# Supporting Information for

### Genetic Constraints Predict Evolutionary Divergence in Dalechampia Blossoms

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### **Tables and figures**

**Table S1.** Name, abbreviation (Abbr.), geographical location given by the state in Mexico and GPS coordinates (WGS84), and meters above sea level (Elevation).

Name	Abbr.	State	Longitude	Longitude	Elevation
Small-glanded populations:					
Cozumel	CO	Quintana Roo	20°22'10" N	86°59'40" W	13
Chemax	CX	Yucatán	20°40'22" N	88°00'25" W	22
Valladolid	V	Yucatán	20°42'31" N	88°15'06" W	31
Peto	Р	Yucatán	20°01'34" N	88°52'49" W	38
Motul de Carillo Puerto	MO	Yucatán	21°08'12" N	89°16'45" W	13
Dzemul	D	Yucatán	21°12'35" N	89°19'10" W	0
Santa Elena	S	Yucatán	20°19'55" N	89°37'55" W	37
Bolonchén de Rejón	BR	Campeche	19°59'23" N	89°45'48" W	112
Hopelchén	НО	Campeche	19°46'34" N	89°49'50" W	58
China	СН	Campeche	19°43'25" N	90°24'52" W	3
El Limón	Е	Veracruz	19°41'06" N	96°29'48" W	133
Tovar diallel		(Venezuela)	8°21' N	71°46' W	
Large-glanded populations:					
Puerto Morelos	PM	Quintana Roo	20°51'11" N	86°53'43" W	7
Tulúm	Т	Quintana Roo	20°12'26" N	87°27'04" W	21
Carillo Puerto	СР	Quintana Roo	19°38'58" N	87°59'00" W	15
Bacalar	BA	Quintana Roo	18°36'40" N	88°26'32" W	27
Graciano Sánches	GS	Quintana Roo	19°08'04" N	88°30'18" W	40
Cacalchén	CA	Yucatán	20°58'01" N	89°13'18" W	13
Champotón	CN	Campeche	19°21'49" N	90°43'06" W	4
Ciudad del Carmen	CC	Campeche	18°56'29" N	91°18'01" W	2
Comalcalco	С	Tabasco	18°21'26" N	93°20'43" W	6
La Mancha	LM	Veracruz	19°37'15" N	96°28'09" W	205
Martinez de la Torre	Μ	Veracruz	20°05'09" N	97°01'55" W	67
Tulum diallel		Quintana Roo	20°13' N	87°26' W	

**Table S2.** Summary statistics for the populations and species (averages of the populations). Number of plants and blossoms measured, and trait means and standard error (in mm) for the functional traits. Posterior means with standard errors are obtained from univariate Bayesian mixed models with plant and measurement date as random factors, and population as fixed factor. Separate models were fitted for small- and large-glanded populations. The estimates for the diallel populations were from the multivariate mixed models described in the methods.

