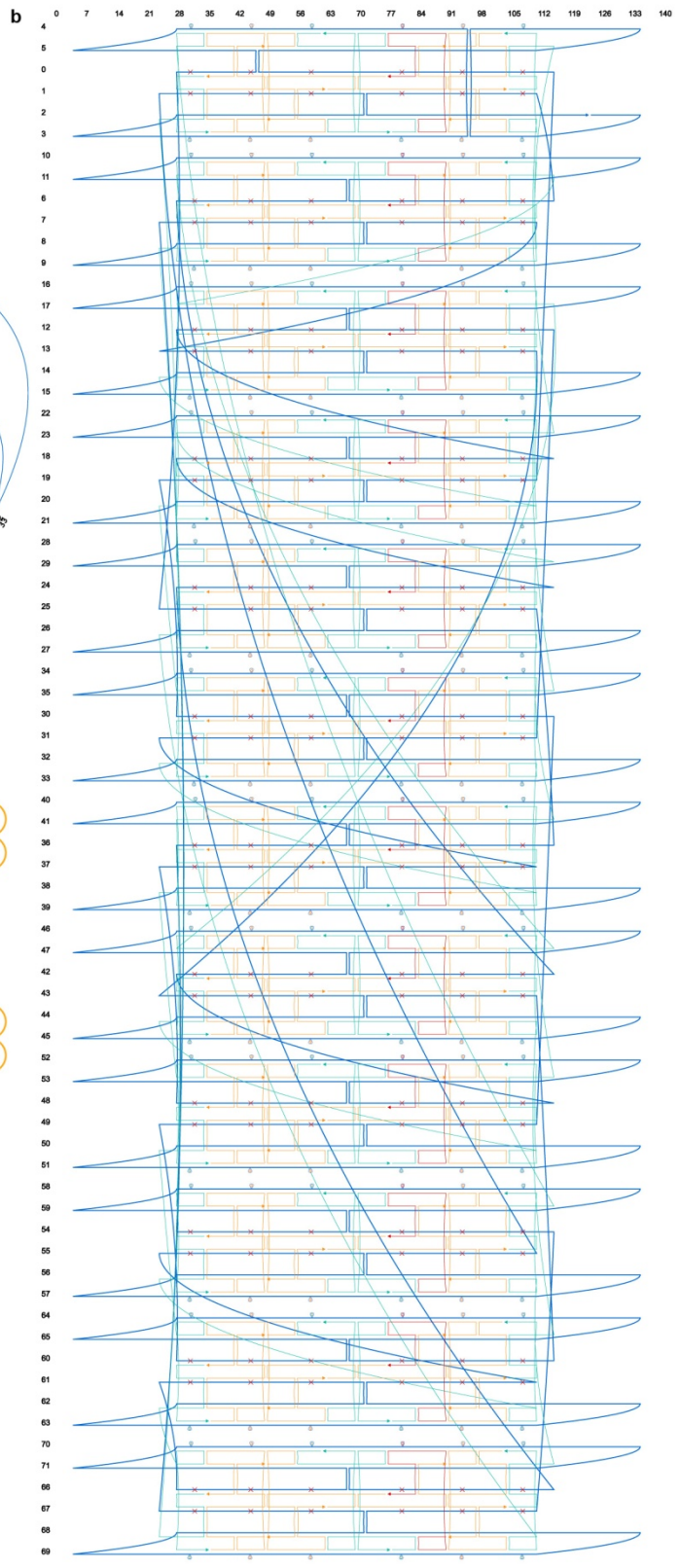
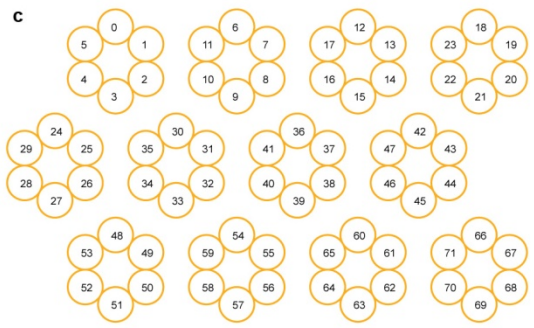
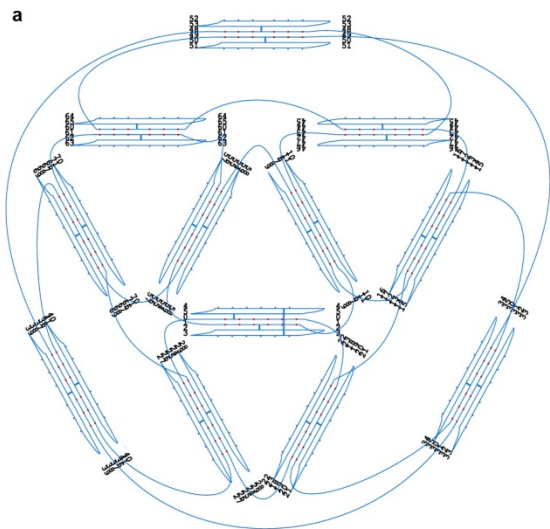


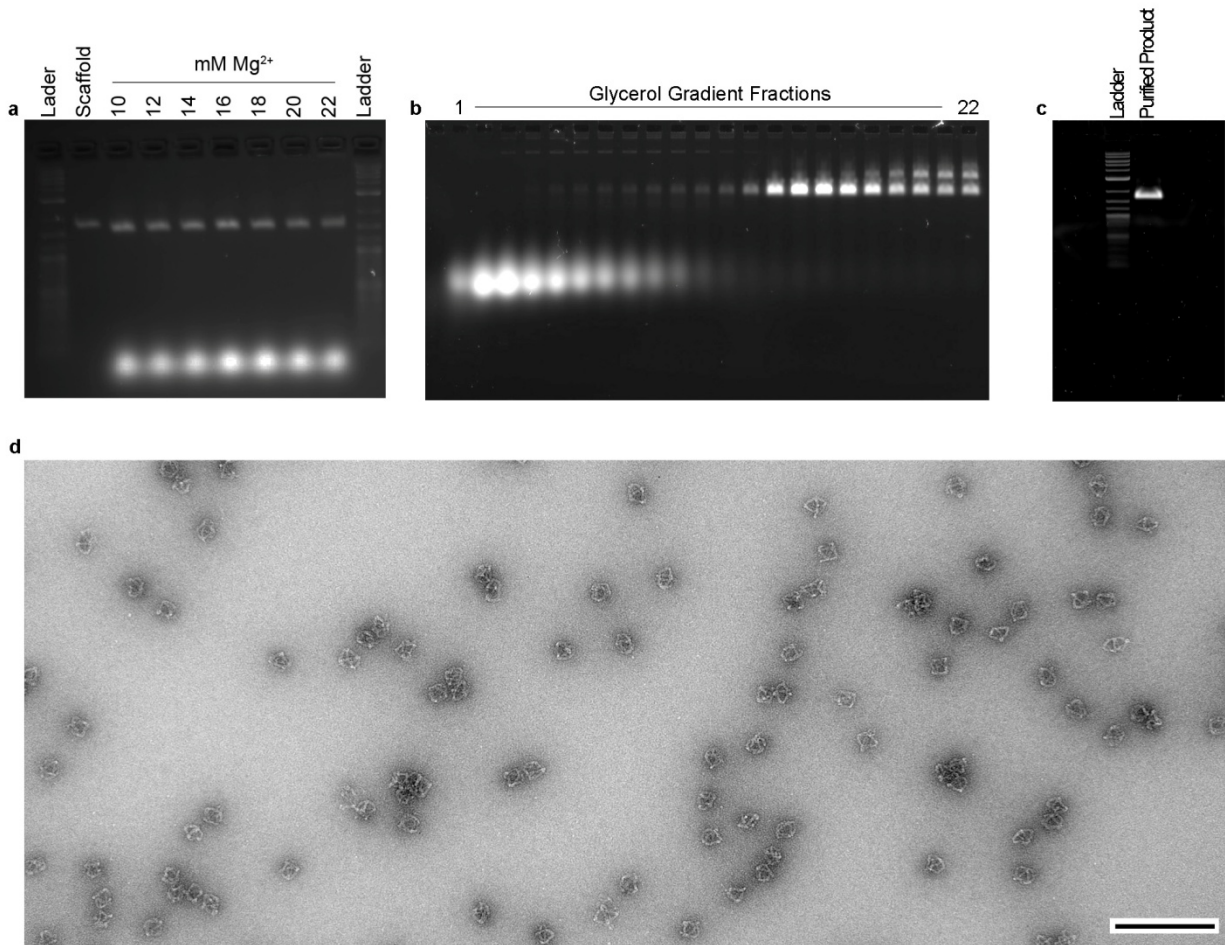
Virus-Inspired Membrane Encapsulation of DNA Nanostructures to Achieve *In Vivo* Stability

