

Supplementary material for:
Towards more accurate ancestral protein genotype–phenotype
reconstructions with the use of species tree-aware gene trees.

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Supplementary Material

Homogeneous and site-heterogeneous models employed in this study

Site-homogeneous substitution models assume that the evolutionary process is constant among sites. When the Markovian process is time-reversible, the transition probability matrix is computed by multiplying the matrix of exchangeabilities with the diagonal matrix of equilibrium frequencies (Whelan and Goldman, 2001). Hereafter, the latter matrix is referred to as a profile of equilibrium frequencies. In the case of site-homogeneous models, both the exchangeabilities and the profile are constant among sites. The LG site-homogeneous model (Le and Gascuel, 2008) is one of the models employed in our study.

To model the heterogeneity of the process among sites, mixture models were considered. These approaches use sets of different models in which each model is assigned a particular weight. The likelihood of a given site is then the sum of all weighted likelihoods computed with each model of the mixture (Le et al., 2008b). The models of the mixture may have been learned to take into account protein properties that are heterogeneous along the sequence and that influence the substitution process, such as solvent exposure or secondary structure. In line with this, Le et al. (2008b) and Le and Gascuel (2010) proposed a series of empirical mixture models that outperform any site-homogeneous models. They learned their models on the HSSP database (Schneider et al., 1997) of aligned protein sequences in a supervised or unsupervised way. In the supervised way, sites were *a priori* assigned to a component of the mixture given knowledge about their localization in the protein, and the exchangeabilities and equilibrium frequencies of each model were subsequently learned from these sites. Le et al. (2008b) and Le and Gascuel (2010) inferred four models in this way:

- EX2, which is composed of two matrices corresponding to exposed/buried sites
- EX3, which is composed of three matrices corresponding to highly exposed/intermediate/buried sites
- EHO, which is composed of three matrices corresponding to extended/helix/other sites
- EX_EHO, which is composed of six matrices corresponding to the combination of EX2 and EHO.

In the unsupervised way, both site partitions and their corresponding matrices were directly learned from the data. Two models were proposed by Le et al. (2008b):

- UL2, which is composed of two matrices
- UL3, which is composed of three matrices

Note that all these models are mixtures of matrices with both exchangeabilities and equilibrium frequencies varying among components.

Mixture of profiles were also previously proposed (Le et al., 2008a). In these site-heterogeneous models, only the profiles vary among the components of the mixture, which share the same exchangeabilities. The components of these mixtures were learned in an unsupervised way. Six models were proposed, with 10, 20, 30, 40, 50 or 60 different profiles and named C10 to C60.

All these site-homogeneous and site-heterogeneous models were run on the LeuB data to evaluate their ability to efficiently fit the data (see Material & Methods in the main text and below)

Data fitting

To determine the best model in terms of data fitting to perform ASR on the LeuB data, we used the AIC criterion (Akaike, 1973). This criterion allows the evaluation of non-nested models by penalizing the number of parameters influencing the likelihood. The AIC criterion is computed as follows:

$$AIC = -2 \times \ln L + 2 \times K,$$

with $\ln L$ the final likelihood and K the total number of parameters. For a site-homogeneous model, only the α parameter of the Γ distribution is involved, so that $K = 1$. For site-heterogeneous models, the sum of all component-specific weights equals 1, so that $K = (n - 1) + 1$, with n the number of components of the mixture model.

Differences between LeuB_{S-unaw} and LeuB_{S-aw} enzymes

LeuB_{S-unaw} and LeuB_{S-aw} differ by approximately 10% in terms of amino acid sequence. In an attempt to rationalise the biochemical differences between LeuB_{S-unaw} and LeuB_{S-aw}, we modelled the structure of LeuB_{S-aw} with SWISS-MODEL (Arnold et al., 2006) (Supplementary Figure 4) and mapped on this structure the amino acid differences with LeuB_{S-unaw}. The active site, as well as the co-factor binding site and residues involved in the interaction between LeuB monomers are unchanged between the two enzymes. The large majority of the amino acid differences are located at the surface of the protein. One of these differences is located near the active site, although it does not involve a change in physicochemical properties: this residue is VAL in LeuB_{S-aw} and ALA in LeuB_{S-unaw}. In conclusion, deciphering the exact reason(s) of the biochemical differences between the two enzymes would require additional experiments that are beyond the scope of this manuscript.

