Supporting Material

Mechanical properties of base-modified DNA are not strictly determined by base stacking or electrostatic interactions

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S.1 DNA Characterization

DNA Constructs

Cloned intrinsically straight ∼200-bp sequences were created using unique 5-bp direct repeats to eliminate long-range sequence-directed curvature [\(1\)](#page-21-1) and were the kind gift of A. Vologodskii. [Figure S.1](#page-2-0) shows the longest construct in a series with flanking NarI sites [\(2\)](#page-21-2), designated pJ1506.

Plasmid pJ1506

Figure S.1: Plasmid pJ1506. Forward (LJM-3222, LJM-4762) and reverse (LJM-3223, LJM-4763) primers are used to PCR amplify fragments for tweezers (cyan), AFM (magenta), and cyclization (orange), all of which share central NarI restriction sites (bold red) flanking the 5-bp direct repeats.

Thermal Denaturation

Stability of Inosine-substituted DNA Duplex

Thermal denaturation experiments monitored SYBR Green I (Invitrogen) fluorescence using an ICycler thermocycler (BioRad) over a temperature range of 50–100◦C, measurements collected every 0.1[°]C with a temperature slope of $24°C/h$. DNA fragments 418 base pairs in length with inosine completely replacing guanosine were PCR amplified from pJ1506 using conditions described in Materials and Methods (main manuscript). Samples (20 µL) contained 100 ng DNA (∼30 nM) in 10 mM sodium cacodylate, pH 6.6 with 10 mM NaCl and either 0.06X, 0.08X, 0.1X, or 0.2X SYBR Green I (Invitrogen).

The melting temperature (T_m) and change in standard free energy (ΔG°) , enthalpy (ΔH°) , and entropy (ΔS°) of a melting reaction were determined using the classic van't Hoff equation assuming a two-state transition model as described previously [\(2\)](#page-21-2). This analysis assumes that the van't Hoff plots are absolutely linear, that ΔH° and ΔS° are temperature independent, and that there is no change in heat capacity for the melting transition, i.e. $\Delta C_p = 0$. Slight curvature in van't Hoff plots due to $\Delta C_p \neq 0$ can lead to significant errors in graphically evaluated thermodynamic parameters. However, since the enthalpies and entropies derived in this graphical manner are correlated, the relative error of ΔG° is typically smaller than the relative errors of ΔH° and ΔS° .

To eliminate the effects of potential binding affinity differences of the dye, each experiment was performed in triplicate for a given dye concentration, and dye-free values of the parameters were determined by linear extrapolation to zero dye concentration. The current and previously reported [\(2\)](#page-21-2) parameter estimates in [Table S.1](#page-3-0) are the mean and standard deviation from three independent repeats of this extrapolation procedure.

Table S.1: Estimates of thermodynamic parameters from thermal denaturation of inosine-substitued DNA. The reported values of melting temperature (T_m) and change in standard free energy (ΔG°) , enthalpy (ΔH°) , and entropy (ΔS°) of the dissociation reaction are the mean and standard deviation from three independent repeats. Data collected for inosine-substituted DNA are compared to data previously reported [\(2\)](#page-21-2) for natural and diaminopurine-substituted DNA.

DNA	T_m (°C)		ΔH° (kcal mol ⁻¹) ΔS° (cal mol ⁻¹ K ⁻¹) ΔG°_{37} (kcal mol ⁻¹)	
natural	87.1 ± 0.5	400 ± 50	1100 ± 130	56 ± 7
diaminopurine 93.0 ± 0.5		490 ± 30	1350 ± 80	76 ± 5
inosine	72.8 ± 2.3	370 ± 30	1060 ± 90	$45 + 4$

Inosine Free Energy of Stacking

The stacking ability of an unpaired nucleotide (X) was evaluated from "dangling end" thermody-namic measurements of the self-complementary DNA oligonucleotide 5'-XCGCGCG [\(2\)](#page-21-2). The oligo with $X = 2'$ -deoxyinosine (I) was purchased from TriLink BioTechnologies. Thermal denaturation experiments monitored SYBR Green I (Invitrogen) fluorescence using an ICycler thermocycler (BioRad) over a temperature range of $20-80°C$, measurements collected every $0.1°C$ with a temperature slope of 24°C/h. Samples (20 µL) contained 300–900 ng DNA (∼5–25 µM) in 10 mM sodium phosphate, pH 7.0 with 1 M NaCl and either 0.05X, 0.1X, 0.15X, or 0.2X SYBR Green I (Invitrogen). The thermal denaturation data were processed following a two-state transition model as described previously [\(2\)](#page-21-2). Briefly, the two states are referred to as "folded" (fully associated) and

"unfolded" (fully dissociated) for simplicity. The data were converted from fluorescence (F) as a function of temperature (T) to fraction folded (θ) as a function of temperature

$$
\theta(T) = \frac{F(T) - u(T)}{f(T) - u(T)}\tag{S.1}
$$

where the unfolded (u) and folded (f) baselines were determined from the data by linear regression. Within the analysis interval $(0.15 < \theta < 0.85)$ the melting temperature (T_m) was evaluated from $\theta =$ 0.5. To eliminate the effects of potential binding affinity differences of the dye, each experiment was performed in triplicate for a given dye concentration, and dye-free values of T_m were determined by linear extrapolation to zero dye concentration. Values for the thermodynamic parameters (assumed independent of temperature) were determined by fitting (linear regression analysis) plots of T_m^{-1} as a function of the natural logarithm of DNA concentration $ln(C_t)$

$$
\frac{1}{T_m} = \frac{R}{\Delta H^{\circ}} \ln C_t + \frac{\Delta S^{\circ}}{\Delta H^{\circ}}
$$
\n(S.2)

where R is the ideal gas constant (details about this variation of the van't Hoff equation have been discussed elsewhere) [\(2\)](#page-21-2). Finally, ΔG ^{*°*} was determined from the Gibbs free energy equation

$$
\Delta G^{\circ} = \Delta H^{\circ} - T\Delta S^{\circ} \tag{S.3}
$$

[Figure S.2](#page-4-0) compares the new data for I to data previously reported [\(2\)](#page-21-2).

Figure S.2: van't Hoff plots of dangling DNA nucleotides. Data collected for I are compared to data previously reported [\(2\)](#page-21-2).

The current and previously reported [\(2\)](#page-21-2) parameter values in [Table S.2](#page-5-1) are the mean and standard deviation from three independent repeats. Stabilization of the core sequence duplex from base stacking is reported as both ΔT_m and $\Delta \Delta G^{\circ}$. While I stabilized the core hexamer duplex, it displayed the least increase in T_m , only 5.1°C, and least favorable free energy of stacking $(\Delta\Delta G_{37}^{\circ})$, only 0.7 kcal/mol. Thus, in dangling end experiments I is a poorer stacker than the G it replaces. As reported previously [\(2\)](#page-21-2), D is a better stacker than the A it replaces, and the overall stacking order for these nucleotides is $D > A > G > I$.

$\boldsymbol{\mathrm{X}}$	T_m (°C) for ΔT_m (°C)		ΔH°	ΔS°	ΔG_{37}°	$\Delta\Delta G_{37}^\circ$
	$5 \mu M$ DNA		(kcal/mol)	$(cal/mol-K)$	(kcal/mol)	(kcal/mol)
core	49.5 ± 0.4	$\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$ and $\mathcal{L}^{\mathcal{L}}(\mathcal{L}^{\mathcal{L}})$	37 ± 2	89 ± 6	8.9 ± 0.1	
A	56.6 ± 0.3	7.1 ± 0.5	41 ± 3	101 ± 10	10.0 ± 0.2	1.1 ± 0.2
G	55.5 ± 0.4	6.0 ± 0.6	38 ± 4	92 ± 13	9.7 ± 0.3	0.8 ± 0.3
D		61.3 ± 0.6 11.8 \pm 0.7	42 ± 7	101 ± 22	10.6 ± 0.6	1.7 ± 0.6
\mathbf{I}		54.6 ± 0.5 5.1 ± 0.6	38 ± 4	93 ± 13	9.6 ± 0.3	0.7 ± 0.3

Table S.2: Free energy of stacking $(\Delta \Delta G^{\circ}_{37})$ for inosine (I) determined from dangling end thermal denaturation. Data collected for I are compared to data previously reported [\(2\)](#page-21-2).

S.2 Atomic Force Microscopy (AFM)

Background

Biopolymers like DNA can be visualized using atomic force microscopy (AFM), with the goal of deriving mechanical properties (e.g. persistence length). Since AFM is a surface technique, however, the way in which the molecules adhere to the surface must be considered. The high charge density of DNA allows for its immobilization onto a planar two-dimensional surface by virtue of ionic interactions between DNA phosphates and surface charges. The adsorption of DNA onto (negatively-charged) mica surfaces is typically promoted using either divalent cations or polyamines. Two modes of DNA adsorption have been proposed [\(3\)](#page-21-3): i) strong adsorption without equilibration (i.e. kinetic trapping) leading to a conformation reflecting a projection of the DNA conformation in solution onto a plane and ii) weak adsorption so that the DNA molecule has time to freely equilibrate on the surface before immobilization in a particular two-dimensional equilibrium conformation. These processes diminish the number of possible DNA configurations; therefore, any quantitative description of the apparent DNA conformation confined to a plane requires twodimensional (2D) reformulation of the existing models for three-dimensional (3D) conformations. In particular, the wormlike chain (WLC) model has proven to be an effective theory of DNA mechanics that can successfully describe experiments on single DNA molecules in two or three dimensions [\(4\)](#page-21-4).