Authors

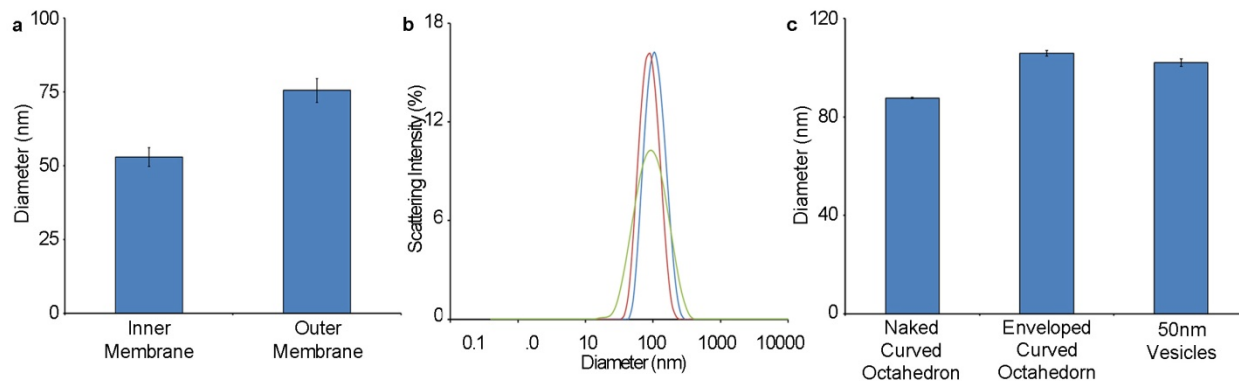
Steven D. Perrault,^{1,2} William M. Shih^{1,2,3*}



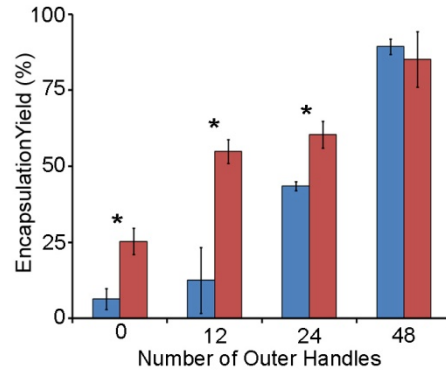
Supporting Information Fig. 1. Schematic of the DNO design and scaffold routing. (a) Schlegel diagram illustrating the routing of the p7308 scaffold through the 12 struts. (b) Staple oligonucleotide strand and scaffold organization from caDNAo. (c) Numerical organization of helices into six-helix bundles for the 12 struts. **Note:** the aspect ratio of the strut width (estimated to be 7.5nm based on known helical properties) to the DNO diameter shown illustrated in **Figure 1** is not meant to be to scale. Discrepancies between the illustrated model and TEM data could be due to less actual curvature in struts than anticipated from design, expansion of the DNO due to the presence of 5T linkers between struts, and errors in experimental measurement of DNO diameter.



Supporting Information Fig. 2. Synthesis and purification of the DNO. (a) Folding of the DNO was tested over a range of 10-22mM Mg²⁺, and 14mM was chosen as the best condition based on analysis from agarose gel electrophoresis and negative stain TEM. (b) Large quantities of structures were folded, concentrated, and separated *via* ultracentrifugation through glycerol gradients. The gradients were fractionated and an aliquot of each fraction was loaded into an agarose gel for analysis. This representative gel shows the excess staples remained at the top (fractions 1 ~ 12), and folded product migrated into the lower half of the gradient. Appropriate fractions were combined and run through a second glycerol gradient to achieve a high purity. (c) The final product was analyzed by agarose gel electrophoresis, showing a single product band, (d) as well as by TEM, which revealed a homogenous population of nanostructures. Scale bar = 200nm.

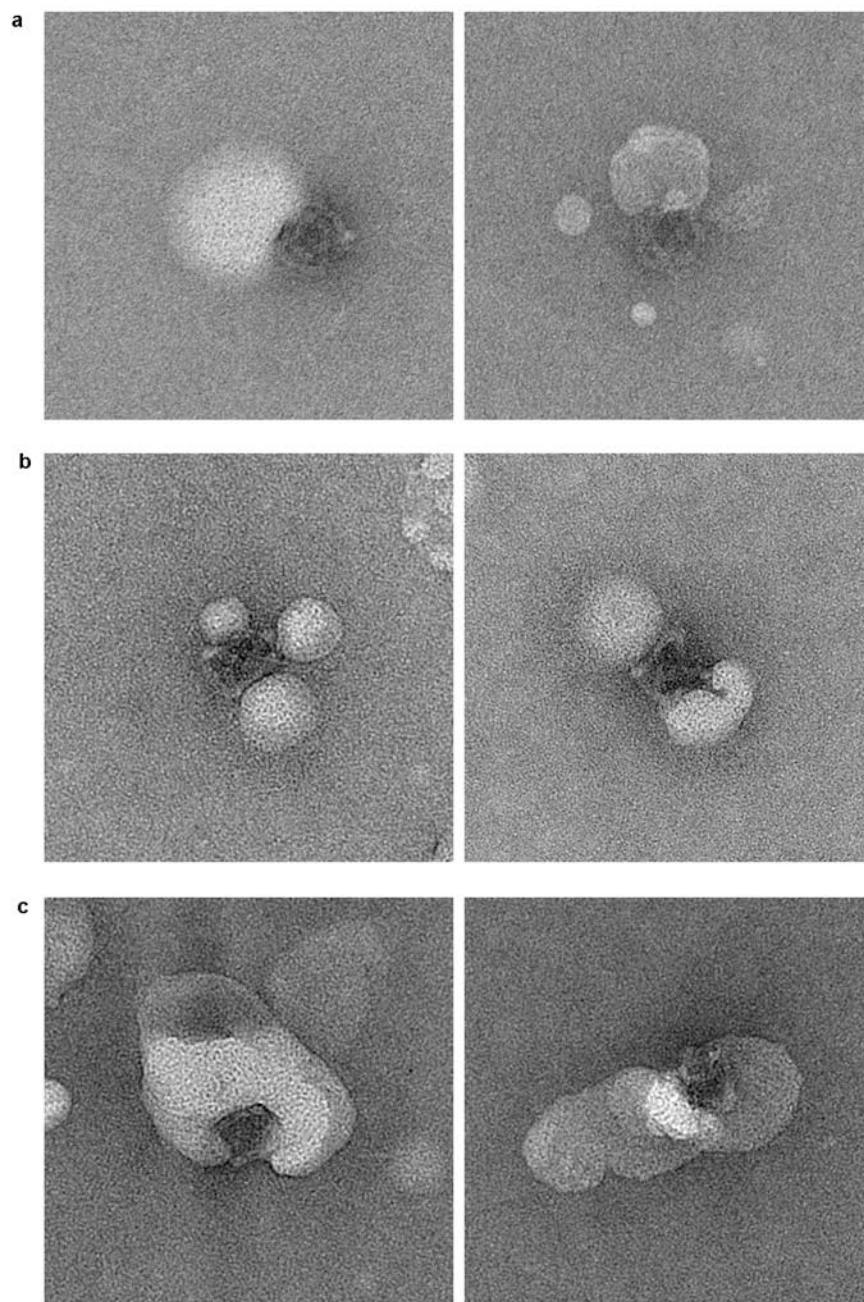


Supporting Information Fig. 3. Encapsulated-DNO sizing data. (a) Measurements of the inner and outer membrane diameters from TEM images. (b) Dynamic light scattering data of 50nm vesicles (—), the naked 48x-outer handle curved octahedron (—), and the enveloped, purified nanostructures (—). (c) Dynamic light scattering measured the N-DNO hydrodynamic diameter to be $93 \pm 0.3\text{nm}$, slightly smaller than for E-DNO and 50nm vesicles at 113 ± 1.3 and $115 \pm 1.0\text{nm}$, respectively (Error bars indicate SEM).

