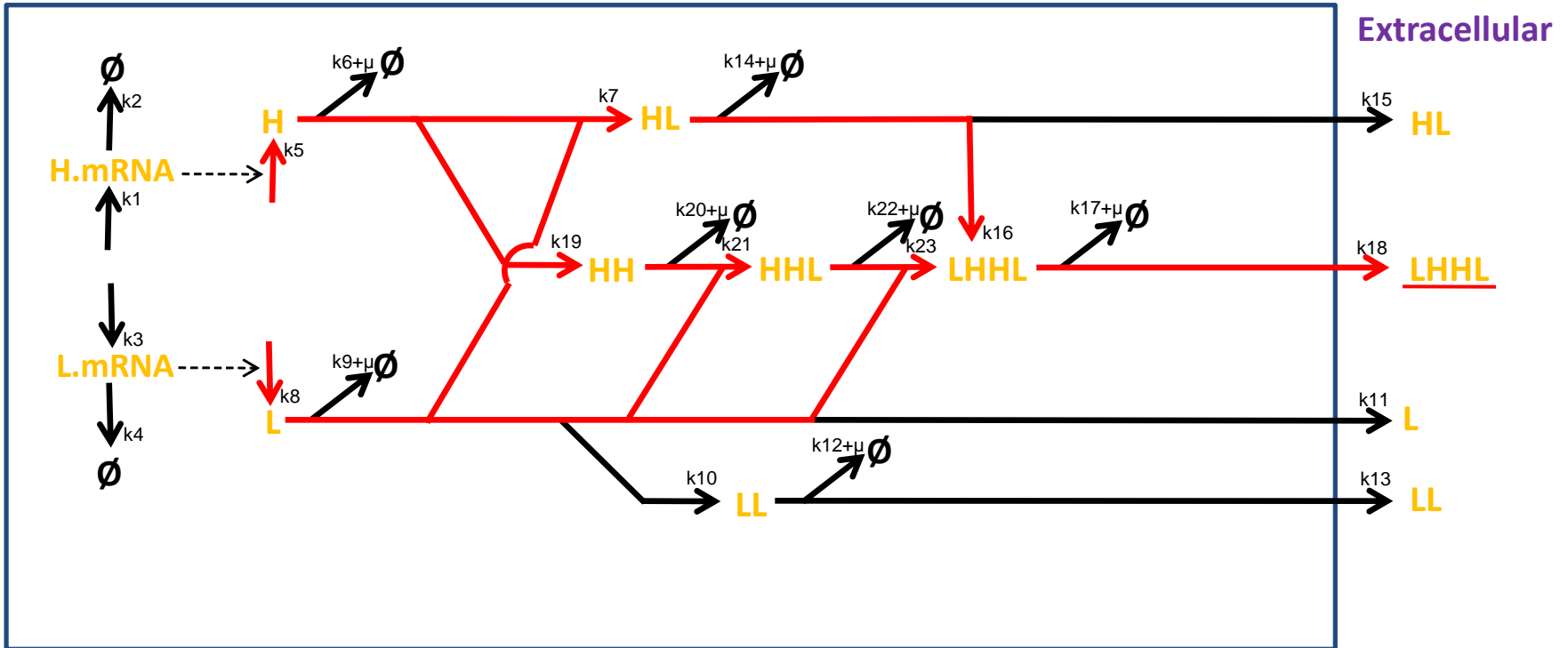
Species	Name	Eq.
S1	H.RNA	$dS1/dt = k1 - (k2 + \mu)*S1$
S2	L.RNA	$dS2/dt = k3 - (k4 + \mu)*S2$
S3	H	$dS3/dt = k5*S1 - (k6 + \mu)*S3 - k19*S3*S3 - k7*S3*S4$
S4	L	$dS4/dt = k8*S2 - (k9 + \mu)*S4 - k10*S4*S4 - k11*S4 - k21*S10*S4 - k23*S11*S4 - k7*S3*S4$
S5	L(Medium)	$dS5/dt = k11*S4$
S6	LL	$dS6/dt = k10*S4*S4 - (k12 + \mu)*S6 - k13*S6$
S7	LL(Medium)	$dS7/dt = k13*S6$
S8	HL	$dS8/dt = k7*S3*S4 - (k14 + \mu)*S8 - k15*S8$
S9	HL(Medium)	$dS9/dt = k15 * S8$
S10	HH	$dS10/dt = k19*S3*S3 - (K20 + \mu)*S10 - k21*S10*S4$
S11	LHH	$dS11/dt = K21*S10*S4 - (k22 + \mu)*S11 - k23*S11*S4$
S12	LHHH	$dS12/dt = k23*S11*S4 - (k17 + \mu)*S12 - k18*S12$
S13	LHHH(Medium)	$dS13/dt = k18*S12$

