Modulating water-exchange rates of lanthanide(III)-containing polyaminopolycarboxylate-type complexes using polyethylene glycol

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General Experimental Procedures

Commercially available chemicals were of reagent-grade purity and were used without further purification unless otherwise noted. Water was purified using a PURELAB Ultra Mk2 (ELGA) water purification system. Flash chromatography was carried out with silica gel 60, 230−400 mesh (EMD chemicals).¹ Thin-layer chromatography was performed on ASTM TLC plates with a silica gel 60 F_{254} coating (250 µm layer thickness). Visualization of TLC was carried out with a UV lamp followed by staining with potassium permanganate $(2 \text{ g KMnO}_4, 20)$ g K_2CO_3 , 5 mL 5% w/v aqueous NaOH, and 300 mL H₂O). Spectra/Por Biotech cellulose ester dialysis membranes of 100−500 and 500−1000 Da molecular weight cut off (MWCO) were used for dialysis. Freeze drying was carried out using a LABCONCO FreeZone 2.5 freeze dryer. Resin reactions were performed in Poly-Prep chromatography columns on a Barnstead/Thermolyne LABQUAKE rotator. Centrifugation was carried out using a Fisher Scientific Centrific centrifuge 225. High-performance liquid chromatography (HPLC) was carried out on a Shimadzu HPLC system equipped with fluorescence ($\lambda_{ex} = 273$, $\lambda_{em} = 622$ and $\lambda_{\text{ex}} = 396$, $\lambda_{\text{em}} = 593$ nm, for Gd^{III} and Eu^{III} complexes, respectively), photodiode array (traces at 210 nm included in the SI), and refractive index detectors and a C4 column (RESTEK Ultra C4, $5.0 \text{ µm} \times 250 \text{ mm}$). Aqueous size-exclusion chromatography (SEC) was performed on the same HPLC system using three aquagel-OH columns in series (VARIAN PLaquagel-OH-mixed, 8 μm \times 300 mm). A binary gradient method (pump A: H₂O, pump B: CH₃CN; 95–5% B over 20 min; flow rate: 1 mL/min) was used with the C4 column, and an isocratic method (100% H_2O ; flow rate: 1 mL/min) was used with the aquagel-OH columns.

¹H NMR spectra were acquired using a Varian Unity 400 (400 MHz) or a Varian-500S (500 MHz) spectrometer, and ¹³C NMR spectra were acquired using a Varian Unity 400 (101)

MHz) or a Varian-500S (125 MHz) spectrometer. Chemical shifts (ppm) for ${}^{1}H$ NMR spectra are reported relative to residual CHCl₃ in CDCl₃ (7.27 ppm) or CH₃OH in CD₃OD (3.30 ppm). Multiplicities are reported as "s" = singlet, "m" = multiplet, and "brs" = broad singlet. The elements responsible for particular shifts are noted with italicized font. Chemical shifts for ${}^{13}C$ NMR spectra are reported relative to CDCl₃ (77.23 ppm) in CDCl₃ or CD₃CN (118.26 ppm) as an internal standard in D_2O . High-resolution electrospray ionization mass spectra (HRESIMS) were obtained on an electrospray time-of-flight high-resolution Waters Micromass LCT Premier XE mass spectrometer. Matrix-assisted laser desorption ionization (MALDI) mass spectrometry was performed on a Waters SYNAPT G2 mass spectrometer (Manchester, UK) equipped with a commercial MALDI source and a Nd:YAG laser (355 nm, 200 Hz) or a Bruker Ultraflex MALDI-TOF mass spectrometer. α -Cyano-4-hydroxycinnamic acid (5 mg in 50:50 CH₃CN/H₂O with 0.1% formic acid) was used as the matrix. Prior to plating, samples $\sim 1 \,\mu g/mL$ in water with 0.1% formic acid or ~1 mg/mL in water) and matrix were mixed in 1:1 or 1:100 v/v ratios. *N*- (*tert*-Butoxycarbonyl)-*N'*-aminoacetylchloride, **4**, was synthesized according to a published procedure.²

Inductively coupled plasma optical emission spectroscopy (ICP-OES) measurements were performed on a HORIBA Jobin Yvon *ULTIMA* spectrometer or by Columbia Analytical Services Inc., Tucson, Arizona, USA. Samples measured with the *ULTIMA* spectrometer were diluted with nitric acid (2% v/v, aqueous), and standards were prepared by serial dilution of Gd, Eu, and Y standards (High-Purity Standards).