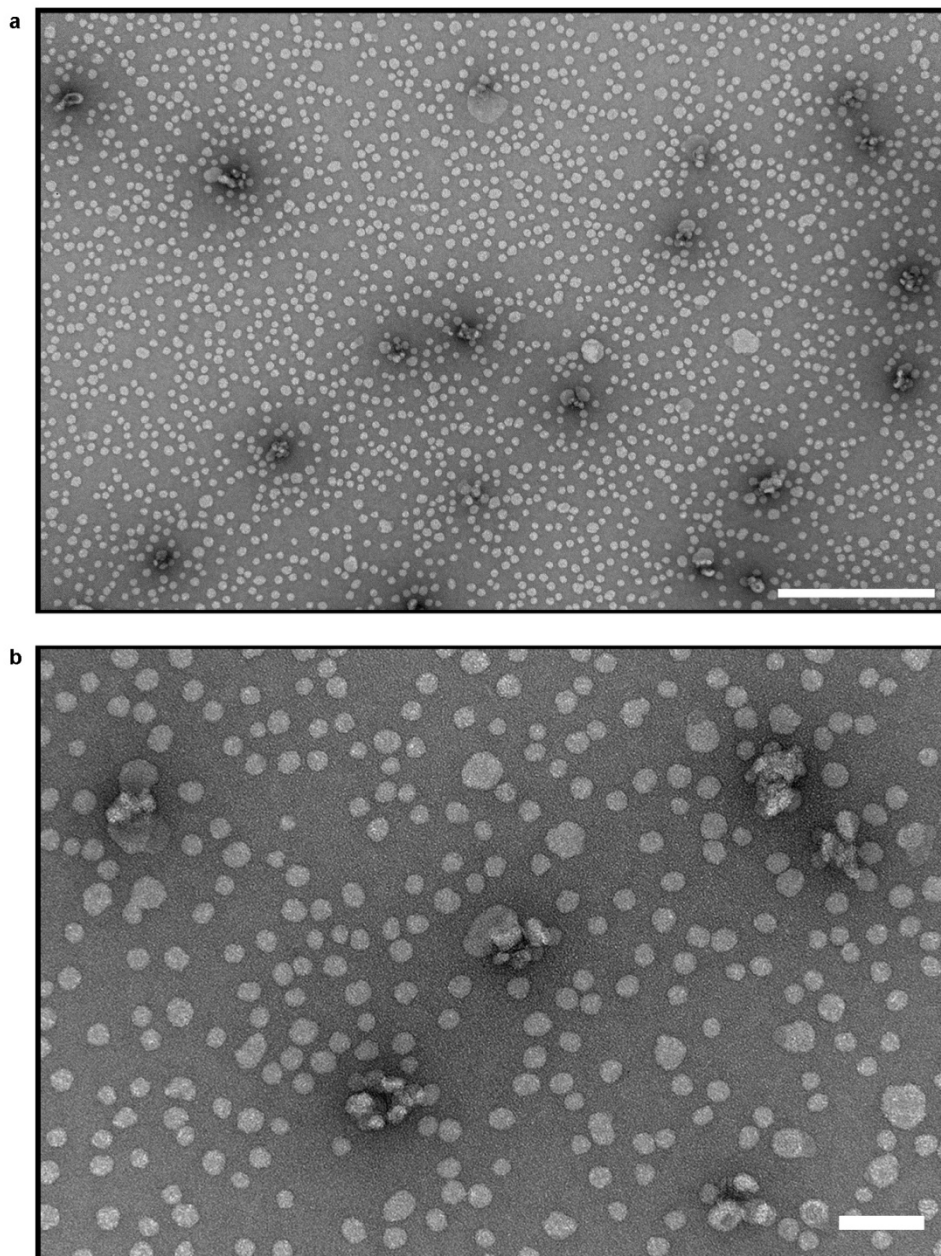


Supporting Information Fig. 4. Encapsulation yield dependence on membrane formulation.

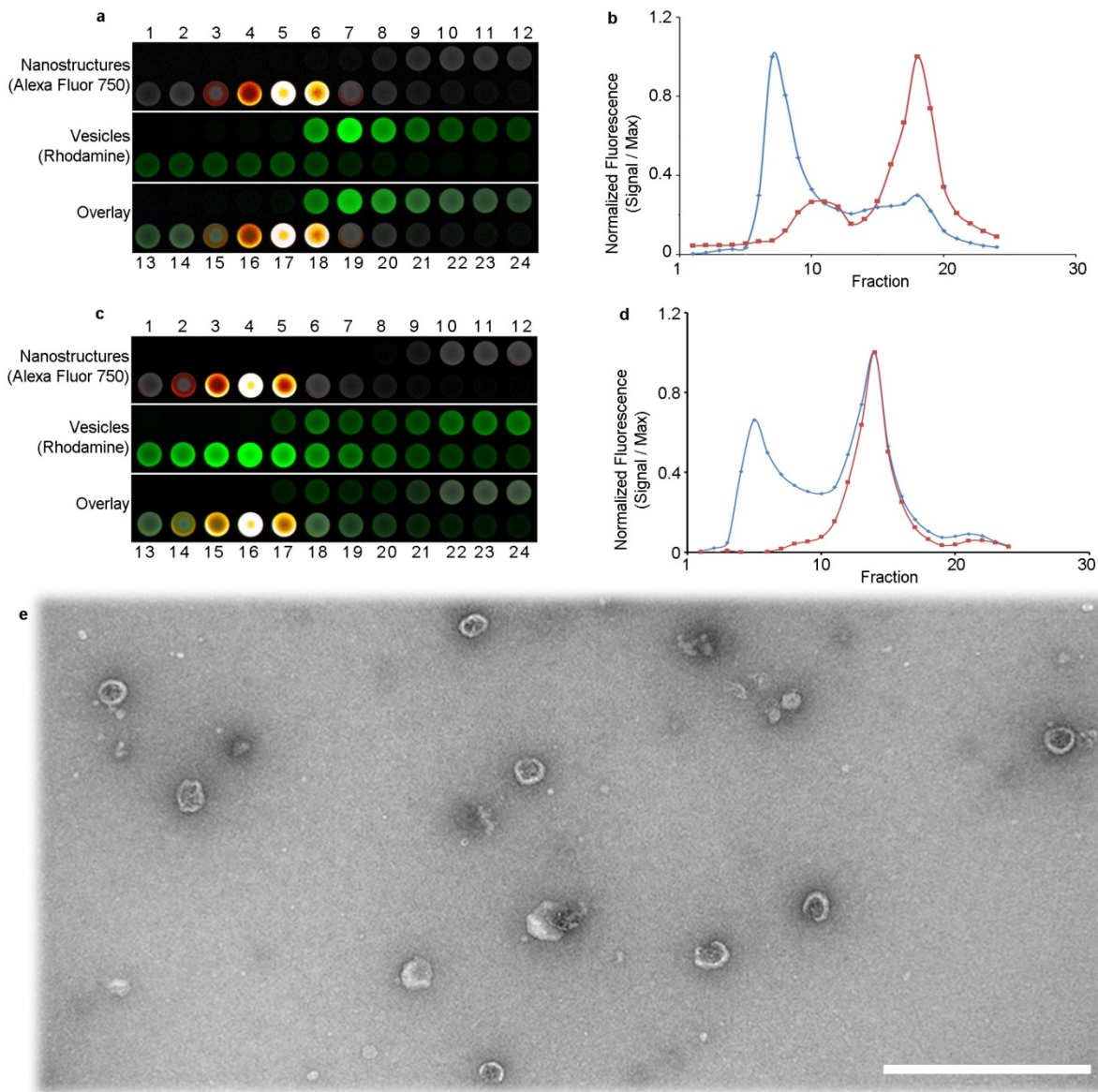
Two membrane formulations were compared for encapsulation yield using the PicoGreen dye exclusion assay; PC/PS/PEG-PE/Rhodamine-PE (84.1, 15.0, 5.0, 0.9%) (■) and PC/PEG-PE/Rhodamine-PE (94.1, 5.0, 0.9%) (■). Inclusion of negatively-charged PS reduced encapsulation yield with 0, 12 and 24 handles ($p < 0.05$), but did not have an effect on the 48-handle version. (*Student's t-test, $p < 0.05$, error bars indicate SEM).