HL model



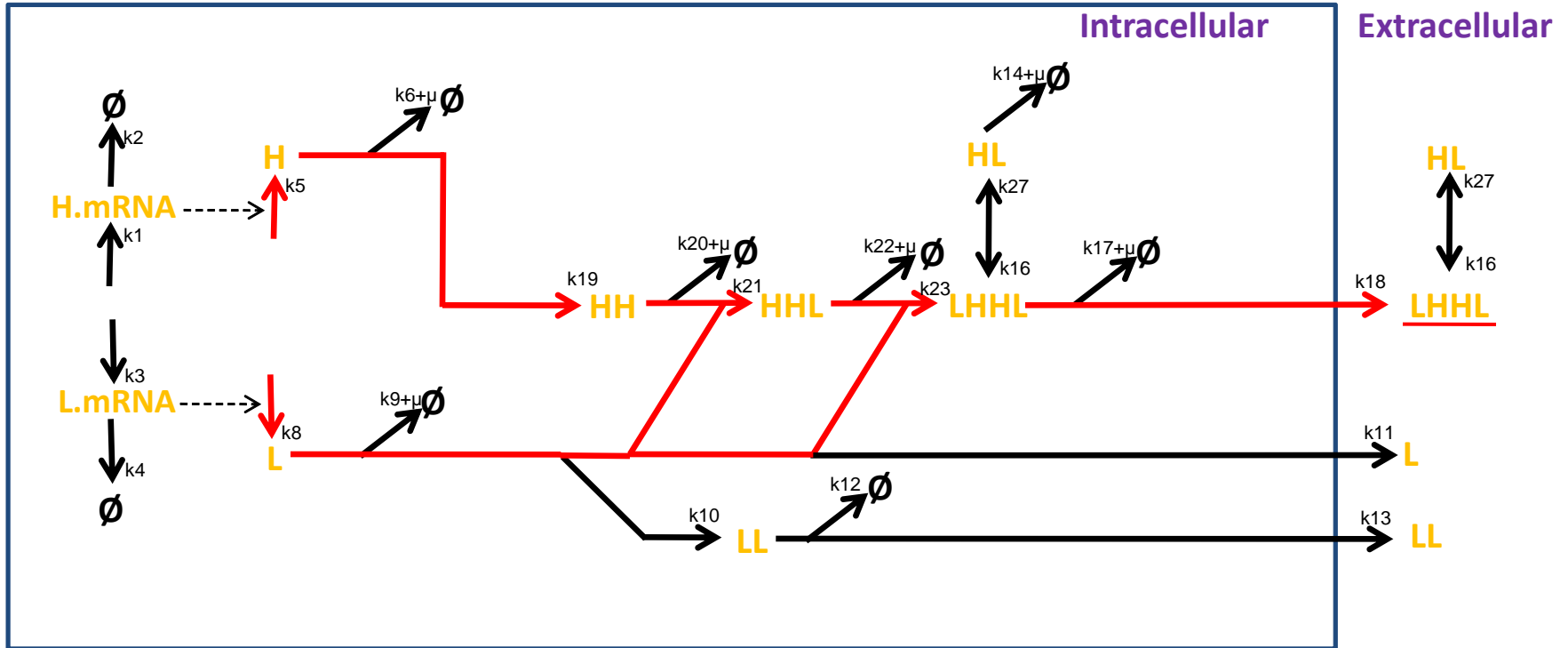
Species	Name	Eq.
S1	H.RNA	$dS1/dt = k_1 - (k_2 + \mu) * S1$
S2	L.RNA	$dS2/dt = k_3 - (k_4 + \mu) * S2$
S3	H	$dS3/dt = k_5 * S1 - (k_6 + \mu) * S3 - k_7 * S3 * S4$
S4	L	$dS4/dt = k_8 * S2 - (k_9 + \mu) * S4 - k_7 * S3 * S4 - k_{10} * S4 * S4 - k_{11} * S4$
S5	L(Medium)	$dS5/dt = k_{11} * S4$
S6	LL	$dS6/dt = k_{10} * S4 * S4 - (k_{12} + \mu) * S6 - k_{13} * S6$
S7	LL(Medium)	$dS7/dt = k_{13} * S6$
S8	HL	$dS8/dt = k_7 * S3 * S4 - (k_{14} + \mu) * S8 - k_{15} * S8 - k_{16} * S8 * S8$
S9	HL(Medium)	$dS9/dt = k_{15} * S8$
S12	LHHL	$dS12/dt = k_{16} * S8 * S8 - (k_{17} + \mu) * S12 - k_{18} * S12$
S13	LHHL(Medium)	$dS13/dt = k_{18} * S12$

