

## Additional File 1.

### Multicriteria global optimization for biocircuit design

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This additional file contains the generic equations for the model of the genetic circuit used as a working example through the main text. The dynamic model equations and the kinetic parameters have been obtained from Ref. [1].

#### Model Equations and Parameters

The states of the generic model are the concentrations of all the species involved  $lacI$ ,  $LacIIP TG$ ,  $tetR$ ,  $tetRaTc$ ,  $cI$ ,  $araC$  and the generic model consists of 6 ordinary differential equations representing the mass balances for the system. The coefficients  $Y(i, j)$  for  $i = 1, \dots, 8$  and  $j = 1, \dots, 4$  are binary variables that take value 1 if the corresponding pair is active and 0 if it is inactive for a given circuit.

$$\begin{aligned} dlacI &= +Y(1, 2)\alpha_{lac}/(1 + K_{lac1}lacI^4) \\ &+ Y(2, 2)\alpha_{lac}/(1 + K_{lac2}lacI^4) \\ &+ Y(3, 2)\alpha_{lac}/(1 + K_{lac3}lacI^4) \\ &+ Y(4, 2)\alpha_{lac}/(1 + K_{lac4}lacI^4) \\ &+ Y(5, 2)\alpha_{\lambda}/(1 + K_{lambda}cI^2) \\ &+ Y(6, 2)\alpha_{tet}/(1 + K_{tet1}tetR^2) \\ &+ Y(7, 2)\alpha_{tet}/(1 + K_{tet2}tetR^2) \\ &+ Y(8, 2)\alpha_{ara}/(1 + K_{araC}araC^2) \\ &- Kf \cdot lacI \cdot IPTG \\ &+ Kb \cdot lacIIP TG \\ &- K_{deglacI} \cdot lacI \\ dlacIIP TG &= +Kf \cdot lacI \cdot IPTG \\ &- Kb \cdot lacIIP TG \\ &- K_{degcpx} \cdot lacIIP TG \\ dtetR &= +Y(1, 1)\alpha_{lac}/(1 + K_{lac1}lacI^4) \\ &+ Y(2, 1)\alpha_{lac}/(1 + K_{lac2}lacI^4) \\ &+ Y(3, 1)\alpha_{lac}/(1 + K_{lac3}lacI^4) \\ &+ Y(4, 1)\alpha_{lac}/(1 + K_{lac4}lacI^4) \\ &+ Y(5, 1)\alpha_{\lambda}/(1 + K_{lambda} \cdot cI^2) \\ &+ Y(6, 1)\alpha_{tet}/(1 + K_{tet1}tetR^2) \\ &+ Y(7, 1)\alpha_{tet}/(1 + K_{tet2}tetR^2) \end{aligned}$$

$$\begin{aligned}
& + Y(8, 1)\alpha_{tet}/(1 + K_{araC}araC^2) \\
& - K_{ftetR} \cdot aTc \\
& + K_b \text{ tetRaTc} \\
& - K_{degtetR} \text{ tetR} \\
dtetRaTc = & + K_f \cdot tetR \cdot aTc \\
& - K_b \cdot tetRaTc \\
& - K_{degcpx} \cdot tetRaTc \\
dcI = & + Y(1, 3)\alpha_{lac}/(1 + K_{lac1}lacI^4) \\
& + Y(2, 3)\alpha_{lac}/(1 + K_{lac2}lacI^4) \\
& + Y(3, 3)\alpha_{lac}/(1 + K_{lac3}lacI^4) \\
& + Y(4, 3)\alpha_{lac}/(1 + K_{lac4}lacI^4) \\
& + Y(5, 3)\alpha_{\lambda}/(1 + K_{lambda} \cdot cI^2) \\
& + Y(6, 3)\alpha_{tet}/(1 + K_{tet1}tetR^2) \\
& + Y(7, 3)\alpha_{tet}/(1 + K_{tet2}tetR^2) \\
& + Y(8, 3)\alpha_{tet}/(1 + K_{araC}araC^2) \\
& - K_{degcI}cI \\
daraC = & + Y(1, 4)\alpha_{lac}/(1 + K_{lac1}lacI^4) \\
& + Y(2, 4)\alpha_{lac}/(1 + K_{lac2}lacI^4) \\
& + Y(3, 4)\alpha_{lac}/(1 + K_{lac3}lacI^4) \\
& + Y(4, 4)\alpha_{lac}/(1 + K_{lac4}lacI^4) \\
& + Y(5, 4)\alpha_{\lambda}/(1 + K_{lambda} \cdot cI^2) \\
& + Y(6, 4)\alpha_{tet}/(1 + K_{tet1}tetR^2) \\
& + Y(7, 4)\alpha_{tet}/(1 + K_{tet2}tetR^2) \\
& + Y(8, 4)\alpha_{tet}/(1 + K_{araC}araC^2) \\
& - K_{degaraC}araC.
\end{aligned}$$

The values of the parameters are included in the following Table S1.

Table S1 Parameters from Dasika and Maranas [1]

Parameter	value	units
$\alpha_{lac}$	1.215	
$\alpha_{tet}$	1.215	
$\alpha_{\lambda}$	2.92	
$\alpha_{ara}$	1.215	
$K_{\lambda}$	0.33	$nm^{-2}$
$K_{tet1}$	0.014	$nm^{-2}$
$K_{tet2}$	1.4	$nm^{-2}$
$K_{lac1}$	10	$nm^{-2}$
$K_{lac2}$	0.01	$nm^{-2}$
$K_{lac3}$	0.001	$nm^{-2}$
$K_{lac4}$	0.00001	$nm^{-2}$
$K_{araC}$	2.5	$nm^{-2}$
$K_{deglacI}$	0.0346	$s^{-1}$
$K_{degtetR}$	0.0346	$s^{-1}$
$K_{degcI}$	0.0693	$s^{-1}$
$K_{degarac}$	0.0115	$s^{-1}$
$K_{degcp\bar{x}}$	0.0693	$s^{-1}$
$K_f$	0.05	$nm^{-1}s^{-1}$
$K_b$	0.1	$s^{-1}$

## References

- [1] Dasika, M.S., Maranas, C.D.: Optcircuit: An optimization based method for computational design of genetic circuits. BMC Syst Biol 2, 24 (2008)