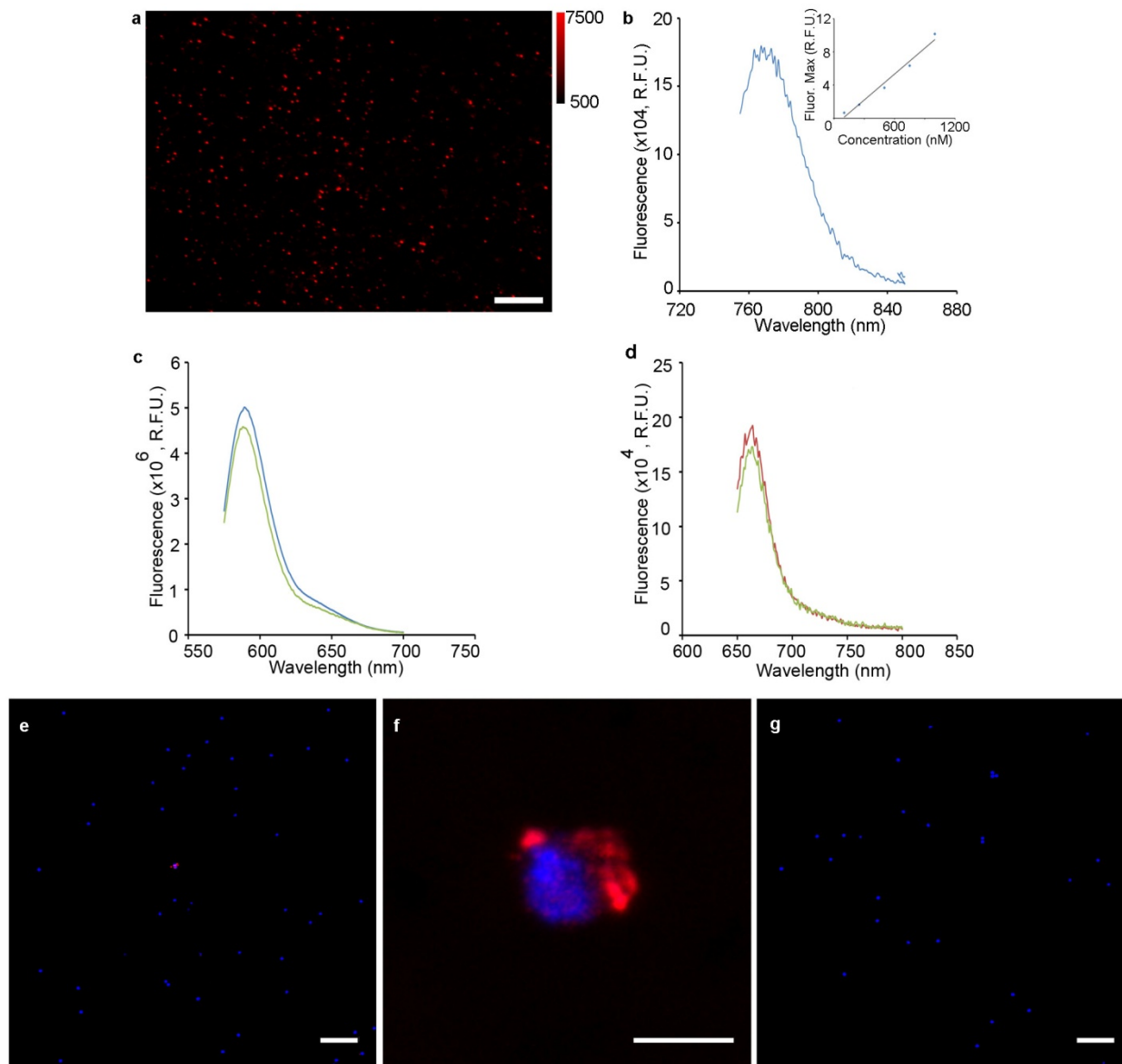
Supporting Information Fig. 5. Negative stain TEM images of DNO 0-24 outer handle variants after lipid treatment. (a) The 0-handle variant displayed some non-specific interaction with liposomes. (b) The 12-handle variant displayed a stronger interaction overall, but liposomes formed primarily away from the DNA surface, rather than around it. (c) The 24-handle variant showed greater capacity for encapsulation in membranes, but most cases were within larger liposome bodies, rather than tight-wrapping of the nanostructure.



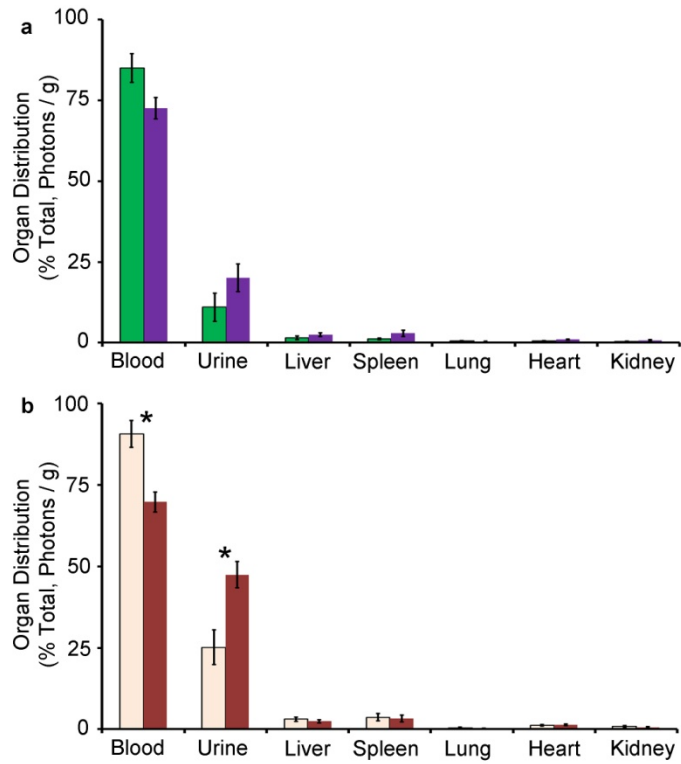
Supporting Information Fig. 6. Negative stain TEM Imaging of vesicle fusion. Low magnification (a) and high magnification (b) images of the post-encapsulation DNO after altering the lipid formulation to include 15% cholesterol. This resulted in a population of reconstituted vesicles of ~20nm, smaller than in the absence of cholesterol. Neighboring vesicles on the DNO were inhibited from fusing and fully encapsulating the nanostructures. Scale bars = 500nm (a) and 100nm (b).



