

## SUPPLEMENTARY TEXT, TABLE AND FIGURES

Manuscript entitled “**Macrophage polarization drives granuloma outcome during *Mycobacterium tuberculosis* infection**”.

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### Macrophage Polarization Ratio - $R_{MP}$ Calculation

Macrophage stimulation is represented by 3 integer counters: pro-inflammatory STAT1counter, NFkBcounter, and anti-inflammatory STAT3counter. These are initialized to 1 and are incremented by 1 when stimulation events occur (see Figure 1A), up to a specified maximum value (STAT1MaxLevel, STAT3MaxLevel, NFkBMaxLevel). These counters are used to calculate the downstream metabolic events of variables stat3Genes, stat1Genes and nfkbGenes.

When stimulation occurs and the counter is increased, a linear decay function maps the change in counter into the signal dynamics shown in Figure 1E using the parameters  $\beta$  ("gene production") and  $\delta$  ("gene degradation"). The gene levels (with a minimum set to 1) are calculated every 10 minutes of simulation based on the following equation (e.g, for STAT1):

$$\text{tempSTAT1} = \text{stat1Genes} + (\text{STAT1counter} * \beta_{\text{STAT1}}) - \text{stat1Genes} * \delta_{\text{STAT1}};$$

$$\text{stat1Genes} = \max(\text{tempSTAT1}, 1);$$

The Macrophage Polarization Ratio [ $R_{MP}$ ] for each macrophage is then calculated as:

$$R_{MP} = (\text{stat1Genes} + \text{NFkBGenes})/2 * (\text{stat3Genes})$$

For STAT1 (and similarly for the other two pathways) the max gene levels are calculated as:

$$\text{maxSTAT1Gene} = \log_{10}(\text{stat1MaxLevel} * (\beta_{\text{STAT1}} / \delta_{\text{STAT1}})).$$

The maxGeneLevel is used to define the range [min,max] for  $R_{MP}$ . Log10 is used to prevent bias in signaling due to the range of  $\beta$  ("gene production") and  $\delta$  ("gene degradation") parameters over orders of magnitude. The maximum value for  $R_{MP}$  is calculated as:

$$\text{max}R_{MP} = \log_{10}((\text{maxSTAT1Gene} + \text{maxNFkBGene})/2 * 1).$$

The minimum value for the ratio is calculated as:

$$\text{min}R_{MP} = \log_{10}(1/\text{maxSTAT3Gene}).$$

$R_{MP}$  is normalized between 0 and 1 by defining a linear interpolation of  $R_{MP}$  using:

i) **slope** =  $1/(\text{max}R_{MP} - \text{min}R_{MP})$

ii) **intercept** =  $-1 * (\text{min}R_{MP} / (\text{max}R_{MP} - \text{min}R_{MP}))$

and adjusting  $R_{MP}$  as:

$$\text{Normalized\_}R_{MP} = \text{slope} * \log_{10}(R_{MP}) + \text{intercept}$$

The Normalized\_  $R_{MP}$  is used to scale parameters related to immune functions (lifespan, killing and secretion parameters) for each individual macrophage.

## **TNF and IL-10 secretion**

TNF is secreted by all macrophage phenotypes (except M0) and by T cells. The rates of secretion are defined by the parameters  $k_{synthMac}$  and  $kRNAMac$  (for macrophages) and  $k_{synthTcell}$  and  $kRNATcell$  (for T cells). These parameters are modulated by the macrophage polarization ratio (see the details in the Supplementary Text “*Macrophage Polarization Ratio -  $R_{MP}$  Calculation*”).

IL-10 is secreted by all macrophage phenotypes (except M0) and by regulatory T cells. The rates of secretion are defined by the parameters  $IkSynthMacInf$  and  $IkSynthMacAct$  (for macrophages) and  $dIL10$  (for T cells). Similarly to TNF, these parameters are modulated by the macrophage polarization ratio (see the details in the Supplementary Text “*Macrophage Polarization Ratio -  $R_{MP}$  Calculation*”).

As far as describing how IL-10 and TNF regulate macrophages, the reader is referred to Figure 1 of (2), where a schematic diagram illustrates all TNF and IL-10 mechanisms included in the ABM.

**Tables S1:** sensitivity analysis results obtained from calculating PRCCs on many different outputs measured on the in silico granulomas shown in Figure 3. Many time points post infection were considered (i.e., day 10, 20, 30, 40, 50, 100, 150 and 200). Each parameter listed in the tables has a PRCC significantly (i.e.,  $p < 1e-3$ ) different from zero. The outputs are CFU/Granuloma,, Granuloma Polarization Ratio, total count of macrophages, unpolarized M0, infected, M1, M2, M1M2 macrophages, total TNF molecules, total IL10 molecules, lesion size, Caseation/necrosis and macrophage apoptosis. Details on the parameters can be found in Table 1.

### CFU/granuloma PARAMETERS

Days	PARAMETERS							
10	prob <sub>KillExtMtb-M0</sub> -0.0861							
20	prob <sub>KillExtMtb-M0</sub> -0.1201							
30	prob <sub>KillExtMtb-M0</sub> time <sub>Rec</sub> -0.1441                      0.3914							
40	$\delta_{NFkB}$ -0.2779	prob <sub>KillExtMtb-M0</sub> -0.1001	$k_{NFkB}$ 0.1674	time <sub>Rec</sub> 0.5753				
50	$\delta_{NFkB}$ -0.3671	$\tau_{NFkB-TNF}$ -0.1171	$\delta_{NFkB}$ -0.1058	Synth <sub>IL10-MI</sub> -0.0901	$\beta_{NFkB}$ 0.1167	$k_{NFkB}$ 0.2346	time <sub>Rec</sub> 0.5860	
100	$\delta_{NFkB}$ -0.3604	prob <sub>KillIntMtb</sub> -0.1603	$\tau_{NFkB-TNF}$ -0.1247	prob <sub>KillExtMtb-M0</sub> 0.0959	$\beta_{NFkB}$ 0.1972	$k_{NFkB}$ 0.2540	time <sub>Rec</sub> 0.2670	prob <sub>STAT1-Ty</sub> 0.5365
150	$\delta_{NFkB}$ -0.2209	prob <sub>KillIntMtb</sub> -0.1578	$\tau_{STAT3-IL10}$ -0.1054	$\tau_{NFkB-TNF}$ -0.0904	time <sub>Rec</sub> 0.1449	$\beta_{NFkB}$ 0.1695	$k_{NFkB}$ 0.1770	prob <sub>STAT1-Ty</sub> 0.5214
200	$\delta_{NFkB}$ -0.1641	prob <sub>KillIntMtb</sub> -0.1439	$\tau_{STAT3-IL10}$ -0.1284	time <sub>Rec</sub> 0.0977	IkSynthMA 0.1032	$\beta_{NFkB}$ 0.1383	$k_{NFkB}$ 0.1398	prob <sub>STAT1-Ty</sub> 0.4834