Name         #plants         #blossoms         GAD         GSD         SW $\sqrt{GA}$ $\sqrt{BA}$ Small-glanded:         D         2         4 $3.55\pm 0.27$ $4.50\pm 0.48$ $0.85\pm 0.08$ $2.66\pm 0.21$ $38.71\pm 2.41$ CH         9         16 $3.03\pm 0.11$ $3.71\pm 0.21$ $1.21\pm 0.05$ $2.90\pm 0.12$ $36.90\pm 1.17$ MO         3         6 $3.49\pm 0.23$ $4.04\pm 0.39$ $1.29\pm 0.09$ $2.91\pm 0.20$ $37.78\pm 1.98$ E         9         15 $3.97\pm 0.16$ $5.12\pm 0.31$ $0.89\pm 0.04$ $2.95\pm 0.13$ $36.94\pm 1.15$ V         15         29 $3.32\pm 0.09$ $3.02\pm 0.11$ $4.029\pm 0.04$ $3.03\pm 0.11$ $36.07\pm 1.01$ HO         4         8 $2.88\pm 0.51$ $5.75\pm 0.29$ $9.91\pm 0.06$ $3.08\pm 0.18$ $3.69\pm 1.51$ CX         7         14 $3.07\pm 0.12$ $3.99\pm 0.24$ $1.11\pm 0.05$ $3.30\pm 0.18$ $3.69\pm 1.51$ CX         7         14 $3.07\pm 0.15$ $4.77\pm 0.32$ $1.06\pm 0.05$ $3.71\pm 0.23$ $3.78\pm 0.$	populations it							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Name	#plants	#blossoms	GAD	GSD	SW	√GA	$\sqrt{BA}$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Small-glanded:							
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	D	2	4	$3.55 \pm 0.27$	$4.50 \pm 0.48$	$0.85 \pm 0.08$	$2.66 \pm 0.21$	38.71±2.41
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	СН	9	16	3.03±0.11	3.71±0.21	1.21±0.05	$2.90 \pm 0.12$	36.90±1.17
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	MO	3	6	$3.49 \pm 0.23$	$4.04 \pm 0.39$	$1.29 \pm 0.09$	2.91±0.20	37.78±1.98
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Е	9	15	3.97±0.16	5.12±0.31	$0.89 \pm 0.04$	2.95±0.13	36.94±1.15
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	V	15	29	$3.32 \pm 0.09$	$3.80 \pm 0.16$	$1.14 \pm 0.04$	$2.98 \pm 0.09$	$35.00 \pm 0.84$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	S	10	20	$3.07 \pm 0.11$	4.79±0.25	$1.13 \pm 0.04$	3.03±0.11	36.07±1.01
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	НО	4	8	2.88±0.15	3.57±0.29	$0.91 \pm 0.06$	$3.08 \pm 0.18$	33.69±1.51
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	CX	7	14	3.07±0.12	3.99±0.24	1.11±0.05	3.30±0.15	37.98±1.28
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	BR	2	4	3.46±0.26	4.79±0.54	1.11±0.09	3.31±0.27	$37.82 \pm 2.40$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	CO	11	22	3.26±0.10	3.43±0.16	1.15±0.04	3.37±0.12	37.89±0.98
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Р	7	14	3.11±0.13	3.50±0.21	$1.06 \pm 0.05$	3.37±0.15	35.94±1.18
Tovar diallel412821 $3.22\pm0.08$ $5.47\pm0.13$ $1.13\pm0.02$ $4.15\pm0.06$ $37.94\pm0.60$ Large-glanded populations:2 $5.49\pm0.38$ $4.20\pm0.27$ $1.38\pm0.09$ $3.99\pm0.19$ $38.50\pm1.81$ C1121 $5.26\pm0.19$ $6.43\pm0.22$ $1.35\pm0.05$ $4.47\pm0.12$ $46.72\pm1.18$ LM59 $5.00\pm0.31$ $6.07\pm0.33$ $1.47\pm0.08$ $4.70\pm0.19$ $53.94\pm2.07$ Tulum*916 $4.66\pm0.19$ $5.28\pm0.20$ $1.84\pm0.08$ $4.70\pm0.14$ $41.51\pm1.22$ CP12 $5.99\pm0.68$ $5.68\pm0.60$ $1.91\pm0.21$ $4.75\pm0.39$ $43.97\pm3.59$ PM1122 $5.57\pm0.20$ $5.36\pm0.18$ $1.69\pm0.06$ $4.81\pm0.12$ $45.06\pm1.15$ GS1223 $5.15\pm0.19$ $5.30\pm0.17$ $1.72\pm0.06$ $4.90\pm0.12$ $42.86\pm1.03$ CC2137 $6.34\pm0.19$ $5.70\pm0.16$ $1.32\pm0.04$ $5.00\pm0.10$ $46.99\pm0.88$ M1018 $4.86\pm0.20$ $5.60\pm0.21$ $1.60\pm0.06$ $5.07\pm0.14$ $47.47\pm1.22$ T1525 $5.03\pm0.16$ $5.67\pm0.18$ $1.75\pm0.06$ $5.10\pm0.12$ $45.40\pm1.11$ CN23 $5.93\pm0.59$ $6.09\pm0.59$ $1.42\pm0.13$ $5.51\pm0.39$ $51.73\pm3.39$ BA713 $5.29\pm0.24$ $4.98\pm0.21$ $1.71\pm0.08$ $6.11\pm0.20$ $51.59\pm1.60$ Tulum diallel562 $1042$ $4.63\pm0.04$ $4.61\pm0.05$ $1.36\pm0.01$ $4.37\pm0.04$ $38.19\pm0.34$ <	Tovar*	7	10	3.17±0.15	4.77±0.32	$1.06 \pm 0.06$	3.87±0.20	38.42±1.43
