¹ S4 Detailed model description

² S4.1 Statistical model

The statistical model formally describes the framework and assumptions of the model for the kitchen task scenario. First, an extension of the CSSM to correctly handle durative actions is described. Then the overall DBN interpretation of the model is given. Afterward, the sensor model, duration model, and action selection heuristics are discussed in detail.

7 S4.1.1 Durative actions

The model given in Appendix S2 assumes that actions take a single time step, where progression of time 8 is given by observation events. This requires that sensor data – usually some kind of real time signal – 9 is already partitioned into segments that correspond to individual actions, each segment representing a 10 single observation. In this case, the subscript t in y_t simply counts the number of actions that have been 11 observed. However, in general correct segmentation needs additional context information for disambigua-12 tion [1], such as the possible sequence of actions. The assumption that the CSSM will be presented with 13 observations that represent complete action sightings, as for instance used in all but one of the previous 14 CSSM studies (Sec. 1.3.2), thus hides important aspects of the real-world inference problem. 15

Therefore, a model was chosen where multiple observations may correspond to a single action. This model introduces real-valued random variables U and V that represent the starting time of an action Aand its duration. The action duration density $\tau(v \mid a, u) := p(V \mid A, U)$ defines the probability that action A stops at time V if started at time U. Let $F_{\tau}(v \mid a, u)$ be the cumulative distribution function of τ . The probability that an action's duration lies in the interval (v, v'] then is $\zeta_{a,u}^{v,v'} := P(v < V \le v' \mid a, u) =$ $F_{\tau}(v' \mid a, u) - F_{\tau}(v \mid a, u)$. If this duration is known to be greater than v, the corresponding conditional probability is $P(v < V \le v' \mid a, u, V > v) = \zeta_{a,u}^{v,v'}/\zeta_{a,u}^{v,\infty}$.

²³ Note that durative actions will increase state space complexity.

24 S4.1.2 Overall CSSM model structure

For the probabilistic model of Sec. 1.2 (see Appendix S2 for details), a DBN with the structure given in Fig. 1 was used. $Y_t = (W_t, Z_t)$ is the observation data for time step t. V_t is the associated time stamp, required to be strictly increasing. As discussed in Appendix S2, state and action observations were assumed to be conditionally independent, i. e., $p(y_t | a_t, s_t) = p(w_t | s_t) p(z_t | a_t)$.

 $X_{t} = (A_{t}, D_{t}, G_{t}, S_{t}, U_{t}) \text{ defines the hidden state. For this study, } G_{t}, \text{ the current goal, could be}$ assumed to be constant, so that $p(g_{t} | x_{t-1}) = [g_{t} = g_{t-1}]$. This allowed to efficiently precompute goal distance values, which depend on G_{t} . The boolean flag D_{t} signals termination of A_{t-1} in the interval $(v_{t-1}, v_{t}]$. It is a Bernoulli random variable defined by $p(D_{t}=1 | v_{t}, v_{t-1}, a_{t-1}, u_{t-1}) = \zeta_{t}/\zeta_{a_{t-1}, u_{t-1}}^{v_{t-1}, \infty}$ where $\zeta_{t} := \zeta_{a_{t-1}, u_{t-1}}^{v_{t-1}, v_{t}}$. The variable D_{t} introduces a context-specific independence [2] into the DBN: if $d_{t} = 0$, then A_{t}, S_{t} , and U_{t} carry over their values from the previous state and are independent of their other parents. Otherwise, new values for A_{t}, S_{t} , and U_{t} are selected as follows:

A new action is selected according to γ by: $p(a_t \mid d_t = 1, s_{t-1}, a_{t-1}, g_t) = \gamma(a_t \mid g_t, s_{t-1}, a_{t-1})$. U_t 36 is the starting time of action A_t , given by $p(u_t | d_t = 1, u_{t-1}, v_t, v_{t-1}, a_{t-1}) = \bar{\tau}(u_t | u_{t-1}, v_t, v_{t-1}, a_{t-1}),$ 37 where $\bar{\tau}(u_t | u_{t-1}, v_t, v_{t-1}, a_{t-1}) := [v_{t-1} < u_t \le v_t] \tau(u_t | a_{t-1}, u_{t-1})/\zeta_t$ is the truncated duration density, 38 constrained by $v_{t-1} < u_t \leq v_t$. S_t is the LTS state for time step t: either the result of applying the 39 new action to the previous state, or by carrying over the old state. For the purpose of this study, 40 actions could be assumed to be deterministic and with instantaneous effect, giving the simple model 41 $p(s_t | d_t = 1, s_{t-1}, a_t) = [s_t = a_t(s_{t-1})]$. As outlined for aLTS model development in Appendix S3. 42 non-deterministic effects for modeling complex interleaving were represented by multiple actions. 43



