

Table S1. Reactions and respective stoichiometry of biological processes used in the models

Process	Solute		Biomass		Rate expression
	R	E	X_A	X_B	
Growth of producer, A	-1	$Y_{E,A}$	$Y_{R,A}$	-	$\mu_{\max,A} \frac{R}{K_{R,A} + R} \frac{K_{i,E}}{K_{i,E} + E} X_A$
Growth of cross-feeder, B	-1	-1	-	$Y_{R,B} + Y_{E,B}$	$\mu_{\max,B} \left(\frac{R}{K_{R,B} + R} + \frac{E}{K_E + E} \right) X_B$