Supporting Information Fig. 7. Float-up purification of E-DNO. (a) An iodixanol gradient with encapsulation product is prepared, centrifuged overnight, and fractionated. 50 μ L of each fraction is transferred into a 96-well fluorescence plate, which is imaged for fluorescence in the Alexa Fluor 750 (DNO) and rhodamine (vesicles) channels. (b) Analysis of rhodamine and (—) and Alexa Fluor 750 (—) fluorescence in the fractions shows separation of the excess vesicles higher and DNO lower in the gradient. (c) A second float-up is prepared with appropriate fractions from the first float-up, and measured by fluorescence in a 96-well plate. (d) Analysis of the second float-up shows further enrichment for E-DNO into lower fractions, which are collected for use in *in vitro* and *in vivo* experiments. (e) Negative stain TEM of purified E-DNO. Scale bar = 500nm.



Supporting Information Fig. 8. Imaging, measurement of DNO fluorescence and confocal microscopy of splenocytes. (a) Total internal reflectance fluorescence microscopy was used to image Cy5-labeled E-DNO. (b) Measurement of E-DNO Alexa Fluor 750 emission intensity, relative to a standard curve (upper right) of fluor-labelled oligonucleotides in encapsulation buffer. (c) The rhodamine emission profile was measured for the E-DNO (—) and a prepared solution of 50nm vesicles (—) used for *in vitro* and *in vivo* experiments. (d) The Cy5 emission profile was measured for N-DNO (—) and E-DNO (—) samples prepared for *in vitro* experiments. Scale bar = 10 μ m. (e) Splenocytes stained with Hoechst 33342 (blue, nucleus) and incubated with Cy5-labeled N-DNO (red) show rare, bright phagocytic cells (scale bar = 50 μ m), (f) higher magnification of same (scale bar = 5 μ m). (g) Splenocytes incubated with E-DNO showed no highly bright cells (scale bar = 50 μ m).



Supporting Information Fig. 9. Biodistribution profiling of the E-DNO membrane and nanostructure, and of the E-DNO vs. 50nm liposomes. (a) Organs were harvested 120 minutes post-injection of EDNO, and were imaged for Alexa Fluor 750 (■) and rhodamine (■) to profile nanostructure and membrane distribution, respectively. No significant differences were observed in distribution. **(b)** Organs were harvested 120 minutes post-injection of EDNO (■) and 50 nm liposomes (■) and imaged for rhodamine fluorescence to profile distribution (*Student's t-test, $p < 0.05$, error bars indicate SEM).

Supporting Information Table 1. DNA NanoOctahedron Staple Sequence List. Lipid handle sequences are in red, fluorophore handle sequences in blue. The “Start” and “End” columns correspond to the helix number and [nucleotide position] along the helix (see Supporting Fig. 1).

Start	End	Sequence	Length
69[78]	70[62]	CCAGCGAGTTACTTAGCCGACTAAAGACACTCATCAGCGCTAA TTTTTCTTCACACCACACTCCATCTA	70
40[61]	39[77]	TTCTTAACAGGGAGTTAAATAGAAAGGAGCTTTCGATCATCAT TTTTTCTTCACACCACACTCCATCTA	70
33[78]	34[62]	GAAAACACCTTGCTTCTGTCAATCGGGAGTGAAACATTTTCCCA TTTTTCTTCACACCACACTCCATCTA	70
4[61]	3[77]	CCTGCCTCGGCAAAATCCCTTATAAATCAAACAGTTGGTAATA TTTTTCTTCACACCACACTCCATCTA	70
67[105]	58[104]	ACCGAACATATTGAATAACTTTTCTCAGAGCCGGAACCCGTAACAAA TTTTTCTTCACACCACACTCCATCTA	74
0[34]	27[35]	CTCAGTGCAGCAGAATGGTTTTAGCTACACTTAAATCCGCCACCCT TTTTTCTTCACACCACACTCCATCTA	74
37[105]	28[104]	GTAGATATTTTGTTCACACTTTTACAGACAACCAGTACATCAGATAT TTTTTCTTCACACCACACTCCATCTA	74
66[34]	39[35]	GGAAACGCATCGGGTAAAAATTTAACCGATGCCGACAAAATTATCATT TTTTTCTTCACACCACACTCCATCTA	74
9[78]	10[62]	GGCTTTTTCATTGAATCCCTAGGAATACACCAAAATTTGACGA TTTTTCTTCACACCACACTCCATCTA	70
16[61]	15[77]	AAACTTAAATAAGAATAAATAGTGAATTACAAAGAGATTAGAG TTTTTCTTCACACCACACTCCATCTA	70
12[34]	22[104]	TTTAGTAAATCACCGAAAGTTTTGTATTGGAATCGGCCTCGAGCCAG TTTTTCTTCACACCACACTCCATCTA	74
70[61]	69[77]	TATCAGATTTTAAAGAAAATTAACGTCAGTAATGTTTGACCC TTTTTCTTCACACCACACTCCATCTA	70
63[78]	64[62]	AATTCATTAAGGTGAATTTTAAAGACTCTACAATACAAAGGC TTTTTCTTCACACCACACTCCATCTA	70
13[105]	45[35]	CATATAAACATACTTTTATTTTGAATAATTACATTGGGTGGCATC TTTTTCTTCACACCACACTCCATCTA	74
27[78]	28[62]	ACCCATGATCTAAAGTTTTTCGGAATAGGGCAAGCCTTTAGCGA TTTTTCTTCACACCACACTCCATCTA	70
15[78]	16[62]	AGTACCTTTTAAATATGCAGCAAAGCGAGGTCAGACGCGAGA TTTTTCTTCACACCACACTCCATCTA	70
61[105]	46[104]	TTAGAGCTCATAATCACCATTTTGTACCAAATAAAGCATATTACC TTTTTCTTCACACCACACTCCATCTA	74
22[61]	21[77]	TCCAGACATCCCATCCTAAAACAGTAGGGTAAAGTCCAGTCG TTTTTCTTCACACCACACTCCATCTA	70
18[34]	33[35]	GGCTGTAATTCGAGCATAATTTTCTTTGACCAAGCTTGAATTATC TTTTTCTTCACACCACACTCCATCTA	74
60[34]	69[35]	AAATATGAAACGGAAAAATTTTAAATAGCATTAAAGCCCAACCTAAA TTTTTCTTCACACCACACTCCATCTA	74
19[105]	4[104]	GCCCTGTATGCGACGCCAATTTTATCACCCGGCGAAATAAAGAACG TTTTTCTTCACACCACACTCCATCTA	74
21[78]	22[62]	GGAAACCTCACCAAGTATCCGCTCCCGCTTAAATTCG TTTTTCTTCACACCACACTCCATCTA	70
28[61]	27[77]	ACCTCCCAGCTAACGAGCTCATCGAGAGAGGCGTCAATAGGA TTTTTCTTCACACCACACTCCATCTA	70
64[61]	63[77]	TATCAGTTGATAATCAGAAAGATTCAAGAGATCTCAATAGAA TTTTTCTTCACACCACACTCCATCTA	70
57[78]	58[62]	CGTTTGCCCTCAGAGCCAACGTCACCATAGCCCAACACCA TTTTTCTTCACACCACACTCCATCTA	70
24[34]	70[104]	AATAAAGGCGGACCGCCACTTTTTGTGTCTACAACGGCGGGAGAA TTTTTCTTCACACCACACTCCATCTA	74
31[105]	16[104]	AATCTCACCGCGGGCCCTTTTGTGTAATGGTCATTTTAACTATAT TTTTTCTTCACACCACACTCCATCTA	74
25[105]	21[35]	TCTGTACCTTATAGGAATCTTTTATAGATAAAGCTAATGGAGTGAGCT TTTTTCTTCACACCACACTCCATCTA	74
55[105]	3[35]	CAGAGCCCAACTACAAGAATTTTAAAGAGAAAACATGAATTCCAGTAA TTTTTCTTCACACCACACTCCATCTA	74
43[105]	9[35]	TTTTAGTCCATCACTATCGTTTTAGGGATTTAGAGCGACACTATCA TTTTTCTTCACACCACACTCCATCTA	74
34[61]	33[77]	GTCACGAGACCGTATACGCCATTACGGCGCCAGGGAACATCAA TTTTTCTTCACACCACACTCCATCTA	70
54[34]	64[104]	GAACTACAAAATCAGTAGCTTTTAAAGGTAAAAAGGGCGCTGATAAA TTTTTCTTCACACCACACTCCATCTA	74
30[34]	40[104]	ACCGAGAGGTTTTGAATACTTTTCTGAATATCAATATATCCAAAAGG TTTTTCTTCACACCACACTCCATCTA	74
10[61]	9[77]	GCACGTAGAATCCTGAGAAAGAAAGCGATGGTTGCTAGCGAGA TTTTTCTTCACACCACACTCCATCTA	70
1[105]	10[104]	GATTTAAGTTCGCTGTCTTTTCCAAATAGGGTAAATACCCGCCCG TTTTTCTTCACACCACACTCCATCTA	74
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Start	End	Sequence	Length