Figure 1. CSSM DBN structure. Boxes represent tuples of random variables. An arc starting / ending at a box (= a tuple) represents a set of arcs connected to the tuple's components. Nodes with double outline signify observed random variables.

44 S4.1.3 Sensor models and scrambling

As construction of an elaborate observation model was not in the focus of this study, the following model 45 was selected for its conceptual and computational simplicity: all actions a of a given class c = class(a)46 share the same observation distribution, such that $p(z \mid a) := p(z \mid c)$ and the distributions $p(z \mid c) :=$ 47 $N(z \mid \mu_c, \Sigma_c)$ were represented by multivariate normal distributions with unconstrained covariance Σ_c . 48 The parameters μ_c , Σ_c were computed from the pool of all observations annotated with class c from all 49 data sets. Although there is no reason to believe that the observation data is particularly well represented 50 by this model, it was found to perform reasonably well in the baseline models, justifying its further use in 51 this study. The 16 action classes can be seen in Fig. 6 or Fig. S3. For example, an action class is TAKE, 52 while the actions belonging to it are take carrot, take bottle, take spoon etc. 53

A potential significant limitation of this model is its stationarity with respect to durative actions, 54 which might be violated by the sensor data. A "run" for class c is a consecutive sequence of observations 55 labeled with c. A run (often) represents an action that lasts several time steps. It might be the case that 56 observations in the middle of a run are more "typical" for action class c than at the beginning (or end) of 57 the run, where the transition to a different action class takes place and both kinds of motions are mixed. 58 In this case, the expected probability of observations should increase from the run borders towards the 59 run center. This effect should be specifically prominent for actions with long durations (which have long 60 stable "center periods"). This could, for instance, impact the ability to correctly detect the start of such 61 actions and eventually degrade recognition performance. 62

⁶³ Conceptually, a better option to solve this problem is either to include temporal information into the ⁶⁴ observations [3] or – more general – to use a hierarchical approach, where the temporal structure of an ⁶⁵ action's observations are represented by suitable sub-models [4]. A much simpler potential solution is to scramble observations within a run. This will destroy order effects and other dependencies between
 observations in a run. Clearly this approach is only possible in offline situations with data where the
 runs are already delimited (either by annotations or by some suitable segmentation algorithm). However,
 regarding the study objectives, the use of scrambling is considered a justified surrogate for defining
 appropriate sub-models.

As alternative to the IMU sensors, which give continuous-domain observations of the A state component, a location-based model was set up, giving categorical observations (place names) of the S state component. Motivation for introducing this alternative observation model was to demonstrate that CSSMs allow an exchange of observed X component without requiring adaptation of the system model. In addition, it was of interest to:

(i) Test in how far a switch from continuous (IMU) to discrete (place names) observation modalities
 introduces additional challenges for inference.

(ii) Provide a non-peaked observation model that assigns a non-negligible probability to every state, in
 order to test susceptibility of inference method to this observation model property.

With respect to these objectives, a very simple model was considered sufficient, where the locations of 80 the protagonist (3 places) and the food (6 places) were used (see Tbl. S5). For the conditional probability 81 $p(z_t | s_t)$ the value 10⁻⁶ was used in case the locations observations z_t did not match the locations found 82 in s_t and essentially 1 otherwise. The observations themselves were computed from the aLTS model by 83 stepwise execution of the aLTS ground actions recorded in the annotations and using the location slot 84 values of the observed objects in the resulting state. While being realistic with respect to the temporal and 85 causal structure of the underlying human activity, these synthetic observations are unrealistic concerning 86 the precision of temporal alignment and error model; they can be expected to exaggerate the achievable 87 precision. Nevertheless, as this was a convenient mechanism to obtain data for new observation models 88 for simple comparison purposes, its use was considered legitimate. 89

90 S4.1.4 Duration model

For simplification it was assumed that all actions of a given class share the same action duration distribution and that the duration of an action does not depend on the time the action has started. Therefore, $\tau(v | a, u) = \tau^*(v - u | class(a))$ where $\tau^*(d | c)$ is the class-specific duration distribution. As there is yet no prior knowledge on action durations, it was necessary to use the durations found in the training data as proxy.

