

**Table S1:** Local parameter sensitivity analysis.

Parameter	Sensitivity coefficient <sup>1</sup>	Comment
$k_{s,b}$	1.02	$\beta$ -catenin synthesis rate constant
$AXIN_{tot}$	$-9.74 \times 10^{-01}$	Axin concentration
$k_{p,b}$	$-9.22 \times 10^{-01}$	$\beta$ -catenin phosphorylation rate constant
$k_{f,apa}$	$-5.07 \times 10^{-01}$	Axin binding to the APC SAMP repeats (forward rate constant)
$APC_{tot}$	$4.84 \times 10^{-01}$	APC concentration
$k_{r,apa}$	$4.60 \times 10^{-01}$	Axin binding to the APC SAMP repeats (dissociation rate constant)
$k_{-p,b}$	$3.45 \times 10^{-01}$	$\beta$ -catenin dephosphorylation rate constant
$CK1\alpha_{tot}$	$-3.00 \times 10^{-01}$	CK1 $\alpha$ concentration
$k_{f,ca}$	$-2.85 \times 10^{-01}$	CK1 $\alpha$ binding to Axin (forward rate constant)
$k_{r,ca}$	$2.59 \times 10^{-01}$	CK1 $\alpha$ binding to Axin (dissociation rate constant)
$GSK_{tot}$	$-2.32 \times 10^{-01}$	GSK-3 $\beta$ concentration
$k_{d,b2}$	$-2.24 \times 10^{-01}$	$\beta$ -catenin degradation (fast degradation rate constant)
$k_{f,ga}$	$-2.19 \times 10^{-01}$	GSK-3 $\beta$ binding to Axin (forward rate constant)
$k_{r,ga}$	$2.04 \times 10^{-01}$	GSK-3 $\beta$ binding to Axin (dissociation rate constant)
$k_{d,b1}$	$-6.56 \times 10^{-02}$	$\beta$ -catenin degradation (slow degradation rate constant)
$k_{f,ba}$	$-3.55 \times 10^{-02}$	$\beta$ -catenin ARM repeats 3 and 4 binding to Axin (forward rate constant)
$k_{r,ba}$	$2.85 \times 10^{-02}$	$\beta$ -catenin ARM repeats 3 and 4 binding to Axin (dissociation rate constant)
$k_p$	$2.54 \times 10^{-02}$	APC phosphorylation rate constant
$k_{-p}$	$-2.50 \times 10^{-02}$	APC dephosphorylation rate constant
$k_{f2,bap}$	$2.15 \times 10^{-02}$	$\beta$ -catenin ARM repeats 3 and 4 binding to phosphorylated APC 20-aa repeat (forward rate constant)
$k_{r1,bap}$	$1.06 \times 10^{-02}$	$\beta$ -catenin ARM repeats 5-9 binding to APC 15-aa repeat region (dissociation rate constant)
$k_{r2,bap}$	$-1.03 \times 10^{-02}$	$\beta$ -catenin ARM repeats 3 and 4 binding to phosphorylated APC 20-aa repeat (dissociation rate constant)
$\chi$	$-1.01 \times 10^{-02}$	Enhancement factor for intracomplex binding
$k_{f1,bap}$	$-7.53 \times 10^{-03}$	$\beta$ -catenin ARM repeats 5-9 binding to APC 15-aa repeat region (forward rate constant)
$BCAT_{tot}$	N/A	$\beta$ -catenin concentration

<sup>1</sup>In general local (differential) sensitivity coefficients are defined as  $\frac{x_i}{y_j} \left( \frac{\partial y_j}{\partial x_i} \right)$ , where  $x_i$  represents the

value of a model parameter and  $y_j$  represents the steady-state value of a model variable. Here, we focus on sensitivity coefficients for the steady-state level of  $\beta$ -catenin. The partial derivative appearing in the definition of each sensitivity coefficient is calculated via a finite-difference approximation:  $\frac{\partial y_j}{\partial x_i} \sim \frac{\Delta y_j}{\Delta x_i}$ ,

where  $\Delta x_i$  represents a 1% change in the nominal value of parameter  $x_i$  (Table 1) and  $\Delta y_j$  represents the resulting change in the steady-state value of the variable  $y_j$  (i.e., the steady-state concentration of  $\beta$ -catenin). A positive (negative) sensitivity coefficient indicates that an increase in the value of the corresponding parameter value causes an increase (decrease) in the steady-state value of the corresponding variable ( $y_j$ , the steady-state concentration of  $\beta$ -catenin). The sensitivity coefficients given here characterize the robustness of the nominal steady state for a normal cell (i.e., the form of the model used to consider the case of full-length APC).