Water proton relaxation rate data were obtained using a Bruker mq 60 NMR Analyzer (1.4 T) at 37 °C for Gd^{III} -containing conjugates **1a–d** in phosphate-buffered saline (pH 7.4). The relaxivities of Gd^{III}-containing conjugates were obtained from the slopes of the linear plots of

 $1/T_1$ versus Gd^{III} concentration. Measurements were repeated three times with independently prepared solutions for each Gd^{III} -containing conjugate. The Gd^{III} concentration was verified by ICP–OES.

Variable-temperature 17 O NMR measurements of Gd^{III}-containing conjugates **1a** (6 mM), **1b** (6 mM), **1c** (4 mM), and **1d** (17 mM) and their diamagnetic Y^{III} analogues (3a-d) in H₂O were carried out on a Varian-500S spectrometer. Enrichment in ${}^{17}O$ (1%) was achieved using ¹⁷O-enriched water (10% H_2 ¹⁷O, Cambridge Isotope Laboratories, Inc.). Line widths at half height were measured at 20 (or 25), 30, 40, 50, 60, and 70 °C. *A*/ \hbar and ∆*E* were fixed to –3.8 × 10^{-6} rad/s and 2.5×10^{-11} J/mol, respectively, for Gd^{III}-containing conjugates, **1a–d**. The watercoordination number, *q*, was set to the value obtained from luminescence-decay measurements for Eu^{III}-containing conjugates **2a–d**. The least-squares fits of the ¹⁷O NMR relaxation data were calculated using origin software $(8.0951 B951)$ following a previously published procedure³ to obtain the water-exchange rates of Gd^{III} -containing conjugates, $1a-d$. Gd^{III} and Y^{III} concentrations were verified by ICP–OES.

Luminescence-decay measurements of Eu^{III} -containing conjugates 2**a–d**, in H₂O and D₂O were acquired using a HORIBA Jobin Yvon Fluoromax-4 spectrofluorometer in decay by delay scan mode using the phosphorescence lifetime setting. Excitation and emission wavelengths of 393 and 596 nm were used, respectively, while the other parameters were kept constant: excitation and emission slit widths (5 nm), flash count (100), initial delay (0.01 ms), maximum delay (2 ms for solutions in H₂O and 8 ms for solutions in D₂O), and delay increment (0.01 ms). The number of coordinated water molecules, *q*, was determined using the method developed by Horrocks and coworkers. 4

Electron paramagnetic resonance (EPR) measurements of **1a–d** in water were performed on a Bruker EMX X-band spectrometer. From the EPR spectra, the electronic Landé *g* factors, g_L , peak-to-peak line widths, ΔH_{pp} , and transverse electronic relaxation rates, $1/T_{2e}$, were obtained according to a previously reported method.⁵

Synthetic Procedures

1,4,7-Tris(*tert***-butyloxycarbonylmethyl)-1,4,7,10-tetraazacyclododecane (5):** This procedure is based on a previous report with modifications as noted in the following text.⁶ To a mixture of cyclen $(1.00 \text{ g}, 5.80 \text{ mmol}, 1 \text{ equiv})$ and NaHCO₃ $(1.61 \text{ g}, 19.2 \text{ mmol}, 3.3 \text{ equiv})$ in anhydrous CH3CN (15 mL) at 0 °C under Ar was added a solution of *tert*-butyl bromoactetate (2.90 mL, 19.4 mmol, 3.3 equiv) in anhydrous CH3CN (20 mL) over a period of 18 h (instead of 30 min as described in the previous report). The reaction mixture was allowed to warm to ambient temperature during the addition of *tert*-butyl bromoactetate (instead of after the addition as previously reported). The reaction mixture was stirred under Ar for 48 h after the addition of

