Gene network requirements and limits for regulating metabolic gene expression to a desired state

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Supplementary Figure 1



Figure S1: Residuals of the gene network fit. Shown are the residuals, in μ M, for the four metabolic enzymes as function of intracellular galactose. The number on top of each graph represents the sum over all internal galactose concentration of all residuals for that enzyme. A gal2p; B gal1p; C gal7pd; D gal10dp.

Supplementary Table 1

| parameter | description | value | unit | # in Fig. 6 |
|---------------|---|--------------------------------|--|-------------|
| idg10d | intrinsic degradation constant of gal10pd | $1.851 \ge 10^{-1}$ | \min^{-1} | 37 |
| idg10 | intrinsic degradation constant of gal10p | $5.150 	ext{ x } 10^{-1}$ | \min^{-1} | 44 |
| idg1 | intrinsic degradation constant of gal1p | $2.650 \ge 10^{-1}$ | \min^{-1} | 42 |
| idg2 | intrinsic degradation constant of gal2p | $2.727 	ext{ x } 10^{-1}$ | \min^{-1} | 1 |
| idg3i | intrinsic degradation constant of gal3p [*] | 1.010 | \min^{-1} | 18 |
| idg3 | intrinsic degradation constant of gal3p | 1.065 | \min^{-1} | 8 |
| idg4dg80d | intrinsic degradation constant of gal4pd-gal80pd complex | 1.537 | \min^{-1} | 22 |
| idg4d | intrinsic degradation constant of gal4pd | 1.050 | \min^{-1} | 23 |
| idg4 | intrinsic degradation constant of gal4p | 1.167 | \min^{-1} | 19 |
| idg7d | intrinsic degradation constant of gal7pd | $2.952 \ge 10^{-1}$ | \min^{-1} | 38 |
| idg7 | intrinsic degradation constant of gal7p | 2.252 | \min^{-1} | 36 |
| idg80d | intrinsic degradation constant of gal80pd | 2.518 | \min^{-1} | 32 |
| idg80g3i | intrinsic degradation constant of $gal80p-gal3p^*$ complex | 1.331 | \min^{-1} | 47 |
| idg80 | intrinsic degradation constant of gal80p | 1.996 | \min^{-1} | 45 |
| idr10 | intrinsic degradation constant of GAL10 | 5.997 | \min^{-1} | 41 |
| idr1 | intrinsic degradation constant of GAL1 | 4.889 | \min^{-1} | 43 |
| idr2 | intrinsic degradation constant of $GAL2$ | 9.803×10^{-2} | \min^{-1} | 2 |
| idr3 | intrinsic degradation constant of $GAL3$ | $2.549 \ge 10^{1}$ | \min^{-1} | 5 |
| idr7 | intrinsic degradation constant of GAL7 | 5.984 | \min^{-1} | 40 |
| idr80 | intrinsic degradation constant of $GAL80$ | 8.584×10^{1} | \min^{-1} | 52 |
| kfvg3i | association rate constant of Gal_{in} -gal3p complex | $2.788 \ge 10^{-4}$ | $(m/c)^{-1} min^{-1}$ | 48 |
| kfvg10d | association rate constant of gal10p-gal10p dimer | $1.835 \ge 10^{-1}$ | $(m/c)^{-1} min^{-1}$ | 17 |
| kfvg4dg80d | association rate constant of Gal_{in} -gal3p complex | $1.505 \ge 10^2$ | $(m/c)^{-1} min^{-1}$ | 21 |
| kfvg4d | association rate constant of gal4p-gal4p dimer | $2.163 	ext{ x } 10^{1}$ | $(m/c)^{-1} min^{-1}$ | 31 |
| kfvg7d | association rate constant of gal7p-gal7p dimer | 4.729 | $(m/c)^{-1} min^{-1}$ | 20 |
| kfvg80d | association rate constant of gal80p-gal80p dimer | 9.641 | $(m/c)^{-1} min^{-1}$ | 10 |
| kfvg80g3i | association rate constant of gal80p-gal3p* complex | 9.353 | $(m/c)^{-1} min^{-1}$ | 49 |
| kipg2 | maximum initiation rate constant of gal2p | $8.698 \ge 10^2$ | $(m/c)^{-1} min^{-1}$ | 53 |
| kipg3 | maximum initiation rate constant of gal3p | $4.419 \ge 10^{3}$ | $(m/c)^{-1} min^{-1}$ | 50 |
| kipg4 | maximum initiation rate constant of gal4p | 1.508×10^{1} | $(m/c)^{-1} min^{-1}$ | 35 |
