

Smooth functions in Hurdle Poisson model

Consider the binomial and the the Poisson component of the Hurdle Poisson model which are both modeled with several predictors $x_{j,bc}$ and $y_{j,bc}$

$$\begin{aligned}\text{logit}(\pi_{bc}) &= \beta_{0,bc} + \sum_{j=1}^k f_j(x_{j,bc}) \\ \log(\lambda_{bc}) &= \gamma_{0,bc} + \sum_{j=1}^l g_j(y_{j,bc})\end{aligned}$$

In this model f_j and g_j are specified using cubic smoothing splines, which can be represented as a linear combination of a set of basis functions with m knots,

$$h(z) = \sum_{r=0}^3 \delta_{0r} z^r + \sum_{s=1}^m \delta_s (z - t_s)_+^3,$$

where t_s , $s = 1, \dots, m$ are the m knots (e.g. Thilakarathne et al., 2011). The different predictors used in the model are given in the main text.

Reference: Thilakarathne, P., Clement, L., Lin, D., Shkedy, Z., Kasim, A., Talloen, W., Versele, M., and Verbeke, G. (2011). The Use of Semi-parametric Mixed Models to Analyze PamChip Peptide Array Data: an Application to an Oncology Experiment. *Bioinformatics*, 27 (20), 2859-2865.