Image Processing and Data Analysis

Intrinsically straight DNA fragments 753 bp in length and containing the desired base substitutions were prepared for AFM studies. The 3D image in [Figure S.3](#page-6-0) shows 2D equilibrium conformations of

Figure S.3: AFM image.

these DNA fragments when subjected to thermal fluctuations. From a large set of images collected for each DNA variant, the DNA molecules were digitized into pixel skeletons using an algorithm previously described [\(5\)](#page-21-5) and illustrated in [Figure S.4.](#page-6-1)

Figure S.4: Image processing. AFM images (a) were transformed into bi-color maps (b) with a threshold. Pixels above the threshold were then iteratively eroded from the edge of the DNA segments, if the removal of a pixel did not severe the segment. This thinning process was repeated until no more pixels could be removed, leaving behind DNA skeletons only one pixel wide (c) for later analysis.

The generated sets of pixel coordinates (skeletons) were aligned along the positive x-axis in [Figure S.5\(](#page-7-0)a), graphically illustrating the bending stiffness. Next, the skeletons were analyzed to determine the distribution of DNA contour lengths using the (n_e, n_o, n_c) -based corner chain estimator [\(6\)](#page-21-6). When the next pixel in the DNA skeleton only has one coordinate (x or y) different from the previous pixel, the segment between two pixels is considered even. If both coordinates $(x \text{ and } y)$ are different from the previous pixel, the segment is considered odd. If moving from

Figure S.5: Analysis of DNA pixel skeletons.

one pixel to the next there is an odd to even or even to odd transition, the segment is treated as a corner. Therefore, (n_e, n_o, n_c) represents the number of even, odd, and corner segments in the DNA skeleton. For the corner chain estimator (6) , the contour length is given by

$$
L_C = 0.980n_e + 1.406n_o - 0.091n_c
$$
\n(S.4)

The values of L_C appear normally distributed, as shown in [Figure S.5\(](#page-7-0)b), with mean and standard deviation reported in [Table S.3](#page-7-1) for the indicated number of skeletons, N. Only DNA molecules satisfying the following criteria were included in the data set for analysis: i) both ends were visible and the molecule was not in touch with (or crossed over by) any other molecules and ii) the estimated contour length L_C fell within the range 100–400 nm (bounds chosen given the expected contour length of ∼250 nm for natural DNA). Although the detection and thinning of the molecules was automated, a human supervisor could reject erroneously segmented skeletons or those not meeting the above criteria during interactive steps.

DNA variant	$N_{\rm c}$	L_C (nm)	$h\left(\rm \AA/bp\right)$
natural	166-	$234 + 26$	3.11 ± 0.34
diaminopurine		$146 \quad 229_{\pm 27}$	3.04 ± 0.36
inosine		$172 \quad 221 + 30$	2.93 ± 0.40

Table S.3: Summary of DNA pixel skeletons

The value for DNA helical rise (h) was determined by dividing the average estimated contour length by the expected total number of base pairs, [Table S.3.](#page-7-1) As reported in previous studies [\(3,](#page-21-3) [6,](#page-21-6) [7,](#page-21-7) [8\)](#page-21-8) estimates of helical rise determined using tapping-mode AFM in air (e.g. $h = 3.11 \pm 0.34$ $\rm \AA/bp$ for natural DNA) underestimate the 3.38 $\rm \AA/bp$ value measured by crystallography.

After detection of DNA skeletons, the trajectories of DNA centerlines were extracted automatically (but with human supervision) using a routine developed with the particular goal of analyzing local bend angles [\(9\)](#page-21-9), as shown in [Figure S.6.](#page-8-0) This initial analysis revealed the importance of step

Figure S.6: Generating DNA centerline representations. Using the algorithm of Wiggins *et al.* [\(9\)](#page-21-9) along with start and end points¹ defined from the pixel skeletons, (x, y) coordinate pairs separated by step size l were generated for each DNA molecule using each of $l = 3, 4, 5, ..., 17$ nm.

sizes in the range 4–9 nm so that subsequent coordinate representations were generated for each of $l = 4, 4.25, 4.5, \ldots, 9$ nm. From a set of coordinates (which can be thought of as a representation of the DNA axis) we computed statistical quantities such as the the Euclidean distance between

 1 ¹The true end point actually lies within a circular region centered on the pixel end point with radius equal to one percent of the chosen step size.

the first and the last points of a DNA representation with contour length separation distance d (where d is an obligate multiple of l), the so called end-end distance $R(d)$.^{[2](#page-9-0)} Extra precaution was taken during sampling to avoid intrinsic correlations. It is known that reusing data (i.e. computing a quantity for each separation distance along a DNA contour) yields highly correlated points [\(7\)](#page-21-7). To avoid this, each DNA representation was randomly dividend into shorter length segments such that no piece was used twice and the maximal segment length was restricted to 80% of the expected contour length (∼200 nm). This yielded a logarithmic distribution of the segment lengths, [Fig](#page-9-1)[ure S.7.](#page-9-1) Additionally, non-overlapping logarithmic sampling of the DNA representations allowed

Figure S.7: Non-overlapping logarithmic sampling of DNA representations generated with the indicated step size l.

for estimation of the statistical reliability of the measurements. The error bars in [Figure S.7](#page-9-1) (and [Figure S.9](#page-11-0) – [Figure S.16\)](#page-16-0) show one standard deviation computed from 1000 different random draws from the same set of DNA representations. For the quantities that are quotients we applied error propagation to determine the standard deviation.

The measured quantities were then fit with corresponding equations from wormlike chain (WLC) theory. The WLC model captures the entropic elastic behavior of a semi-flexible biopolymer through idealization as an intrinsically straight, inextensible elastic rod [\(10\)](#page-21-10). In fact, the WLC model is the continuous limit of the discrete freely rotating chain, as illustrated in [Figure S.8.](#page-10-0) For a chain of contour length L ($L \equiv nl$ for the discrete chain of n segments of length l), the end-end distance vector **R** is given from the unit tangent vector $\mathbf{u}(s)$ at arc length position s by

$$
\int_{0}^{L} \mathbf{u}(s) ds = \mathbf{R}
$$
 (S.5)

In the WLC model, bending deformations induced by thermal fluctuations (k_B) is the Boltzmann constant and T is the absolute temperature) are attributed to a classical (obeying Hooke's law) elastic energy function

$$
\frac{E_{\text{WLC}}}{k_B T} = \frac{P\theta^2}{2d} \tag{S.6}
$$

where the elastic bend constant P controls the exponential decay of the orientational correlation between unit tangent vectors separated by curvilinear (arc length) distance d with angle θ between them [\(Figure S.8\)](#page-10-0)

$$
\langle \mathbf{u}(s') \cdot \mathbf{u}(s'+d) \rangle = e^{-\frac{d}{P}}
$$
\n(S.7)

²Clearly, $R \equiv R(d)$ is a function of arc length separation d, but only R is written for simplicity. Similarly, $\theta(d)$ and other length and angle moments will be assumed implicit functions of d.

Figure S.8: Comparison of the continuous wormlike chain (WLC) with the discrete freely rotating chain (FRC) and illustration of the geometric quantities discussed in the text.

and the $\langle \ \rangle$ notation stands for averaging over thermal realizations. [Equation S.7](#page-9-2) can be reinterpreted using the definition of scalar projection as

$$
\langle \cos \theta \rangle = e^{-\frac{d}{P}} \tag{S.8}
$$

The elastic bend constant P is referred to as the *persistence length* (length through which the memory of the initial orientation of the chain persists) and quantifies the chain's resistance to bending. The bending energy function E_{WLC} is called classical (or harmonic) because it is a quadratic function of the bending strain variable θ . The probability distribution of θ (angular distribution function) is given by Boltzmann statistics

$$
G(\theta; d, P) = \frac{e^{-\frac{P\theta^2}{2d}}}{\int_{-\infty}^{\infty} e^{-\frac{P(\theta')^2}{2d}} d\theta'} = \sqrt{\frac{P}{2\pi d}} e^{-\frac{P\theta^2}{2d}}
$$
(S.9)

Thus, the harmonic energy function makes the WLC angular distribution Gaussian. However, even if E is chosen to be non-harmonic, the angular distribution will approach a Gaussian form at large separations d because the iterated convolution of any distribution with itself converges to a Gaussian form. That is, even if non-harmonic elastic behavior is present, it will be hidden on long length scales by thermal fluctuations. The prediction that $G(\theta)$ is normally distributed can be explored by examining the moments of θ , which are given by

$$
\langle \theta^m \rangle = \int_{-\infty}^{\infty} \theta^m G(\theta) \, d\theta \tag{S.10}
$$

All odd moments are zero (regardless of dimensionality of the molecules)

$$
\langle \theta \rangle = \langle \theta^3 \rangle = \langle \theta^5 \rangle = \ldots = 0 \tag{S.11}
$$

as [Figure S.9](#page-11-0) demonstrates

$$
\frac{\langle \theta \rangle}{\langle \theta^2 \rangle^{\frac{1}{2}}} \approx \frac{\langle \theta^3 \rangle}{\langle \theta^2 \rangle^{\frac{3}{2}}} \approx \frac{\langle \theta^5 \rangle}{\langle \theta^2 \rangle^{\frac{5}{2}}} \approx \frac{\langle \theta^7 \rangle}{\langle \theta^2 \rangle^{\frac{7}{2}}} \approx 0
$$
\n(S.12)

Figure S.9: First four odd moments of θ . The mean of the filled symbols is indicated with a solid line, while the mean of all symbols (filled and open) is indicated with a dashed line.