Supplementary Table

Supplementary Table 1: **Patterns of Grantham scores for reconstruction errors obtained with the LG S-unaware trees.** Number of reconstruction errors were sorted increasingly along the Grantham score. All 190 possible pairwise substitutions are represented. To a given Grantham score may correspond several amino acid pairs. Categories of Grantham scores with a percentage of errors higher than 1% are in bold lines. The patterns of Grantham scores for the S-unaware trees reconstructed with the C60 model or for the S-aware trees were similar and are not represented here.

Grantham Score	AA substitution	Number of errors	% of errors
5	L--I	3178	3.96
10	M--I	668	0.83
15	M--L	1612	2.01
21	F--I V--M	903	1.12
22	F--L Y--F	3791	4.72
23	D--N	1317	1.64
24	H--Q	382	0.48
26	K--R	2053	2.56
27	P--A	1191	1.48
28	F--M	218	0.27
29	E--Q H--R V--I	6011	7.49
32	K--H V--L	2576	3.21
33	Y--I	179	0.22
36	Y--L Y--M	619	0.77
37	Y--W	486	0.61
38	T--P	314	0.39
40	H--E W--F	697	0.87
42	E--N P--G T--Q	1188	1.48
43	Q--R	682	0.85
45	E--D	2256	2.81
46	Q--N S--N	1290	1.61
47	T--H	156	0.19
50	V--F	374	0.47
53	K--Q	801	1.00
54	E--R	480	0.60
55	V--Y	238	0.30
56	K--E S--G	2459	3.06
58	T--A T--S	3267	4.07
59	T--G	393	0.49
60	G--A	2678	3.33

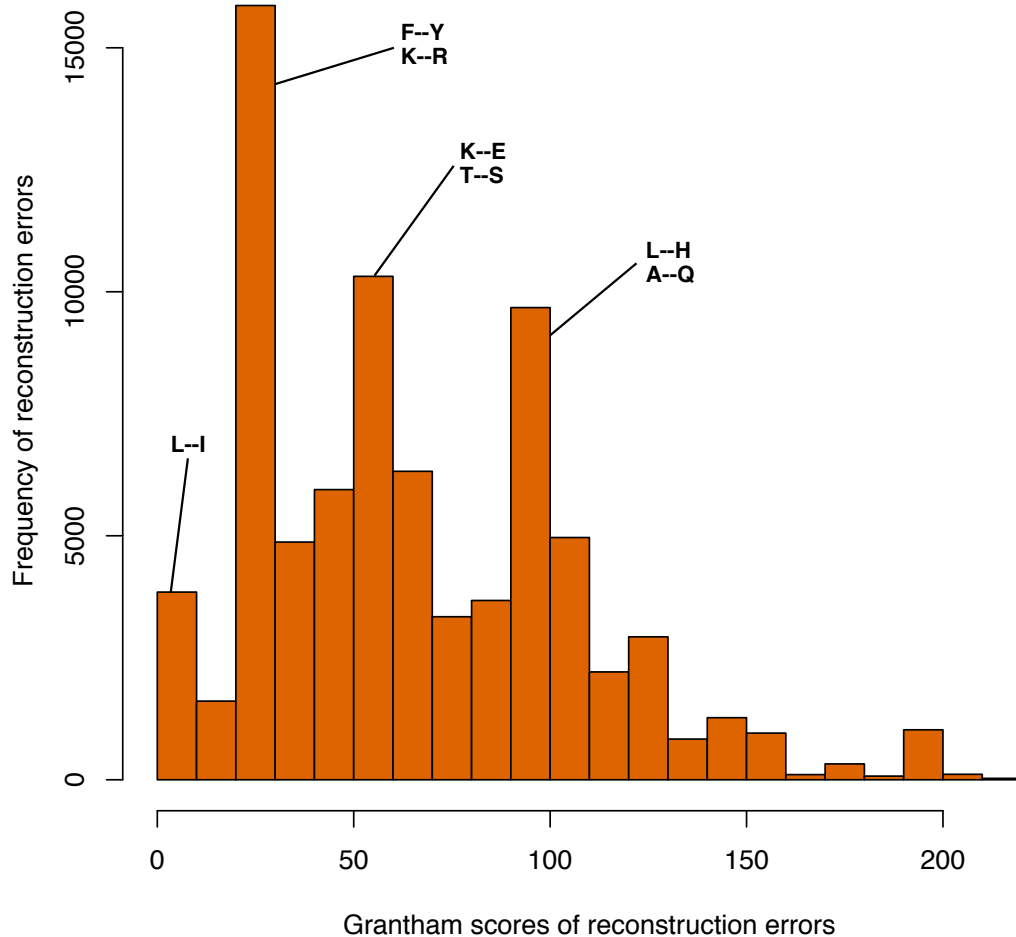
61	Q--D W--I W--L	744	0.93
64	V--A	1762	2.19
65	S--D T--N T--E	1739	2.17
67	W--M	68	0.08
68	H--N S--Q V--P	1097	1.37
69	V--T	911	1.13
71	T--R	384	0.48
74	S--P	644	0.80
76	P--Q	215	0.27
77	P--H Y--R	222	0.28
78	T--K	506	0.63
80	G--N S--E	1370	1.71
81	H--D T--M	414	0.52
83	Y--H	555	0.69
84	M--A V--H	356	0.44
85	T--D Y--K	506	0.63
86	N--R H--A	573	0.71
87	G--Q M--H P--M	383	0.48
88	V--W	48	0.06
89	S--H T--I	839	1.04
91	Q--A M--R P--N	822	1.02
92	T--L Y--T	560	0.70
93	P--E	387	0.48
94	G--D I--A I--H K--N	1874	2.33

