Fig. S1: Electron microscope images of  $A\beta_{1-40}$  fibrils prepared as described in "Methods" section. a) the batch used to prepare frozen solution A $\beta$ -VF fibrils; b) batch used to prepare frozen solution A $\beta$ -VF fibrils.

Fig. S2: DNP build-up curves measured using proton signals and <sup>13</sup>C-CP signals, monoexponential fitting curves are shown in red. a) A $\beta$ -VF fibrils in frozen solution, b) A $\beta$ -VF peptide in frozen solution, c)A $\beta$ -VG fibrils in frozen solution, d) transverse relaxation curves for samples in frozen solution.

Fig. S3: Schematic representation of relative orientation of CSA tensors in the molecular frame and with respect to each other.

Fig. S4: Series of simulated 2D patterns for a wide range of various  $(\phi, \psi)$  angles. Spectral broadening is set to match the one found in room temperature measurements, exchange time 2.5 s

Fig. S5:  $\tau_{exchange}$  plots for the best fits to individual 2D exchange spectra of A $\beta$ -VF fibrils with various  $\tau_{exchange}$ . (data are shown in Fig. 6), a)  $\tau_{exchange}$ .=0.1 s, b)  $\tau_{exchange}$ .=0.5 s, c)  $\tau_{exchange}$ .=1.0 s, d)  $\tau_{exchange}$ .=2.5 s, e)  $\tau_{exchange}$ .=10 s.

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Fig. S6: RMSD plot for simulated data. The RMSD calculated is as  $RMSD(\phi,\psi) = \sum_{i} (\lambda S_i(\phi,\psi) - \lambda S_i(\phi_0,\psi_0))^{\alpha}$ , where a spectrum  $S_i$  simulated for specific  $(\phi_1 \phi_1 \psi_1 \phi)$  angles is compared to all other simulations, the optimal scaling factor l is calculated  $\Sigma_{f}^{N}S_{f}(\phi_{0},\psi_{0})S_{f}$  $\Sigma S_t(\phi_0, \psi_0) S_t$ a)  $(\phi_1 0, \psi_1 0) = (-50^\circ, -60^\circ)$ ; b)  $(\phi_1 0, \psi_1 0) = (-120^\circ, 120^\circ)$ ; c) as  $(\phi_1 0, \psi_1 0) = (-150^\circ, 150^\circ); d) (\phi_1 0, \psi_1 0) = (-75^\circ, -150^\circ)$