51[78]	52[62]	CCGTGGGGGGACGACGACATTGTTAAATAACCCGTATGAAAAA TTTTTCTTCACACCACACTCCATCTA	70
3[78]	4[62]	AGTTTAAAGGTGCCGTAAACTTGATATTAGTGTACTAATGCC TTTTTCTTCACACCACACTCCATCTA	70
6[34]	57[35]	AAAGAGAACAACCCAAAAGTTTTTATGCGTTTAAATTTGTCAGACTG TTTTTCTTCACACCACACTCCATCTA	74
39[78]	40[62]	ATTCCTGATATCAAAATTAACAAACAATCGGAATTAGGTGAAT TTTTTCTTCACACCACACTCCATCTA	70
49[105]	34[104]	AGCTTTTTTGAAGCAGAAGTTTTACATAAATCATTTGAAAAGGGGG TTTTTCTTCACACCACACTCCATCTA	74
36[34]	51[35]	GCGAAACAATAGGAACGTTTTTGCAAATCTATCAAAC TTTTTCTTCACACCACACTCCATCTA	74
7[105]	15[35]	GAATGATTGACGTGTAGCGTTTTTACCGACTCATCTCGAGCTTCA TTTTTCTTCACACCACACTCCATCTA	74
48[34]	63[35]	TTAGAGATTGTACATCAAATTTACTAGCAAAACAAGAAAAGAAACG TTTTTCTTCACACCACACTCCATCTA	74
42[34]	52[104]	AGACAATTGATTCTATATTTTTATCGTAAATGGGATATATTAAC TTTTTCTTCACACCACACTCCATCTA	74
46[61]	45[77]	TTGACGCAGATAGAACCCCTTAGTAATAAGGAAATAATCATACA TTTTTCTTCACACCACACTCCATCTA	70
52[61]	51[77]	TCTAAAGAAGGTTATCTAATAAAACATCGCAGCAACGGATTCT TTTTTCTTCACACCACACTCCATCTA	70
45[78]	46[62]	GGCAAGGACTTTTGCGGATTAGATACCCAATAACCTACATT TTTTTCTTCACACCACACTCCATCTA	70
56[90]	54[77]	ACCGCCACATCTTTGAATAAGGCTTGCCTGGCTGAGGTG AAAAATTATCTACCACA ACTCAC	42
62[90]	60[77]	TATTCATATGGTTGGTAGCTATTTTGAAGGGTGAGTA AAAT TATCTACCACA ACTCAC	42
44[90]	42[77]	CTGTAATCAAAGAAAGGAAAAACGCTCATCACTCAATCA AAAT TATCTACCACA ACTCAC	42
50[90]	48[77]	GTTTGAGAACAAACCCACGCTGAGAGCCAGCCATTAGCGA AAAT TATCTACCACA ACTCAC	42
8[90]	6[77]	TAAATATGCAAAAGACAGGGCGCTACTAAAGGAGCCGAG AAAAATTATCTACCACA ACTCAC	42
32[90]	30[77]	TGAATAAAAATTAATAAGTTGGGTA ACTGCGCAACAAAGCAAAT TATCTACCACA ACTCAC	42
68[90]	66[77]	GCTCCATTATACCGAACAAAGTCAGAGGAAAAAGAGAA AGCAAAT TATCTACCACA ACTCAC	42
20[90]	18[77]	TTTCTTTGTCGTGAAAGTACCGACAAAAGCTTAATATA AAAGAAAT TATCTACCACA ACTCAC	42
38[90]	36[77]	ACCTACCATTATCATCGGTTTATCAGCTTACA ACTATCAGCGAAAT TATCTACCACA ACTCAC	42
2[90]	0[77]	GGGGTCGACGGGTTAACAGTGCCCGTATAAAAGAA TTGCCAAAT TATCTACCACA ACTCAC	42
26[90]	24[77]	CGTAACGTACCGTAGTATTCTAAGAACGCACAAGCAA ACAAAAAT TATCTACCACA ACTCAC	42
14[90]	12[77]	CAACATGTTAATTGAAATCCAATCGCAAGTATCA AGCTGAGAAAT TATCTACCACA ACTCAC	42
27[36]	29[48]	CAGAGCTTAGTATAAGTGCCGTCGATTGCCACCTGAAT	39
34[103]	32[91]	TGTGCTGATCGGTTTCTGGTGCCGAAATTTTATGTGAG	39
49[63]	50[49]	ATTAATCCAATATCTTTAGGAGCACTTGTTAAATTTTTTA	41
35[91]	31[104]	GAAGGGCGCAAGGCGTTACATTTAACAATTTCAATATCCCTTAG	44
59[91]	55[104]	CAAGAGTCATTAGTTCATAATCAAAATCACCGCCACCACCAC	44
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31[63]	32[49]	TACCTTTGCATGGCTAGTACCCGTATATATACAGAACGGAT	41
59[49]	55[62]	CTCATTATAGTAAACGGCATTTCGGTCAATGAAACTTAGCA	42
66[76]	71[90]	ATTTTTGGGAACGAGGCGCAGACGGTCAAATAAAAAATAGC	41
38[48]	36[35]	TAAATCCAACAAAGAGATACCGATAGTTGCATATTCGCTCAGCA	44
42[76]	47[90]	TTCTTTGCAGAAGCCTTATTTCAACGGTTGTAGTGCCTGA	41
55[63]	56[49]	AGGCCGGGGCGTTGGGAAGAAAATCTATTACCACATCGAT	41
54[76]	59[90]	CAGACCAAACCACCCTCAGAGCCGCAGATGAACCTTTCAT	41
43[63]	44[49]	GTTTGACATTCTGACCTGAAAGCGTAAACGAGTAAATGGTC	41
47[91]	43[104]	GTAGAAGATTGCAACTTAGCAAAATTAAGCAAAACATTA AAAAAT	44
50[48]	48[35]	ACCAATAAACATTAATTGCTGAACCTCAAAAACAGTTTAA TAGA	44
47[49]	43[62]	CCAACAGTCAATCGTAGTAGCATTAACATTTTCGCAGATTTA	42
Start	End	Sequence	Length

