# **Supporting Information**

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SI Text

#### **Field Data Collection**

Field data were collected from six sites in south Iceland (Table S1) affected by tephra fall from the eruptions of Eyjafjallajökull in April 2010 (Ey2010) and Grímsvötn in May 2011 (G2011). Transect sites T1 and T2 were located within the fallout area for Ey2010, where the initial tephra deposition was 40-50 mm at T1 and 30-40 mm at T2 (1). Maps of the G2011 fallout have not yet been published. Field sites T3-T6 were selected to have 30-50 mm of fine-grained G2011 tephra, and thus to be similar to those selected from Ey2010. The locations of transects, slope angles, and geomorphological details are shown in Table S1. All sites were located from 120-145 m above sea level in areas of contemporary outfield grazing. The modern vegetation consists of forb meadow, grassland, and moss banks (2, 3), it and ranges from complete coverage to none. All study sites lie within the presettlement Betula woodlands of Iceland (4), and the present open landscape with discontinuous vegetation cover and active soil erosion is a result of 1,200 y of human actions, climate change, and volcanic impacts (5, 6). Photographs show vegetation cover in June 2012 and the key geomorphological features (Fig. S1).

The modification of tephra exposed at the surface is swift and comprehensive because of its lack of cohesion and the wide range of commonly occurring meteorological conditions that can mobilize these sediments (7, 8). The recently deglaciated forelands of Eyjafjallajökull immediately to the south of the 2010 eruption received some of the greatest depths of fallout, yet observations undertaken as part of the research reported here show that within 2 y, these areas had been effectively stripped clean of exposed tephra. Once incorporated within the root mat and surface andisol stratigraphy, morphological change of the tephra layer is dramatically reduced; bioturbation is limited due to the depauperate nature of the Icelandic biota and the prevailing climate. Cryoturbation, where it exists, produces easily recognizable structures (9, 10).

#### Climate

The climate of Iceland has warmed since the early 1980s, although there is significant interannual variability (11). At Kirkjubæjarklaustur (~25 km southwest from T3–T6), the number of days per year with temperatures below 0 °C has declined over the past 20 y, from 118  $\pm$  13.1 (average  $\pm$  1 SD, 1992–2002) to 105  $\pm$  13.7 (average  $\pm$  1 SD, 2003–2011). This means that processes related to and intensified by cold temperatures, such as cryoturbation, are also likely to be in decline.

#### **Data Analysis**

Both the original thickness measurements and the residuals of detrended datasets were analyzed for the presence of early warning signals. Detrending was achieved using a Gaussian filter to remove

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long-term trends and high-frequency variation. A rolling, two-sided window of bandwidth n = 30 (480 mm of transect length) was used for the filter. This filter size is 5–17% of the dataset, depending on the length of the transect. These filter sizes are comparable to filters used by others (12), and it was confirmed by visual inspection that this methodology did not overfit the data and reduce the short-term variations we were interested in.

Three metric-based indicators of early warning signals were calculated. Increasing autocorrelation indicates rising memory in the system (13); in this study, it was the correlation coefficient of a first-order autoregressive model computed in the R package earlywarnings, version 1.0.2 (12). Increases in SD were used to evaluate increasing variability in the system (14). Change in skewness is an indicator of a system moving between two stability domains (15), and this indicator was calculated for T1 and T6. All metric indicators were calculated for a rolling window half the length of the dataset (Table S1). In addition, the moving average skewness of the last 30 data points was calculated for transect T1.

To determine the strength of observed trends, the nonparametric Kendall  $\tau$  rank correlation coefficient statistic was calculated for both the original and detrended datasets (twotailed at P = 0.05 significance).

#### **Sensitivity Analysis**

Trends in autocorrelation and SD within detrended datasets are sensitive to choices made in both the rolling window size and the filtering bandwidth (12, 13). To assess the sensitivity of our analysis, we calculated the Kendall  $\tau$  rank correlation coefficient statistic for trends in autocorrelation and SD for a range of rolling window and bandwidth sizes. Window sizes of 25–75% of the dataset length (increasing in increments of five) and filtering bandwidths of 2–50% (in increments of five) were evaluated. The sensitivity of SD and autocorrelation is presented in Fig. S2. Because all transects were collected with the same sampling interval, we followed best practice (12) and used a consistent bandwidth filter size across all transects.

