

2 **CAR model estimation and testing**

3 In order to estimate the parameters in the CAR model, we first set up a linear regression model corresponding
 4 to equation (1) including all covariates, with spatial dependence modeled through first and second order
 5 neighbors as described above. A product likelihood was found through successive conditioning of the full
 6 likelihood in the conditioning series, so that each trap catch was conditioned with all trap catches with
 7 higher index in the conditioning series. In the situation with missing first order neighbors, conditioning was
 8 performed on both first and relevant second order neighbors. The conditioning series impacted through first
 9 and second order neighbors with higher index, following the pattern in fig. 2 so that, using Besag's (1974)
 10 block design, only 1st order neighbors impact if none of these are missing, and 2nd order neighbors enters if
 11 any 1st order neighbors are missing. For example, if the 1st order neighbor in position 3 in Fig. 2 is missing,
 12 the 2nd order neighbors in positions 5, 6 and 7 will enter the list of neighbors on which conditioning is
 13 performed. If the 1st order neighbors at position 2 and 3 are both present, $\varphi(\rho)$ is a 1 x 2 matrix with values
 14 equal to $2\rho/(1 + \sqrt{1 + 8\rho^2})$ at both entries. This transforms the model (1), with spatial autocorrelation, into
 15 the linear regression model for independent variables (2) by essentially including the spatial autocorrelation
 16 as a regression parameter. Parameter estimation was performed in a two-step procedure, where estimates of
 17 β were calculated conditionally on ρ , subsequently maximizing the profile likelihood for rho. First we fixed
 18 a value $\rho_0 \geq 0$ for ρ . Then the effects of neighbor observations $\varphi(\rho_0)N$ in equation (2) was written as
 19 $\varphi(\rho_0)(\log(X_N) - Z_N^T \beta)$, were X_N is a vector containing the neighbor abundances, and Z_N is a matrix with
 20 each column containing the covariates for the corresponding neighbor. Now observe that:

$$\varphi(\rho)N = \varphi(\rho)(\log(X_N) - Z_N^T \beta) = \varphi(\rho) \log(X_N) - \beta^T Z_N \varphi(\rho)^T \quad (3)$$

21 To write the model (2) on a standard form with independent variables, (2) is re-written by splitting the
 22 term $\varphi(\rho)N$ as described in (3), subtracting $\varphi(\rho_0) \log(X_N)$ from (the log of) each observation and similarly
 23 subtracting $Z_N \varphi(\rho_0)^T$ from each set of covariates, thus transforming the model (2) back to a model of the
 24 same form as (1), but differing from an ordinary regression model in that variances for the observations are
 25 not identical, but differ as the neighbor configurations differ. Estimation of β for $\rho = \rho_0$ was then carried out
 26 by weighted linear regression with the variances acting as weights, thus taking within-neighbor correlation
 27 into account. In the event where successive conditioning yielded only approximate independence, because
 28 neither 1st nor 2nd order neighbors were observed in full in the configuration in fig. 2, full independence was

29 assumed for the estimation purpose. Taking the value of the likelihood function maximized for β this way
 30 as the value of the profile likelihood for rho at ρ_0 , the estimation procedure was completed by maximizing
 31 the profile likelihood to obtain simultaneous estimates for β and rho that yielded the maximum value of the
 32 likelihood function.

33 To test if there was significant temporal autocorrelation between the catch nights in the dataset, we
 34 expanded the developed model to include the trap catch from the previous catch night as a regression
 35 parameter, W in (3), with the coefficient θ :

$$\log(X) \sim \beta^T Z + \theta W + \varphi(\rho)N + \epsilon \quad (4)$$

36 Estimation was then performed as described above. The CAR models were reduced sequentially with
 37 the likelihood ratio test at a 5% significance level, and a forward selection procedure similar to the ordinary
 38 regression analysis was subsequently performed. To finally test if the spatial autocorrelation was significant,
 39 we set ρ to zero and tested if this model performed significantly worse than the developed CAR model
 40 (significance level = 5%). The same procedure was used to test if the temporal autocorrelation was significant,
 41 setting θ to zero.

42 Impact of spatial autocorrelation

43 To investigate the impact of spatial autocorrelation on two traps, A and B, placed with 50 m distance, we
 44 use this formula to find the adjusted expected level of abundance in trap B:

$$A_{B|A} = E_B * (E_A/O_A)^\rho \quad (5)$$

45 Where A_B is the adjusted expected catch size of trap B given trap A, E_B is the general expected catch
 46 level of trap B, E_A is the expected catch level of trap A and O_A is the observed catch in trap A. ρ is the
 47 spatial autocorrelation at 50 m distance.

48 References

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