tert-butyl bromoactetate. The reaction mixture was filtered through celite, and the filtrate was reduced to dryness under reduced pressure to yield a pale yellow solid that was purified using silica gel column chromatography $(9:1 \text{ CHCl}_{3}/\text{CH}_{3}OH)$ (not described in the previous report). Fractions with R_f values (9:1 CHCl₃/CH₃OH) between 0.39 and 0.63 were combined, and the solvent was removed under reduced pressure. The resulting solid was recrystallized from hot toluene, dissolved in saturated NaHCO₃ (50 mL), extracted with CHCl₃ (3 \times 50 mL), and dried over anhydrous MgSO4. Solvent was removed under reduced pressure to obtain 1.46 g (49%) of **5** as an off-white solid. ¹H NMR (500 MHz, CDCl₃, δ): 1.34−1.52 (m, CH₃, 27H), 2.70−2.91 (m, C*H*₂C*H*₂, 12H), 3.00 (brs, C*H*₂C*H*₂, 4H), 3.30 (s, C*H*₂C=O, 2H), 3.35 (s, C*H*₂C=O, 4H); ¹³C NMR (125 MHz, CDCl3, δ): 28.20 (*C*H3), 28.24 (*C*H3), 47.8 (*C*H2*C*H2), 50.4 (*C*H2C=O), 51.3 (CH_2CH_2) , 51.7 (CH_2CH_2) , 58.1 $(CH_2C=O)$, 81.5 $(C(CH_3)_3)$, 81.6 $(C(CH_3)_3)$, 170.4, 171.1; $R_f =$ 0.47 (9:1 CH₃Cl/CH₃OH); HRESIMS (m/z) : $[M + H]^+$ calcd for C₂₆H₅₁N₄O₆, 515.3809; found 515.3817.

1,4,7-Tris(*tert***-butyloxycarbonylmethyl)-10-(***N***-(2-***tert***-butoxycarbonylaminoethyl)**

acetamide-1,4,7,10-tetraazacyclododecane (6): To a mixture of **5** (0.394 g, 0.765 mmol, 1 equiv), Cs_2CO_3 (0.584 g, 1.79 mmol, 2.3 equiv), and KI (0.278 g, 1.67 mmol, 2.2 equiv) in anhydrous CH₃CN (16 mL) was added a solution of 4 (0.219 g, 0.925 mmol, 1.2 equiv) in anhydrous $CH₃CN$ (16 mL) under Ar. The reaction mixture was heated at reflux under Ar for 28 h. The reaction mixture was cooled to ambient temperature and filtered through celite, and the solvent was removed under reduced pressure. The resulting residue was dissolved in CHCl₃ (40) mL) and washed sequentially with H₂O (40 mL) and saturated aqueous KCl (3×40 mL). The organic layer was dried over anhydrous K_2CO_3 and concentrated under reduced pressure to obtain 0.470 g (86%) of **6** as a light brown solid. ¹H NMR (400 MHz, CDCl₃, δ): 1.32–1.52 (m, CH₃, 36H), 2.51 (brs, CH₂CH₂, 4H), 2.68 (brs, CH₂CH₂, 4H), 2.89 (brs, CH₂C=O, 6H), 3.07 (s, C*H*2C*=*O, 2H), 3.16−3.58 (m, C*H*2C*H*2, 12H), 5.99 (brs, N*H*, 1H), 8.79 (brs, N*H*, 1H); 13C NMR $(101 \text{ MHz}, \text{CDCl}_3, \delta)$: 27.9 (CH_3), 28.0 (CH_3), 28.2 (CH_3), 28.6 (CH_3), 39.6 (CH_2CH_2), 41.1 (CH_2CH_2) , 51.7 (CH_2CH_2) , 52.3 $(CH_2C=O)$, 53.7 $(CH_2C=O)$, 55.1 (CH_2CH_2) , 56.2 (CH_2CH_2) , 57.1 (*C*H2*C*H2), 57.8 (*C*H2C=O), 79.1 (*C*(CH3)3), 80.9 (*C*(CH3)3), 81.0 (*C*(CH3)3), 81.9 $(C(CH_3)$ ³), 155.9, 156.5, 170.6, 171.8, 172.7; HRESIMS (m/z) : $[M + H]^+$ calcd for $C_{35}H_{67}N_6O_9$, 715.4970; found 715.4976.