$\begin{array}{llllllllllllllllllllllllllllllllllll$	Tovar diallel	412	821	$3.22 \pm 0.08$	5.47±0.13	1.13±0.02	4.15±0.06	$37.94 \pm 0.60$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Large-glanded	populatic	ons:					
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	CA	4	6	$5.49 \pm 0.38$	4.20±0.27	$1.38 \pm 0.09$	3.99±0.19	38.50±1.81
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	С	11	21	5.26±0.19	6.43±0.22	$1.35 \pm 0.05$	4.47±0.12	46.72±1.18
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	LM	5	9	$5.00 \pm 0.31$	6.07±0.33	$1.47 \pm 0.08$	4.70±0.19	53.94±2.07
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Tulum*	9	16	4.66±0.19	$5.28 \pm 0.20$	$1.84{\pm}0.08$	4.70±0.14	41.51±1.22
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	СР	1	2	5.99±0.68	$5.68 \pm 0.60$	1.91±0.21	4.75±0.39	43.97±3.59
GS1223 $5.15\pm0.19$ $5.30\pm0.17$ $1.72\pm0.06$ $4.90\pm0.12$ $42.86\pm1.03$ CC2137 $6.34\pm0.19$ $5.70\pm0.16$ $1.32\pm0.04$ $5.00\pm0.10$ $46.99\pm0.88$ M1018 $4.86\pm0.20$ $5.60\pm0.21$ $1.60\pm0.06$ $5.07\pm0.14$ $47.47\pm1.22$ T1525 $5.03\pm0.16$ $5.67\pm0.18$ $1.75\pm0.06$ $5.10\pm0.12$ $45.40\pm1.11$ CN23 $5.93\pm0.59$ $6.09\pm0.59$ $1.42\pm0.13$ $5.51\pm0.39$ $51.73\pm3.39$ BA713 $5.29\pm0.24$ $4.98\pm0.21$ $1.71\pm0.08$ $6.11\pm0.20$ $51.59\pm1.60$ Tulum diallel5621042 $4.63\pm0.04$ $4.61\pm0.05$ $1.36\pm0.01$ $4.37\pm0.04$ $38.19\pm0.34$ Species averages: $3.24\pm0.20$ $4.22\pm0.43$ $1.07\pm0.09$ $3.27\pm0.23$ $36.86\pm1.04$ Large glanded $5.31\pm0.35$ $5.64\pm0.40$ $1.54\pm0.12$ $4.88\pm0.32$ $47.60\pm3.43$	PM	11	22	5.57±0.20	5.36±0.18	1.69±0.06	4.81±0.12	45.06±1.15
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	GS	12	23	5.15±0.19	5.30±0.17	$1.72 \pm 0.06$	4.90±0.12	42.86±1.03
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	CC	21	37	6.34±0.19	5.70±0.16	$1.32 \pm 0.04$	$5.00 \pm 0.10$	46.99±0.88
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	М	10	18	4.86±0.20	5.60±0.21	$1.60\pm0.06$	5.07±0.14	47.47±1.22
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Т	15	25	5.03±0.16	5.67±0.18	1.75±0.06	5.10±0.12	45.40±1.11
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	CN	2	3	5.93±0.59	6.09±0.59	$1.42\pm0.13$	5.51±0.39	51.73±3.39
Tulum diallel5621042 $4.63\pm0.04$ $4.61\pm0.05$ $1.36\pm0.01$ $4.37\pm0.04$ $38.19\pm0.34$ Species averages:3.24\pm0.20 $4.22\pm0.43$ $1.07\pm0.09$ $3.27\pm0.23$ $36.86\pm1.04$ Large glanded $5.31\pm0.35$ $5.64\pm0.40$ $1.54\pm0.12$ $4.88\pm0.32$ $47.60\pm3.43$	BA	7	13	5.29±0.24	4.98±0.21	1.71±0.08	6.11±0.20	51.59±1.60
Species averages:Small glandedLarge glanded3.24±0.204.22±0.431.07±0.093.27±0.2336.86±1.045.31±0.355.64±0.401.54±0.124.88±0.3247.60±3.43	Tulum diallel	562	1042	4.63±0.04	4.61±0.05	$1.36\pm0.01$	$4.37 \pm 0.04$	38.19±0.34
Small glanded3.24±0.204.22±0.431.07±0.093.27±0.2336.86±1.04Large glanded5.31±0.355.64±0.401.54±0.124.88±0.3247.60±3.43	Species average	es:						
Large glanded 5.31±0.35 5.64±0.40 1.54±0.12 4.88±0.32 47.60±3.43	Small glanded			3.24±0.20	$4.22 \pm 0.43$	$1.07 \pm 0.09$	3.27±0.23	36.86±1.04
	Large glanded			5.31±0.35	$5.64 \pm 0.40$	1.54±0.12	4.88±0.32	47.60±3.43