The even moments give non-zero predictions and each is a function of the three dimensional persistence length (i.e. $P \equiv P_{3D}$ $P \equiv P_{3D}$ $P \equiv P_{3D}$).³ Consider

$$
\langle \theta^2 \rangle = \frac{2d}{P} \tag{S.13}
$$

This equation has an identical mathematical form in 2D

$$
\langle \theta^2 \rangle_{2\text{D}} = \frac{2d}{P_{2\text{D}}} \tag{S.14}
$$

Due to the loss of one degree of freedom moving $3D \rightarrow 2D$, there exists a scaling relationship between the two persistence lengths, so that the substitution $P_{2D} = 2P$ gives this 2D conformational statistic in terms of the desired 3D persistence length

$$
\langle \theta^2 \rangle_{2\text{D}} = \frac{d}{P} \tag{S.15}
$$

A similar argument applies to the fourth moment

$$
\langle \theta^4 \rangle_{\text{2D}} = 3 \frac{d^2}{P^2} \tag{S.16}
$$

and sixth moment

$$
\langle \theta^6 \rangle_{2\text{D}} = 15 \frac{d^3}{P^3} \tag{S.17}
$$

Persistence length estimates were obtained from these functions $f(d; P)$ by employing a weighted nonlinear least squares method, i.e. minimizing the cost function $C(P)$ with respect to the free parameter P

$$
\chi^2 = \min_P C(P) = \min_P \sum_{d=0}^{l_{\text{max}}} \left(\frac{\mu_d - f(d; P)}{\sigma_d} \right)^2 \tag{S.18}
$$

where μ_d and σ_d are experimentally determined mean values and standard deviations, respectively, from sampling and $f(d; P)$ are theoretical predictions of the WLC model. We restrict the fitting to $0 < d < l_{\text{max}}$, with $l_{\text{max}} \approx 2P$ (∼100 nm). Owing to self-avoiding interactions, fitting over the entire range can yield an overestimation of $P(7)$ $P(7)$. Consistent with previous reports (3) , self-avoiding interactions affect θ at shorter separations than R. The fitted value of P (and its uncertainty) along with the average persistence length value from from 10 distinct estimates, P_{ave} , are shown in [Figure S.10](#page-13-0) for the first three even moments of θ . Each of the additional 7 estimates will be discussed forthwith.

The ratio of the fourth moment to the square of the second moment, the so-called kurtosis (k) , satisfies the following

$$
k = \frac{\langle \theta^4 \rangle}{\langle \theta^2 \rangle^2} = 3 \tag{S.19}
$$

which along with the ratio

$$
\frac{\langle \theta^6 \rangle}{\langle \theta^2 \rangle^3} = 15 \tag{S.20}
$$

serve as additional checks of the normality prediction, as shown in [Figure S.11.](#page-13-1)

³As a convention, the subscript will be omitted when referring to the 3D case.

Figure S.10: The second, fourth, and sixth moments of θ yield estimates of P.

Figure S.11: Normality prediction. See [Figure S.9](#page-11-0) legend.

Recall the prediction of [Equation S.8](#page-10-1) (adjusted for dimensionality)

$$
\langle \cos \theta \rangle_{2\text{D}} = e^{-\frac{d}{(2P)}} \tag{S.21}
$$

The fitted value of P is shown in [Figure S.12.](#page-14-0)

Figure S.12: Estimate of P from $\cos \theta$.

The WLC model also makes predictions about projection of the end-end distance vector **onto** the initial tangent vector \mathbf{u}_0

$$
\langle \mathbf{R} \cdot \mathbf{u}_0 \rangle_{2D} = \int_0^d \langle \mathbf{u}(s) \cdot \mathbf{u}_0 \rangle ds = \int_0^d e^{-\frac{s}{2P}} ds = 2P \left(1 - e^{-\frac{d}{2P}} \right) \tag{S.22}
$$

and the second moment of R

$$
\langle R^2 \rangle_{2D} = \int_0^d \int_0^d \langle \mathbf{u}(s) \cdot \mathbf{u}(s') \rangle ds ds' \qquad (S.23)
$$

=
$$
\int_0^d \int_0^d e^{-\frac{|s-s'|}{2P}} ds ds' \qquad (S.24)
$$

=
$$
\int_0^d 2 \int_0^{s'} e^{-\frac{s-s'}{2P}} ds ds' \qquad (S.25)
$$

=
$$
4dP \left[1 - \frac{2P}{d} \left(1 - e^{-\frac{d}{2P}} \right) \right]
$$

The same result is reached by observing that $d\langle R^2 \rangle_{\text{2D}} = 2\langle \mathbf{R} \cdot \mathbf{u}_0 \rangle_{\text{2D}} ds$

$$
\langle R^2 \rangle_{\text{2D}} = \int_0^d 2 \langle \mathbf{R} \cdot \mathbf{u}_0 \rangle_{\text{2D}} ds = \int_0^d 4P \left(1 - e^{-\frac{s}{2P}} \right) ds = 4dP \left[1 - \frac{2P}{d} \left(1 - e^{-\frac{d}{2P}} \right) \right]
$$
(S.24)

Unlike $\langle \mathbf{R} \cdot \mathbf{u}_0 \rangle$ and the second moment of R, the fourth moment of R does not possess the same mathematical form in 3D as in 2D, so that this conformational statistic has been shown [\(7\)](#page-21-7) to provide a reliable means of determining the dimensionality of the deposited molecules

$$
\langle R^4 \rangle_{2D} = 32d^2P^2 - 240dP^3 + 696P^4 - \frac{320}{3}dP^3e^{-\frac{d}{2P}} - \frac{6272}{9}P^4e^{-\frac{d}{2P}} + \frac{8}{9}P^4e^{-\frac{2d}{P}} \tag{S.25}
$$

Additionally, the normalized difference $(\langle R^4 \rangle - \langle R^2 \rangle^2)/d^4$ does not vanish for large separations. Fits using these equations are shown in [Figure S.13.](#page-15-0) These last two fits provide confirmation that the imaged DNA molecules were immobilized in 2D equilibrium confirmations.

Figure S.13: Estimates of P from the moments of R.

We now revisit the WLC angular distribution [\(Equation S.9\)](#page-10-2). Binning of the measured angles is necessary to calculate the histogram $-\ln G(\theta; d, P)$ [\(7\)](#page-21-7). For a bin size of $\Delta\theta$ around a bin center of θ , the probability is evaluated using the error function

$$
erf(x) = \frac{2}{\sqrt{\pi}} \int_0^{\pi} e^{-t^2} dt
$$
 (S.26)

so that

$$
G(\theta; d, P) = \text{erf}\left(\sqrt{\frac{P}{2d}}\left(\theta + \frac{\Delta\theta}{2}\right)\right) - \text{erf}\left(\sqrt{\frac{P}{2d}}\left(\theta - \frac{\Delta\theta}{2}\right)\right)
$$
(S.27)

The negative logarithm of this equation was used for the fitting shown in [Figure S.14.](#page-16-1)

Finally, [Figure S.8](#page-10-0) shows that the angle between adjacent segments is denoted as χ (a special case of θ when $d = l$). [Equation S.21](#page-14-1) is still applicable

$$
\langle \cos \chi \rangle_{2\text{D}} = e^{-\frac{l}{2P}} \tag{S.28}
$$

and can be rearranged to yield

$$
P = \frac{-l}{2\ln(\langle \cos \chi \rangle_{2\text{D}})}\tag{S.29}
$$

Abels *et al.* [\(11\)](#page-21-11) looked at multiple segment lengths l and showed that the value of $\langle \cos \chi \rangle$ peaks at a particular value of l and decreases at lower and higher l . The authors reasoned that as l decreased below the pixel resolution for the AFM setup, discretization of χ angles led to an underestimation of $\langle \cos \chi \rangle$. Additionally, they proposed an undercount of the number of large and small χ angles as l became large enough to average over them, similarly leading to underestimation of $\langle \cos \chi \rangle$. Therefore, the quantity $\langle \cos \chi \rangle_{\text{max}}$ provides a reliable means for determining the optimal segment length for analysis and provides an additional estimate of P at this optimal segment length. This is illustrated in [Figure S.15](#page-16-2) for step sizes l ranging from 3 nm to 17 nm and [Figure S.16](#page-16-0) for step

Figure S.15: Estimate of $P(\langle \cos \chi \rangle_{\text{max}})$ when l ranges from 3 nm to 17 nm.