1,4,7-Tris(carbonylmethyl)-10-(aminoethyl-*N'***)acetyl)-1,4,7,10-tetraazacyclododecane (7):** To *tert*-butylester **6** (0.248 g, 0.347 mmol) was added concentrated HCl (25 mL), and the resulting mixture was stirred at ambient temperature for 3 h. The reaction mixture was concentrated under reduced pressure, and the resulting residue was dissolved in H_2O and freeze dried to obtain 0.161 g (96%) of **7** as a yellow–brown solid. ¹H NMR (400 MHz, CD₃OD, δ at 55 °C): 3.02−3.24 (m, C*H*2C*H*2, 10H), 3.36−3.58 (m, C*H*2C*H*2, and C*H*2C=O, 12H), 3.70 (s, CH₂C=O, 2H), 3.94 (s, CH₂C=O, 4H); ¹³C NMR (125 MHz, D₂O, δ at 65 °C): 35.4 (CH₂CH₂), 38.3 (*C*H2*C*H2), 48.2 (*C*H2*C*H2), 48.3 (*C*H2*C*H2), 48.9 (*C*H2*C*H2), 49.0 (*C*H2*C*H2), 52.1 $(CH_2C=O)$, 52.3 $(CH_2C=O)$, 52.9 $(CH_2C=O)$, 169. 0, 169.3, 170.0; HRESIMS (m/z) : $[M + H]^+$ calcd for $C_{18}H_{35}N_6O_7$, 447.2567; found 447.2562.

General procedure for the synthesis of Ln^{III} **(8 and 9) and** Y^{III} **complexes (10):**

Ligand **7** (0.100 g, 0.207 mmol, 1 equiv) was dissolved in H_2O (20 mL) and the pH of the solution was adjusted to between 6 and 7 using 1 M NH4OH. To the resulting solution was added MCl₃·6H₂O (0.311 mmol, 1.5 equiv), and the pH of the solution was adjusted to between 6 and 7 using 1 M NH₄OH. The reaction mixture was heated at 90 \degree C for 24 h and then cooled to ambient temperature. The pH of the solution was increased to 11 by adding 1 M NH4OH followed by centrifugation, and the supernatant was filtered through a 0.2 µm hydrophilic syringe filter (Millipore, IC MILLEX-LG). The filtrate was dialyzed in a 500 Da molecular weight cut off (MWCO) dialysis membrane against H_2O (4 L). The dialysis reservoir was changed at 2–4, 6–8, and 10–14 h. After the last change, dialysis was continued for 7 h. Contents within the dialysis membrane were freeze dried to obtain 0.0948 g (74%) of **8**, 0.0851 g (67%) of **9**, or 0.0981 g (85%) of **10** as off-white solids.

Gd^{III} **complex** (8): HRESIMS (m/z) : $[M + H]^+$ calcd for GdC₁₈H₃₂N₆O₇, 599.1559; found 599.1579. SEC chromatogram is on page S24.

Eu^{III} complex (9): **HRESIMS** (m/z) : $[M + H]^+$ calcd for $EuC_{18}H_{32}N_6O_7$, 595.1531; found 595.1523. SEC chromatogram is on page S24.

Y^{III} complex (10): **HRESIMS** (m/z) : $[M + H]^+$ calcd for $YC_{18}H_{32}N_6O_7$, 533.1391; found 533.1396. SEC chromatogram is on page S24.