Note that duration distributions $\tau^*(d|c)$ with large or even infinite support increase the branching factor. In order to determine this effect on inference performance, an instance based model (with finite 97 support) and a parametric duration model (infinite support) was built. Let $(d_{c,1},\ldots,d_{c,n_c})$ be the set 98 of durations observed for actions of class c. The instance based model was given by the corresponding 99 empirical distribution function, so that $F_{\tau^*}(d \mid c) := n_c^{-1} \sum_{i=1}^{n_c} [d_{c,i} \leq d]$, where F_{τ^*} is the distribution 100 function of τ^* . For the parametric models, an approach was chosen that would provide a trade-off between 101 technical simplicity and flexibility. First, a lognormal model for the pooled observation was built, see 102 Fig. 2 for a comparison with the actual durations and a kernel density estimate. Then those classes were 103 determined whose means were significantly (at the .05 α level) different from the pooled mean by fitting 104 an ANOVA model (analysis of variance). For these special classes as well as for the remaining pooled 105 classes, the distribution giving the maximum likelihood was selected from a set of candidate distributions 106 whose parameters were fitted to the observed class durations. The set of candidate distributions was 107 Cauchy, exponential, gamma, geometric, lognormal, negative binomial, normal, Poisson, and Weibull. 108

The parametric models were expected to have an impact on performance for two reasons: (i) they might not provide a good fit to the empirical data, (ii) since they are continuous, they provide a greater number of possible durations, thereby increasing the branching factor and thus inference complexity.



Figure 2. Kernel density estimate of pooled action durations vs. fitted lognormal density. Blue circles are the observed action durations. The red line is the kernel density estimate, the green line the fitted lognormal density.

112 S4.1.5 Action selection model

As primary goal-driven action selection feature, the goal distance feature f_{δ} as discussed in Appendix S2 was chosen. Goal distances were computed by an exhaustive process, computing the set of LTS states reachable from the initial state and then for all reachable states the shortest path to a goal state. For simplicity, unit costs were used for actions. This approach will become intractable with models of increasing state space complexity. In addition, it is not yet established that goal distance indeed best describes human action selection preferences. Approximate distance values therefore might achieve the same result, for a much lower computational cost. Two approximations were considered in this study:

• A goal distance heuristic f_h , that assigns heuristic distances to LTS states based on values of LTS state variables. The trial task's script consisting of 14 serial task steps was used to define a map from LTS state s to remaining script steps h(s) based on its state variable values (see Tbl. S1 for this map). h(s) then was used as distance value. (Most script tasks required several LTS actions for their realization.) The motivation of this heuristic is the idea that prior knowledge on the typical coarse-grained sequential structure of everyday activities should be easy to obtain [5,6]. Analyzing f_h thus should provide insight into the usefulness of such knowledge.

• A restricted goal distance feature $f_{\bar{\delta}}$. Here, only those LTS states were considered that are visited when using the annotations as exact observations. All other states discovered during inference received the nominal goal distance 100. Restricted goal distance $f_{\bar{\delta}}$ should give an upper limit to the gain achievable by a goal distance measure.

To gain insight on the effect of weight factors, each of these features was tested with the weight values $\lambda_i = -(2^k), k \in \{0, \dots, 4\}$, using exponential probing. To limit experimental complexity, we refrained from evaluating interactions between features by only assigning one of $f_{\delta}, f_h, f_{\bar{\delta}}$ a non-zero weight. In the special case $\lambda_{\bar{\delta}} = \lambda_h = \lambda_{\bar{\lambda}} = 0$ all applicable actions receive the same selection probability.

In the special case $\lambda_{\delta} = \lambda_h = \lambda_{\bar{\delta}} = 0$ all applicable actions receive the same selection probability, resulting in uniform selection. (This *locally uniform* selection strategy is not the same as giving each possible action sequence the same probability – such a globally uniform action selection model requires a
 considerable more complex feature computation.)