Figure S.16: Estimate of $P(\langle \cos \chi \rangle_{\text{max}})$ when l ranges from 4 nm to 9 nm.

 $l~(\mathrm{nm})$) and P $P \pm$ SEM (nm) $\frac{M (nm)}{P \pm SD (nm)}$ $\langle \cos \theta \rangle$ $\langle \theta^2 \rangle$ $\langle \theta^4 \rangle$ $\langle \theta^6 \rangle$ $\langle \mathbf{R}$ $\mathbf{R} \cdot \mathbf{u}_0$ $\langle R^2 \rangle$ $\langle R^4 \rangle - \langle R^2 \rangle^2$ − ln $G(\theta)$ $\langle \cos \chi \rangle$ average natural 47.4 ± 0.9 3 $40.0 \pm$ \pm 0.9 \pm 0.8 \pm 4.9 \pm 1.0 \pm 1.0 \pm 1.3 \pm 6.7 \pm 0.8 \pm 7.4 \pm 0.9 \pm 48.7 \pm 0.9 \pm 49.4 \pm 1.5 \pm 2.5 \pm 2.2 \pm 2.5 \pm 0.0 \pm 1.9 \pm 9.5 4 43.7 \pm 1.0 1.8 ± 0.9 1.6 ± 0.1 1.1 51.2 ± 1.4 1.9 ± 0.8 1.9 ± 0.9 1.6 ± 0.9 1.6 ± 0.9 1.5 ± 1.5 1.5 ± 2.9 1.5 ± 2.9 1.5 ± 0.1 1.5 ± 0.0 5 47.1 \pm \pm 1.1 $46.7 \pm$ 1.0 $47.2 \pm$ 1.1 $52.5 \pm$ 1.4 $52.3 \pm$ 0.7 $52.1 \pm$ 0.9 $54.1 \pm$ 0.9 $48.2 \pm$ 1.4 $41.4 \pm$ 2.5 $47.3 \pm$ 0.1 $48.9 \pm$ 3.8 6 $\frac{6}{7} \qquad \frac{50.2 \pm 1.2}{52.7 \pm 1.3}$ \pm 1.2 $49.3 \pm$ 1.1 $47.9 \pm$ 1.2 $51.9 \pm$ 1.4 $55.1 \pm$ 0.7 $53.8 \pm$ 0.9 $56.3 \pm$ 0.9 $48.0 \pm$ 1.5 $50.6 \pm$ 4.3 $57.3 \pm$ 0.2 $52.0 \pm$ 3.4 7 $52.7 \pm$ 1.3 51.7 ± 1.2 49.9 ± 1.2 52.6 ± 1.4 56.8 ± 0.7 55.3 ± 0.9 58.0 ± 0.9 48.4 ± 1.5 53.0 ± 3.5 65.9 ± 0.3 54.4 ± 5.0 8 $54.8 \pm$ \pm 1.4 $53.6 \pm$ 1.3 $50.7 \pm$ 1.3 $52.3 \pm$ 1.4 $58.7 \pm$ 0.8 $56.6 \pm$ 0.9 $59.4 \pm$ 0.9 $48.0 \pm$ 1.5 $59.0 \pm$ 4.0 $73.1 \pm$ 0.4 $56.6 \pm$ 6.9 9 $56.6 \pm$ \pm 1.4 $\frac{55.2 \pm 1.4}{55.2 \pm 1.4}$ $\frac{51.7 \pm 1.4}{53.4 \pm 1.4}$ $\frac{60.2 \pm 0.8}{57.7 \pm 0.9}$ $\frac{60.7 \pm 0.9}{60.7 \pm 0.9}$ $\frac{48.0 \pm 1.4}{58.2 \pm 4.6}$ $\frac{78.0 \pm 0.5}{78.0 \pm 0.5}$ $\frac{58.0 \pm 8.1}{58.0 \pm 0.5}$ 10 $57.7 \pm$ \pm 1.5 $56.2 \pm$ 1.5 $51.7 \pm$ 1.4 $53.2 \pm$ 1.4 $61.2 \pm$ 0.8 $58.2 \pm$ 0.9 $61.5 \pm$ 1.0 $47.5 \pm$ 1.4 $61.2 \pm$ 5.1 $81.4 \pm$ 0.5 $59.0 \pm$ 9.1 11 $58.4 \pm$ \pm 1.6 $56.0 \pm$ 1.6 $49.9 \pm$ 1.4 $53.0 \pm$ 1.5 $63.6 \pm$ 0.9 $59.5 \pm$ 1.0 $63.1 \pm$ 1.0 $47.4 \pm$ 1.4 $64.5 \pm$ 5.6 $84.1 \pm$ 0.6 $60.0 \pm$ 10.3 $12 \t 60.8 \pm$ 1.7 59.2 ± 1.7 53.7 ± 1.6 53.4 ± 1.6 65.8 ± 0.9 60.4 ± 1.0 64.1 ± 1.1 48.0 ± 1.5 63.4 ± 6.2 84.8 ± 0.7 61.4 ± 9.9 $13 \qquad 60.0 \pm$ 1.7 58.1 ± 1.7 52.6 ± 1.5 54.0 ± 1.5 65.2 ± 0.9 60.1 ± 1.0 63.9 ± 1.1 47.1 ± 1.4 64.7 ± 6.8 86.1 ± 0.7 61.2 ± 10.5 14 60.8 \pm \pm 1.8 $58.0 \pm$ 1.7 $50.8 \pm$ 1.5 $53.2 \pm$ 1.6 $68.9 \pm$ 1.0 $62.0 \pm$ 1.1 $65.8 \pm$ 1.1 $47.6 \pm$ 1.4 $63.1 \pm$ 7.4 $85.4 \pm$ 0.8 $61.6 \pm$ 10.7 15 60.5 \pm \pm 1.8 $58.2 \pm$ 1.7 $52.1 \pm$ 1.6 $54.2 \pm$ 1.6 $68.5 \pm$ 1.1 $61.6 \pm$ 1.1 $65.9 \pm$ 1.2 $46.4 \pm$ 1.4 $64.1 \pm$ 8.0 $85.7 \pm$ 0.9 $61.7 \pm$ 10.8 $16 \t 62.0 \pm$ \pm 2.0 $59.6 \pm$ 1.9 $52.0 \pm$ 1.7 $52.8 \pm$ 1.7 $72.9 \pm$ 1.2 $63.8 \pm$ 1.3 $68.3 \pm$ 1.3 $47.5 \pm$ 1.5 $65.8 \pm$ 8.5 $85.6 \pm$ 0.9 $63.0 \pm$ 11.2 $\frac{17}{2}$ 62.8 \pm \pm 2.0 60.2 \pm 1.9 52.7 \pm 1.7 54.1 \pm 1.7 73.0 \pm 1.2 63.9 \pm 1.3 68.3 \pm 1.3 47.5 \pm 1.5 65.8 \pm 9.2 85.6 \pm 0.9 63.4 \pm 11 diaminopurine 47.3 \pm 1.7 3 41.1 \pm \pm 1.7 $42.6 \pm$ 1.6 $47.4 \pm$ 2.1 $53.4 \pm$ 2.6 $49.3 \pm$ 1.8 $47.3 \pm$ 1.7 $47.8 \pm$ 1.6 $55.9 \pm$ 3.1 $21.2 \pm$ 2.2 $22.0 \pm$ 0.1 $42.8 \pm$ 12 $44.6 \pm$ 1.8 45.0 ± 1.7 47.5 ± 2.1 53.0 ± 2.7 52.4 ± 1.7 50.5 ± 1.7 51.4 ± 1.6 55.2 ± 3.1 27.5 ± 2.4 29.7 ± 0.1 45.7 ± 9.6 5 $48.5 \pm$ \pm 2.0 $48.4 \pm$ 1.9 $50.0 \pm$ 2.2 $54.9 \pm$ 2.7 $55.7 \pm$ 1.5 $52.3 \pm$ 1.5 $53.6 \pm$ 1.5 $53.6 \pm$ 2.9 $39.3 \pm$ 3.6 $38.3 \pm$ 0.2 $49.5 \pm$ 6.2 6 $52.2 \pm$ \pm 2.2 $51.6 \pm$ 2.1 $50.9 \pm$ 2.2 $54.3 \pm$ 2.7 $59.2 \pm$ 1.5 $55.0 \pm$ 1.6 $56.3 \pm$ 1.6 $55.0 \pm$ 3.2 $48.0 \pm$ 4.3 $47.1 \pm$ 0.3 $53.0 \pm$ 3.7 7 $\frac{7}{8}$ $\frac{55.6 \pm 2.4}{58.7 \pm 2.6}$ \pm 2.4 $\frac{54.7 \pm 2.3}{52.9 \pm 2.4}$ $\frac{55.5 \pm 2.8}{55.5 \pm 2.8}$ $\frac{62.8 \pm 1.6}{57.7 \pm 1.7}$ $\frac{59.5 \pm 1.7}{59.5 \pm 1.7}$ $\frac{54.9 \pm 3.1}{54.9 \pm 3.1}$ $\frac{53.7 \pm 5.1}{53.7 \pm 5.1}$ $\frac{55.8 \pm 0.4}{55.8 \pm 0.4}$ $\frac{56.3 \pm 3.0}{5$ 8 $58.7 \pm$ \pm 2.6 $57.5 \pm$ 2.6 $54.4 \pm$ 2.6 $55.5 \pm$ 2.9 $65.1 \pm$ 1.6 $58.9 \pm$ 1.7 $60.9 \pm$ 1.7 $54.5 \pm$ 3.1 $52.7 \pm$ 4.1 $63.4 \pm$ 0.5 $58.2 \pm$ 4.1 9 61.3 \pm \pm 2.8 $60.2 \pm$ 2.7 $57.3 \pm$ 2.7 $58.0 \pm$ 2.9 $66.8 \pm$ 1.6 $60.1 \pm$ 1.6 $62.6 \pm$ 1.7 $53.6 \pm$ 3.0 $59.3 \pm$ 6.6 $70.7 \pm$ 0.7 $61.0 \pm$ 4.9 10 63.8 \pm $\frac{3.5}{2.4 \pm 3.0}$ $\frac{57.7 \pm 3.0}{57.7 \pm 3.0}$ $\frac{57.9 \pm 3.2}{57.9 \pm 3.2}$ $\frac{69.5 \pm 1.7}{62.3 \pm 1.8}$ $\frac{64.8 \pm 1.8}{64.8 \pm 1.8}$ $\frac{55.3 \pm 3.1}{55.3 \pm 3.1}$ $\frac{61.2 \pm 5.1}{61.2 \pm 5.1}$ $\frac{75.4 \pm 0.8}{75.4 \pm 0.8}$ $\frac{6$ 11 65.8 \pm \pm 3.1 $64.5 \pm$ 3.1 $60.2 \pm$ 3.3 $59.4 \pm$ 3.4 $71.3 \pm$ 1.7 $63.0 \pm$ 1.8 $65.7 \pm$ 1.8 $55.2 \pm$ 3.1 $67.6 \pm$ 8.1 $80.0 \pm$ 1.0 $65.3 \pm$ 6.9 12 $66.9 \pm$ $\frac{3.5}{2}$ \pm 3.4 $\frac{59.4}{2}$ \pm 3.4 $\frac{57.1}{2}$ \pm 3.4 $\frac{72.9}{2}$ \pm 1.8 $\frac{64.4}{2}$ \pm 1.9 $\frac{67.3}{2}$ \pm 1.9 $\frac{55.0}{2}$ \pm 3.2 $\frac{71.3}{2}$ \pm 8.9 $\frac{84.3}{2}$ \pm 1.2 $\frac{66.4}{2}$ \pm 8.6 13 67.2 \pm $\frac{3.5}{2.5}$ \pm 3.4 60.1 \pm 3.4 59.3 \pm 3.6 74.4 \pm 1.9 65.5 \pm 2.0 68.8 \pm 2.1 54.9 \pm 3.1 71.5 \pm 9.8 86.5 \pm 1.3 67.4 \pm 8.9 14 69.4 \pm \pm 3.6 $68.1 \pm$ 3.6 $64.7 \pm$ 3.6 $65.4 \pm$ 3.8 $77.5 \pm$ 2.0 $67.2 \pm$ 2.0 $70.5 \pm$ 2.1 $55.8 \pm$ 3.1 $73.7 \pm$ 10.6 $87.6 \pm$ 1.4 $70.0 \pm$ 8.5 15 67.7 \pm \pm 3.7 66.0 \pm 3.6 60.3 \pm 3.4 59.7 \pm 3.5 76.8 \pm 2.1 66.8 \pm 2.2 70.2 \pm 2.2 54.8 \pm 3.1 68.6 \pm 7.9 87.7 \pm 1.5 67.9 \pm 9.3 16 68.5 \pm \pm 3.8 $59.1 \pm$ 3.6 $58.3 \pm$ 3.8 $82.7 \pm$ 2.5 $69.7 \pm$ 2.5 $73.5 \pm$ 2.5 $55.0 \pm$ 3.3 $69.4 \pm$ 8.5 $88.8 \pm$ 1.5 $69.2 \pm$ 10.6 $\frac{17}{15}$ 69.7 \pm \pm 4.0 $67.0 \pm$ 4.0 $58.1 \pm$ 3.7 $59.2 \pm$ 3.7 $81.3 \pm$ 2.5 $69.5 \pm$ 2.5 $73.8 \pm$ 2.5 $53.4 \pm$ 3.0 $69.9 \pm$ 9.1 $89.7 \pm$ 1.7 $69.1 \pm$ 10.9 inosine 44.4 ± 1.3 3 $39.5 \pm$ 1.5 40.3 ± 1.4 43.9 ± 1.6 51.1 ± 2.2 46.7 ± 1.4 44.4 ± 1.3 45.6 ± 1.3 45.3 ± 2.3 26.1 ± 2.2 26.6 ± 0.1 40.9 ± 8.3 $4 \t 43.6 \t \pm$ 1.7 43.7 ± 1.6 45.4 ± 1.8 51.3 ± 2.2 49.1 ± 1.3 46.3 ± 1.3 48.0 ± 1.3 43.7 ± 2.3 34.1 ± 2.9 37.9 ± 0.2 44.3 ± 5.1 5 $\frac{5}{6} \qquad \frac{46.7 \pm 1.8}{49.2 \pm 2.0}$ \pm 1.8 $46.5 \pm$ 1.7 $47.2 \pm$ 1.8 $52.9 \pm$ 2.3 $50.6 \pm$ 1.1 $47.7 \pm$ 1.2 $49.7 \pm$ 1.2 $43.5 \pm$ 2.2 $39.6 \pm$ 3.6 $47.9 \pm$ 0.3 $47.2 \pm$ 3.7 6 49.2 \pm \pm 2.0 $48.6 \pm$ 1.9 $47.2 \pm$ 1.9 $51.4 \pm$ 2.3 $52.6 \pm$ 1.1 $49.4 \pm$ 1.2 $51.5 \pm$ 1.3 $44.1 \pm$ 2.3 $50.1 \pm$ 4.3 $57.5 \pm$ 0.4 $50.2 \pm$ 3.5 7 $51.7 \pm$ \pm 2.1 $51.0 \pm$ 2.0 $49.5 \pm$ 2.0 $52.7 \pm$ 2.3 $54.2 \pm$ 1.1 $50.2 \pm$ 1.2 $52.6 \pm$ 1.3 $43.8 \pm$ 2.2 $57.4 \pm$ 5.1 $64.7 \pm$ 0.5 $52.8 \pm$ 5.4 8 $53.4 \pm$ \pm 2.3 $52.6 \pm$ 2.2 $50.0 \pm$ 2.2 $52.7 \pm$ 2.5 $56.7 \pm$ 1.2 $52.0 \pm$ 1.3 $54.6 \pm$ 1.4 $44.0 \pm$ 2.3 $60.4 \pm$ 5.8 $69.8 \pm$ 0.6 $54.6 \pm$ 6.8 9 $54.0 \pm$ \pm 2.3 $53.3 \pm$ 2.3 $51.3 \pm$ 2.2 $54.0 \pm$ 2.4 $57.7 \pm$ 1.3 $52.9 \pm$ 1.4 $55.4 \pm$ 1.4 $44.5 \pm$ 2.3 $62.1 \pm$ 6.6 $73.2 \pm$ 0.7 $55.8 \pm$ 7.6 $10 \t 55.5 \pm$ \pm 2.5 $54.7 \pm$ 2.4 $53.3 \pm$ 2.3 $55.8 \pm$ 2.5 $58.7 \pm$ 1.3 $53.8 \pm$ 1.4 $56.6 \pm$ 1.5 $44.8 \pm$ 2.3 $65.9 \pm$ 7.4 $76.5 \pm$ 0.8 $57.6 \pm$ 8.4 11 $56.4 \pm$ \pm 2.6 $55.5 \pm$ 2.5 $53.5 \pm$ 2.3 $55.5 \pm$ 2.5 $60.3 \pm$ 1.3 $54.4 \pm$ 1.4 $57.3 \pm$ 1.5 $44.9 \pm$ 2.3 $63.9 \pm$ 8.2 $78.0 \pm$ 1.0 $58.0 \pm$ 8.6 12 $56.4 \pm$ \pm 2.7 $54.6 \pm$ 2.6 $49.5 \pm$ 2.4 $52.9 \pm$ 2.7 $62.1 \pm$ 1.5 $54.7 \pm$ 1.5 $57.7 \pm$ 1.6 $43.9 \pm$ 2.3 $62.5 \pm$ 6.2 $77.0 \pm$ 1.0 $57.1 \pm$ 8.9 13 $56.0 \pm$ \pm 2.8 $54.1 \pm$ 2.7 $50.2 \pm$ 2.5 $55.1 \pm$ 2.8 $62.7 \pm$ 1.6 $55.3 \pm$ 1.7 $58.6 \pm$ 1.7 $42.6 \pm$ 2.2 $63.0 \pm$ 6.8 $77.5 \pm$ 1.1 $57.5 \pm$ 9.2 14 $58.2 \pm$ \pm 2.8 $57.0 \pm$ 2.8 $53.7 \pm$ 2.6 $55.0 \pm$ 2.7 $65.6 \pm$ 1.6 $56.8 \pm$ 1.6 $60.1 \pm$ 1.7 $45.1 \pm$ 2.4 $64.1 \pm$ 7.4 $77.8 \pm$ 1.2 $59.3 \pm$ 8.6