\* The Tulum and Tovar populations are descendants from the diallel populations, but measured by a different observer. For the species averages these data are used, but not the diallel data.

**Table S3.** Summary statistics (mean±SE) for the bract traits in the different populations and species (average of the populations). Description of how the parameters were obtained is given in Table S2.

Population	UBLc	UBLs	UBW	LBLc	LBLs	LBW	
Small-glanded p	opulations:						
D	19.80±1.23	16.22±0.93	19.86±1.36	21.28±1.46	$18.07 \pm 1.05$	21.57±1.50	
СН	$18.42 \pm 0.57$	15.79±0.46	18.57±0.62	20.20±0.70	17.21±0.49	$20.27 \pm 0.70$	
MO	18.66±0.99	$16.05 \pm 0.76$	19.39±1.13	20.35±1.18	$17.23 \pm 0.81$	21.27±1.28	
Е	18.99±0.61	16.20±0.49	17.47±0.61	21.79±0.75	18.55±0.54	19.93±0.72	
V	$17.86 \pm 0.42$	15.24±0.33	17.78±0.45	19.15±0.50	16.24±0.36	19.01±0.53	
S	$17.85 \pm 0.50$	15.35±0.39	18.55±0.59	19.01±0.59	16.87±0.43	19.77±0.67	
НО	17.26±0.74	15.13±0.60	16.97±0.86	18.37±0.87	$16.01 \pm 0.67$	$17.81 \pm 0.88$	
CX	19.34±0.66	16.07±0.51	19.46±0.76	20.68±0.76	17.27±0.53	20.91±0.86	
BR	$17.23 \pm 1.09$	$15.50 \pm 0.90$	19.87±1.37	$20.05 \pm 1.40$	16.91±0.94	22.02±1.60	
CO	$18.89 \pm 0.49$	15.98±0.39	19.90±0.60	20.81±0.60	$17.52 \pm 0.44$	20.61±0.64	
Р	17.47±0.59	15.33±0.49	19.08±0.72	18.85±0.67	16.31±0.49	$19.82 \pm 0.75$	
Tovar*	19.80±0.76	$17.28 \pm 0.64$	19.32±0.85	21.47±0.90	18.36±0.67	19.57±0.91	
Tovar diallel	18.97±0.31	16.54±0.26	19.49±0.33	21.24±0.38	18.27±0.32	19.99±0.34	
Large-glanded p	opulations:						
CA	19.37±1.07	17.12±0.94	$20.03 \pm 0.98$	20.95±1.11	17.85±0.86	19.95±0.99	
С	23.82±0.71	21.31±0.64	23.57±0.61	25.35±0.76	22.02±0.59	24.23±0.69	
LM	26.45±1.16	21.67±1.02	27.92±1.12	30.75±1.46	25.60±1.09	30.33±1.29	
Tulum*	$18.50 \pm 0.66$	17.22±0.59	22.59±0.66	21.40±0.75	19.06±0.61	22.89±0.73	
СР	21.53±1.98	$20.32 \pm 1.82$	23.86±2.05	23.14±2.03	20.57±1.68	21.95±1.94	
PM	21.91±0.67	$19.98 \pm 0.60$	$23.76 \pm 0.60$	24.25±0.69	20.67±0.56	23.47±0.61	
GS	19.98±0.59	18.33±0.56	23.29±0.61	22.28±0.62	19.26±0.50	23.62±0.64	
CC	24.45±0.54	22.55±0.53	$23.48 \pm 0.48$	25.90±0.60	22.66±0.48	23.88±0.53	
М	23.89±0.77	22.01±0.72	$24.65 \pm 0.75$	26.31±0.85	22.57±0.65	24.68±0.75	
Т	$20.48 \pm 0.58$	19.15±0.54	24.11±0.57	24.51±0.67	20.99±0.54	24.81±0.68	
CN	25.95±2.07	23.89±1.87	26.71±1.89	27.82±2.14	23.75±1.58	28.10±1.99	
BA	25.87±0.97	$23.34 \pm 0.88$	$27.62 \pm 0.93$	26.78±1.02	$23.50 \pm 0.78$	27.19±0.99	
Tulum diallel	$18.88 \pm 0.17$	16.63±0.13	$20.32 \pm 0.18$	$20.52 \pm 0.20$	17.38±0.16	$20.49 \pm 0.22$	
Species averages:							
Small glanded	18.61±0.58	15.98±0.46	$18.78 \pm 0.68$	$20.33 \pm 0.80$	17.39±0.62	20.01±0.83	
Large glanded	23.45±1.92	$20.83 \pm 1.46$	24.76±0.18	26.03±1.92	22.29±1.56	25.40±1.72	