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53[91]	49[104]	CGAACGACAACAGTGGGCGGATTGACCGTACCGTGATCCAGCC	44
45[36]	47[48]	AATTCTTGTTTAGCCCAATTCTGCGAGAATACATTCTGG	39
46[103]	44[91]	CCAGCCAACCTCAAACGCAAATTAACCCAAGGATATGACC	39
53[49]	49[62]	ATTGAGGCATCACCATGTGAGCGAGTAACCAGCTCAATTCGC	42
39[36]	41[48]	TTGCGGTTTGCCATAATACATTGAGTCACCGTCGCTG	39
52[103]	50[91]	CGCCTGACCACCATGGCTATTAGTCTTCGACTCTGCCA	39
51[36]	53[48]	TTCATCGGAACGCAACGTTAATATTTAACAACGAAAGGA	39
44[48]	42[35]	AATAACCACTAATAGTCTGAAATGGATTATAAGGGACGTGGCAC	44
56[48]	54[35]	AGCAGCAGTTTTCATTTGGGCTTGAGATGGATTTTAAATAAAAC	44
25[63]	26[49]	AGTATAGACGTCTTTCCAGAGCCTAATGAGGGTTCCGTA	41
24[76]	29[90]	GTACCGCCCGTCGCTTTCCAGACGTTGGTATTAAGCCGTT	41
57[36]	59[48]	TAGCGCCCGTAATCACCAGTAGCACCCAGTTAGAACTGG	39
29[91]	25[104]	TTTATTTCTTATCCGACACTGAGTTTCGTCGCCCTCATGAATTT	44
29[49]	25[62]	CTTACCAGACTTGCTCATTTTCAGGGATATGTATCAGATATA	42
28[103]	26[91]	AGAAGGTCATCGTCATTCCAAGAACGAGTAAATAGTTAG	39
64[103]	62[91]	TTAATGCAGTCAATATTTTAAATGCAAGCCATCGGAAAT	39
65[49]	61[62]	ACCCCGGTCATTGCAATAAGTTTATTTTGCTTATTTAAAGAA	42
21[36]	23[48]	AACTCAAGCCGGATAATCATGGTCATCCAATCACAAGAA	39
32[48]	30[35]	TCGCTGATTACCTGAAACGACGCCAGTGTAGCGAGCCCGGGT	44
20[48]	18[35]	ACATACGCATTAATTATAAAACAACATGTTTCGTCCTGAAATAATC	44
65[91]	61[104]	CCGGAGACCGGAGAGACCAGCGCCAAAGACATATTGATTGGGAA	44
19[63]	20[49]	GTGAAATTCTTTACGAGCATGTAGAAAAGCTGTTCCACACA	41
18[76]	23[90]	CCAACGCTGCGGGCAACAGCTGATTGCTACCAGTTGAGAAT	41
60[76]	65[90]	GTGTAGGGAATCACCCTCACCGACTTGATGCCTGAGAAAGG	41
23[91]	19[104]	CGCCATAGAGAATATCCAGCTGCATTAATGGCGCCAGCCGCTG	44
23[49]	19[62]	AAATAATGACGACAGCGTTGCGCTCACTGCACAATTTCTGT	42
22[103]	20[91]	TAATAATTTAACATTATACAAATCTCCTTCAGGTGGTT	39
61[63]	62[49]	CTGGCATTAAAAGCCCCAAAAACAGGAATACCCACGCAGTA	41
62[48]	60[35]	TGTTAGCCACCACGGCTGAGAGTCTGGAGCTGTCAATTATAAGC	44
15[36]	17[48]	AGCGAAAGGAAGCAAAATCAGGTCTTTAGAAATAAATAA	39
35[49]	31[62]	CGCTAGCCGTTGTAAGCAAAAGAAGATGAAAACAATTAACAG	42
14[48]	12[35]	GATTAAGCCAGACCGATATTTTAGTTAATTCGTGTGAAAGCCTG	44
63[36]	65[48]	CAAAGAAAACGTACAATAATAACGGAAGATTGCATATGT	39
13[63]	14[49]	ATAGTCAAACACCGGAATCATAATTACTACCCTGTCAAAAA	41
12[76]	17[90]	AAGAGTCGAAACTAAAGTACGGTGTCTTTAAGACATCATAG	41
70[103]	68[91]	TAACTGACAGAGAATTTATCCCAATCCAATCAGCGACCT	39
17[91]	13[104]	GTCTGAGGCTGATGCCTCCTTTTGATAAGAATAATGCTTCATTC	44
17[49]	13[62]	GGCGTTATTCAAATGAAGCAAACCTCAACGATTGCAACTATT	42
16[103]	14[91]	GTAATAGACTACGCGATAGCTTAGAGGAAGTTGTAGCT	39
71[49]	67[62]	GAAGCCCGAGATAAAGAATACACTAAAACCTTTTCAACAGAG	42
Start	End	Sequence	Length

71[91]	67[104]	AGCCTTTAACACCCTAAGCGCGAAACAAAGGAAATCCTAAGGGA	44
9[36]	11[48]	TAACCCCAT AACGATTATTACAGGTAAGGCCAGGAACGG	39
26[48]	24[35]	CAGGAGGCACCACCCGGGAGGTTTTGAAGCATTATGTTACAA	44
8[48]	6[35]	GCAGATATCGTTTACCTTTCCTCGTTAGAATTAGACACCGAGTA	44
37[63]	38[49]	TTAGACTAAGGCCGCTTTTGCGGGATCGGATTTACTCGTAT	41
7[63]	8[49]	GTTGAGAGAGTGTTTTATAATCAGTGGAAAGATAACTAAT	41
6[76]	11[90]	AGGAAGGTTCTCAAATGCTTTAAACAAACGTGGGGGCGCT	41
36[76]	41[90]	GAGTGAGTTTTTGCACGTA AACAGAAAACAGTTAAGGAAT	41
11[91]	7[104]	AGGGCGCGCGCCGCTAAGTTTTGCCAGAGGCTGCGGAAAAACGA	44
11[49]	7[62]	TACGCCATAACGTGCAGACGACGATAAACACATTCTCATCA	42
10[103]	8[91]	CTTAATTGGCAAGGGGAAAGCCGGCGGTT CAGATCGTCA	39
41[91]	37[104]	TGCGAATTAATTGTAGATGATGGCAATTC AATGGAAGAAATTGC	44
41[49]	37[62]	AGGCTTGACAGCTTAACCACCAGAAGGAGTCGACAAGAAGTA	42
3[36]	5[48]	GCGTCATAAAGCCATTGACAGGAGGTGGGCGGATTATT	39
40[103]	38[91]	AGCCTTAATAATTCTAAACAACCTTTCATAAAGGGTTAGA	39
2[48]	0[35]	TCCTCATTACATGGCAACCTATTATTCTGAGGATTAGGGTTTTG	44
68[48]	66[35]	GTTTCCAGAGGCCAAACCCACAAGAATTGAGATAGCTAACCAGAA	44
1[63]	2[49]	ACGATTGCGAAAATCCTGTTTGATGGTTGAGGCAAAATAAA	41
0[76]	5[90]	CAGCAGGGCGCACTAAATCGGAACCTCGCTGGTTAGCCCG	41
69[36]	71[48]	ACGAAATTAACGGAACGAGGGTAGCAAAGTTCTTACC	39
5[91]	1[104]	AGATAGGCCCTTGAGCAGTGCAACGTCAAAAAATCAAAGCCCC	44
5[49]	1[62]	CCGAAATATTTTCGTTTTGATGATACAGGCACAAACGGTCAG	42
4[103]	2[91]	TGGACTGTTGAGTAGCAAGCGGTCCAAAAGGGTTTTTTT	39
33[36]	35[48]	ATTCAATTGCTTAACGTCAGATGAAAGGATCGCAAGTC	39
67[63]	68[49]	GCTTTGAGTGTAAGCAGATAGCCGAACAACGGCTTGAGGAA	41
58[103]	56[91]	GCTGCTAATCTTGTGAAAGAGGACACCAGAACCTCAGA	39

Supporting Information Note 1: Prediction of DNO Six Helix Bundle Curvature Analytical Derivation

Approximation of Energy for bending DNA bundle:

Please see Dietz *et al.*, Supporting Figure 1 for additional data¹.