| kipg80 | maximum initiation rate constant of gal80p | $3.117 \ge 10^3$ | $(m/c)^{-1} min^{-1}$ | 4 |
| kipstructg10 | maximum initiation rate constant of gall0p | 1.216×10^4 | $(m/c)^{-1} min^{-1}$ | 16 |
| kipstructgl | maximum initiation rate constant of gallp | 1398 x 104 | $(m/c)^{-1}$ min ⁻¹ | 13 |
| kipstructg7 | maximum initiation rate constant of gal7p | $1.456 \ge 10^4$ | $(m/c)^{-1} min^{-1}$ | 11 |
| kir2 | maximum initiation rate constant of GAL2 | 3.666×10^{4} | $(m/c)^{-1} min^{-1}$ | 54 |
| kir3 | maximum initiation rate constant of GAL3 | 7.819×10^{2} | $(m/c)^{-1} min^{-1}$ | 51 |
| kir80 | maximum initiation rate constant of GAL80 | 2.392×10^2 | $(m/c)^{-1} min^{-1}$ | 3 |
| kirstructr10 | maximum initiation rate constant of GAL10 | 3.154×10^{-1} | $(m/c)^{-1} \min^{-1}$ | 15 |
| kirstructr1 | maximum initiation rate constant of GALI | 1.408×10^{-1} | $(m/c)^{-1}$ min ⁻¹ $(m/c)^{-1}$ min ⁻¹ | 14 |
| Kirstructri | maximum initiation rate constant of GAL/ | 1.928 x 10 ⁻ | (m/c) - min - | 12 |
| Kpr10 Vrr1 | equilibrium constant for binding of gal4pd to GAL1 | 2.373 X 10 | - | 20 |
| Kpr1 Vmr2 | equilibrium constant for binding of gal4pd to GAL1 | 0.020 4.954 10 ¹ | - | 20 |
| Kpr2 Kpr2 | equilibrium constant for binding of gal4pd to $GAL2$ | 4.234 x 10 5.062 | - | 30 22 |
| Kpr5 Kpr7 | equilibrium constant for binding of gal4pd to $GAL3$ | 1.034×10^{1} | - | 33 97 |
| Kpr80 | equilibrium constant for binding of gal4pd to CAL80 | 3.482×10^{1} | | 21 |
| Ka | equilibrium constant for binding of gal\$0nd to gal4nd-DNA | 1.555×10^{1} | | 0 |
| krya3i | dissociation rate constant of Gal: _gal3p complex() | 3.493×10^5 | min^{-1} | 7 |
| kryg10d | dissociation rate constant of σ_{all} all σ_{all} dimer | 1.564×10^5 | min^{-1} | 39 |
| krvg4dg80d | dissociation rate constant of Gal - cal complex | 6405×10^1 | min^{-1} | 29 |
| krvg4d | dissociation rate constant of gal4n-gal4n dimer | 1.681×10^2 | min^{-1} | 24 |
| kryg7d | dissociation rate constant of gal7p-gal7p dimer | 1.860×10^3 | min^{-1} | 34 |
| krvg80d | dissociation rate constant of gal80p-gal80p dimer | 5.982×10^4 | \min^{-1} | 46 |
| krvg80g3i | dissociation rate constant of gal80n-gal3n* complex | 1.489×10^2 | min^{-1} | 6 |
| | | | | - |

Table S1: Fitted parameter values of the gene network.

Supplementary Figure 2



Figure S2: The effect of perturbation of gene network parameters on metabolic steady state flux. (A) For every parameter in \mathbf{p}_{g}^{o} a reference flux profile for a galactose range of 0 and 50 mM was calculated. The squared distance of this reference flux profile and the flux profile with the perturbed value is plotted for all gene network parameters. (B) The five parameters that have the biggest effect on the galactose flux profile are shown. Left column corresponds to the highest effect when the indicated parameter was perturbed 5-fold down. Right column corresponds to the highest effect when the indicated parameter was perturbed 5-fold up. (C) Explanation of occurrence of multiple minima for some of the gene network parameters, using parameter idg10 as an example. For three values of parameter idg10 (indicated by the red circles), the corresponding galactose flux profiles (red) are shown together with the reference flux profile (blue) in the right columns. The squared flux difference that corresponds with the perturbed value is shown in the black box of every plot.