General procedure for the synthesis of Ln^{III} **(1a–c and 2a–c) and** Y^{III} **conjugates (3a–c):**

To a flask containing N-acetoxysuccinimide, **a**, or a succinimidyl ester derivative of PEG, **b** or **c**, (5 equiv), was added dropwise a mixture of Ln^{III} complex **8** or **9**, or Y^{III} complex **10**, (1 equiv), and diisopropylethylamine (5 equiv) in anhydrous $CH₃OH$ (5 mL). The resulting mixture was allowed to stir at ambient temperature under Ar for 24 h. The resulting reaction mixture was added to aminomethylated polystyrene HL (100–200 mesh) resin (5 equiv, pre-swollen in ethanol for 0.5–1 h), and the resulting mixture was allowed to rotate for 15 to 18 h. The liquid portion of the reaction mixture was separated from the resin via filtration, and the resin was washed with ethanol (3×7 mL). The washings were combined with the liquid portion of the reaction mixture, and the solvents were removed under reduced pressure to obtain an oil that was dissolved in H₂O (10 mL) and washed with hexanes (4×10 mL). The H₂O layer was dialyzed in

either a 500 (**1a**, **2a**, **3a**, **1b**, **2b**, and **3b**) or 1000 Da (**1c**, **2c**, and **3c**) MWCO dialysis membrane against H₂O (4 L). The dialysis reservoir was changed at $2-4$, $6-8$, and $10-14$ h. After the last change, dialysis was continued for 7 h. Contents within the dialysis membrane were freeze dried and the resulting solids were washed with CH₃CN (3×5 mL) to yield Ln^{III} conjugates **1a–c** and **2a–c** and YIII conjugates **3a–c** as white solids. The purity of conjugates **1a–c**, **2a–c**, and **3a–c** was verified by HPLC, and the chromatograms are on pages S25–S27.

Conjugate 1a: 18.6 mg (46%), HRESIMS (m/z) : $[M + H]^+$ calcd for GdC₂₀H₃₄N₆O₈, 641.1664; found 641.1640.

Conjugate 1b: 29.1 mg (43%), HRESIMS (m/z) : $[M + H]$ ⁺ calcd for GdC₂₈H₅₀N₆O₁₂, 817.2713; found 817.2708.

Conjugate 1c: 18.8 mg (51%), MALDI-MS: median peak $[M + H]$ ⁺ calcd for $GdC_{57}H_{107}N_7O_{26}$ 1463.65; found 1463.19

Conjugate 2a: 18.9 mg (47%), HRESIMS (m/z) : $[M + H]^+$ calcd for EuC₂₀H₃₄N₆O₈, 637.1637; found 637.1634.

Conjugate 2b: 22.5 mg (34%), HRESIMS (m/z) : $[M + H]^+$ calcd for EuC₂₈H₅₀N₆O₁₂, 813.2685; found 813.2682.

Conjugate 2c: 12.87 mg (49%), MALDI-MS: median peak $[M + H]$ ⁺ calcd for EuC₅₇H₁₀₇N₇O₂₆, 1458.65; found 1458.19

Conjugate 3a: 16.0 mg (48%), HRESIMS (m/z) : $[M + H]$ ⁺ calcd for YC₂₀H₃₄N₆O₈, 575.1497; found 575.1498.

Conjugate 3b: 27.2 mg (39%), HRESIMS (m/z) : $[M + H]^{+}$ calcd for $YC_{28}H_{50}N_{6}O_{12}$, 751.2545; found 751.2543.