\* The Tulum and Tovar populations are descendants from the diallel populations, but measured by a different observer. For the species averages these data are used and not the diallel data.

**Table S4.** Posterior distribution of the Tovar G-matrix for the functional traits, provided in the external file "G\_posterior\_Tovar\_functional\_traits.csv" (comma delimited). The traits are on mean standardized scale. Each row is one sample from the joint posterior distribution. The columns are the elements of the G-matrix given row wise (or column vise, the matrix is symmetrical). The format of the column names are best described by an example. The column with name GAD:GAD gives the posterior distribution of the variance in GAD, while the column with name GAD:GSD gives the posterior distribution of the covariance between GAD and GSD. Note that  $\sqrt{GA}$  and  $\sqrt{BA}$  are simplified to GA and BA. The file can be read into R by the command:

G = read.csv("filename.csv"). The posterior median of each matrix element can be computed, and printed in matrix format, by the command: matrix(apply(G, 2, median), ncol = sqrt(ncol(G))).

**Table S5.** Posterior distribution of the Tulum G-matrix for the functional traits, provided in the external file "G\_posterior\_Tulum\_functional\_traits.csv". See table S4 for explanation.

**Table S6.** Posterior distribution of the Tovar G-matrix for the bract traits, provided in the external file "G\_posterior\_Tovar\_bract\_traits.csv". See table S4 for explanation.

**Table S7.** Posterior distribution of the Tulum G-matrix for the bract traits, provided in the external file "G\_posterior\_Tulum\_bract\_traits.csv". See table S4 for explanation.



### **Functional traits**

**Conditional evolvability (%) Conditional evolvability (%) Figure S1** Scaling relationship between evolutionary rate ( $\sigma^2_{rate}$ ) and the evolvability estimates for a population of the other species for the functional traits. Grey circles represent 1000 uniformly distributed random directions (selection gradients). The solid line indicates the isometric relationship (a slope of 1) through the mean of the random directions. Crosses are the measured traits, squares are the directions with highest or lowest trait divergence, and black circles are the directions with highest and lowest evolvability out of the 1000 random directions. The circles, crosses, and squares are the modes from the posterior distributions and the grey lines give the 95% highest posterior density intervals. The vertical dotted lines are the posterior modes for the parameters named above each plot, and the vertical thick grey bars are their 95% highest posterior density intervals (see Table 2). The differences between minimum and maximum evolvability and the lowest and highest evolvability of the random directions are partly due to sampling error and partly due to bias in the estimates of  $e_{min}$  and  $e_{max}$ .