95	M--K P--I	204	0.25
96	D--R L--A V--R V--Q	1334	1.66
97	I--R F--R V--K	472	0.59
98	G--E H--G P--L	951	1.18
99	L--H S--A Y--Q	2857	3.56
100	F--H	215	0.27
101	K--D M--Q W--R	683	0.85
102	L--R K--I F--K	576	0.72
103	P--R P--K T--F	581	0.72
106	K--A	611	0.76
107	E--A K--L	1394	1.74
108	P--D	239	0.30
109	I--Q V--G	301	0.37
110	S--R W--K Y--P	579	0.72
111	N--A	414	0.52
112	R--A S--C Y--A	1068	1.33
113	L--Q F--A	548	0.68
114	P--F	57	0.07
115	W--H	54	0.07
116	F--Q	69	0.09
121	S--K V--E	795	0.99
122	Y--E	70	0.09

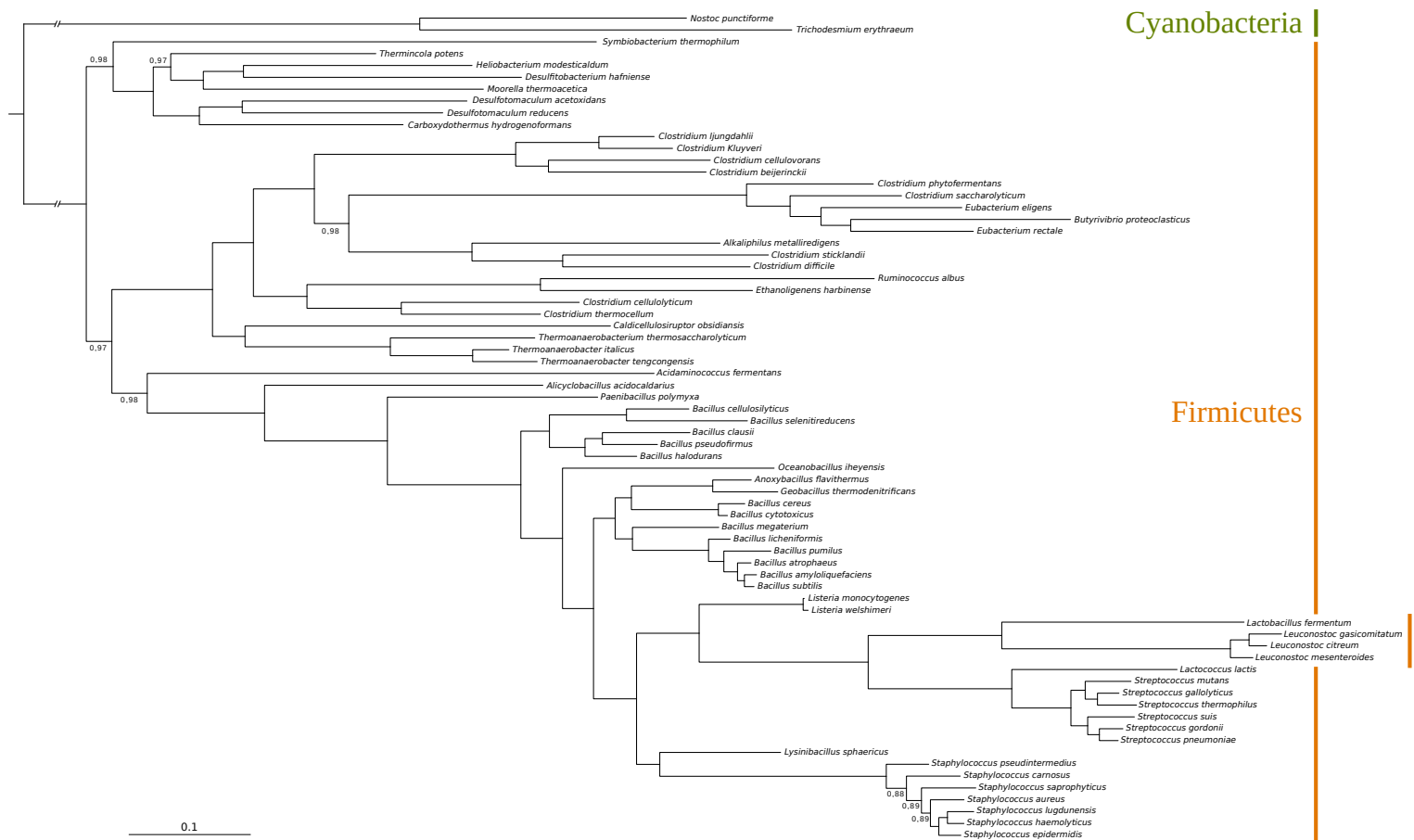
124	V--S	434	0.54
125	G--R	405	0.50
126	D--A M--E	729	0.91
127	K--G M--G	439	0.55
128	W--T	24	0.03
130	W--Q	33	0.04
133	V--N	117	0.15
134	I--E	133	0.17
135	I--G S--M	198	0.25
138	L--E L--G	295	0.37
139	C--N	55	0.07
140	F--E	36	0.04
142	M--N S--I	248	0.31
143	Y--N	171	0.21
144	Y--S	135	0.17
145	S--L	320	0.40
147	W--P Y--G	84	0.10
148	W--A	47	0.06
149	I--N T--C	267	0.33
152	W--E V--D	179	0.22
153	L--N F--G	204	0.25
154	C--D Q--C	64	0.08
155	S--F	148	0.18
158	F--N	69	0.09
159	G--C	172	0.21
160	M--D Y--D	120	0.15
168	I--D	55	0.07
169	P--C	17	0.02
170	E--C	34	0.04
172	L--D	101	0.13
174	H--C W--N	62	0.08
177	F--D W--S	93	0.12
180	C--R	69	0.09

181	W--D	22	0.03
184	W--G	53	0.07
192	V--C	250	0.31
194	Y--C	69	0.09
195	C--A	413	0.51
196	M--C	40	0.05
198	I--C L--C	252	0.31
202	K--C	27	0.03
205	F--C	85	0.11
215	W--C	29	0.04