### Granuloma Polarization Ratio PARAMETERS

Days	PARAMETERS									
10	$\delta_{NFkB}$ -0.7330	$\tau_{NFkB-TNF}$ -0.0950	$k_{NFkB}$ 0.2606	$\beta_{NFkB}$ 0.7653						
20	$\delta_{NFkB}$ -0.7038	Synth <sub>IL10-MI</sub> -0.4258	Synth <sub>IL10-MA</sub> -0.1714	$\tau_{NFkB-TNF}$ 0.0865	prob <sub>KillExtMtb-M0</sub> 0.1111	$\tau_{STAT3-IL10}$ 0.2547	$\beta_{NFkB}$ 0.6543			
30	$\delta_{NFkB}$ -0.6186	Synth <sub>IL10-MI</sub> -0.5011	Synth <sub>IL10-MA</sub> -0.2377	$k_{STAT3-IL10}$ -0.1020	$\delta_{STAT1}$ -0.0946	$\beta_{STAT1}$ 0.2209	time <sub>Rec</sub> 0.2432	$\tau_{STAT3-IL10}$ 0.2881	$\beta_{NFkB}$ 0.5674	
40	Synth <sub>IL10-MI</sub>	$\delta_{NFkB}$	Synth <sub>IL10-MA</sub>	time <sub>Rec</sub>	prob <sub>STAT1-Ty</sub>	prob <sub>KillExtMtb-M0</sub>	$\tau_{STAT3-IL10}$	$\beta_{STAT1}$	$\beta_{NFkB}$	

<b>50</b>	-0.4246	-0.3837	-0.2612	-0.1393	-0.1202	0.0922	0.2360	0.2562	0.7238	
	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	prob <sub>STAT1-Ty</sub>	$\delta_{STAT1}$	$k_{NFkB}$	$\tau_{STAT3-IL10}$	$\beta_{STAT1}$	$\beta_{NFkB}$	
	-0.4458	-0.3658	-0.2565	-0.1554	-0.1201	-0.1036	0.2184	0.2329	0.7142	
<b>100</b>	$\delta_{NFkB}$	prob <sub>STAT1-Ty</sub>	Synth <sub>IL10-MI</sub>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	Act_Time <sub>STAT3</sub>	$\tau_{STAT3-IL10}$	time <sub>Rec</sub>	$\beta_{STAT1}$	$\beta_{NFkB}$
	-0.5887	-0.2859	-0.2349	-0.2031	-0.1253	0.1016	0.1061	0.1684	0.3287	0.4804
<b>150</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	$k_{STAT3-IL10}$	prob <sub>STAT1-Ty</sub>	$\tau_{STAT3-IL10}$	$\beta_{STAT1}$	$\beta_{NFkB}$	
	-0.4806	-0.2339	-0.2116	-0.1563	-0.1030	0.1156	0.1357	0.2960	0.4492	
<b>200</b>	$\delta_{NFkB}$	$\delta_{STAT1}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{STAT3-IL10}$	Act_Time <sub>STAT1</sub>	prob <sub>STAT1-Ty</sub>	$\beta_{STAT1}$	$\beta_{NFkB}$	
	-0.4231	-0.2154	-0.1682	-0.0990	0.0915	0.0965	0.2048	0.3112	0.4302	

### Total Macrophages PARAMETERS

<b>Days</b>										
<b>10</b>	$\delta_{NFkB}$	$k_{NFkB}$								
	-0.1050	0.1387								
<b>20</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	Synth <sub>IL10-MA</sub>	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	$k_{NFkB}$			
	-0.6476	-0.2519	-0.1832	-0.0979	0.1198	0.1918	0.3078			
<b>30</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	stat3GeneDeg	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	$k_{NFkB}$	prob <sub>STAT1-Ty</sub>		
	-0.6977	-0.2883	-0.1638	-0.1060	0.1226	0.2006	0.3459	0.4872		
<b>40</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	prob <sub>KillExtMtb-M0</sub>	$\beta_{NFkB}$	$k_{NFkB}$	prob <sub>STAT1-Ty</sub>			
	-0.5982	-0.1923	-0.1715	0.1190	0.1431	0.3006	0.8334			
<b>50</b>	$\delta_{NFkB}$	$\tau_{NFkB-TNF}$	Synth <sub>IL10-MI</sub>	timeRec	Act_t <sub>STAT1</sub>	$\tau_{AgeTrans}$	$\beta_{NFkB}$	prob <sub>KillExtMtb-M0</sub>	$k_{NFkB}$	prob <sub>STAT1-Ty</sub>
	-0.4799	-0.1530	-0.1501	-0.1345	0.0899	0.1053	0.1333	0.1853	0.2415	0.9031
<b>100</b>	$\delta_{STAT1}$	timeRec	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{AgeTrans}$	$\delta_{STAT3}$	prob <sub>STAT1-Ty</sub>			
	-0.1416	-0.1320	-0.1302	-0.1051	0.0952	0.1047	0.9431			
<b>150</b>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	$\tau_{NFkB-TNF}$	prob <sub>KillIntMtb</sub>	prob <sub>STAT1-Ty</sub>					
	-0.2276	-0.1385	0.0859	0.1142	0.9219					
<b>200</b>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	$\tau_{STAT3-IL10}$	$\tau_{NFkB-TNF}$	prob <sub>KillIntMtb</sub>	prob <sub>STAT1-Ty</sub>			
	-0.2347	-0.1535	-0.1426	0.0855	0.0928	0.1046	0.8845			

### Total Infected Macrophages PARAMETERS

<b>Days</b>										
<b>10</b>	prob <sub>KillExtMtb-M0</sub>									
	-0.0973									
<b>20</b>	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$k_{NFkB}$	$\tau_{STAT3-IL10}$	$\delta_{NFkB}$					
	-0.2420	-0.1688	-0.1203	0.1620	0.2725					
<b>30</b>	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\delta_{NFkB}$	prob <sub>KillExtMtb-M0</sub>	$\tau_{STAT3-IL10}$	timeRec				
	-0.2760	-0.1710	-0.1545	-0.1094	0.1638	0.2038				
<b>40</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	$k_{NFkB}$	prob <sub>STAT1-Ty</sub>	timeRec		