**Figure S2** Scaling relationship between evolutionary rate ( $\sigma^2_{rate}$ ) and the evolvability estimates for a population of the other species for the bract traits. See Figure S1 for explanation of symbols.

# **Bract traits**

# **Functional traits**



**Figure S3.** Scaling relationship between respondability, computed along selection gradients, and evolutionary rates ( $\sigma^2_{rate}$ ), computed along corresponding response vectors, for the functional traits. Unit length response vectors are given by  $\mathbf{G\beta}/||\mathbf{G\beta}||$ , where  $\boldsymbol{\beta}$  is the column vector of the corresponding unit length selection gradient and  $||\mathbf{x}||$  denotes the norm of  $\mathbf{x}$ . See Figure S1 for explanation of symbols. Note that the traits are not included in this figure as we do not have information about the direction.



**Figure S4.** Scaling relationship between respondability, computed along selection gradients, and evolutionary rates ( $\sigma^2_{rate}$ ), computed along corresponding response vectors, for the bract traits. See Figure S3 for further explanation.

#### **Appendix A: Tracking optimum model**

Here we consider a simplified model of a trait tracking an optimum that moves according to an Ornstein-Uhlenbeck process. We assume the selection gradient on the trait is  $\beta = -2s(z - \theta)$ , where z is (log) trait mean and  $\theta$  is the optimum. The parameter s is the (mean-scaled) curvature of an assumed quadratic fitness function. The model is

$$dz = e\beta = -2es(z - \theta)dt, d\theta = -\alpha\theta dt + \sigma dB,$$

where dz,  $d\theta$ , and dt are differentials in the trait mean, optimum and time, respectively, e is the evolvability, dB is white noise (i.e. the stochastic differential of a unit variance Brownian motion), and  $\alpha$  and  $\sigma$  are parameters describing the Ornstein-Uhlenbeck process. By use of Ito's formula for stochastic differentiation we can then form the stochastic differentials:

$$\begin{aligned} dz^2 &= 4ez(\theta - z)dt, \\ dz\theta &= (2es\theta(\theta - z) - \alpha\theta z)dt + \sigma zdB, \\ d\theta^2 &= (\sigma^2 - 2\alpha\theta^2)dt + 2\sigma\theta dB, \end{aligned}$$

By integrating these over the joint distribution of z and  $\theta$ , we can form differential equations in the first and second moments of the distribution

$$dE[z] = e\beta = -2es(E[z] - E[\theta])dt,$$
  

$$dE[\theta] = -\alpha E[\theta]dt,$$
  

$$dE[z^2] = 4es(E[z\theta] - E[z^2])dt,$$
  

$$dE[z\theta] = (2esE[\theta^2] - (2es + \alpha)E[z\theta])dt,$$
  

$$dE[\theta^2] = (\sigma^2 - 2\alpha E[\theta^2])dt,$$

where E[x] denotes expectation of x. Because the model is a system of linear stochastic differential equations, the distribution of the variables is multivariate normal, and the time development of these moments fully specify the time development of the distribution. These equations can be solved to find the time development of the system, but for the present purpose it suffices with the stationary distribution, which can be found by setting all the differentials to zero and solve for the moments. This gives

$$\operatorname{Var}[z] = V \frac{2es}{2es+\alpha},$$

where  $V = \sigma^2/2\alpha$  is the stationary variance of the optimum,  $\theta$ . Note that if the dynamics of the optimum converges on a white noise, i.e. that  $\alpha \to \infty$  and V stays constant, the variance in the trait mean goes to zero. This is because the optimum moves so fast that the trait can not track it. More generally, if the characteristic time of the optimum,  $1/\alpha$ , is much shorter (i.e. faster) than the characteristic time of the adaptation, 1/2es, then the variance of the trait mean goes to zero, because the trait mean can not track the movements of the optimum. If, on the other hand, the adaptation is much faster than the movements of the optimum, the trait mean will track the optimum perfectly, and the variance of the trait mean converges on the variance of the optimum, V.