Supplementary Figures

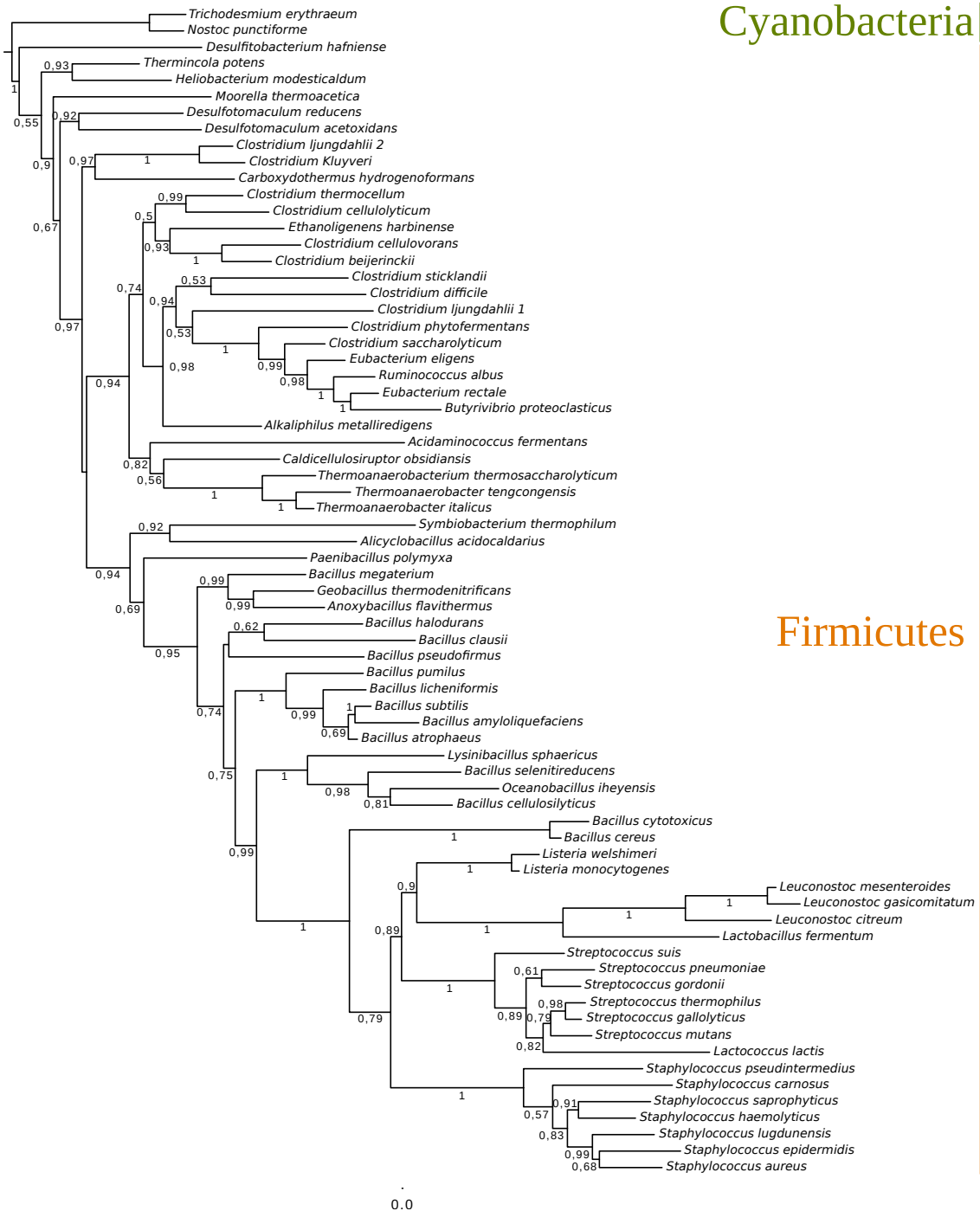


Supplementary Figure 1: **Distribution of the Grantham scores for reconstruction errors obtained with the LG S-unaware trees.** The distribution of Grantham scores for the S-unaware trees reconstructed with the C60 model or for the S-aware trees were similar and are not represented here. For each reconstruction error, the biochemical distance between the two different amino acids was determined with the Grantham matrix, which accounts for volume, polarity and composition of the amino acids. For certain categories of Grantham scores, examples of pairs of amino acids are shown.