<b>50</b>	-0.5393 $\delta_{NFkB}$ -0.4900	-0.2214 Synth <sub>IL10-MI</sub> -0.1593	-0.1316 $\tau_{NFkB-TNF}$ -0.1457	0.0872 $\beta_{NFkB}$ 0.1744	0.1524 timeRec 0.2033	0.2917 $k_{NFkB}$ 0.2861	0.3555 prob <sub>STAT1-Ty</sub> 0.6081	0.3705
<b>100</b>	$\delta_{NFkB}$ -0.1050	$\tau_{STAT3-IL10}$ -0.0941	$\beta_{NFkB}$ 0.1366	prob <sub>STAT1-Ty</sub> 0.6733				
<b>150</b>	$\beta_{NFkB}$ 0.0882	prob <sub>STAT1-Ty</sub> 0.5701						
<b>200</b>	Synth <sub>IL10-MA</sub> 0.0948	prob <sub>STAT1-Ty</sub> 0.5553						

### Total M0 PARAMETERS

<b>10</b>	$\delta_{NFkB}$ -0.0871	$k_{NFkB}$ 0.1286											
<b>20</b>	$\delta_{NFkB}$ -0.5600	Synth <sub>IL10-MI</sub> -0.3076	Synth <sub>IL10-MA</sub> -0.1779	$\tau_{NFkB-TNF}$ -0.1327	$\beta_{NFkB}$ 0.1673	$\tau_{STAT3-IL10}$ 0.1915	$k_{NFkB}$ 0.1953						
<b>30</b>	$\delta_{NFkB}$ -0.6391	Synth <sub>IL10-MI</sub> -0.3889	Synth <sub>IL10-MA</sub> -0.1955	timeRec -0.1185	$\tau_{NFkB-TNF}$ -0.1144	$\delta_{STAT3}$ -0.1027	$k_{STAT3-IL10}$ -0.0903	$\delta_{STAT1}$ 0.1100	$\beta_{NFkB}$ 0.1949	$\tau_{STAT3-IL10}$ 0.2125	$k_{NFkB}$ 0.2807	prob <sub>STAT1-Ty</sub> 0.4087	
<b>40</b>	$\delta_{NFkB}$ -0.5763	Synth <sub>IL10-MI</sub> -0.3077	$\tau_{NFkB-TNF}$ -0.1485	Synth <sub>IL10-MA</sub> -0.1175	prob <sub>KillExtMtb-M0</sub> 0.1171	$\tau_{STAT3-IL10}$ 0.1325	$\beta_{NFkB}$ 0.1531	$k_{NFkB}$ 0.2752	prob <sub>STAT1-Ty</sub> 0.8330				
<b>50</b>	$\delta_{NFkB}$ -0.4529	Synth <sub>IL10-MI</sub> -0.2740	timeRec -0.1357	Synth <sub>IL10-MA</sub> -0.1292	$\tau_{NFkB-TNF}$ -0.1281	$k_{STAT3-IL10}$ -0.0887	Act <sub>I</sub> STAT1 0.0873	$\tau_{AgeTrans}$ 0.0922	$\tau_{STAT3-IL10}$ 0.1155	$\beta_{NFkB}$ 0.1462	prob <sub>KillExtMtb-M0</sub> 0.1695	$k_{NFkB}$ 0.2228	prob <sub>STAT1-Ty</sub> 0.9003
<b>100</b>	Synth <sub>IL10-MI</sub> -0.3026	Synth <sub>IL10-MA</sub> -0.2768	timeRec -0.1233	$\tau_{STAT3-IL10}$ 0.1925	prob <sub>STAT1-Ty</sub> 0.8568								
<b>150</b>	Synth <sub>IL10-MI</sub> -0.2891	Synth <sub>IL10-MA</sub> -0.2624	$\delta_{STAT1}$ -0.0930	$\tau_{STAT3-IL10}$ 0.1926	prob <sub>STAT1-Ty</sub> 0.7781								
<b>200</b>	Synth <sub>IL10-MI</sub> -0.2607	Synth <sub>IL10-MA</sub> -0.2435	$\delta_{STAT1}$ -0.0989	$k_{NFkB}$ -0.0973	$\tau_{STAT3-IL10}$ 0.1551	prob <sub>STAT1-Ty</sub> 0.7381							

### Total M1 PARAMETERS

<b>10</b>	$\delta_{NFkB}$ -0.3702	$\tau_{NFkB-TNF}$ -0.1537	$k_{NFkB}$ 0.2676										
<b>20</b>	$\delta_{NFkB}$ -0.6823	Synth <sub>IL10-MI</sub> -0.4716	$\tau_{NFkB-TNF}$ -0.2045	Synth <sub>IL10-MA</sub> -0.1748	$\delta_{STAT1}$ 0.1164	$\tau_{STAT3-IL10}$ 0.2199	$\beta_{NFkB}$ 0.2308	$k_{NFkB}$ 0.4671					
<b>30</b>	$\delta_{NFkB}$ -0.5489	Synth <sub>IL10-MI</sub> -0.4790	Synth <sub>IL10-MA</sub> -0.2127	$\delta_{STAT3}$ -0.0923	$\tau_{NFkB-TNF}$ -0.0908	$\tau_{STAT3-IL10}$ -0.0885	$\delta_{STAT1}$ 0.1103	$\beta_{NFkB}$ 0.1272	$\tau_{STAT3-IL10}$ 0.2514	$k_{NFkB}$ 0.3284	prob <sub>STAT1-Ty</sub> 0.4280	timeRec 0.4319	
<b>40</b>	$\delta_{NFkB}$ -0.4147	Synth <sub>IL10-MI</sub> -0.3481	Synth <sub>IL10-MA</sub> -0.1808	$\tau_{NFkB-TNF}$ -0.1170	$\delta_{STAT1}$ 0.0877	$\beta_{NFkB}$ 0.1074	prob <sub>KillExtMtb-M0</sub> 0.1696	$\tau_{STAT3-IL10}$ 0.1712	$k_{NFkB}$ 0.2394	prob <sub>STAT1-Ty</sub> 0.7597			

<b>50</b>	Synth <sub>IL10-MI</sub> -0.3512	$\delta_{Nf\kappa B}$ -0.3119	Synth <sub>IL10-MA</sub> -0.1862	$k_{Nf\kappa B}$ 0.1657	prob <sub>KillExtMtb-M0</sub> 0.1792	$\tau_{STAT3-IL10}$ 0.1877	prob <sub>STAT1-Ty</sub> 0.8253
<b>100</b>	Synth <sub>IL10-MI</sub> -0.3105	Synth <sub>IL10-MA</sub> -0.2962	$\delta_{Nf\kappa B}$ -0.2392	kSTAT3IL10 -0.1118	$k_{Nf\kappa B}$ 0.0902	$\tau_{STAT3-IL10}$ 0.2056	prob <sub>STAT1-Ty</sub> 0.8231
<b>150</b>	Synth <sub>IL10-MA</sub> -0.3152	Synth <sub>IL10-MI</sub> -0.2944	$\delta_{Nf\kappa B}$ -0.2328	$\delta_{STAT1}$ -0.1223	$k_{Nf\kappa B}$ 0.1071	$\tau_{STAT3-IL10}$ 0.2094	prob <sub>STAT1-Ty</sub> 0.8230
<b>200</b>	Synth <sub>IL10-MA</sub> -0.2773	Synth <sub>IL10-MI</sub> -0.2589	$\delta_{Nf\kappa B}$ -0.2525	-0.1241	$k_{Nf\kappa B}$ 0.1089	$\tau_{STAT3-IL10}$ 0.1950	prob <sub>STAT1-Ty</sub> 0.8178

