

Table S1. Parameters of 5 Models

Parameter	Run number					Parameter	Run number				
	1	2	6	7	4cs_7		1	2	6	7	4cs_7
RMS	2.27	2.33	2.40	5.29	1.48	A_{Bcd}^P	1.36	0.69	0.03	0.08	3.99
$S_{\text{M3}_2}^R \dagger$	1	1	1	1	1	A_{Cad}^P	0.02	0.01	0.05	0.03	0.05
$S_{\text{M32}}^R \dagger$	1	1	1	1	1	$A_{\text{D-STAT}}^P$	3.98	3.98	1.09	3.99	3.98
$S_{\text{M2}_3}^R \dagger$	1	1	1	1	1	A_{Dichaete}^P	3.85	0.41	3.89	0.18	0.09
$S_{\text{M23}}^R \dagger$	1	1	1	1	1	A_{Hb}^P	0.82	2.73	2.72	0.04	0.09
$S_{1.7\text{kb}}^R$	0.3	0.3	0.2	1.41	N/A	A_{Kr}^P	0.07	0.13	0.03	2.95	0.1
S_{MSE2}^R	0.2	0.2	0.2	0.2	N/A	A_{Kni}^P	2.58	3.99	2.23	0.27	2.8
S_{MSE3}^R	0.8	0.8	0.8	0.8	N/A	A_{Gt}^P	3.99	2.07	2.53	0.04	0.02
$R_{\text{max}} \dagger$	255	255	255	255	255	A_{Tll}^P	2.88	3.96	0.02	1.95	0.004
Θ	6.7	6.4	6.1	5.96	10.6	λ_{Bcd}	1.53	1.99	4.99	2.16	1.68
$E_{\text{B-H}}^C$	0.34	0.44	0.21	0.35	0.35	λ_{Cad}	4.98	4.98	4.97	3.18	4.99
$E_{\text{C-H}}^C$	0.66	0.99	0.33	0.88	0.88	$\lambda_{\text{D-STAT}}$	1.62	1.98	2.58	0.69	0.89
$K_{\text{B-B}}^{\text{coop}}$	52	982	189	127	86	$\lambda_{\text{Dichaete}}$	0.91	2.33	1.98	4.54	3.49
$D_{\text{B-H}}^C$	165	161	158	150	150	λ_{Hb}	1.93	1.5	1.83	4.99	4.25
$D_{\text{C-H}}^C$	57	58	70	22	28	λ_{Kr}	3.08	2.31	4.04	0.98	4.99
$D_{\text{B-B}}^{\text{coop}} \dagger$	60	20	60	60	60	λ_{Kni}	1.6	1.17	2.48	1.56	1.82
E_{Bcd}^A	0.5	0.5	0.06	0.0001	0.001	λ_{Gt}	1.25	1.47	1.71	4.99	4.63
E_{Cad}^A	0.0001	0.0001	0.0001	0.0001	0.39	λ_{Tll}	0.87	1.26	4.98	0.96	4.99
$E_{\text{D-STAT}}^A$	19.9	19.9	0.0001	19.9	16.6	$T_{\text{Bcd}} \dagger$	1.71	1.71	1.71	1.71	1.71
E_{Dichaete}^A	0.0001	0.0001	0.0001	0.45	0.004	T_{Cad}	2.53	2.22	3.06	2.06	3.0
E_{Hb}^A	14.4	13.5	20.41	29.9	19.1	$T_{\text{D-STAT}}$	2.21	2.19	2.83	3.63	2.83
E_{Hb}^Q	0.99	0.99	0.99	0.99	0.99	T_{Dichaete}	2.22	4.92	4.79	2.96	2.08
E_{Kr}^Q	0.99	0.99	0.9	0.99	0.51	$T_{\text{Hb}} \dagger$	0.63	0.63	0.63	0.63	0.63
E_{Kni}^Q	0.54	0.75	0.06	0.99	0.26	T_{Kr}	0.009	0.02	2.11	0.07	2.06
E_{Gt}^Q	0.75	0.43	0.72	0.74	0.99	T_{Kni}	2.2	2.48	2.23	4.85	2.46
E_{Tll}^Q	0.99	0.14	0.99	0.99	0.81	T_{Gt}	0.6	0.59	0.59	0.50	0.71
E_{Hb}^D	0.53	0.31	0.32	0.58	0.37	T_{Tll}	1.83	1.82	1.97	1.97	1.97
E_{Kr}^D	0.99	0.73	0.99	0.99	0.6						
E_{Kni}^D	0.24	0.14	0.12	0.99	0.05						
E_{Gt}^D	0.87	0.99	0.17	0.99	0.51						
E_{Tll}^D	0.0001	0.0001	0.0002	0.0001	0.98						
$D_{\text{all}}^Q \dagger$	100	100	100	100	100						
$D_{\text{all}}^D \dagger$	100	100	100	100	100						

These parameters are inferred from the observed expression patterns by fitting transcription models to quantitative data. Daggers indicate parameters held fixed during the training process. $S_{\text{construct}}^R$ is the positional effect scale factor for each reporter construct. R_{max} is the maximum rate of transcription. S_{ligand}^P is the scale factor for protein concentration. Other parameters are described in the main text.