 \pm 2.9 $55.6 \pm$ 2.8 $51.4 \pm$ 2.6 $55.5 \pm$ 2.8 $64.8 \pm$ 1.7 $56.3 \pm$ 1.7 $59.8 \pm$ 1.8 $43.5 \pm$ 2.2 $61.8 \pm$ 8.0 $78.4 \pm$ 1.4 $58.4 \pm$ 9.1

 \pm 3.1 $55.3 \pm$ 3.0 $50.4 \pm$ 2.7 $54.1 \pm$ 3.0 $67.6 \pm$ 1.9 $57.2 \pm$ 1.9 $60.9 \pm$ 1.9 $43.0 \pm$ 2.3 $63.1 \pm$ 8.6 $76.3 \pm$ 1.4 $58.6 \pm$ 9.2

 \pm 3.1 $54.6 \pm$ 2.9 $50.6 \pm$ 2.7 $55.6 \pm$ 3.0 $67.2 \pm$ 1.9 $57.5 \pm$ 1.9 $61.2 \pm$ 2.0 $43.0 \pm$ 2.3 $60.7 \pm$ 9.3 $76.7 \pm$ 1.6 $58.4 \pm$ 9.1

15 57.3 \pm

16 57.8 \pm

 $\frac{17}{15}$ 56.9 \pm

Table S.4: Summary of P estimates for step sizes l ranging from 3 nm to 17 nm. The optimal l is indicated in gray.

sizes l ranging from 4 nm to 9 nm .

The complete analysis for step sizes l ranging from 3 nm to 17 nm is summarized in [Table S.4.](#page-17-0) Several trends can be observed from these data. First, all but one of the ten WLC predictions strongly depends on choice of step size l . Generally, the estimates of P are strictly increasing functions of increasing l. In some cases, the dependence on l is so dramatic that P increases 400% from $l=3$ nm to $l=17$ nm. In contrast, the estimate of P from the $\langle R^4 \rangle - \langle R^2 \rangle^2$ prediction is a decreasing function of increasing l. However, the maximal observed decrease in P is less than 5%. Overall, this estimator appears to be the most reliable: it is the most insensitive to choice of step size and it provides a means of assessing the dimensionality of the molecules being imaged. If choosing only one of the ten WLC predictions to estimate P, the $\langle R^4 \rangle - \langle R^2 \rangle^2$ prediction would certainly be the first choice.

This initial analysis revealed the importance of identifying the proper step size to obtain the best possible estimates of P . In particular, we determined that the optimal step size l_{optimal} occurred between 4 nm to 9 nm. We worried that discretization of l might prevent us from identifying the true (non-integral) value of l_{optimal} , with possible negative ramifications. Therefore, we next examined step sizes from 4 nm to 9 nm at every quarter nanometer. This analysis is summarized in [Table S.5.](#page-19-0) Importantly, the estimates of P from the fractional optimal step sizes were consistently within one half nanometer of the previous estimates. This is well within the uncertainty from fitting. These results indicated that discretization of l (to integral values) had little effect on the estimates of P and rendered a more exact determination of l_{optimal} unnecessary.

In order to better determine which physical and thermodynamic feature(s) of base-substituted DNA polymers explain their mechanical properties, we applied AFM experiments to seven thymine variants with functional groups that occupy the major groove (main manuscript Figure 7) that have been previously characterized [\(2\)](#page-21-2). The ten estimates of P at l_{optimal} for the thymine variants (numbered 1-7) are given in [Table S.6.](#page-20-0) Finally, all of the compiled AFM data, including the average and standard deviation of the ten estimates, are summarized in Table 3 of the main manuscript.