### Total M1

#### PARAMETERS

Days	PARAMETERS						
<b>10</b>	Synth <sub>IL10-MI</sub> 0.0911						
<b>20</b>	$\tau_{STAT3-IL10}$ -0.3921	$k_{Nf\kappa B}$ -0.1328	$\beta_{Nf\kappa B}$ -0.0891	$\delta_{Nf\kappa B}$ 0.1416	Synth <sub>IL10-MA</sub> 0.1913	Synth <sub>IL10-MI</sub> 0.6243	
<b>30</b>	$\tau_{STAT3-IL10}$ -0.4855	timeRec -0.1462	$\delta_{STAT1}$ -0.0948	$k_{STAT3-IL10}$ 0.0943	Synth <sub>IL10-MA</sub> 0.2534	Synth <sub>IL10-MI</sub> 0.6908	
<b>40</b>	$\tau_{STAT3-IL10}$ -0.5085	$\delta_{Nf\kappa B}$ -0.1563	$\delta_{STAT1}$ -0.0861	prob <sub>STAT1-Ty</sub> 0.0871	$k_{STAT3-IL10}$ 0.1072	Synth <sub>IL10-MA</sub> 0.2366	Synth <sub>IL10-MI</sub> 0.5914
<b>50</b>	$\tau_{STAT3-IL10}$ -0.4670	$k_{STAT3-IL10}$ 0.0885	prob <sub>STAT1-Ty</sub> 0.1481	Synth <sub>IL10-MA</sub> 0.2374	Synth <sub>IL10-MI</sub> 0.5450		
<b>100</b>	$\tau_{STAT3-IL10}$ -0.3636	Synth <sub>IL10-MA</sub> 0.1665	prob <sub>STAT1-Ty</sub> 0.2934	Synth <sub>IL10-MI</sub> 0.4669			
<b>150</b>	$\tau_{STAT3-IL10}$ -0.3806	Synth <sub>IL10-MA</sub> 0.1764	prob <sub>STAT1-Ty</sub> 0.2292	Synth <sub>IL10-MI</sub> 0.5406			
<b>200</b>	$\tau_{STAT3-IL10}$ -0.3560	$k_{STAT3-IL10}$ 0.1035	Synth <sub>IL10-MA</sub> 0.1732	prob <sub>STAT1-Ty</sub> 0.2363	Synth <sub>IL10-MI</sub> 0.4918		

### Total M1M2

#### PARAMETERS

Days	PARAMETERS						
<b>10</b>	NONE						
<b>20</b>	$\tau_{STAT3-IL10}$ -0.4781	Synth <sub>IL10-MA</sub> 0.1272	Synth <sub>IL10-MI</sub> 0.7512				
<b>30</b>	$\tau_{STAT3-IL10}$ -0.5708	$\delta_{STAT1}$ -0.1002	prob <sub>KillExtMtb-M0</sub> -0.0903	Synth <sub>IL10-MA</sub> 0.1772	Synth <sub>IL10-MI</sub> 0.7644		
<b>40</b>	$\tau_{STAT3-IL10}$ -0.5852	$\delta_{Nf\kappa B}$ -0.1704	prob <sub>STAT1-Ty</sub> 0.0897	$k_{Nf\kappa B}$ 0.1144	$k_{STAT3-IL10}$ 0.1172	Synth <sub>IL10-MA</sub> 0.1940	Synth <sub>IL10-MI</sub> 0.6639

<b>50</b>	$\tau_{\text{STAT3-IL10}}$ -0.5477	$\delta_{\text{NFkB}}$ -0.1566	$k_{\text{NFkB}}$ 0.0956	$\text{Synth}_{\text{IL10-MA}}$ 0.1268	$\text{prob}_{\text{STAT1-Ty}}$ 0.2038	$\text{Synth}_{\text{IL10-MI}}$ 0.6208
<b>100</b>	$\tau_{\text{STAT3-IL10}}$ -0.3808	$\text{Synth}_{\text{IL10-MA}}$ 0.1536	$\text{prob}_{\text{STAT1-Ty}}$ 0.3276	$\text{Synth}_{\text{IL10-MI}}$ 0.4927		
<b>150</b>	$\tau_{\text{STAT3-IL10}}$ -0.3930	$k_{\text{STAT3-IL10}}$ 0.0908	$\text{Synth}_{\text{IL10-MA}}$ 0.1308	$\text{prob}_{\text{STAT1-Ty}}$ 0.2424	$\text{Synth}_{\text{IL10-MI}}$ 0.5409	
<b>200</b>	$\tau_{\text{STAT3-IL10}}$ -0.3837	$\text{Synth}_{\text{IL10-MA}}$ 0.1625	$\text{prob}_{\text{STAT1-Ty}}$ 0.2249	$\text{Synth}_{\text{IL10-MI}}$ 0.5282		