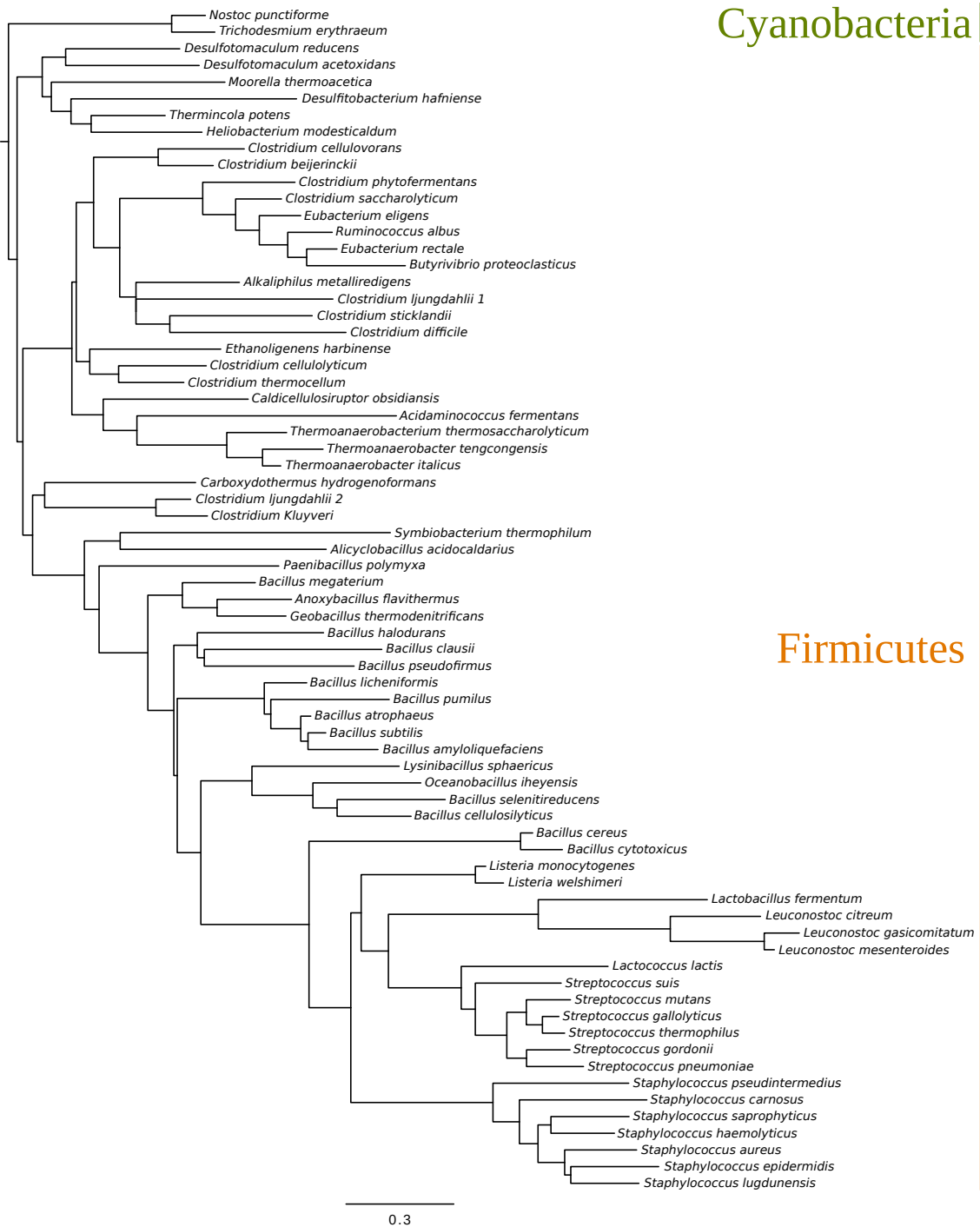
Supplementary Figure 2: **Species tree of Firmicutes.** This consensus posterior tree was reconstructed with the CAT model in Phylobayes. All branches with no support information have a PP of 1.