If the Ornstein-Uhlenbeck process for the optimum converges on a Brownian motion, that is,  $\alpha \to 0$ , and  $\sigma$  is finite, the variance of the optimum is no longer stationary and evolves as  $\sigma^2 t$ . Under these conditions the variance of the trait mean evolves as

$$\operatorname{Var}[z] = \sigma^{2}t - \frac{3\sigma^{2}}{4es} \left(1 + 3\operatorname{Exp}[-4est] - \frac{4}{3}\operatorname{Exp}[-2est]\right) \approx \sigma^{2}t - \frac{3\sigma^{2}}{4es}$$

where Exp is the exponential function and the approximation is for large *t*. This means that the variance of the trait mean eventually settles on the same rate of increase as the variance of the optimum, but with a constant lag that is inversely proportional to the evolvability.

#### **Appendix B: Construction of the Phylogeny**

We constructed the phylogenetic relatedness as follows. Genomic DNA was extracted from leaf tissue using E-Z 96 Pland DNA Kit (Omega Bio-Tek, Norcross, GA, USA). Multiplex PCR reactions were prepared in a total volume of 10  $\mu$ l containing 5  $\mu$ l of 2x type-it Microsatellite PCR Kit (QIAGEN, Hilden, Germany), 1 µl of extracted DNA (10 ng) and 1 µl primer (vary in concentration 0.1-0.4 µM). The thermal condition was set to 95 ° C for 5 min for initial denaturation; 10 initial cycles as touchdown at 94 ° C for 30 s, 60–50 ° C for 45 s, 72 ° C for 45 s; 25 cycles at 94 ° C for 30 s, 50 ° C for 45 s, 72 ° C for 45 s; and final extension at 72 ° C for 10 min in an ABI 9600 thermal cycler (Applied Biosystems, Foster City, California, USA). The 5' end of forward primers for 70 microsatellite loci was labeled with four different fluorophores (6-FAM, HEX, NED, and PET); and fragment analysis was conducted with an ABI 3130xl Genetic Analyzer (Applied Biosystems). Microsatellite alleles were scored using GeneMapper software version 4 (Applied Biosystems). Seventy microsatellite markers (Table S8) that have been recently developed in D. scandens were screened in 76 individuals (Falahati-Anbaran et al., 2013; Falahati-Anbaran et al., Unpublished). In total 23 Mexican populations from different regions of the country and one Venezuelan population were used in this study (Table S9). A neighbour-joining phylogenetic tree (Saitou & Nei, 1987) was constructed at the population level based on the genetic distance D<sub>A</sub> described in Nei et al.(1983) using Populations 1.2.31 program freely available at http://bioinformatics.org/~tryphon/populations/. The branch lengths of the phylogenetic tree were nearly of equal length when the tree was rooted on the centre, and was further ultrametrized by the function "chronopl" in the R-package "ape" (Paradis et al. 2004) with the parameter lambda set to unit, which gives a clock-like model.

Locus	Number of alleles	Size range (base pair)
CCdi4	14	190-218
CCdi9	6	102-126
CCdi10	13	199-247
CCdi11	14	304-340
CCdi13	7	98-115
CCdi23	5	159-172
CCdi24	4	133-148
CCdi25	6	220-241
CCdi27	9	68-86
CCdi29	7	53-75
CCdi33	4	180-196
CCdi38	5	106-118
CCdi39-1	20	313-378
CCdi39-2	4	90-96
CCdi41	8	198-231
CCdi45	6	102-127
CCdi47	4	216-236
CCdi50	19	263-316
CCdi52	4	70-78
CCdi53	16	101-133
CCdi54	12	272-301
CCdi63	3	128-132
CCdi67	11	156-181
CCdi71	3	194-200
CCdi74	6	144-173
CCtri1	1	168
CCtri2	6	77-86
CCtri3	4	88-98
CCtri6	13	97-136
CCtri8	3	165-198
CCtri10	4	175-184
CCtri13	11	215-230
CCtri14-1	5	97-119
CCtri14-2	5	78-85
CCtri15	4	124-127
CCtri17	9	207-248
CCtri21	6	138-157

