

Item S1. State transition probability formulas.

A. One-year probability of death among people of age x without CKD ($Q_{\text{noCKD},x}$):

$$Q_{\text{noCKD},x} = M_x / [1 + P_{\text{CKD},x} * (HR_{\text{CKD},x} - 1)]$$

Source:

Variable	Definition	Source
M_x	One-year probability of death among the entire population of age x	Vital statistics
$P_{\text{CKD},x}$	Prevalence of CKD at age x	NHANES
$HR_{\text{CKD},x}$	Sex- and race-adjusted hazard ratio for mortality associated with CKD for persons of age x (compared with eGFR 90-104, ACR<10)	CKD-PC

Nomenclature:

- $d_{\text{population},x}$: number of deaths in population (total, CKD, or no CKD) of age x to age x+1
 $Q_{\text{population},x}$: one-year probability of death in population (total, CKD, or no CKD) of age x
 $N_{\text{population},x}$: number alive in population (total, CKD, or no CKD) of age x to age x+1

Algebra:

1. Define $d_{\text{total},x} = d_{\text{CKD},x} + d_{\text{noCKD},x}$
 - a. $d_{\text{total},x} = Q_{\text{total},x} * N_{\text{total},x}$
 - b. $d_{\text{CKD},x} = Q_{\text{CKD},x} * N_{\text{CKD},x}$
 - c. $d_{\text{noCKD},x} = Q_{\text{noCKD},x} * N_{\text{noCKD},x}$
2. Substituting 1a-1c, $Q_{\text{total},x} * N_{\text{total},x} = Q_{\text{CKD},x} * N_{\text{CKD},x} + Q_{\text{noCKD},x} * N_{\text{noCKD},x}$
 - a. $N_{\text{CKD},x} = P_{\text{CKD},x} * N_{\text{total},x}$
 - b. $N_{\text{noCKD},x} = P_{\text{noCKD},x} * N_{\text{total},x}$
 - c. $P_{\text{CKD},x} = 1 - P_{\text{noCKD},x}$
 - d. $Q_{\text{CKD},x} = Q_{\text{noCKD},x} * HR_{\text{CKD},x}$
3. Substituting 2a-2d, $Q_{\text{total},x} * N_{\text{total},x} = Q_{\text{noCKD},x} * HR_{\text{CKD},x} * P_{\text{CKD},x} * N_{\text{total},x} + Q_{\text{noCKD},x} * P_{\text{noCKD},x} * N_{\text{total},x}$
4. Solving for $Q_{\text{noCKD},x} = Q_{\text{total},x} / (HR_{\text{CKD},x} * P_{\text{CKD},x} + P_{\text{noCKD},x})$
 - a. $P_{\text{noCKD},x} = 1 - P_{\text{CKD},x}$
 - b. $Q_{\text{total},x} = M_x$
5. Substituting 4a-4b, $Q_{\text{noCKD},x} = M_x / [1 + P_{\text{CKD},x} * (HR_{\text{CKD},x} - 1)]$

*Intuition: if $HR_{\text{CKD},x} = 1$, then $Q_{\text{noCKD},x} = M_x$

**Assumption: HR is modeled appropriately by age, sex, and race (see eTable2)

***Equation is presented as a single CKD category with a single HR_{CKD} . For models with more than one category of CKD, the equations would reflect the prevalence-weighted HRs associated with CKD. For example, for a two CKD category model, #4 is calculated as:

$$Q_{\text{noCKD},x} = Q_{\text{total},x} / (HR_{\text{CKD}1,x} * P_{\text{CKD}1,x} + HR_{\text{CKD}2,x} * P_{\text{CKD}2,x} + P_{\text{noCKD},x})$$

B. One-year probability of developing CKD among people of age x without CKD ($I_{CKD,x}$):

$$I_{CKD,x} = (P_{CKD,x+1} - P_{CKD,x}) / (1 - P_{CKD,x}) + M_x * [(P_{noCKD,x+1} / P_{noCKD,x}) - (Q_{noCKD,x} / M_x)]$$

Source:

Variable	Definition	Source
M_x	One-year probability of death among the entire population of age x	Vital statistics
$Q_{noCKD,x}$	One-year probability of death among those without CKD at age x	Previous step
$P_{CKD,x}$	Prevalence of CKD at age x	NHANES

Nomenclature:

$Q_{population,x}$: one-year probability of death in population (total, CKD, or no CKD) of age x
 $N_{population,x}$: number alive in population (total, CKD, or no CKD) of age x to age x+1

Algebra:

1. Define $N_{noCKD,x+1} = N_{noCKD,x} - (N_{noCKD,x} * Q_{noCKD,x}) - (N_{noCKD,x} * I_{CKD,x})$
 - a. i.e., the number alive without CKD at age x+1 is the number alive without CKD at age x, less the number who died during the year, less the number who developed CKD during the year
2. Solve for $I_{CKD,x} = (N_{noCKD,x} - (N_{noCKD,x} * Q_{noCKD,x}) - N_{noCKD,x+1}) / N_{noCKD,x}$
3. Simplifying, $I_{CKD,x} = 1 - Q_{noCKD,x} - (N_{noCKD,x+1} / N_{noCKD,x})$
 - a. $N_{noCKD,x} = N_{total,x} * P_{noCKD,x}$
 - b. $N_{noCKD,x+1} = N_{total,x+1} * P_{noCKD,x+1}$
4. Substituting 3a-3b, $I_{CKD,x} = 1 - Q_{noCKD,x} - (N_{total,x+1} * P_{noCKD,x+1} / N_{total,x} * P_{noCKD,x})$
 - a. $N_{total,x+1} = N_{total,x} - N_{total,x} * Q_{total,x}$
5. Substituting 4a, $I_{CKD,x} = 1 - Q_{noCKD,x} - [(N_{total,x} - N_{total,x} * Q_{total,x}) * P_{noCKD,x+1}] / (N_{total,x} * P_{noCKD,x})$
6. Simplifying, $I_{CKD,x} = 1 - Q_{noCKD,x} - [(1 - Q_{total,x}) * (P_{noCKD,x+1} / P_{noCKD,x})]$
7. Rearranging, $I_{CKD,x} = 1 - (P_{noCKD,x+1} / P_{noCKD,x}) + (Q_{total,x} * P_{noCKD,x+1} / P_{noCKD,x}) - Q_{noCKD,x}$
 - a. $P_{noCKD,x} = 1 - P_{CKD,x}$
 - b. $P_{noCKD,x+1} = 1 - P_{CKD,x+1}$
 - c. $Q_{total,x} = M_x$
8. Substituting 7a-7c,

$$I_{CKD,x} = (P_{CKD,x+1} - P_{CKD,x}) / (1 - P_{CKD,x}) + M_x * [(P_{noCKD,x+1} / P_{noCKD,x}) - (Q_{noCKD,x} / M_x)]$$

*Intuition: as M_x approaches 0, then $I_{CKD,x} = (P_{CKD,x+1} - P_{CKD,x}) / (P_{noCKD,x})$

**Assumption: Population steady state (since N_{x+1} is derived from N_x in previous year)