**Total TNF  
PARAMETERS**

<b>Days</b>													
<b>10</b>	$\delta_{\text{NFkB}}$ -0.1738	$\text{Synth}_{\text{IL10-MI}}$ -0.0939	$k_{\text{NFkB}}$ 0.1467										
<b>20</b>	$\delta_{\text{NFkB}}$ -0.5845	$\text{Synth}_{\text{IL10-MI}}$ -0.5720	$\text{Synth}_{\text{IL10-MA}}$ -0.1753	$\tau_{\text{NFkB-TNF}}$ -0.1656	$\delta_{\text{STAT3}}$ -0.1122	$\text{stat3Beta}$ 0.0918	$\delta_{\text{NFkB}}$ 0.1721	$\tau_{\text{STAT3-IL10}}$ 0.1975	$\beta_{\text{NFkB}}$ 0.2593	$k_{\text{NFkB}}$ 0.4117			
<b>30</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.5612	$\delta_{\text{NFkB}}$ -0.4848	$\text{Synth}_{\text{IL10-MA}}$ -0.2268	$\delta_{\text{STAT3}}$ -0.1147	$\beta_{\text{NFkB}}$ 0.1403	$\delta_{\text{NFkB}}$ 0.1424	$\tau_{\text{STAT3-IL10}}$ 0.2463	$k_{\text{NFkB}}$ 0.3125	$\text{prob}_{\text{STAT1-Ty}}$ 0.3876	$\text{timeRec}$ 0.5299			
<b>40</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.4723	$\delta_{\text{NFkB}}$ -0.4519	$\text{Synth}_{\text{IL10-MA}}$ -0.2017	$\tau_{\text{NFkB-TNF}}$ -0.1261	$\delta_{\text{STAT3}}$ -0.0930	$\text{timeRec}$ 0.1103	$\delta_{\text{NFkB}}$ 0.1291	$\text{prob}_{\text{KillExtMtb-M0}}$ 0.1300	$\beta_{\text{NFkB}}$ 0.1348	$\tau_{\text{STAT3-IL10}}$ 0.1655	$k_{\text{NFkB}}$ 0.2476	$\text{prob}_{\text{STAT1-Ty}}$ 0.7225	
<b>50</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.4444	$\delta_{\text{NFkB}}$ -0.3448	$\text{Synth}_{\text{IL10-MA}}$ -0.1967	$\delta_{\text{NFkB}}$ -0.1049	$\tau_{\text{NFkB-TNF}}$ -0.0868	$k_{\text{STAT3IL10}}$ -0.0867	$\delta_{\text{NFkB}}$ 0.1097	$\beta_{\text{NFkB}}$ 0.1122	$\text{prob}_{\text{KillExtMtb-M0}}$ 0.1664	$\tau_{\text{STAT3-IL10}}$ 0.1821	$k_{\text{NFkB}}$ 0.1978	$\text{prob}_{\text{STAT1-Ty}}$ 0.8173	
<b>100</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.3171	$\delta_{\text{NFkB}}$ -0.2689	$\text{Synth}_{\text{IL10-MA}}$ -0.2355	$\tau_{\text{NFkB-TNF}}$ -0.1132	$k_{\text{STAT3IL10}}$ -0.0963	$\text{prob}_{\text{KillExtMtb-M0}}$ 0.0903	$\beta_{\text{NFkB}}$ 0.1196	$\tau_{\text{STAT3-IL10}}$ 0.1526	$k_{\text{NFkB}}$ 0.1731	$\text{prob}_{\text{STAT1-Ty}}$ 0.8931			
<b>150</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.3257	$\text{Synth}_{\text{IL10-MA}}$ -0.2906	$\delta_{\text{NFkB}}$ -0.2427	$\delta_{\text{STAT3}}$ -0.1096	$\delta_{\text{NFkB}}$ -0.0970	$\beta_{\text{NFkB}}$ 0.0886	$k_{\text{NFkB}}$ 0.1612	$\tau_{\text{STAT3-IL10}}$ 0.1669	$\text{prob}_{\text{STAT1-Ty}}$ 0.8929				
<b>200</b>	$\text{Synth}_{\text{IL10-MI}}$ -0.2760	$\text{Synth}_{\text{IL10-MA}}$ -0.2473	$\delta_{\text{NFkB}}$ -0.2460	$\delta_{\text{STAT3}}$ -0.1165	$\delta_{\text{NFkB}}$ -0.1029	$\beta_{\text{NFkB}}$ 0.1109	$\tau_{\text{STAT3-IL10}}$ 0.1400	$k_{\text{NFkB}}$ 0.1673	$\text{prob}_{\text{STAT1-Ty}}$ 0.8903				

**Total IL10  
PARAMETERS**

<b>Days</b>									
<b>10</b>	$\text{Synth}_{\text{IL10-MI}}$ 0.6776								
<b>20</b>	$k_{\text{NFkB}}$ -0.1652	$\tau_{\text{STAT3-IL10}}$ -0.1475	$\text{Synth}_{\text{IL10-MA}}$ 0.0941	$\delta_{\text{NFkB}}$ 0.2918	$\text{Synth}_{\text{IL10-MI}}$ 0.8953				
<b>30</b>	$\text{timeRec}$ -0.3206	$\delta_{\text{NFkB}}$ -0.2603	$\tau_{\text{STAT3-IL10}}$ -0.1976	$k_{\text{NFkB}}$ 0.1068	$\text{Synth}_{\text{IL10-MA}}$ 0.2759	$\text{Synth}_{\text{IL10-MI}}$ 0.5882	$\text{prob}_{\text{STAT1-Ty}}$ 0.5954		
<b>40</b>	$\delta_{\text{NFkB}}$ -0.2925	$\tau_{\text{STAT3-IL10}}$ -0.1749	$\tau_{\text{NFkB-TNF}}$ -0.0989	$k_{\text{NFkB}}$ 0.1242	$\text{timeRec}$ 0.1527	$\text{Synth}_{\text{IL10-MA}}$ 0.2934	$\text{Synth}_{\text{IL10-MI}}$ 0.4156	$\text{prob}_{\text{STAT1-Ty}}$ 0.7594	



<b>50</b>	$\delta_{NFkB}$	$\tau_{STAT3-IL10}$	$\tau_{NFkB-TNF}$	timeRec	$k_{NFkB}$	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	prob <sub>STAT1-T<math>\gamma</math></sub>
	-0.2647	-0.2077	-0.1067	0.1002	0.1398	0.2413	0.3920	0.7843
<b>100</b>	$\tau_{STAT3-IL10}$	$\delta_{NFkB}$	timeRec	$k_{NFkB}$	$\beta_{NFkB}$	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	prob <sub>STAT1-T<math>\gamma</math></sub>
	-0.1495	-0.1262	-0.0898	0.0914	0.1110	0.1384	0.3096	0.8295
<b>150</b>	$\tau_{STAT3-IL10}$	$\delta_{NFkB}$	Act_t <sub>STAT3</sub>	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	prob <sub>STAT1-T<math>\gamma</math></sub>		
	-0.1327	-0.1064	-0.0858	0.1748	0.3601	0.7849		
<b>200</b>	$\tau_{STAT3-IL10}$	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	prob <sub>STAT1-T<math>\gamma</math></sub>				
	-0.1390	0.1580	0.3584	0.7607				