l (nm)		$P \pm$ SEM (nm)						$P \pm$ sp (nm)			
	$\langle \cos \theta \rangle$	$\langle \theta^2 \rangle$	$\langle \theta^4 \rangle$	$\langle \theta^6 \rangle$	$\langle \mathbf{R} \cdot \mathbf{u}_0 \rangle$	$\langle R^2 \rangle$	$\langle R^4 \rangle$	$-\langle R^2 \rangle^2$ $\langle R^4 \rangle$	$-\ln G(\theta)$	$\langle \cos \chi \rangle$	average
						natural					
4	43.4 ± 1.0	43.4 ± 0.9	44.3 ± 1.0	49.6 ± 1.2	49.4 ± 0.7	49.6 ± 0.8	51.3 ± 0.9	48.0 ± 1.5	35.1 ± 2.9	35.9 ± 0.1	45.0 ± 5.8
4.25	44.2 ± 1.0	44.1 ± 0.9	45.2 ± 1.0	50.7 ± 1.2	50.2 ± 0.7	$50.5\,\pm\,0.8$	$52.4~\pm$ 0.9	48.2 ± 1.4	34.1 ± 2.1	38.7 \pm 0.1	45.8 ± 5.8
4.5	$45.1~\pm~1.0$	44.9 ± 1.0	45.5 ± 1.0	51.0 ± 1.2	50.6 ± 0.7	50.7 ± 0.8	52.6 ± 0.8	47.5 ± 1.4	38.5 ± 3.2	41.5 ± 0.1	46.8 ± 4.6
4.75	45.8 ± 1.0	45.4 ± 0.9	45.8 ± 1.0	51.1 ± 1.2	51.3 ± 0.7	51.2 ± 0.8	53.3 ± 0.8	47.4 ± 1.4	41.0 ± 3.4	$44.2\,\pm\,0.1$	47.6 ± 3.9
5°	46.7 ± 1.1	46.2 ± 1.0	46.2 ± 1.0	51.4 ± 1.3	51.9 ± 0.7	51.7 ± 0.8	53.9 ± 0.9	47.0 ± 1.4	43.6 ± 3.6	47.2 ± 0.1	48.6 ± 3.4
5.25	47.6 ± 1.1	47.1 ± 1.0	46.8 ± 1.1	51.9 ± 1.3	52.4 ± 0.7	$52.3\,\pm\,0.8$	54.5 ± 0.9	47.4 ± 1.4	41.2 ± 2.6	49.6 \pm 0.2	49.1 ± 3.9
$5.5\,$	$48.4~\pm~1.1$	47.7 ± 1.0	47.1 ± 1.1	51.6 ± 1.3	53.2 ± 0.7	52.7 ± 0.8	55.1 ± 0.9	47.2 ± 1.4	42.6 ± 2.8	52.2 ± 0.2	49.8 ± 3.8
5.75	49.4 ± 1.1	48.6 ± 1.1	47.4 ± 1.1	51.5 ± 1.3	54.1 ± 0.7	53.2 ± 0.8	55.7 ± 0.9	47.3 ± 1.4	45.9 ± 2.9	55.1 ± 0.2	50.8 ± 3.6
6 ¹	49.8 ± 1.2	48.9 ± 1.1	47.4 ± 1.1	51.0 ± 1.3	54.8 ± 0.7	53.6 ± 0.9	56.1 ± 0.9	47.5 ± 1.5	$52.4~\pm~4.3$	57.1 ± 0.2	51.8 ± 3.5
6.25	50.4 ± 1.2	49.5 ± 1.1	48.2 ± 1.1	52.1 ± 1.3	54.7 ± 0.7	53.8 ± 0.8	56.3 ± 0.9	47.1 ± 1.4	50.0 ± 3.1	59.5 ± 0.2	52.2 ± 3.9
$6.5\,$	50.9 ± 1.2	49.9 ± 1.2	48.2 ± 1.2	51.8 ± 1.4	55.6 ± 0.7	54.1 ± 0.9	56.8 ± 0.9	47.0 ± 1.4	53.8 ± 4.7	61.8 ± 0.3	53.0 ± 4.4
6.75	51.7 ± 1.2	50.7 ± 1.2	48.5 \pm 1.2	51.0 ± 1.3	56.3 ± 0.7	54.6 ± 0.9	57.2 ± 0.9	47.4 ± 1.5	57.0 ± 4.9	63.8 ± 0.3	53.8 ± 4.9
7°	52.4 \pm 1.3	51.4 ± 1.2	49.3 ± 1.2	52.3 ± 1.4	56.7 ± 0.7	55.0 ± 0.9	57.7 ± 0.9	47.3 ± 1.4	52.5 ± 3.5	65.7 \pm 0.3	54.0 ± 5.2
$7.25\,$	52.8 ± 1.3	51.6 ± 1.3	48.9 ± 1.2	51.2 ± 1.4	57.4 ± 0.8	55.3 ± 0.9	58.1 ± 0.9	47.2 ± 1.4	52.9 ± 3.7	67.6 ± 0.3	54.3 ± 5.8
7.5	53.2 ± 1.3	52.0 ± 1.3	49.4 ± 1.3	52.2 ± 1.4	57.6 ± 0.8	55.6 ± 0.9	58.5 ± 0.9	46.9 ± 1.4	55.5 ± 3.8	69.2 ± 0.3	55.0 ± 6.1
7.75	54.0 ± 1.3	52.7 ± 1.3	50.0 ± 1.3	52.8 ± 1.4	57.4 ± 0.7	55.6 ± 0.9	58.6 ± 0.9	46.9 ± 1.4	55.2 \pm 3.9	71.0 ± 0.4	55.4 ± 6.5
8	54.5 ± 1.4	53.2 ± 1.3	50.3 ± 1.3	52.1 ± 1.4	58.6 ± 0.8	56.2 ± 0.9	59.3 ± 0.9	47.0 ± 1.4	58.0 ± 4.0	72.6 ± 0.4	56.2 ± 7.0
8.25	54.4 ± 1.3	53.1 ± 1.3	50.6 ± 1.3	52.8 ± 1.4	58.3 ± 0.8	56.3 ± 0.9	59.3 ± 0.9	46.8 ± 1.4	56.4 ± 4.2	73.8 ± 0.4	56.2 ± 7.2
8.5	55.1 ± 1.4	53.8 ± 1.4	50.4 ± 1.3	51.5 ± 1.4	59.4 ± 0.8	56.5 ± 0.9	59.6 ± 0.9	47.0 ± 1.5	57.2 ± 4.3	74.6 ± 0.4	56.5 ± 7.5
8.75	55.6 ± 1.4	54.2 ± 1.4	50.4 ± 1.3	51.8 ± 1.4	59.9 ± 0.8	57.0 ± 0.9	60.2 ± 1.0	46.8 ± 1.4	57.7 ± 4.5	76.3 ± 0.4	57.0 ± 8.0
9	55.8 ± 1.4	54.4 ± 1.4	51.1 ± 1.3	52.9 ± 1.4	59.9 ± 0.8	57.1 ± 0.9	60.3 ± 0.9	46.8 ± 1.4	57.4 ± 4.6	77.5 ± 0.4	57.3 ± 8.2
						diaminopurine					
$\overline{4}$	45.1 ± 1.9	45.7 ± 1.8	48.9 \pm 2.2	54.1 ± 2.8	53.2 ± 1.7	50.9 ± 1.7	51.6 ± 1.6	57.1 ± 3.3	29.3 ± 2.0	29.7 \pm 0.1	46.6 ± 9.7
4.25	45.4 ± 1.8	45.9 ± 1.7	48.8 ± 2.1	53.6 ± 2.6	53.2 ± 1.6	50.8 ± 1.6	51.6 ± 1.6	55.5 ± 3.1	30.4 ± 2.1 33.2 \pm 3.3	31.2 ± 0.1	46.6 ± 8.9
4.5 4.75	46.4 ± 1.9	46.6 ± 1.8	48.9 \pm 2.1 50.0 ± 2.2	54.0 ± 2.6 55.0 ± 2.8	53.7 ± 1.6 55.2 ± 1.6	51.2 ± 1.6	52.1 ± 1.6 53.1 ± 1.5	55.0 ± 3.0		33.5 ± 0.1 35.9 ± 0.2	47.5 ± 8.0 48.4 ± 7.8
5°	47.8 ± 1.9 49.1 ± 2.0	47.9 ± 1.8 49.0 ± 1.9	49.9 ± 2.1	54.6 ± 2.5	56.9 ± 1.6	51.9 ± 1.6 53.1 ± 1.6	54.3 ± 1.6	53.9 ± 3.0 55.4 ± 3.1	32.9 ± 2.4 $38.8~\pm~3.6$	38.4 ± 0.2	49.9 ± 6.6
5.25	49.6 ± 2.1	49.6 ± 1.9	50.8 ± 2.2	55.6 ± 2.7	56.9 ± 1.6	53.7 ± 1.6	54.9 ± 1.6	56.2 ± 3.1	41.7 ± 3.8	40.3 ± 0.2	50.9 ± 5.9
5.5	50.3 ± 2.1	50.1 ± 2.0	50.8 ± 2.3	54.8 ± 2.8	57.7 ± 1.6	53.7 ± 1.6	55.0 ± 1.6	54.6 ± 3.0	41.6 ± 4.0	$42.1\,\pm\,0.2$	51.1 ± 5.4
5.75	50.9 ± 2.1	50.4 ± 2.0	50.7 \pm 2.2	54.5 ± 2.7	58.0 \pm 1.5	53.8 ± 1.5	55.5 ± 1.6	52.9 ± 2.9	46.4 ± 4.1	44.8 ± 0.3	51.8 ± 4.0
6	52.5 \pm 2.2	51.9 ± 2.1	51.0 ± 2.2	54.3 ± 2.7	59.8 ± 1.6	55.4 ± 1.6	56.9 ± 1.6	55.1 ± 3.1	47.3 ± 6.7	$47.2~\pm~0.3$	53.1 ± 4.0