Cyanobacteria



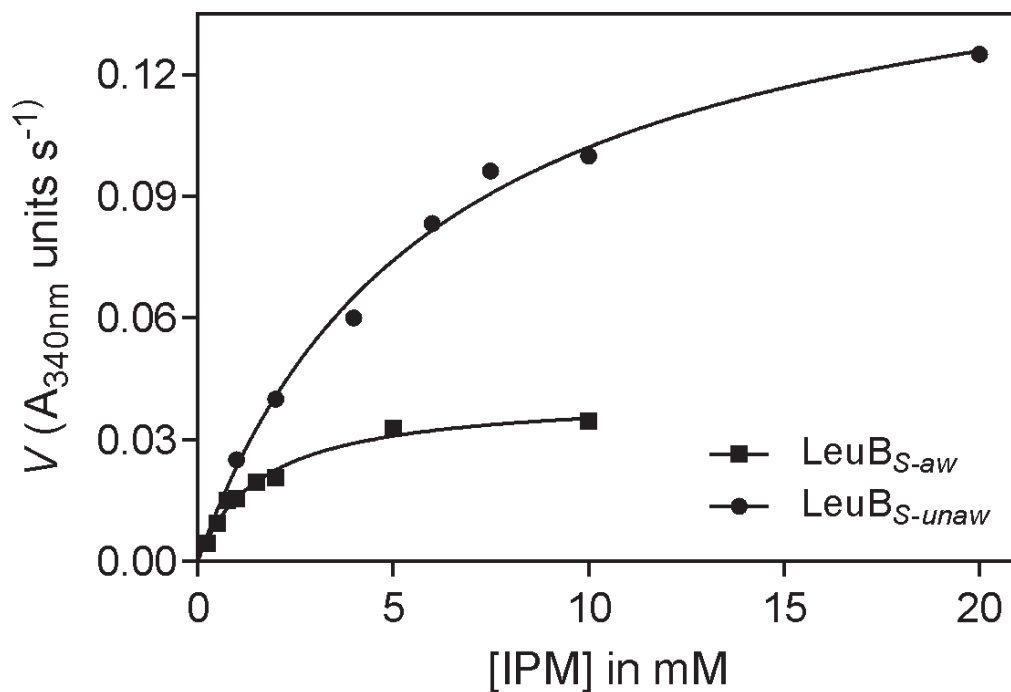
Supplementary Figure 3: **Species tree-unaware Gene tree of LeuB sequences.** This tree represents the consensus posterior tree of LeuB sequences reconstructed with PhyloBayes, using the LG+ $\Gamma(4)$ model.

