Effects of behavioral response and vaccination policy on epidemic spreading - an approach based on evolutionary-game dynamics

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(Dated: June 3, 2014)

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Figure S1: Quantitative characterization of impacts of the selection strength *β* on epidemic spreading for partial- and free-subsidy policies for small vaccination cost. For homogeneous small-world networks $[1, 2]$ and cost of vaccination $c = 0.2$, vaccination coverage $(V,$ top panels) and epidemic size (R , bottom panels) for the two subsidy policies for $\delta = 0.1$, 0.4 and 0.7 (corresponding to the left, central, and

right panels, respectively). Insets in the top panels show the difference in the vaccination coverage, $V_P - V_F$, between the partial- and free-subsidy policies. Insets in the bottom panels display the difference in epidemic size, $R_P - R_F$, between the two subsidy policies. Blue squares in the insets are simulation results, and the red circles are the theoretical predictions based on the mean-field method (see analysis in **Methods** in main text). Other parameters are: network size $N = 1000$, transmission rate $\lambda = 0.072$, $\mu = 0.25$ and average degree $\bar{k} = 10$.

Figure S2: Impacts of the selection strength *β* on epidemic dynamics for the Barabasi-Albert scale-free networks [3] for small ´ vaccination cost. Vaccination coverage *V* (top panels) and epidemic size *R* (bottom panels) under the two subsidy policies for scale-free networks for $c = 0.2$ and $\delta = 0.1$, 0.4 and 0.7 (corresponding to the left, central, and right panels, respectively). Insets in top and bottom panels show the difference in the vaccination coverage, $V_P - V_F$, and the difference in the final epidemic size, $R_P - R_F$, respectively, between the two subsidy policies, where the blue squares and red circles are simulation results and mean-field based theoretical prediction (see analysis in **Methods**), respectively. Other parameters are: $N = 1000$, $\lambda = 0.18$, and average degree $\langle k \rangle = 6$.

Figure S3: Quantitative characterization of impacts of the selection strength *β* on epidemic spreading for partial- and free-subsidy policies for small vaccination cost. For configuration network [4] (degree distribution $P(k) \sim k^{-3}$ with network size $N = 2500$, minimum degree $k_{min} = 4$, and maximal degree $k_{max} = 50$.) and cost of vaccination $c = 0.2$, vaccination coverage (*V*, top panels) and epidemic size (*R*, bottom panels) for the two subsidy policies for $\delta = 0.1$, 0.4 and 0.7 (corresponding to the left, central, and right panels, respectively). Insets in the top panels show the difference in the vaccination coverage, *V^P − V^F* , between the partial- and free-subsidy policies. Insets in the bottom panels display the difference in epidemic size, *R^P − R^F* , between the two subsidy policies. Blue squares in the insets are simulation results, and the red circles are the theoretical predictions based on the mean-field method (see analysis in Methods). Other parameters are: transmission rate $\lambda = 0.15$, $\mu = 0.25$ and average degree $\langle k \rangle = 8$.

Figure S4:Quantitative characterization of impacts of the selection strength *β* on epidemic spreading for partial- and free-subsidy **policies for intermediate vaccination cost**. For configuration network and cost of vaccination $c = 0.5$, vaccination coverage (*V*, top panels) and epidemic size (*R*, bottom panels) for the two subsidy policies for $\delta = 0.1$, 0.4 and 0.7 (corresponding to the left, central, and right panels, respectively). Others are the same as for Fig. S3.

Figure S5:Quantitative characterization of impacts of the selection strength *β* on epidemic spreading for partial- and free-subsidy policies for large vaccination cost. For configuration network and cost of vaccination $c = 0.9$, vaccination coverage (V , top panels) and epidemic size (R , bottom panels) for the two subsidy policies for $\delta = 0.1$, 0.4 and 0.7 (corresponding to the left, central, and right panels, respectively). Others are the same as for Fig. S3.