### Lesion Size

#### PARAMETERS

<b>Days</b>										
<b>10</b>	$k_{NFkB}$									
	0.1373									
<b>20</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	Synth <sub>IL10-MA</sub>	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	$k_{NFkB}$			
	-0.5973	-0.2830	-0.1724	-0.1166	0.1327	0.2047	0.3255			
<b>30</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	Synth <sub>IL10-MA</sub>	$\delta_{STAT3}$	$\delta_{STAT1}$	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	$k_{NFkB}$	prob <sub>STAT1-T<math>\gamma</math></sub>
	-0.6571	-0.3572	-0.1528	-0.1213	-0.1141	0.1014	0.1608	0.2098	0.3469	0.4816
<b>40</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	$\delta_{STAT3}$	prob <sub>KillExtMtb-M0</sub>	$\beta_{NFkB}$	$k_{NFkB}$	prob <sub>STAT1-T<math>\gamma</math></sub>		
	-0.5811	-0.2393	-0.1676	-0.0920	0.1099	0.1421	0.3030	0.8234		
<b>50</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	$\tau_{NFkB-TNF}$	timeRec	$\beta_{NFkB}$	prob <sub>KillExtMtb-M0</sub>	$k_{NFkB}$	prob <sub>STAT1-T<math>\gamma</math></sub>		
	-0.4616	-0.2011	-0.1484	-0.0967	0.1336	0.1843	0.2456	0.8944		
<b>100</b>	Synth <sub>IL10-MI</sub>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	$\delta_{NFkB}$	$\beta_{NFkB}$	prob <sub>STAT1-T<math>\gamma</math></sub>				
	-0.1721	-0.1554	-0.1505	-0.1416	0.0951	0.9501				
<b>150</b>	$\delta_{STAT1}$	Synth <sub>IL10-MA</sub>	Synth <sub>IL10-MI</sub>	$\delta_{NFkB}$	prob <sub>STAT1-T<math>\gamma</math></sub>					
	-0.2591	-0.1638	-0.1316	-0.0950	0.9422					
<b>200</b>	$\delta_{STAT1}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{STAT3-IL10}$	prob <sub>STAT1-T<math>\gamma</math></sub>					
	-0.2746	-0.1825	-0.1695	0.0926	0.9302					

### Caseation/Necrosis

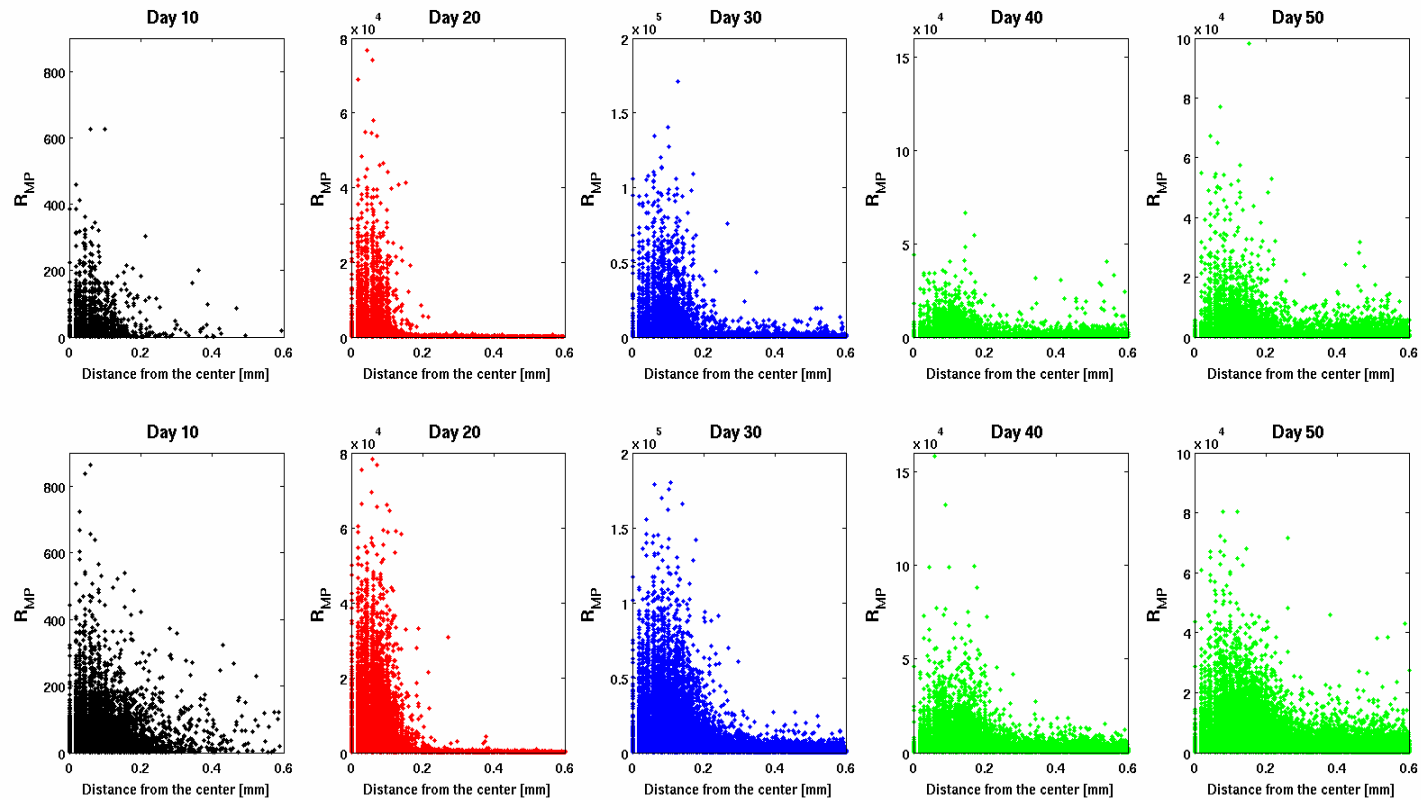
#### PARAMETERS

<b>Days</b>			
<b>10</b>	NONE		
<b>20</b>	NONE		
<b>30</b>	NONE		
<b>40</b>	prob <sub>STAT1-T<math>\gamma</math></sub>	timeRec	$\delta_{NFkB}$
	-0.1511	-0.1313	0.1140

