

## Supporting Information Text S3

### Modeling results for foxes of all ages

This is similar to Table 1 in the main manuscript but for the models fitting to the data from foxes of all ages.

Model	Description	Prior for $\mu$	Log marginal likelihood
1-C	no immunity ( $\alpha = 0$ )	$N(1.2, 0.2)$	-354.6 ( $\Delta_{ML} = 22.8$ )
	Constant FOI: $\log \beta(a) = \beta_0$	$N(1.3, 0.3)$	-354.0 ( $\Delta_{ML} = 21.6$ )
1-L	no immunity ( $\alpha = 0$ )	$N(1.2, 0.2)$	-360.6 ( $\Delta_{ML} = 34.8$ )
	Linear FOI: $\log \beta(a) = \beta_0 + \beta_1 a$	$N(1.3, 0.3)$	-359.6 ( $\Delta_{ML} = 32.8$ )
1-Q	no immunity ( $\alpha = 0$ )	$N(1.2, 0.2)$	-365.5 ( $\Delta_{ML} = 44.6$ )
	Quadratic FOI: $\log \beta(a) = \beta_0 + \beta_1 a + \beta_2 a^2$	$N(1.3, 0.3)$	-365.1 ( $\Delta_{ML} = 43.8$ )
1-P	no immunity ( $\alpha = 0$ )	$N(1.2, 0.2)$	-343.3 ( $\Delta_{ML} = 0.2$ )
	Periodic FOI: $\log\{\beta(a)\} = \beta_0 + \beta_1 \sin \left\{ 2\pi \left( a - \frac{\exp(a_s)}{1 + \exp(a_s)} \right) \right\}$	$N(1.3, 0.3)$	-343.2 ( $\Delta_{ML} = 0.0$ )
2	lifelong immunity ( $\gamma = 0$ )	$N(1.2, 0.2)$	-344.6 ( $\Delta_{ML} = 2.8$ )
	periodic FOI: $\log\{\beta(a)\} = \beta_0 + \beta_1 \sin \left\{ 2\pi \left( a - \frac{\exp(a_s)}{1 + \exp(a_s)} \right) \right\}$	$N(1.3, 0.3)$	-344.8 ( $\Delta_{ML} = 3.2$ )
3	transient immunity ( $\gamma \neq 0$ )	$N(1.2, 0.2)$	-345.7 ( $\Delta_{ML} = 5.0$ )
	periodic FOI: $\log\{\beta(a)\} = \beta_0 + \beta_1 \sin \left\{ 2\pi \left( a - \frac{\exp(a_s)}{1 + \exp(a_s)} \right) \right\}$	$N(1.3, 0.3)$	-349.3 ( $\Delta_{ML} = 12.2$ )