combined model



Species	Name	Eq.
S1	H.RNA	$dS1/dt = k_1 - (k_2 + \mu) * S1$
S2	L.RNA	$dS2/dt = k_3 - (k_4 + \mu) * S2$
S3	H	$dS3/dt = k_5 * S1 - (k_6 + \mu) * S3 - k_7 * S3 * S4 - k_{19} * S3 * S3$
S4	L	$dS4/dt = k_8 * S2 - (k_9 + \mu) * S4 - k_7 * S3 * S4 - k_{10} * S4 * S4 - k_{11} * S4 - k_{21} * S_{10} * S4 - k_{23} * S_{11} * S4$
S5	L(Medium)	$dS5/dt = k_{11} * S4$
S6	LL	$dS6/dt = k_{10} * S4 * S4 - (k_{12} + \mu) * S6 - k_{13} * S6$
S7	LL(Medium)	$dS7/dt = k_{13} * S6$
S8	HL	$dS8/dt = k_7 * S3 * S4 - (k_{14} + \mu) * S8 - k_{16} * S8 * S8 - k_{15} * S8$
S9	HL(Medium)	$dS9/dt = k_{15} * S8$
S10	HH	$dS10/dt = k_{19} * S3 * S3 - (k_{20} + \mu) * S_{10} - k_{21} * S_{10} * S4$
S11	LHH	$dS11/dt = k_{21} * S_{10} * S4 - (k_{22} + \mu) * S_{11} - k_{23} * S_{11} * S4$
S12	LHHL	$dS12/dt = k_{23} * S_{11} * S4 + k_{16} * S8 * S8 - (k_{17} + \mu) * S_{12} - k_{18} * S_{12}$
S13	LHHL(Medium)	$dS13/dt = k_{18} * S_{12}$

James model



Species	Name	Eq.
S1	H.RNA	$dS1/dt = k_1 - (k_2+\mu)*S1$
S2	L.RNA	$dS2/dt = k_3 - (k_4+\mu)*S2$
S3	H	$dS3/dt = k_5*S1 - (k_6+\mu)*S3 - k_{19}*S3*S3$
S4	L	$dS4/dt = k_8*S2 - (k_9+\mu)*S4 - k_{10}*S4*S4 - k_{11}*S4 - k_{21}*S10*S4 - k_{23}*S11*S4$
S5	L(Medium)	$dS5/dt = k_{11}*S4$
S6	LL	$dS6/dt = k_{10}*S4*S4 - (k_{12}+\mu)*S6 - k_{13}*S6$
S7	LL(Medium)	$dS7/dt = k_{13}*S6$
S8	HL	$dS8/dt = k_{27}*S12 - (k_{14}+\mu)*S8 - k_{16}*S8*S8$
S9	HL(Medium)	$dS9/dt = k_{27}*S13 - k_{16}*S9*S9$
S10	HH	$dS10/dt = k_{19}*S3*S3 - (k_{20}+\mu)*S10 - k_{21}*S10*S4$
S11	LHH	$dS11/dt = k_{21}*S10*S4 - (k_{22}+\mu)*S11 - k_{23}*S11*S4$
S12	LHHL	$dS12/dt = k_{23}*S11*S4 + k_{16}*S9*S9 - (k_{17}+\mu)*S12 - k_{18}*S12 - k_{27}*S12$
S13	LHHL(Medium)	$dS13/dt = k_{18}*S12 - k_{27}*S13$

Nomenclature

Rate constants:

	type	description	unit
μ	rate constant	cell growth rate	h^{-1}
k1	rate	H.RNA transcription	mRNAs h^{-1}
k2	rate constant	H.RNA turnover	h^{-1}
k3	rate	L.RNA transcription	mRNAs h^{-1}
k4	rate constant	L.RNA turnover	h^{-1}
k5	rate constant	H translation	molecules mRNA $^{-1}$ h^{-1}
k6	rate constant	H turnover	h^{-1}
k7	rate constant	H + L \rightarrow HL	molecule $^{-1}$ h^{-1}
k8	rate constant	L translation	molecules mRNA $^{-1}$ h^{-1}
k9	rate constant	L turnover	h^{-1}
k10	rate constant	L + L \rightarrow LL	molecule $^{-1}$ h^{-1}
k11	rate constant	L export	h^{-1}
k12	rate constant	LL turnover	h^{-1}
k13	rate constant	LL export	h^{-1}
k14	rate constant	HL turnover	h^{-1}
k15	rate constant	HL export	h^{-1}
k16	rate constant	HL + HL \rightarrow LHHL	molecule $^{-1}$ h^{-1}
k17	rate constant	LHHL turnover	h^{-1}
k18	rate constant	LHHL export	h^{-1}
k19	rate constant	H + H \rightarrow HH	molecule $^{-1}$ h^{-1}
k20	rate constant	HH turnover	h^{-1}
k21	rate constant	HH + L \rightarrow LHH	molecule $^{-1}$ h^{-1}
k22	rate constant	LHH turnover	h^{-1}
k23	rate constant	LHH + L \rightarrow LHHL	molecule $^{-1}$ h^{-1}
k27	rate constant	LHHL \rightarrow HL+HL	h^{-1}
k28	rate constant	HL + HL \rightarrow LHHL	molecule $^{-1}$ h^{-1}

Species

S1	H.mRNA
S2	L.mRNA
S3	H
S4	L
S5	L(Medium)
S6	LL
S7	LL(Medium)
S8	HL
S9	HL(Medium)
S10	HH
S11	LHH
S12	LHHL
S13	LHHL(Medium)
S14	LH:HL
S15	LH:HL(Medium)