

Additional File 1

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Species

$y_1 = S. cerevisiae$ cells
 $y_2 = E. coli$ cells
 $y_3 = C4HSL$
 $y_4 = 3oxoC6HSL$
 $y_5 = preKanR1$
 $y_6 = KanR1$
 $y_7 = 3oxoC6HSL : LuxR$
 $y_8 = C4HSL : RhlR$
 $y_9 = KanR$

Stochastic Differential Equations capturing the reaction network dynamics

$$\begin{aligned}
dy_1 &= \left(k_1 y_1 \left(1 - \frac{y_1 + y_2}{c_{max}} \right) - \frac{k_3 \cdot Kan \cdot y_1}{1 + \alpha \cdot y_6} \right) dt + \sqrt{k_1 y_1} \frac{y_1 + y_2}{c_{max}} dw_1 - \sqrt{\frac{k_3 \cdot Kan \cdot y_1}{1 + \alpha \cdot y_6}} dw_3 \\
dy_2 &= \left(k_2 y_2 \left(1 - \frac{y_1 + y_2}{c_{max}} \right) - \frac{k_3 \cdot Kan \cdot y_2}{1 + \alpha \cdot y_9} \right) dt + \sqrt{k_2 y_2} \frac{y_1 + y_2}{c_{max}} dw_4 - \sqrt{\frac{k_3 \cdot Kan \cdot y_2}{1 + \alpha \cdot y_9}} dw_6 \\
dy_3 &= \left(k_4 y_1 - \frac{k_9 \cdot RhlR^2 \cdot y_3^2}{Na \cdot V_2} - k_{11} y_3 \right) dt + \sqrt{k_4 y_1} dw_7 - \sqrt{\frac{k_9 \cdot RhlR^2 \cdot y_3^2}{Na \cdot V_2}} dw_8 - \sqrt{k_{11} y_3} dw_9 \\
dy_4 &= \left(k_5 y_2 - \frac{k_6 \cdot LuxR^2 \cdot y_4^2}{Na \cdot V_1} - k_{12} y_4 \right) dt + \sqrt{k_5 y_2} dw_{10} - \sqrt{\frac{k_6 \cdot LuxR^2 \cdot y_4^2}{Na \cdot V_1}} dw_{11} - \sqrt{k_{12} y_4} dw_{12} \\
dy_5 &= \left(\frac{k_7 y_7^{n_1}}{k_{7b}^{n_1} + y_7^{n_1}} - k_8 y_5 \right) dt + \sqrt{\frac{k_7 y_7^{n_1}}{k_{7b}^{n_1} + y_7^{n_1}}} dw_{13} - \sqrt{k_8 y_5} dw_{14} \\
dy_6 &= \left(k_8 y_5 - k_{15} y_6 \right) dt + \sqrt{k_8 y_5} dw_{14} - \sqrt{k_{15} y_6} dw_{15} \\
dy_7 &= \left(\frac{k_6 \cdot LuxR^2 \cdot y_4^2}{Na \cdot V_1} - k_{14} y_7 \right) dt + \sqrt{\frac{k_6 \cdot LuxR^2 \cdot y_4^2}{Na \cdot V_1}} dw_{11} - \sqrt{k_{14} y_7} dw_{16}
\end{aligned}$$

$$dy_8 = \left(\frac{k_9 \cdot RhlR^2 \cdot y_3^2}{Na \cdot V_2} - k_{13}y_8 \right) dt + \sqrt{\frac{k_9 \cdot RhlR^2 \cdot y_3^2}{Na \cdot V_2}} dw_8 - \sqrt{k_{13}y_8} dw_{17}$$

$$dy_9 = \left(\frac{k_{10}y_8^{n_2}}{k_{10b}^{n_2} + y_8^{n_2}} - k_{16}y_9 \right) dt + \sqrt{\frac{k_{10}y_8^{n_2}}{k_{10b}^{n_2} + y_8^{n_2}}} dw_{18} - \sqrt{k_{16}y_9} dw_{19}$$

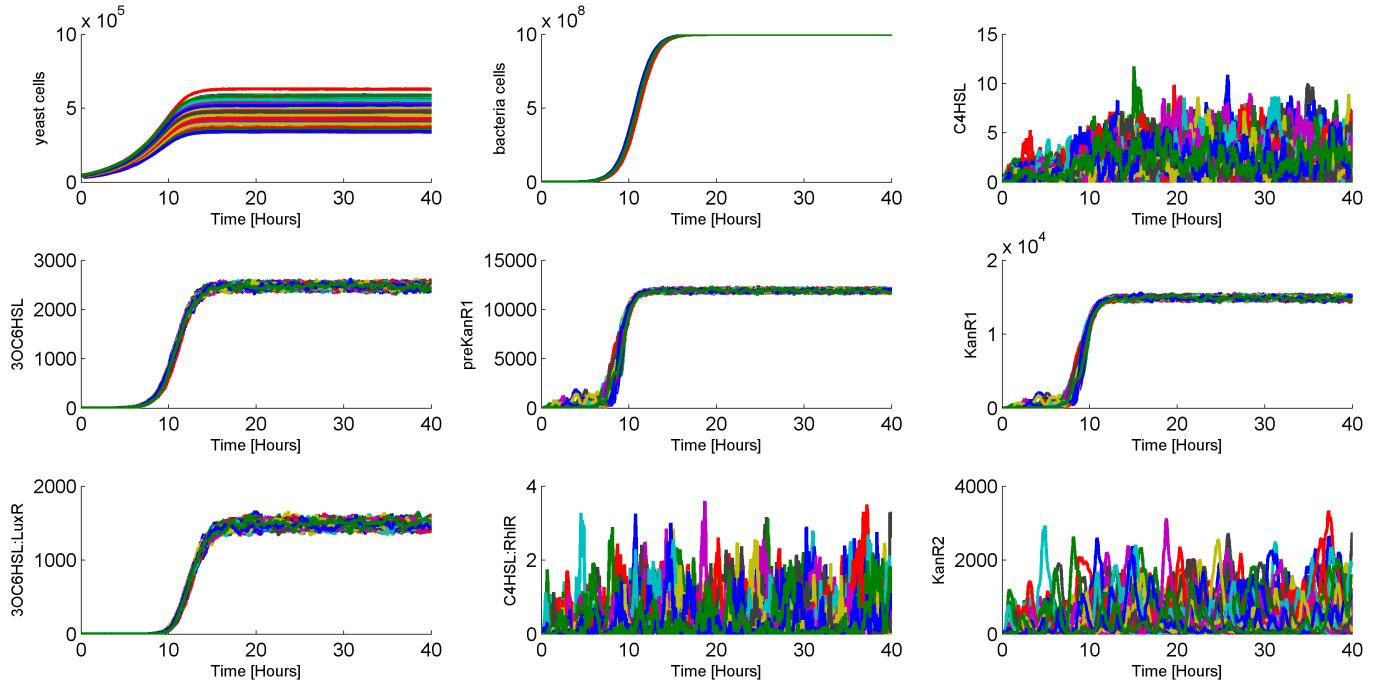


Figure 1: 100 trajectories of the evolution of all the species when yeast and bacteria coexist (In support of Figure 2).