6.25	53.0 ± 2.2	52.5 ± 2.1	51.6 ± 2.2	55.1 ± 2.6	60.0 ± 1.5	55.1 ± 1.5	56.7 ± 1.6	54.4 ± 3.0	47.1 ± 4.5	48.8 ± 0.3	53.4 ± 3.8
$6.5\,$	54.1 ± 2.3	53.4 ± 2.2	52.2 \pm 2.3	54.9 ± 2.7	61.1 ± 1.6	56.5 ± 1.6	58.2 ± 1.6	$54.9~\pm~\!3.1$	50.8 ± 4.7	51.8 ± 0.3	54.8 ± 3.1
6.75	55.0 ± 2.4	54.2 ± 2.3	52.6 ± 2.4	54.7 ± 2.8	61.6 ± 1.6	56.4 ± 1.6	58.0 ± 1.6	$55.1~\pm~3.2$	$47.9~\pm~\!3.4$	52.8 ± 0.4	54.8 ± 3.6
7°	55.2 ± 2.4	54.3 ± 2.3	52.6 ± 2.3	55.2 ± 2.7	62.1 ± 1.6	56.9 ± 1.6	58.6 ± 1.6	54.2 ± 3.1	52.7 ± 5.1	55.5 ± 0.4	55.7 ± 2.9
7.25	55.9 ± 2.4	55.0 ± 2.4	52.8 ± 2.4	54.5 ± 2.8	62.5 ± 1.6	56.7 ± 1.6	58.6 ± 1.6	53.6 ± 3.1	53.5 ± 5.3	57.5 ± 0.4	56.1 ± 2.9
7.5	56.1 ± 2.5	55.1 ± 2.4	52.9 ± 2.4	55.1 ± 2.7	62.7 ± 1.6	57.3 ± 1.6	59.2 ± 1.6	53.9 ± 3.0	53.0 ± 5.5	59.2 ± 0.4	56.4 ± 3.2
7.75	57.7 ± 2.6	56.7 ± 2.5	54.4 ± 2.6	57.0 ± 3.0	64.2 \pm 1.6	58.4 ± 1.6	60.4 ± 1.7	54.9 ± 3.1	57.8 \pm 5.6	61.5 ± 0.5	58.3 ± 3.0
8	58.6 ± 2.6	57.4 ± 2.6	54.3 ± 2.6	55.2 ± 2.8	64.4 ± 1.6	57.7 ± 1.6	59.8 ± 1.6	53.4 ± 3.0	58.5 ± 5.8	62.8 ± 0.5	58.2 ± 3.5
8.25	59.1 ± 2.6	58.0 ± 2.5	55.4 ± 2.6	56.8 ± 2.8	65.1 ± 1.6	58.5 ± 1.6	60.9 ± 1.7	53.4 ± 2.9	52.5 ± 4.2	64.5 ± 0.6	58.4 ± 4.2
8.5	59.7 ± 2.7	58.6 ± 2.6	55.5 ± 2.7	55.9 ± 2.9	66.5 ± 1.6	59.6 ± 1.7	61.6 ± 1.7	55.2 ± 3.2	58.9 ± 6.2	66.5 ± 0.6	59.8 ± 4.1
8.75	59.7 ± 2.7	58.6 ± 2.6	55.5 ± 2.7	56.1 ± 2.9	66.4 ± 1.6	59.5 ± 1.7	61.7 ± 1.7	54.1 ± 3.0	58.8 ± 6.4	68.4 ± 0.6	59.9 ± 4.6
9	60.8 ± 2.7	59.6 \pm 2.7	56.7 ± 2.7	57.5 ± 2.9	66.8 ± 1.6	59.8 \pm 1.6	62.3 ± 1.7	53.4 ± 2.9	59.9 \pm 6.6	$70.2\,\pm\,0.7$	60.7 \pm 4.9
						inosine					
	43.0 \pm 1.6	43.1 \pm 1.5	$44.8~\pm~1.7$	50.9 \pm 2.2	$48.6~\pm$ 1.2	45.8 \pm 1.2	$47.3~\pm{}$ 1.2	$44.1~\pm~2.2$	$34.1~\pm~2.9$	37.9 \pm 0.2	44.0 ± 5.0
4.25	43.7 ± 1.7	43.7 ± 1.6	45.3 ± 1.8	52.1 ± 2.3	48.7 ± 1.2	46.1 ± 1.2	47.9 ± 1.2	43.2 ± 2.2	35.1 ± 3.1	40.2 ± 0.2	44.6 ± 4.7
4.5	44.7 ± 1.7	44.5 \pm 1.6	45.6 ± 1.8	$52.2~\pm~2.3$	49.3 ± 1.2	46.5 ± 1.2	48.3 ± 1.2	$42.8~\pm~2.2$	$33.2~\pm~2.3$	43.3 ± 0.2	45.0 ± 5.1
4.75	44.9 \pm 1.7	44.7 ± 1.6	46.3 ± 1.9	52.7 ± 2.4	49.5 ± 1.2	46.9 ± 1.2	48.7 ± 1.2	42.7 ± 2.2	39.2 ± 3.4	$45.8\,\pm\,0.2$	46.1 ± 3.7
5 ₅	46.0 ± 1.8	45.7 ± 1.7	46.4 ± 1.9	53.0 ± 2.4	49.7 ± 1.1	46.8 ± 1.2	48.7 ± 1.2	42.2 ± 2.1	38.9 ± 3.6	47.8 ± 0.3	46.5 ± 3.9
5.25	46.4 ± 1.8	46.2 ± 1.7	46.5 ± 1.8	52.5 ± 2.3	50.2 ± 1.1	47.5 ± 1.2	49.4 ± 1.2	42.9 ± 2.1	44.0 ± 3.8	50.6 ± 0.3	47.6 ± 3.0
$5.5\,$	48.0 ± 1.8	47.5 ± 1.8	47.0 ± 1.8	52.2 ± 2.2	51.2 ± 1.1	47.9 ± 1.1	49.8 ± 1.2	43.6 ± 2.2	44.9 ± 4.0	53.4 ± 0.3	48.5 ± 3.1
5.75	48.4 ± 1.9	47.9 \pm 1.8	47.2 ± 1.8	52.2 ± 2.2	51.7 \pm 1.1	48.4 ± 1.2	50.3 ± 1.2	43.7 ± 2.2	46.1 ± 6.4	55.9 ± 0.3	49.2 \pm 3.5
6	48.7 ± 1.9	48.1 ± 1.8	47.2 ± 1.9	51.7 ± 2.3	52.3 ± 1.1	49.1 ± 1.2	51.1 ± 1.3	44.1 ± 2.3	49.9 ± 4.3	57.3 ± 0.4	50.0 ± 3.5
6.25	49.2 ± 1.9	48.6 ± 1.8	47.8 ± 1.9	52.7 ± 2.3	52.3 \pm 1.1	48.9 ± 1.2	50.9 ± 1.2	43.7 ± 2.2	51.5 ± 4.5	58.5 ± 0.4	50.4 ± 3.9
$6.5\,$	49.8 ± 2.0	49.3 ± 1.9	48.2 \pm 1.9	52.1 ± 2.3	52.9 ± 1.1	49.1 ± 1.2	51.3 ± 1.2	43.5 ± 2.2	60.2 ± 7.1	61.4 ± 0.4	51.8 ± 5.4
6.75	50.6 ± 2.0	50.0 ± 2.0	48.5 ± 2.0	51.8 ± 2.3	53.8 ± 1.1	49.7 ± 1.2	51.9 ± 1.3	43.9 \pm 2.3	$56.6~\pm~7.5$	62.3 ± 0.5	51.9 ± 4.9
$7\degree$	51.2 ± 2.1	50.6 ± 2.0	49.4 ± 2.0	52.8 ± 2.3	53.7 ± 1.1	49.6 ± 1.2	51.8 ± 1.2	43.8 ± 2.2	57.5 \pm 5.1	64.4 ± 0.5	52.5 \pm 5.4
7.25	51.8 ± 2.1	51.0 ± 2.1	48.3 ± 2.1	51.8 ± 2.4	54.7 ± 1.1	49.9 ± 1.2	52.4 ± 1.3	43.0 ± 2.2	59.4 \pm 5.2	65.9 ± 0.5	52.8 ± 6.2
7.5	52.2 ± 2.1	51.5 ± 2.0	49.7 ± 2.0	52.6 ± 2.3	54.4 ± 1.1	50.3 ± 1.2	52.7 ± 1.3	43.4 ± 2.2	58.8 ± 8.4	67.4 ± 0.5	53.3 ± 6.3
7.75	52.7 ± 2.2	51.9 ± 2.1	49.9 ± 2.0	53.5 ± 2.3	54.6 \pm 1.1	50.5 ± 1.2	52.9 ± 1.3	43.5 ± 2.2	58.3 ± 8.7	69.3 ± 0.6	53.7 \pm 6.7
8	53.5 ± 2.2	52.7 \pm 2.2	50.3 ± 2.2	52.7 ± 2.4	55.7 ± 1.1	51.0 ± 1.2	53.5 \pm 1.3	43.8 ± 2.3	$61.7~\pm~5.8$	69.6 ± 0.6	54.4 \pm 6.9
8.25	53.3 ± 2.2 54.2 \pm 2.3	52.6 ± 2.1	50.5 ± 2.1	53.5 ± 2.4	56.0 ± 1.1	51.5 ± 1.2	53.7 ± 1.3	44.4 ± 2.2	61.5 ± 6.0	70.7 ± 0.6	54.8 ± 7.0
8.5 8.75	55.5 ± 2.3	53.4 ± 2.2 54.8 ± 2.3	50.8 ± 2.2 52.1 ± 2.3	52.6 ± 2.4 53.5 ± 2.4	57.1 ± 1.2 56.9 ± 1.1	51.9 ± 1.3 52.0 ± 1.2	54.2 ± 1.3 54.4 ± 1.3	44.6 ± 2.4	60.3 ± 6.2 67.6 ± 6.3	71.7 ± 0.7	55.1 ± 7.1 56.5 ± 8.2
9	53.6 ± 2.3	52.9 \pm 2.2	51.2 ± 2.2	54.3 ± 2.4	56.8 ± 1.2	51.7 ± 1.3	54.1 ± 1.4	44.9 ± 2.3 $44.2~\pm~2.3$	$61.8\,\pm\,6.6$	73.5 ± 0.7 $72.8\,\pm\,0.7$	55.3 ± 7.6