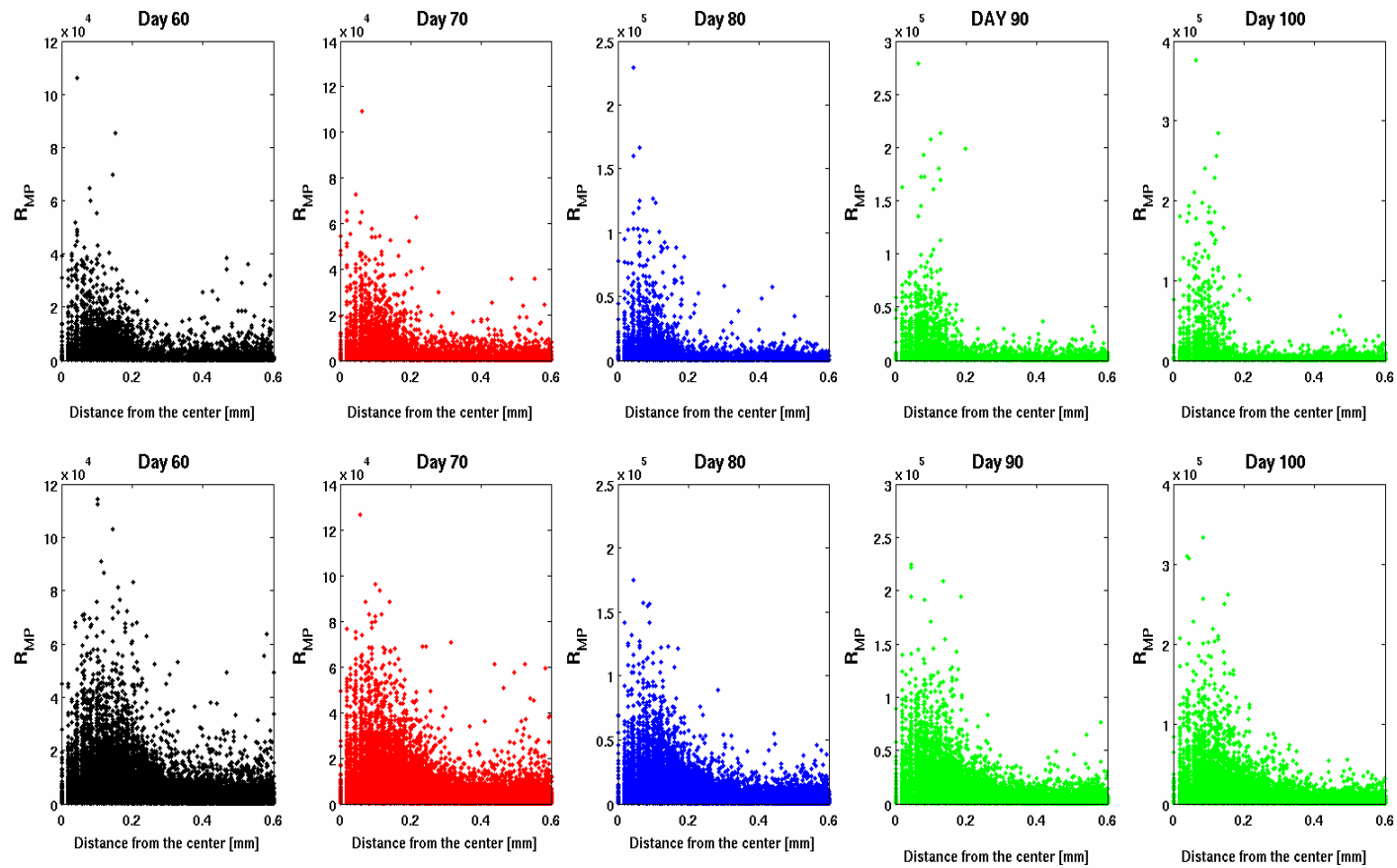
<b>50</b>	prob <sub>STAT1-Ty</sub>	timeRec	prob <sub>KillExtMtb-M0</sub>	k <sub>NFkB</sub>	Synth <sub>IL10-MA</sub>	$\tau_{NFkB-TNF}$	$\tau_{STAT3-IL10}$	$\delta_{NFkB}$
	-0.4270	-0.2712	-0.2338	-0.1701	-0.1658	0.1302	0.1329	0.3591
<b>100</b>	$\delta_{NFkB}$	prob <sub>KillExtMtb-M0</sub>	Synth <sub>IL10-MI</sub>	$\tau_{STAT3-IL10}$	k <sub>NFkB</sub>	timeRec		
	-0.2990	-0.1865	-0.1572	0.1012	0.1152	0.3466		
<b>150</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	prob <sub>KillIntMtb</sub>	$\tau_{NFkB-TNF}$	$\beta_{NFkB}$	k <sub>NFkB</sub>	prob <sub>STAT1-Ty</sub>	
	-0.2955	-0.1489	-0.1470	-0.1117	0.1267	0.1843	0.5631	
<b>200</b>	$\delta_{NFkB}$	prob <sub>KillIntMtb</sub>	$\tau_{NFkB-TNF}$	Synth <sub>IL10-MI</sub>	$\beta_{NFkB}$	k <sub>NFkB</sub>	prob <sub>STAT1-Ty</sub>	
	-0.2297	-0.1572	-0.0944	-0.0929	0.1324	0.1694	0.5966	