#### Significance Testing

As well as testing for sensitivity, it is important to assess the probability that the observed indicator trends are due to chance (12). Probability assessment was done in this study using the *surrogates\_ews* function in the R package earlywarnings, version 1.0.2. This fits a linear autoregressive moving average model to the data and then generates 1,000 surrogate datasets of the same size as the original. Then, the Kendall  $\tau$  correlation coefficient is calculated for each surrogate dataset and compared with the Kendall  $\tau$  value for the real data. The frequency at which the simulated Kendall  $\tau$  value is equal to or larger than the original is *P*, the probability that the trend was due to chance (12).

The probability scores for both the original and detrended datasets are shown in Table S2.

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**Fig. S1.** Photographs of land surface transitions and recent tephra layers within the vegetation and map of source volcanoes for tephra and study sites. Inset in *A* shows the location of the transects (T1–T6) and volcanoes Eyjafjallajökull and Grímsvötn. (*A*) Location of T1 (shown by the tape measure) as it spans the edge of a deflation hollow. (*B*) Location of T2 (shown by the tape measure) with a revegetated rofabard slope in the background. (*C*) Rofabard erosion shows the exposed substrate, eroding andisol slope, and vegetated surface. T3 runs from the figures to top of the eroding slope. (*D*) Tephra from G2011 in T6 has experienced rapid stabilization within surface vegetation (photographed in June 2012). The tephra (uppermost gray-black layer) is clearly distinguished from the brown andisol. The form of the tephra layer mirrors the preexisting land surface.



**Fig. S2.** Sensitivity of trends in autocorrelation and SD as measured by the Kendall  $\tau$  rank correlation coefficient to choices in rolling window size and filtering bandwidth. The black triangle indicates the size of the rolling window and filtering bandwidth used in analysis. ar(1), autoregressive model of order 1.

### Table S1. Details of transects, including location, length, type of land surface transition, and rolling window size used

Transect	Land surface start	Land surface end	Longitude	Latitude	Altitude, m asl	Slope angle, °	N	Total transect length, m	Rolling window size
T1	Vegetated andisol (grasses/forbs/ moss)	Deflating and sol	W 19° 38′ 370″	N 63° 32′ 874′′	200	3	663	10.61	332
Т2	Vegetated andisol (grasses/forbs/ moss)	Exposed diamicton	W 19° 22′ 370′′	N 63° 30′ 466′′	150	2	239	3.82	120
Т3	Vegetated andisol (grasses/forbs/ moss)	Edge of eroding andisol (rofabard)	W 17° 39′ 546′′	N 63° 57′ 552′′	120	3	208	3.33	104
Τ4	Vegetated andisol (grasses/forbs/ moss)	Edge of eroding andisol (rofabard)	W 17° 39′ 781′′	N 63° 57′ 874′′	130	3	181	2.90	91
Τ5	Vegetated andisol (grasses/forbs/ moss)	Earth hummock (thufur)	W 17° 39′ 671′′	N 63° 57′ 737′′	130	7	359	5.74	180
Т6	Vegetated andisol (grasses/forbs/ moss)	Cryoturbation of surface clasts	W 17° 39′ 350′′	N 63° 57′ 628′′	145	8	232	3.71	116

asl, above sea level.

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# Table S2. Probability values that the observed Kendall $\boldsymbol{\tau}$ trend values were due to chance

	Original data			Residuals of detrended data			
Transect	SD	ar(1)	Skewness	SD	ar(1)	Skewness	
T1	0.138	0.001	0.111	0.153	0.001	0.114	
T2	0.014	0.01		0.013	0.018		
Т3	0.001	0.121		0.001	0.126		
T4	0.053	0.143		0.058	0.147		
T5	0.109	0.001		0.11	0.006		
T6	0.002	0.257	0.619	0.003	0.264	0.948	
Combined probability*	<1 <sup>-5</sup>	<1 <sup>-5</sup>		<1 <sup>-5</sup>	<1 <sup>-4</sup>		

Probability values were calculated by summing the frequency that the Kendall  $\tau$  trend values larger than the original Kendall  $\tau$  trend value were found in a set of 1,000 surrogate datasets.

\*Calculated using Fisher's combined probability method.