¹³⁸ S4.2 iLTS model development

Building the inference LTS (iLTS, cf. Appendix S3) requires two steps: choosing an appropriate modeling
language and implementing the model. The following two sections justify the choice and present the model
development process used.

¹⁴² S4.2.1 Modeling language

As pure execution speed was not the primary concern of this study, Common Lisp was chosen as implementation language for the inference procedures. This allowed a very convenient way to represent actions in a PDDL / STRIPS like fashion as S-expressions, providing considerable latitude regarding the expressive power available for defining precondition terms and effect expressions, as essentially any valid Lisp expression could be used. For instance, the action of taking the food from the cutting board was defined by the following expression:

State variables are referred to by symbol lists, such as (\$ location self). The precondition states 155 that the protagonist (self) and the cutting board must be at the same location, the food must be on 156 the cutting board, and the protagonist needs to have at least one free hand. The effect states that the 157 location of the food will now be one of the protagonist's hand and that he has one less free hand available. 158 The state model was created by traversing all action definitions, collecting the state variable references, 159 and compiling this to a Lisp defstruct containing one structure slot for each state variable. At the same 160 time, action definitions were compiled to two pairs of Lisp functions, the first computing the precondition 161 value, the second one for applying the effect to a state. State variable references were replaced by 162 the corresponding slot access functions for the state defstruct; the value assignment in the effect was 163 performed via setf. For efficiency considerations, only atomic values (symbols, characters, integers, and 164 floating point numbers) were allowed as values for state variables. Therefore, states could be considered 165 as words of constant length, allowing the use of tries as dictionaries for handling state sets, providing 166 significantly faster access than hash tables in the Lisp environment [7] used in this study. 167

¹⁶⁸ S4.2.2 Model development process

¹⁶⁹ A two-stage process was used for iLTS model development. First a *feasible solution* \mathcal{A}^* for the domain ¹⁷⁰ model (the set of action definitions) was constructed iteratively, and then this solution was refined to ¹⁷¹ the final model \mathcal{A} using local model modifications. For constructing the feasible solution, the domain ¹⁷² expert used an iterative procedure for successively building action sets $\mathcal{A}_0, \mathcal{A}_1, \ldots, \mathcal{A}_S =: \mathcal{A}^*$ of increasing ¹⁷³ complexity.

Constructing the feasible solution begins by setting $\mathcal{A}_0 := \emptyset$. For the current action set \mathcal{A}_s , the model developer applies all action sequences obtained from the annotations in parallel and identifies the smallest t where the action $a_{i,t}$ of some dataset i fails at time t. For instance, the first action wash hands from the annotations of subject 1 (cf. Tbl. S3) is executed in the iLTS of \mathcal{A}_0 , failing because this action is not included in $\mathcal{A}_0 = \emptyset$. If no action sequence fails, the feasible solution $\mathcal{A}^* := \mathcal{A}_s$ has been found.

Otherwise either (a) $a_{i,t}$ refers to an action not contained in \mathcal{A}_s (as in the example), or (b) $a_{i,t}$ is in 179 \mathcal{A}_s , but its precondition is not met in the current iLTS state after applying the preceding actions (for 180 instance because take is executed twice, but was previously modeled to allow only one object in hand. 181 cf. Tbl. S3, t = 4-8). In case (a), the model developer adds a new action schema with precondition and 182 effect matching the informal semantics of the domain. In case (b), the model developer either relaxes the 183 precondition or extends the effect of some other action such that the precondition of $a_{i,t}$ is met. It is the 184 task of the domain expert to judge which of the refinement strategies to apply for reconciling a failure. 185 The developer repeats the process with $\mathcal{A}_{s+1} := \mathcal{A}_s$ until a feasible solution has been found. 186

In the second step, the domain expert would refine \mathcal{A}^* to the final action set \mathcal{A} by adding preconditions in order to limit the number of possible plans. (For instance, in the case of the given trial setting, the protagonist would sit down at the table only after the food has been cooked). Note that this two stage process – consisting of the iterative construction of a feasible solution and then applying local search to refine the feasible solution towards a local optimum \mathcal{A} – is similar to heuristic optimization strategies for solving integer programming problems.

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