**Table S8** List of microsatellite loci used to construct phylogenetic tree for *Dalechampia scandens* populations.

Locus Number of alleles Size range (base pair)	
Edi2-1 8 134-147	
Edi2-2 13 264-300	
Edi5 11 116-139	
Edi6 5 179-185	
Edi8 2 251-280	
Edi9 4 228-246	
Edi10 13 239-268	
Edi11 2 212-214	
Edi13 8 104-126	
Edi14 5 138-164	
Edi17 19 279-309	
Edi20 3 97-101	
Edi22 5 96-106	
Edi23 9 133-152	
Edi33 7 288-321	
Edi34 10 86-109	
Edi41 11 182-214	
Etril 3 172-177	
Etri2 12 264-308	
Etri4 1 216	
Etri5 4 140-152	
Etri9 8 216-237	
Etri11 7 262-283	
Etri12 5 144-159	
Etri13 4 147-157	
Etri14-1 3 126-132	
Etri14-2 7 183-203	
Etri15 6 117-190	
Etri16 3 160-166	
Etri17 2 88-91	
Etet4 1 348	
Etet7 4 121-133	
Etet12 3 126-134	

 Table S8 Continues.

		Number of
Population	Abbreviation	samples
Carillo Puerto	СР	1
Champotón	CN	2
Cacalchén	CA	3
Comalcalco	С	4
Bacalar	BA	4
Graciano Sánches	GS	3
La Mancha	LM	5
Martinez de la Torre	Μ	4
Tulúm	Т	4
Tulúm diallel		2
Puerto_Morelos	PM	4
Ciudad del Carmen	CC	4
Bolonchén de Rejón	BR	1
Hopelchen	НО	2
Motul de Carillo Puerto	MO	3
China	СН	4
Dzemul	D	2
Peto	Р	3
Santa Elena	S	3
El Limón	E	4
Chemax	СХ	4
Cozumel	СО	4
Valladolid	V	4
Tovar diallel		2

**Table S9** Number of individuals used for microsatellite analyses from *Dalechampia scandens* populations. All populations are distributed throughout Mexico except that Tovar is collected from Venezuela.

## Appendix C: The R-package "evolvability"

The package evolvability contains functions for calculating evolvability parameters described in Hansen and Houle (2008, 2009). The package is distributed through <a href="http://cran.r-project.org/">http://cran.r-</a> <a href="project.org/">project.org/</a>. Updates and additions of this package will be published on the CRAN package repositories. The following functions are currently implemented:

evolvabilityMeans calculates average evolvability, conditional evolvability, respondability, autonomy, integration, maximum evolvability and minimum evolvability from a given G-matrix using the approximation equations in Hansen and Houle (2008)

evolvabilityMeansMCMC calculates the same as evolvabilityMeans, only over a posterior distribution of a G-matrix.

evolvabilityBeta calculates evolvability, conditional evolvability, respondability, autonomy, and integration along each given selection gradient. The function also calculates averages, minimum, and maximum values over a set of given selection gradients.

evolvabilityBetaMCMC calculates the same as evolvabilityBeta, only over a posterior distribution of a G-matrix.

evolvabilityBetaMCMC2 calculates evolvability, conditional evolvability, respondability, autonomy, and integration along one selection gradient when both the G-matrix and the selection gradient is given by a posterior distribution.

randomBeta generates a set of selection gradients uniformly distributed in a hypersphere of dimension k.

meanStdG mean standardizes a G-matrix given the corresponding means. Note that mean standardization is only meaningful for traits on a ratio or log-interval scale. Traits on these scales have a meaningful (unique and non-arbitrary) zero value.

meanStdGMCMC mean standardizes the posterior distribution of a G-matrix by the corresponding posterior distribution of the means.

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