Conjugate 3c: 16.1 mg (49%), MALDI-MS: median peak $[M + H]$ ⁺ calcd for $YC_{57}H_{107}N_7O_{26}$ 1394.63; found 1394.19

General procedure for the synthesis of Ln^{III} - (1d and 2d) and Y^{III} -PEG conjugates (3d):

To a flask containing succinimidylester derivative of PEG **d** (1 equiv), was added dropwise a mixture of Ln^{III} complex **8** or **9**, or Y^{III} complex **10**, (3 equiv), and diisopropylethylamine (3 equiv) in anhydrous $CH₃OH$ (5 mL). The resulting mixture was allowed to stir at ambient temperature under Ar for 24 h. The resulting reaction mixture was concentrated under reduced pressure to obtain a white solid that was dissolved in $H₂O$ (10 mL) and washed with hexanes (4 \times 10 mL). The H₂O layer was dialyzed in a 1000 Da MWCO dialysis membranes against H₂O (4) L). The dialysis reservoir was changed at 2–4, 6–8, and 10–14 h. After the last change, dialysis was continued for 7 h. Contents within the dialysis membrane were freeze dried and the resulting solids were washed with CH₃CN (3 \times 5 mL) to yield Ln^{III} conjugates 1d and 2d, and Y^{III} conjugate **3d**, as white solids. The purity of **1d**, **2d**, and **3d** was verified by aqueous SEC, and the chromatograms are on page S28.

Conjugate 1d: 42.6 mg (45%), MALDI-MS: median peak $[M + H]$ ⁺ calcd for GdC₂₂₈H₄₄₈N₆O₁₁₂, 5222.87; found 5222.03

Conjugate 2d: 44.6 mg (48%), MALDI- MS: median peak $[M + H]$ ⁺ calcd for EuC228H448N6O112, 5217. 87; found 5217.01

Conjugate 3d: 41.9 mg (44%), MALDI-MS: median peak $[M + Na]$ ⁺ calcd for YC₂₂₈H₄₄₇N₆O₁₁₂Na, 5175.84; found 5175.88

Water-Proton Relaxation Rate Data

1a

Trial 1		
Concn (mM)	$1/T_1$ (s ⁻¹)	$T_1(s)$
5.70	15.8	0.0633
2.85	7.84	0.128
1.43	4.44	0.225
0.713	2.64	0.379
0.000	0.259	3.87

Trial 2

Trial 3

1b Trial 1

Trial 3

1c Trial 1

Trial 2

Trial 3

1d Trial 1

Concn (mM) $1/T_1$ (s⁻¹) $T_1(s)$ 0.387 2.61 0.383 0.194 1.41 0.712 0.097 0.842 1.19 0.048 0.547 1.83 0.000 0.260 3.85

Trial 2

Trial 3

Variable-Temperature 17O NMR Data

1a

<u> | Residual vs. Indep </u>

Electron Paramagnetic Resonance Spectra

Estimation of Rotational Correlation Time (^τ*R***)**

To obtain an estimation of τ_R , we started with equation 1 that relates observed relaxivity, r_1^{obs} , to inner- and outer-sphere relaxivities, r_1^{IS} and r_1^{OS} , respectively, at 1.4 T (60 MHz).⁷

$$
r_1^{obs} = r_1^{IS} + r_1^{OS}
$$
 equation 1

Assuming that complexes $1a-d$ behave similarly to small molecular contrast agents, r_1^{obs} is composed of approximately equal contributions from r_1^{IS} and r_1^{OS} .⁷ Therefore, r_1^{IS} can be expressed as half of r_1^{obs} as shown in equation 2.

$$
0.5r_1^{obs} = r_1^{IS} \t\t\t\text{equation 2}
$$

 r_1 ^{IS} is related to the number of coordinated water molecules (*q*), longitudinal relaxation time of the coordinated water proton (T_{1m}) , and residence lifetime of the coordinated water molecule in the inner-sphere (τ_m , reciprocal of water-exchange rate, k_{ex}) as expressed in equation 3.⁷

$$
r_1^{IS} = \frac{q}{55,500} \left[\frac{1}{T_{1m} + \tau_m} \right] \qquad \text{equation 3}
$$

Equations 2 and 3 can be combined to obtain equation 4, which enables the calculation of T_{1m} by substituting r_1^{obs} , τ_m , and *q* with values obtained experimentally for complexes **1a–d** (r_1^{obs} and ^τ*m*) and **2a–d** (*q*).

