# Predicting and characterizing selective multiple drug treatments for metabolic diseases and cancer: SUPPORTING INFORMATION

Giuseppe Facchetti, Mattia Zampieri, Claudio Altafini

### A brief literature survey

In this Section we present a quick overview of the literature and of the main computational methods which investigate drug synergism (or synergism induced by similar network perturbations, like gene knockout). We list them from the most similar to the most different with respect to our algorithm, underlying the main discrepancies.

Optknock and OptOrf [1, 4]: the two works aim to find the best knockout (simple or multiple, up to a limit in cardinality fixed by the user) that maximizes the biosynthesis of a given metabolite while optimizing the biomass production. Both methods are based on FBA (OptOrf includes also some transcriptional regulations). The bilevel optimization contained in both algorithms has been reformulated through the duality theory, which assures the computational efficiency of the method. Indeed, we have been inspired by these works in developing of our algorithm.

Essentiality and synthetic lethality [7]: Through an algorithm which is similar to Optknock, this work identifies pairs, triple and some high-order gene deletions which are lethal in the Escherichia coli metabolism. Also in this method, the optimization is based on the biomass and does not consider any alternative objective reaction.

**OPMET**  $[6]$ : the aim is to search the gene knockout (of any cardinality) which stops a given objective reaction while inducing the minimum damage on the network (estimated as number of stopped reactions and unavailable metabolites). The approach used to model the network is similar to FBA but with a weaker assumption on the steady state: for instance, accumulation of metabolites is allowed. The search on the space of the combinations is performed dynamically through a branch-and-bound algorithm, refined with two filtering strategies. Properties of Linear Programming, like duality theory, which are useful for the efficiency of the algorithm have not been exploited.

Epistasis in human metabolism [3]: the investigation of gene epistasis has been here investigated through FBA formalism; no limitation on the cardinality of the gene deletions is imposed. However, since the search is based on an approximate determination of the elementary modes (called "pathway fragment generation"), solutions are suboptimal. An exact calculation of the elementary modes would have been computationally much more expensive and almost prohibitive for a large network such as the human. Moreover, no information on the side effect on the whole network is included.

Epistasis in yeast metabolism [5]: epistatic interactions are here studied performing an exhaustive search of all pairs of gene knockouts on the S.cerevisiae network modeled according to FBA; the effect is characterized through an epistasis indicator which quantifies the change of the biomass production of the multiple perturbation with respect to the two single perturbations. No objective reaction other than growth rate has been considered.

Drug targets in cancer [2]: also in this case only an exhaustive evaluation of all pairs of knockouts has been carried out; moreover, the side effect of the potential antitumoral treatments on the normal human cell is estimated in terms of ATP production, a central process in the metabolism. However, according to this evaluation criterion, all the antitumoral solutions we have found show the same impact on the human network, meaning that this definition of side effect is not able to discriminate among these different drug treatments, while our definition does. Indeed, instead of considering a single reaction, our approach estimates the impact as a global loss of the cellular functions, which in our opinion is fairly reasonable since no tissue-specific network of the human metabolism is available at the moment.

#### Algorithm for competitive organisms

The following version of the algorithm allows us to study the selectivity problem, in a multi-organism context, in which we would like to stop an objective reaction belonging to a first organism while having a minimal effect on a second metabolic network (whose fluxes are denoted here by  $\bf{w}$ ). We assume that the two organisms live in the same environment and hence are subject to the same drugs.

Minimize 
$$
\sum_{i=1}^{\tilde{N}_r} \alpha_i (1 - y_i) - b \sum_{k=1}^{N_d} d_k
$$
 "outer problem"  
such that  

$$
\begin{bmatrix}\n\text{Maximize} & v_{obj} & \text{``inner problem''} \\
\text{such that} & & \\
& \sum_{j=1}^{N_r} S_{i,j} v_j = 0; \\
v_j \leq U_j; \\
v_j \leq U_j d_k; \\
\sum_{h=1}^{\tilde{N}_r} \tilde{S}_{i,h} w_h = 0; \\
w_h \leq \tilde{U}_h; \\
w_h \leq \tilde{U}_h d_k; \\
v_{obj} = 0; \\
\varepsilon y_h \leq w_h; \\
\tilde{U}_h y_h \geq w_h.
$$

As can be seen, flux constraints ( $\tilde{\mathbf{S}}\mathbf{w} = \mathbf{0}$ , thermodynamical bounds  $w_h \leq \tilde{U}_h$  and common drugs inequalities  $w_h \leq \tilde{U}_h d_k$ ) and side effect on the second network (calculated as  $\sigma(D) = \min_{\mathbf{w}} ||\mathbf{w} - \mathbf{w}^*||$ ) are located only in the outer problem; therefore the fact that the side effect is now evaluated on w instead of on **v** does not interfer with the inner problem, i.e., with the application of the duality theorem for the first network. This separation guarantees the constraint  $\max(v_{obj}) = 0$  and the optimality of the solution.

## References

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## Figures and Tables



Table S1: List of drugs selected from DrugBank database for human and cancer metabolic networks. Selection criteria are explained in the main text. Legend: "M": number of metabolic targets; "NM": number of non-metabolic targets; "R": number of inhibited reactions of the human metabolic network; "S.E.": side effect;"X": the drug acts also on the cancer network; (\*): Simvastatin and Atorvastatin are also present in this group (they induce the same metabolic inhibitions as Pravastatin but they have one and two non-metabolic targets respectively).



Table S2: List of the inhibitions on human metabolism obtained by multiple drug solutions. The reactions are sorted according to the pathway they belong. The solutions are classified as New inhibition, More selective and Less selective from a comparison with a possible single drug treatment; this information is reported in the third column. Last columns reports the class of the synergistic combination which cause the inhibition of the objective reaction (see Figure 2 on the paper).



Figure S1: Side effects comparison. The histogram analysis of the size effect induced by single and multiple drug solutions shows that both types of solution have more or less the same order of magnitude.



Figure S2: Results on cancer metabolic network alone. Like for the human network (see Figure 3), the plot reports the new inhibitions that synergisms make possible and the inhibitions with different selectivity with respect to a single drug treatment. Notice how the number of new inhibitions is significantly higher than in the human metabolism, meaning that the cancer pathways are less robust (and redundant) than their counterparts in the human network.