Table S.5: Summary of P estimates for step sizes l ranging from 4 nm to 9 nm. The optimal l is indicated in gray.

DNA variant	$P \pm$ sem (nm)							$P \pm$ sp (nm)	t_{optimal} (nm)		
	$\langle \cos \theta \rangle$	$\langle \theta^2 \rangle$	$\langle \theta^4$	$\langle \theta^6 \rangle$	$\langle \mathbf{R} \cdot \mathbf{u}_0 \rangle$	$\langle R^2 \rangle$	$\langle R^4 \rangle$	$\langle R^4 \rangle - \langle R^2 \rangle^2$	$-\ln G(\theta)$	$\langle \cos \chi \rangle$	
	53.5 ± 2.3	53.3 ± 2.2	53.1 ± 2.3	54.5 ± 2.5	52.8 ± 1.1	50.3 ± 1.2	51.8 ± 1.2	51.1 ± 3.0	54.7 ± 6.0	58.2 ± 0.3	5.5
$\mathbf{2}$	60.1 ± 3.1	58.0 ± 3.0	52.8 ± 2.9	53.8 ± 3.0	65.7 ± 1.9	59.5 ± 1.9	62.3 ± 2.0	54.0 ± 3.6	55.4 ± 7.5	57.0 ± 0.4	6.75
3	54.3 ± 2.0	53.7 ± 1.9	51.9 ± 2.0	54.2 ± 2.3	55.9 ± 1.1	53.7 ± 1.2	55.4 ± 1.2	52.5 ± 2.6	54.9 ± 6.3	60.8 ± 0.4	5.75
$\overline{4}$	57.8 ± 3.3	56.6 ± 3.2	53.5 ± 3.0	55.0 ± 3.3	61.6 ± 2.0	56.4 ± 1.9	58.8 ± 2.0	52.4 ± 3.9	53.0 ± 6.3	59.6 ± 0.5	5.75
5	53.5 ± 2.1	52.1 ± 2.0	50.0 ± 2.1	54.3 ± 2.4	59.8 ± 1.5	56.5 ± 1.5	59.0 ± 1.6	50.3 ± 2.5	44.0 ± 3.8	49.8 ± 0.3	5.25
6	45.5 ± 1.9	45.6 ± 1.8	46.4 ± 1.9	49.9 ± 2.1	46.6 ± 1.0	44.7 ± 1.1	45.2 ± 1.1	48.5 ± 2.8	49.0 ± 6.1	51.2 ± 0.3	5.5
	79.6 ± 3.7	78.7 ± 3.7	75.2 ± 3.9	74.3 ± 4.5	85.8 ± 2.1	80.5 ± 2.3	82.7 ± 2.4	78.2 ± 5.2	81.0 ± 8.4	84.9 ± 0.7	7.75

Table S.6: Summary of P estimates at optimal step size l_{optimal} for the thymine variants.

Supporting References

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