$$E_{total} = E_{stretch/compression} + E_{bend}$$

$$E_{stretch/compression} = \frac{1}{2} \frac{S}{d_{eq}} \sum_i n_i (d_i - d_{eq})^2$$

$$E_{bend} = \frac{1}{2} B d_{eq} \sum_i \frac{n_i}{r_i^2}$$

where $r_i = r_{ref} \left(\frac{\Delta a_i}{r_{ref}} + 1 \right)$

$$\theta_i = \frac{n_i d_{eq}}{r_i}$$

$$E_{bend} = \frac{1}{2} \frac{B}{d_{eq}} \sum_i \theta_i^2 \frac{1}{n_i}$$

but $\sum_i \theta_i^2 \frac{1}{n_i} \approx \theta^2 \sum_i \frac{1}{n_i}$

$$\therefore E_{bend} \approx \frac{1}{2} \frac{B}{d_{eq}} \theta^2 \sum_i \frac{1}{n_i}$$

The rationale for the above approximation is based on the idea that the underestimate in bending energy for the convex-face helices will be mostly offset by the overestimate in bending energy for the concave-face helices.

$$E_{total} = \frac{1}{2} \frac{S}{d_{eq}} \sum_i n_i (d_i - d_{eq})^2 + \frac{1}{2} \frac{B}{d_{eq}} \theta^2 \sum_i \frac{1}{n_i}$$

Please note that for this approximation of energy, the following relations hold:

At fixed values of d_i

$$\frac{\partial E_{stretch/compression}}{\partial \theta} = 0$$

At fixed values of θ

$$\frac{\partial E_{bend}}{\partial d_i} = 0$$

Step 0: Obtain an expression for the length $n_{ref}d_{ref}$ of a reference double helix in the curved bundle as a function of angle, assuming the bundle is at the equilibrium length for that angle. Do this by letting $\partial E_{stretch/compression}/\partial n_{ref}d_{ref} = 0$ and solving for $n_{ref}d_{ref}$ (recall from the previous page that $\partial E_{bend}/\partial d_{ref} = 0$). The position in the bundle of the reference double helix is encoded in the $delta_i$ offset values. The reference helix could be imaginary, the position within the bundle is arbitrary, and the value of n_{ref} never has to be specified (it cancels out during Step 1).

$$E_{stretch/compression} = \frac{1}{2} \frac{S}{d_{eq}} \sum_i n_i (d_i - d_{eq})^2$$

$$d_i = \frac{n_{ref}d_{ref}}{n_i} \left(\frac{delta_i}{r_{ref}} + 1 \right)$$

$$r_{ref} = n_{ref}d_{ref} / \theta$$

$$E_{stretch/compression} = \frac{1}{2} \frac{S}{d_{eq}} \sum_i n_i \left(\frac{n_{ref}d_{ref}}{n_i} \left(\frac{delta_i}{n_{ref}d_{ref}/\theta} + 1 \right) - d_{eq} \right)^2$$

$$E_{stretch/compression} = \frac{1}{2} \frac{S}{d_{eq}} \sum_i n_i \left(\frac{1}{n_i} (n_{ref}d_{ref} + \theta \cdot delta_i) - d_{eq} \right)^2$$

$$\begin{aligned} \frac{\partial E_{stretch/compression}}{\partial (n_{ref}d_{ref})} &= \frac{S}{d_{eq}} \sum_i n_i \left(\frac{1}{n_i} (n_{ref}d_{ref} + \theta \cdot delta_i) - d_{eq} \right) \frac{1}{n_i} \\ &= \frac{S}{d_{eq}} \sum_i \left(\frac{1}{n_i} (n_{ref}d_{ref} + \theta \cdot delta_i) - d_{eq} \right) \end{aligned}$$

$$\begin{aligned} 0 &= \frac{S}{d_{eq}} \sum_i \left(\frac{1}{n_i} (n_{ref}d_{ref} + \theta \cdot delta_i) - d_{eq} \right) \\ &= n_{ref}d_{ref} \sum_i \frac{1}{n_i} + \theta \sum_i \frac{delta_i}{n_i} - d_{eq} \sum_i 1 \end{aligned}$$

$$n_{ref}d_{ref} = \frac{1}{\sum_i \frac{1}{n_i}} \left(d_{eq} \sum_i 1 - \theta \sum_i \frac{delta_i}{n_i} \right)$$

Step 1: Use the expression for the length $n_{ref}d_{ref}$ from Step 0 to obtain an expression for the length d_i of double helix_i in the curved bundle as a function of angle, assuming the bundle is at its equilibrium length for that angle.

$$n_{ref}d_{ref} = \frac{1}{\sum_i \frac{1}{n_i}} \left(d_{eq} \sum_i 1 - \theta \sum_i \frac{delta_i}{n_i} \right)$$

$$d_i = \frac{n_{ref} d_{ref}}{n_i} \left(\frac{\delta_i}{r_{ref}} + 1 \right)$$

$$\theta = \frac{n_{ref} d_{ref}}{r_{ref}}$$

$$d_i = \frac{1}{n_i} (\theta \cdot \delta_i + n_{ref} d_{ref})$$

$$= \frac{1}{n_i \sum_i \frac{1}{n_i}} \left(\theta \cdot \delta_i \sum_i \frac{1}{n_i} + d_{eq} \sum_i 1 - \theta \sum_i \frac{\delta_i}{n_i} \right)$$

$$d_i = \frac{1}{n_i \sum_i \frac{1}{n_i}} \left(\theta \left(\delta_i \sum_i \frac{1}{n_i} - \sum_i \frac{\delta_i}{n_i} \right) + d_{eq} \sum_i 1 \right)$$

Python Script:

```
deq = 0.335
S = float(660)
B = float(230)
num_helices = 6

n is the number of basepairs installed in region with
# a default of nref base pairs
# e.g. nref = 105
n = [0 for i in range(num_helices)]
n[0] = 96
n[1] = 99
n[2] = 104
n[3] = 106
n[4] = 111
n[5] = 114
#190 degrees
#n[0] = 59
#n[1] = 70
#n[2] = 92
#n[3] = 106
#n[4] = 129
#n[5] = 140

# delta is the distance in nm from an arbitrary axis
delta = [0 for i in range(num_helices)]
delta[0] = 3.5
delta[1] = 2.5
delta[2] = 0.5
delta[3] = -0.5
delta[4] = -2.5
delta[5] = -3.5
```

```

for i in range(num_helices):
    delta[i] *= -1.125

total_n = 0
for i in range(num_helices):
    total_n += n[i]
average_n = float(total_n)/num_helices
print "average n is", average_n, "\n"

# Calculate delta_div_n_sum, one_div_n_sum, and beta values
delta_div_n_sum = 0
one_div_n_sum = 0
for i in range(num_helices):
    delta_div_n_sum += delta[i]/n[i]
    one_div_n_sum += float(1)/n[i]

beta = [0 for i in range(num_helices)]
for i in range(num_helices):
    beta[i] = (delta[i]-delta_div_n_sum/one_div_n_sum)/n[i]

# Calculate theta
beta_n_sum = 0
beta_delta_sum = 0
for i in range(num_helices):
    beta_n_sum += beta[i]*n[i]
    beta_delta_sum += beta[i]*delta[i]
numerator = deq*beta_n_sum
denominator_term_0 = beta_delta_sum
denominator_term_1 = (B/S)*(one_div_n_sum)
denominator = denominator_term_0 + denominator_term_1
theta = numerator/denominator

theta_in_degrees = theta*180/3.1416

```

```

print "theta is", theta_in_degrees,"degrees or ", theta, "radians"

# Calculate d
d = [0 for i in range(num_helices)]
for i in range(num_helices):
    factor_0 = theta*(delta[i] - delta_div_n_sum/one_div_n_sum)
    factor_1 = deq*num_helices/one_div_n_sum
    d[i] = (factor_0 + factor_1)/n[i]

for i in range(num_helices):
    print "helix", i, "\tlength per bp is", d[i]

print
print "delta_div_n_sum is", delta_div_n_sum
print "one_div_n_sum is", one_div_n_sum
print "beta_n_sum is", beta_n_sum
print "beta_delta_sum is", beta_delta_sum
print "numerator is", numerator
print "denominator_term_0 is", denominator_term_0
print "denominator_term_1 is", denominator_term_1
print "denominator is", denominator

```