$$
T_{1m} = \frac{q}{27,750r_1^{obs}} - \tau_m \qquad \text{equation 4}
$$

 T_{1m} is composed of a dipole–dipole contribution (*DD*) and a scalar (*SC*) contribution to longitudinal proton relaxation as shown in equation 5.⁷

$$
\frac{1}{T_{1m}} = \frac{1}{T_1^{DD}} + \frac{1}{T_1^{SC}}
$$
 equation 5

The scalar contribution to overall longitudinal proton relaxation is negligible at field strengths greater than 10 MHz.⁷ Therefore, at field strengths above 10 MHz, the longitudinal proton relaxation becomes equal to the *DD* contribution that can be expressed as shown in equation 6.⁷

$$
\frac{1}{T_{1m}} = \frac{1}{T_1^{DD}} = \frac{2}{15} \left(\frac{\gamma_I^2 g^2 \mu_B^2}{r_{GdH}^6} \right) S(S+1) \left(\frac{\mu_0}{4\pi} \right)^2 \left(7 \frac{\tau_{C2}}{1 + \omega_S^2 \tau_{C2}^2} + 3 \frac{\tau_{C1}}{1 + \omega_I^2 \tau_{C1}^2} \right) \qquad \text{equation 6}
$$

 γ _{*I*}, nuclear gyromagnetic ratio = 2.67 \times 10⁸ s⁻¹ T⁻¹

g, electron g-factor obtained for complexes **1a–d** from EPR spectra

$$
\mu
$$
, Bohr magneton = 9.274 × 10⁻²⁴ J T⁻¹

 μ_0 vacuum permeability = $4\pi \times 10^{-7}$ T mA⁻¹

 r_{GdH} , electron spin-proton distance = 3.1 × 10⁻¹⁰ m (from reference 7 for DOTA-based Gd^{III}containing complexes)

S, electron spin for $Gd = 3.5$

$$
\omega_{S} = \gamma_{S} B
$$

$$
\omega_{I} = \gamma_{I} B
$$

*γ*_{*S*}, electron gyromagnetic ratio = 1.76×10^{11} s⁻¹ T⁻¹

 ω_s and ω_l are the electron and nuclear Larmor frequencies, respectively, at magnetic field strength $B(1.4 \text{ T})$.

 T_{1e} and T_{2e} are the longitudinal and transverse electronic relaxation times, respectively. T_{1e} (obtained from the fitting of ^{17}O NMR data) and T_{2e} (obtained from EPR spectra) for complexes **1a–d** were used in equations 7 and 8 that were combined with equation 6 to solve for τ_R for complexes **1a–d**.

Complex	T_{1m} × 10 ⁻⁶ (s)	$\tau_R \times 10^{-12}$ (s)
1a	13	46
1 _b	2.9	79
1c	5.3	110
1 _d	7.4	220

Estimation of Relaxivity, *r***¹** *obs***, Based on** ^τ*^R*

Estimated relaxivity values for complex **1a** were obtained using τ_R values from complexes **1a–d**, and τ_m and *q* values from complex **1a**: $\tau_m = 3.7 \times 10^{-7}$ s and $q = 0.9$. τ_{C_1} and τ_{C_2} were calculated by substituting τ_m , T_{1e} , and T_{2e} obtained for **1a** and τ_R from **1a–d** into equations 7 and 8 (page S20). The calculated τ_{C_1} and τ_{C_2} values together with other constants were used to calculate values for T_{1m} using equation 6 (page S20), and the calculated T_{1m} values and fixed τ_m and *q* values (from **1a**) were substituted in equation 3 (page S19) to obtain r_1^{IS} values that were used in equation 2 (page S19) to obtain the estimated relaxivity values for **1a** based on changes in ^τ*^R* associated with complexes **1a–d**.

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High Performance Liquid Chromatograms

SEC Chromatograms for Complexes 8–10

HPLC Chromatograms for complexes 1a –c, 2a –c, and 3a – c

1d

S34