Cyanobacteria

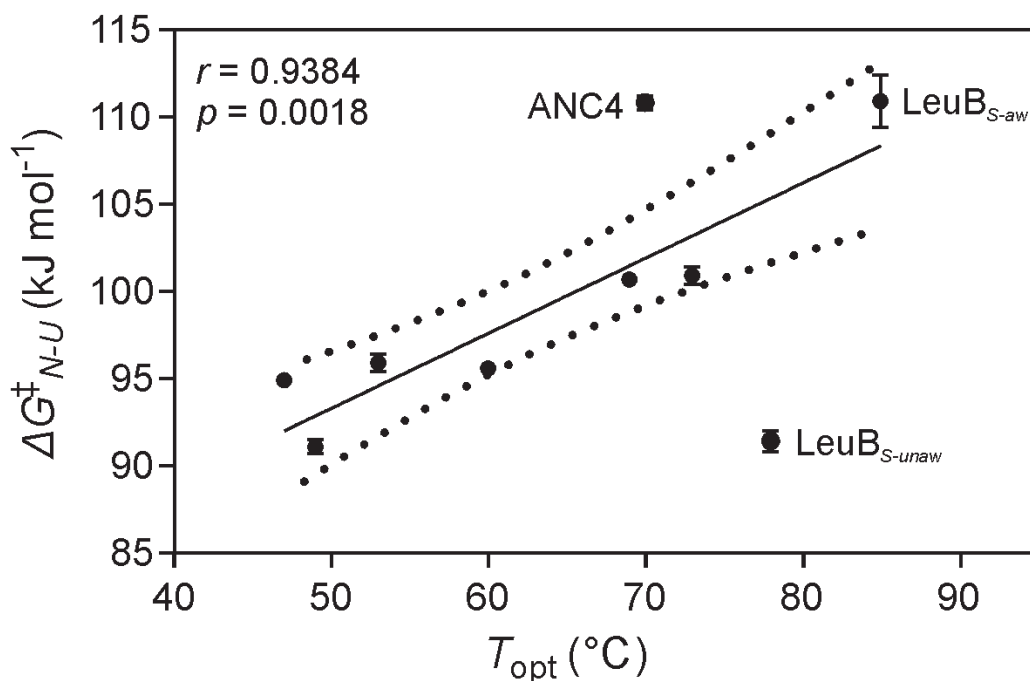


Firmicutes

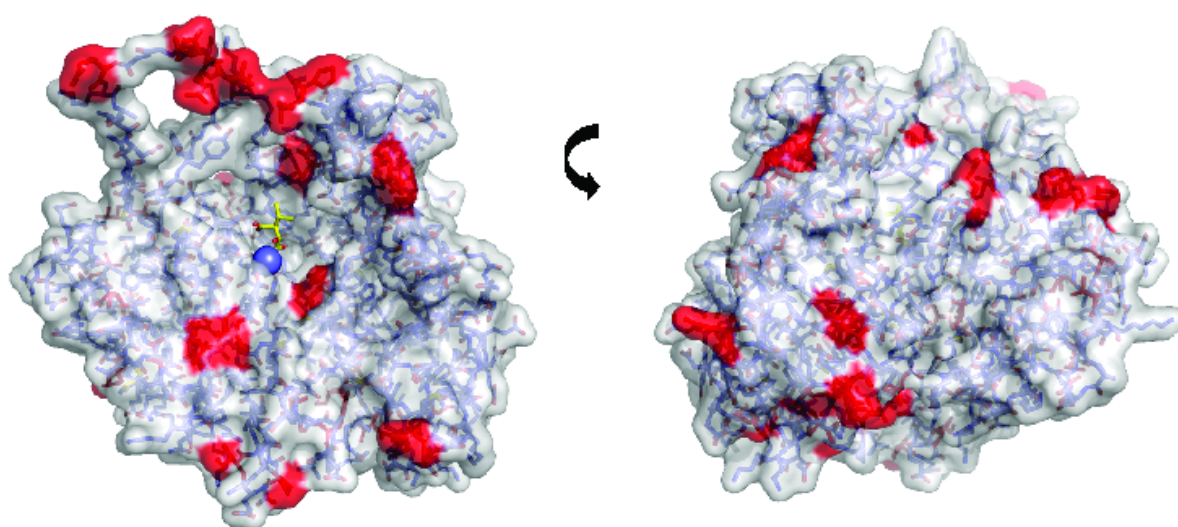
Supplementary Figure 4: **Species tree-aware (reconciled) Gene tree of LeuB sequences.** This ML reconciled joint tree was reconstructed with ALE and represents the tree that maximises the joint sequence-reconciliation likelihood.



Supplementary Figure 5: **Difference in substrate affinity between LeuB_{S-unaw} and LeuB_{S-aw} .** K_M values were measured for the IPM substrate (see Material & Methods). K_M (IPM) for LeuB_{S-unaw} is 4-fold higher than LeuB_{S-aw} , indicating its poorer affinity for this substrate.



Supplementary Figure 6: **Positive correlation between T_{opt} and ΔG_{N-U}^\ddagger .** T_{opt} and ΔG_{N-U}^\ddagger values for each LeuB enzyme mentioned in Table 1 are plotted. T_{opt} and ΔG_{N-U}^\ddagger are positively and significantly correlated. The ΔG_{N-U}^\ddagger value of LeuB_{S-unaw} falls far below the regression line.



Supplementary Figure 7: **Amino acid differences between LeuB_{S-unaw} and LeuB_{S-aw} mapped onto the LeuB_{S-aw} structure.** A homology model of the LeuB_{S-aw} enzyme was generated based on the crystal structure of the ANC4 LeuB (PDB 3U1H, see Hobbs et al. (2012)) using SWISS-MODEL (Arnold et al., 2006). The structure is depicted as a transparent surface with a stick representation beneath. Variable positions are shown in red and surface exposed residues also show a red area at the surface. The active site is shown by placing isopropylmalate (yellow sticks) and Mg²⁺ (purple sphere) from the *Acidithiobacillus ferrooxidans* structure (PDB 1A05).

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