## TNF-induced Apoptosis of Macrophages

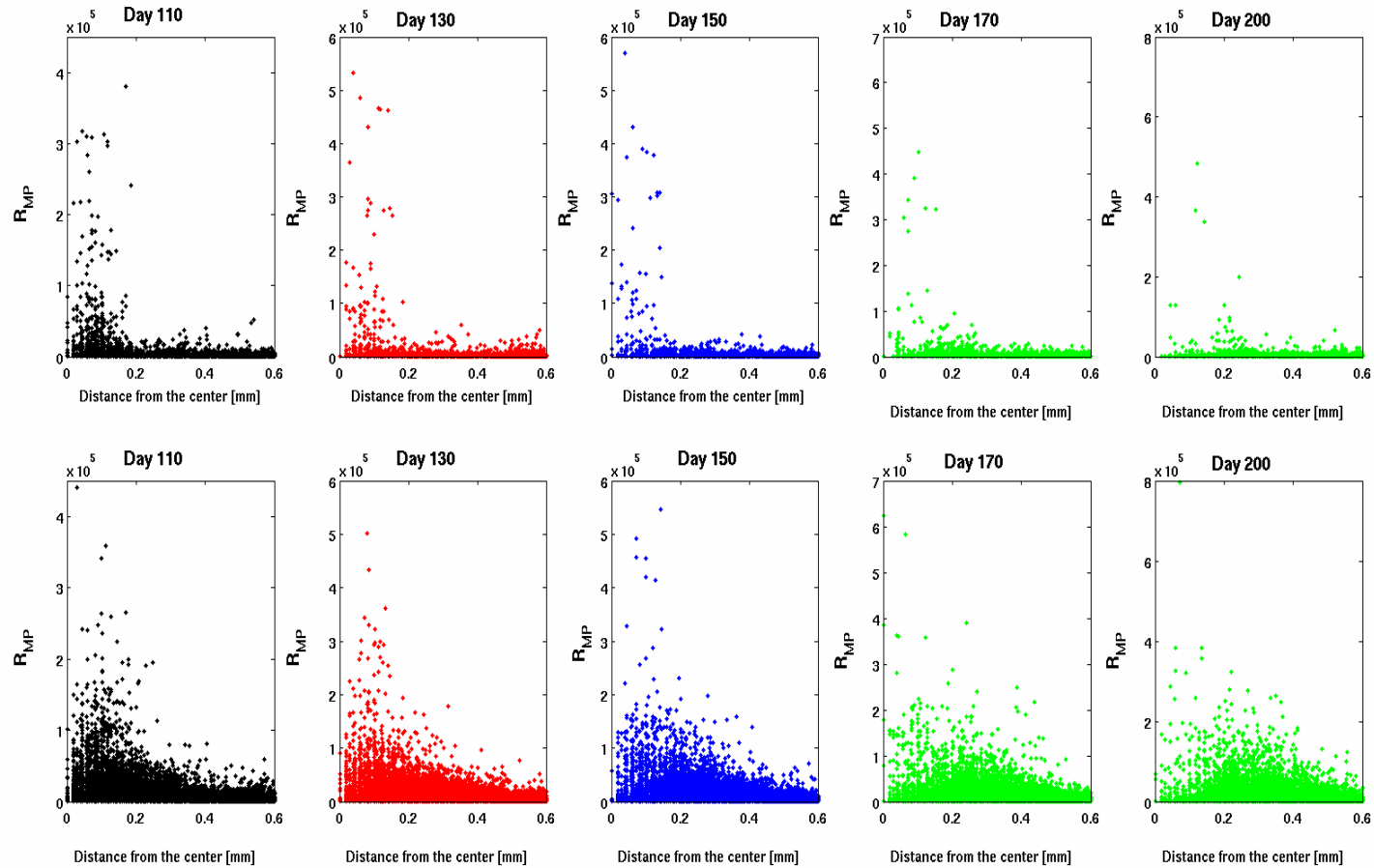
Days	PARAMETERS												
<b>10</b>	k <sub>NFkB</sub>												
	0.0976												
<b>20</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{NFkB-TNF}$	$\delta_{STAT3}$	$\beta_{STAT3}$	$\delta_{STAT1}$	$\tau_{STAT3-IL10}$	$\beta_{NFkB}$	k <sub>NFkB</sub>			
	-0.4613	-0.4500	-0.1411	-0.1288	-0.0983	0.1093	0.1314	0.1373	0.1843	0.3635			
<b>30</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{NFkB-TNF}$	$\delta_{STAT3}$	$\beta_{STAT3}$	prob <sub>STAT1-Ty</sub>	$\delta_{STAT1}$	$\tau_{STAT3-IL10}$	timeRec	$\beta_{NFkB}$	k <sub>NFkB</sub>	
	-0.6030	-0.5616	-0.2095	-0.1495	-0.1299	0.0964	0.1029	0.1733	0.2240	0.2268	0.2335	0.4129	
<b>40</b>	$\delta_{NFkB}$	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\tau_{NFkB-TNF}$	$\delta_{STAT3}$	$\delta_{STAT1}$	$\beta_{NFkB}$	$\tau_{STAT3-IL10}$	prob <sub>STAT1-Ty</sub>	timeRec	k <sub>NFkB</sub>		
	-0.5963	-0.5838	-0.2256	-0.1479	-0.1405	0.1678	0.2079	0.2213	0.2370	0.2820	0.3872		
<b>50</b>	Synth <sub>IL10-MI</sub>	$\delta_{NFkB}$	Synth <sub>IL10-MA</sub>	$\delta_{STAT3}$	$\tau_{NFkB-TNF}$	k <sub>STAT3IL10</sub>	$\delta_{STAT1}$	timeRec	$\beta_{NFkB}$	$\tau_{STAT3-IL10}$	k <sub>NFkB</sub>	prob <sub>STAT1-Ty</sub>	
	-0.5665	-0.5429	-0.2277	-0.1516	-0.1453	-0.0947	0.1718	0.1799	0.1814	0.2228	0.3462	0.4826	
<b>100</b>	Synth <sub>IL10-MI</sub>	$\delta_{NFkB}$	Synth <sub>IL10-MA</sub>	k <sub>STAT3IL10</sub>	$\delta_{STAT3}$	$\tau_{NFkB-TNF}$	$\delta_{STAT1}$	prob <sub>KillExtMtb-M0</sub>	$\beta_{NFkB}$	$\tau_{STAT3-IL10}$	k <sub>NFkB</sub>	prob <sub>STAT1-Ty</sub>	
	-0.4827	-0.3608	-0.2879	-0.1284	-0.1216	-0.1188	0.1086	0.1176	0.1288	0.2226	0.2335	0.8051	
<b>150</b>	Synth <sub>IL10-MI</sub>	$\delta_{NFkB}$	Synth <sub>IL10-MA</sub>	k <sub>STAT3IL10</sub>	$\delta_{STAT3}$	$\tau_{NFkB-TNF}$	prob <sub>KillExtMtb-M0</sub>	$\beta_{NFkB}$	k <sub>NFkB</sub>	$\tau_{STAT3-IL10}$	prob <sub>STAT1-Ty</sub>		
	-0.4452	-0.3256	-0.3253	-0.1226	-0.1213	-0.0968	0.0905	0.1211	0.2191	0.2385	0.8400		
<b>200</b>	Synth <sub>IL10-MI</sub>	Synth <sub>IL10-MA</sub>	$\delta_{NFkB}$	$\delta_{STAT3}$	k <sub>STAT3IL10</sub>	$\beta_{NFkB}$	k <sub>NFkB</sub>	$\tau_{STAT3-IL10}$	prob <sub>STAT1-Ty</sub>				
	-0.4191	-0.3361	-0.3162	-0.1414	-0.1104	0.1193	0.2159	0.2310	0.8541				



**Figure S1: Spatial distribution of Macrophage Polarization Ratio ( $R_{MP}$ , y-axis in all the panels) from day 10 to 50 post infection within granulomas.** Each dot represents a macrophage polarization ratio. The two rows represent the containment (top row) and dissemination (bottom row) clusters of granulomas, respectively (as shown in Figure 3). The x-axis is the distance each macrophage is from the center of the granuloma (shown here in mm), since we restrict our analysis to granuloma within 1-2 mm in diameter (here 0.6 mm is the radius of the lesion).



**Figure S2: Spatial distribution of Macrophage Polarization Ratio ( $R_{MP}$ , y-axis in all the panels) from day 60 to 100 post infection within granulomas.** Each dot represents a macrophage polarization ratio. The two rows represent the containment (top row) and dissemination (bottom row) clusters of granulomas, respectively (as shown in Figure 3). The x-axis is the distance each macrophage is from the center of the granuloma (shown here in mm), since we restrict our analysis to granuloma within 1-2 mm in diameter (here 0.6 mm is the radius of the lesion).



**Figure S3: Spatial distribution of Macrophage Polarization Ratio ( $R_{MP}$ , y-axis in all the panels) from day 100 to 200 post infection within granulomas.** Each dot represents a macrophage polarization ratio. The two rows represent the (top row) containment and dissemination (bottom row) clusters of granulomas, respectively (as shown in Figure 3). The x-axis is the distance each macrophage is from the center of the granuloma (shown here in mm), since we restrict our analysis to granuloma within 1-2 mm in diameter (here 0.6 mm is the radius of the lesion).